

# Motif Search. Multiple Alignments

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Bioinformatics course  
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inspired by materials from Aleksandra Galitsyna 🧡

**Skoltech**

Skolkovo Institute of Science and Technology

# Outline

1. Motif, motif discovery problem ~ 15
2. Multiple sequence alignment ~ 20
3. Task 1 (part of HW) ~ 30
4. ChIP-seq ~ 10
5. Motif representation ~ 20
6. Task 2-4 (part of HW) ~ 45
7. Motif scanning ~ 10
8. In class command line training ~ 10
9. Task 5 (part of HW)

# Motif

In general, **motif** is a recurring (**conserved**) **pattern** that is presumed to have **biological significance** (have biological function)

can found in:

- structure or sequence
- RNA/protein/DNA

can be involved in **interactions** with other molecules (proteins/nucleic acids)

Major **living processes** of the cells are **regulated** via **interactions** between proteins and nucleic acids: protein-DNA, protein-RNA, RNA-DNA

During our seminar, we will deal with **DNA sequence motifs** recognized by protein (**transcription factor**)

# DNA sequence motif

Often indicate sequence-specific binding sites for proteins such as nucleases and transcription factors (TFs)

Others are involved in processes such as: ribosome binding, mRNA processing (splicing etc), transcription termination

## Examples:

- transcription factor binding sites (TFBS)
- motifs recognized by RNA polymerase (e.g. TATA-box in the promoters of *E. coli* genes)
- restriction sites in *E. coli* genome

**Motif knowledge** is very useful in defining genetic regulatory networks and regulatory program of individual genes

# How to find a DNA sequence motif?

## Experimental approach:

- DNase footprinting
- SELEX
- electrophoretic mobility shift assays
- more examples

<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC3080775/>

## Computational approach – motif discovery problem

- search for overrepresented (and/or conserved) DNA patterns upstream of functionally related genes (e.g. genes with similar expression patterns)

# Motif discovery problem

It is the computational task of searching for regulatory DNA motifs

The motif discovery problem can be formulated as follows:

**Given:** a set of DNA sequences

**Assumption:** respective genes are **co-regulated** and thus likely to be bound by one or more regulatory proteins

**Find:** parameters of **motif(s)** that could explain this binding:

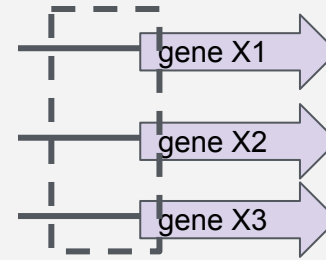
- number of motifs
- the width of each motif
- its location in input sequences

# Motif discovery problem: flowchart

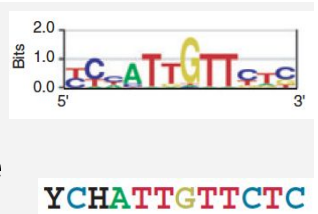
## identify **co-regulated genes**

- co-expressed under certain condition and same functional category
- orthologous genes
- ChIP-seq
- ...

## get **upstream regions** of selected genes



## select a **motif model** (consensus or PWM) – to access and compare obtained motifs



## Motif discovery

**“phylogenetic footprinting”:**  
perform MSA of input sequences  
(Multiple sequence alignment)  
  
find gapless conserved block of MSA  
  
represent it as a motif

### motif discovery algorithm

- a) Enumeration\*
- b) Expectation-Maximization (EM)
- a) Gibbs sampling\*

set of input sequences

database(s) of known motifs

**candidate motif(s)**

sequence (e.g. genome)

## Motif enrichment

find which known motifs might be overrepresented in an input set of sequences

## Motif comparison

compare candidate motif with known motifs

## Motif scanning

scan input sequence to find occurrences of the motif

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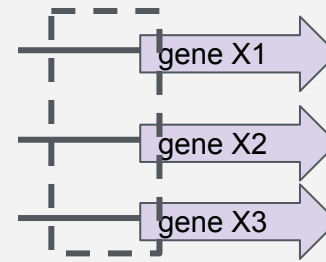
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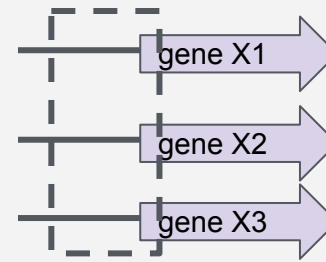
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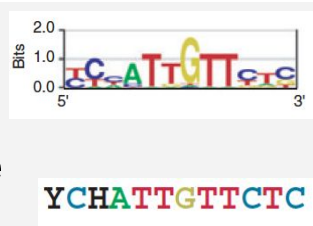
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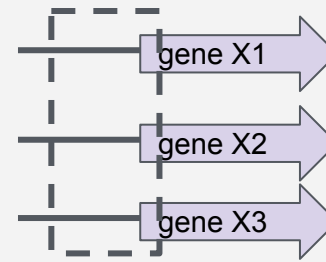


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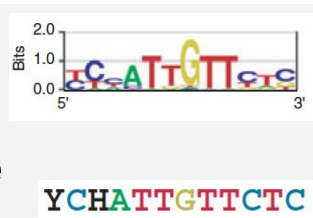
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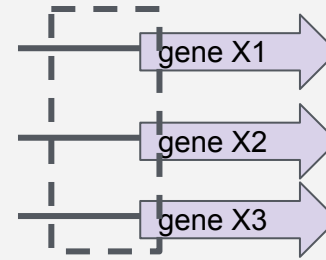
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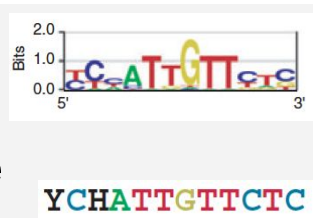
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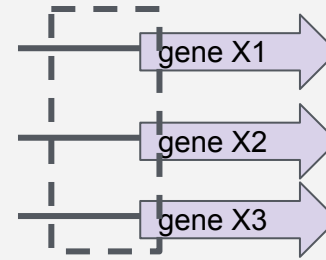
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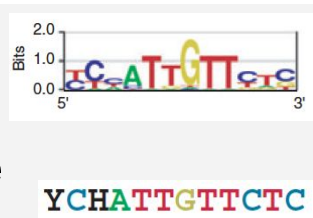
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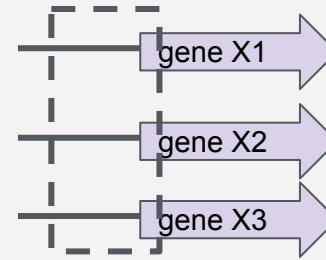
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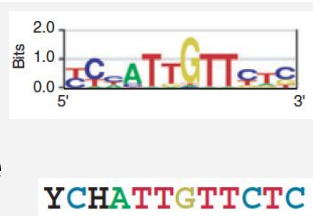
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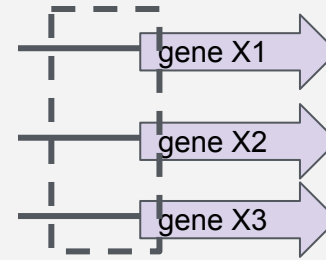
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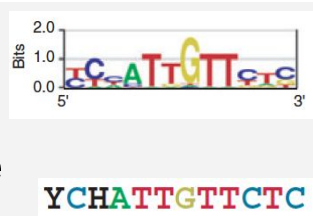
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**candidate motif(s)**

**How to use multiple sequence alignment for motif discovery  
(TASK 1)**

# Alignment

- Can be applied to any sequence (DNA, RNA, protein or other)
- Pairwise alignments (2 sequences):

```
ENSMUSG000000000 tgcattgttagcatctcttgataaacttaattgtctc---tcgtcactgacggcacagagctattgatgggtct
ENSG00000113520 tgcattgttagcatctcttgataaac-taattgcctcacattgtcactgcaaatacagacctaataatgggtct
***** ***** **** ***** ***** *** ***** * * ***** *****
```

- Multiple alignments ( $\geq 3$  sequences):

```
ENSG00000143632 ctggcatgtaggatgtgcctagggagataaacgggttttgcttttagttgtcgccaag-----gcagttcccttc
ENSMUSG000000031 ctgggatcaaatactgggctcttgtgatgcaagagggttggttgatctccactgagctacaccccagctcctgg
ENSRNOG000000017 ctgggatcaaatactgggcccttgtgatgcaagagggtgggctggatctccacagag-----ccagcccctgg
***** ** * ** ** * ** * * ** * * * * * * *
```



# Multiple sequence alignment may be used in:

- **phylogenetic analysis:** identify evolutionary relationships between sequences
- **structural bioinformatics:** detect similarities in structure or functions between proteins
- **motif search:** identify shared patterns between sequences

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# Alignment formats

## Clustal W:

```
CPZANT ATGGGAGCGGGGGCGTCTGTTTTGAGGGGAGAGAAGCTAGATACATGGGA
U455   ATGGGTGCGAGAGCGTCAGTATTAAGCGGGAAAAAATTAGATTCATGGGA

CPZANT AAGTATCAGGCTTCGGCCCCGGTGGCAAGAAAAAGTACATGATAAAACATC
U455   GAAAATTCGGTTAAGGCCAGGGGGAAACAAAAAATATAGACTGAAACATT

CPZANT TGGTTTGGGCAAGATCGGAGCTGCAGCGTTTTGCGCTCAGCTCCTCCCTT
U455   TAGTATGGGCAAGCAGGGAGCTGGAAAAATTCACACTTAACCCTGGCCTT

CPZANT CTAGAAACATCAGAAGGTTGTGAAAAGGCTATCCATCAATTGAGCCCTTC
U455   TTAGAAACAGCAGAAGGATGTCAGCAAATACTGGGACAATTACAACCAGC

CPZANT CATAGAAATAAGATCCCCTGAAATAATATCTTTGTTTAAACACCATTGTG
U455   TCTCCAGACAGGAACAGAAGAAGCTTAGATCATTATATAATACAGTAGCAG
```

## FastA:

```
>CPZANT
ATGGGAGCGGGGGCGTCTGTTTTGAGGGGAGAGAAGCTAGATACATGGGA
AAGTATCAGGCTTCGGCCCCGGTGGCAAGAAAAAGTACATGATAAAACATC
TGGTTTGGGCAAGATCGGAGCTGCAGCGTTTTGCGCTCAGCTCCTCCCTT
CTAGAAACATCAGAAGGTTGTGAAAAGGCTATCCATCAATTGAGCCCTTC
CATAGAAATAAGATCCCCTGAAATAATATCTTTGTTTAAACACCATTGTG
>U455
ATGGGTGCGAGAGCGTCAGTATTAAGCGGGAAAAAATTAGATTCATGGGA
GAAAATTCGGTTAAGGCCAGGGGGAAACAAAAAATATAGACTGAAACATT
TAGTATGGGCAAGCAGGGAGCTGGAAAAATTCACACTTAACCCTGGCCTT
TTAGAAACAGCAGAAGGATGTCAGCAAATACTGGGACAATTACAACCAGC
TCTCCAGACAGGAACAGAAGAAGCTTAGATCATTATATAATACAGTAGCAG
```

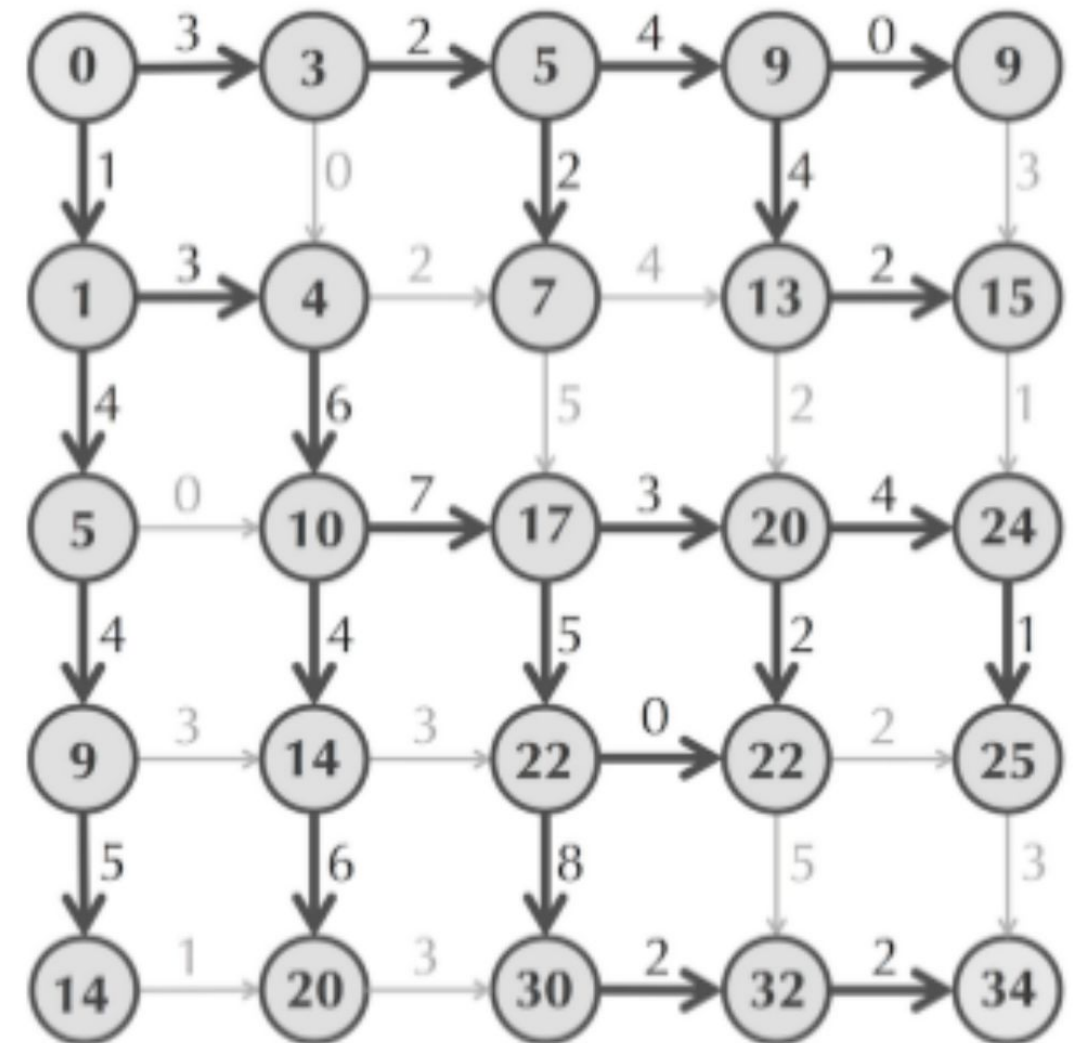
More examples:

<https://www.hiv.lanl.gov/content/sequence/HelpDocs/SEQsamples.html>

# Algorithms for multiple sequence alignment

- Ideal: **Dynamic Programming** – optimal solution but not computationally tractable
- **Heuristics\*** – approach to reduce the complexity of a problem (~make a computation faster):
  - progressive alignment construction
  - iterative methods
  - consensus methods
  - genetic algorithms

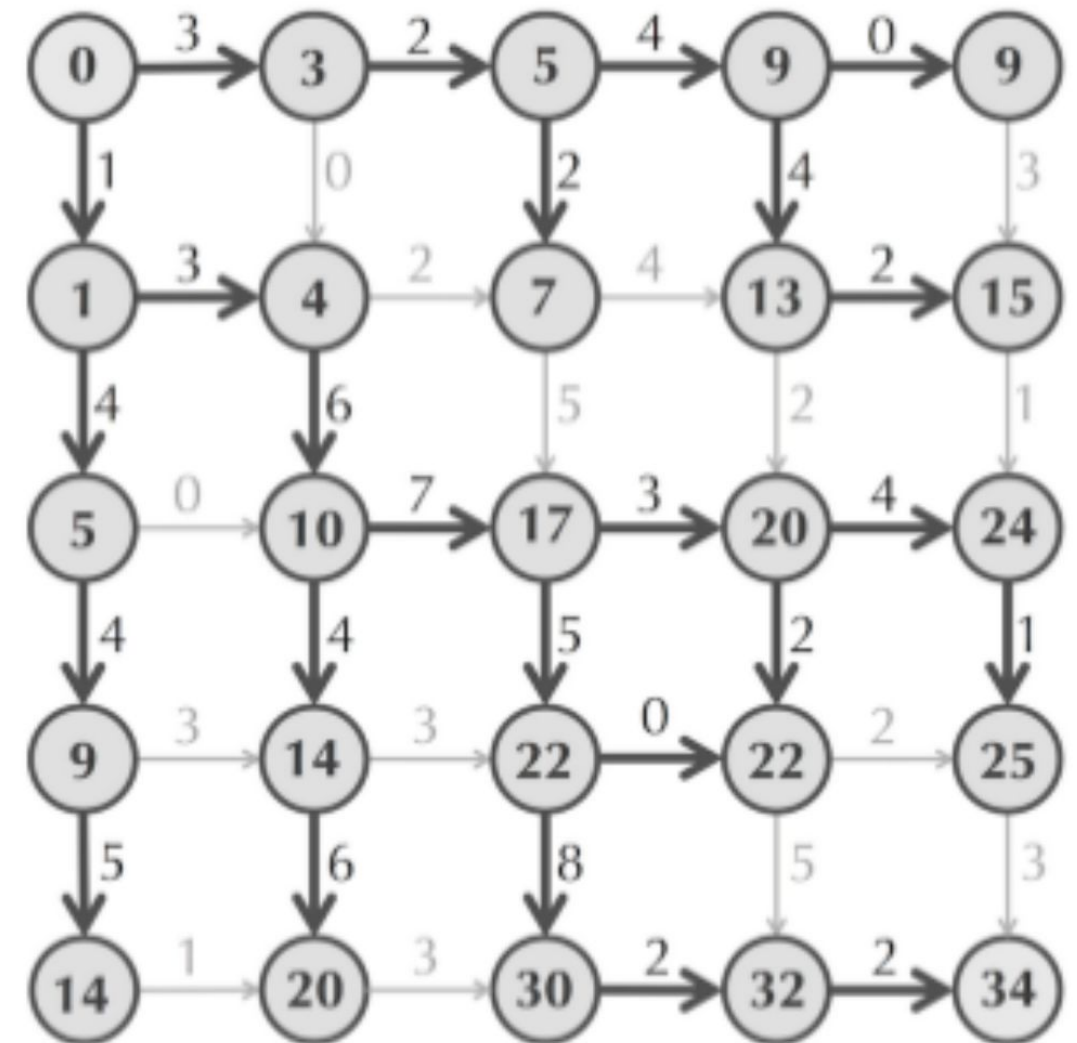
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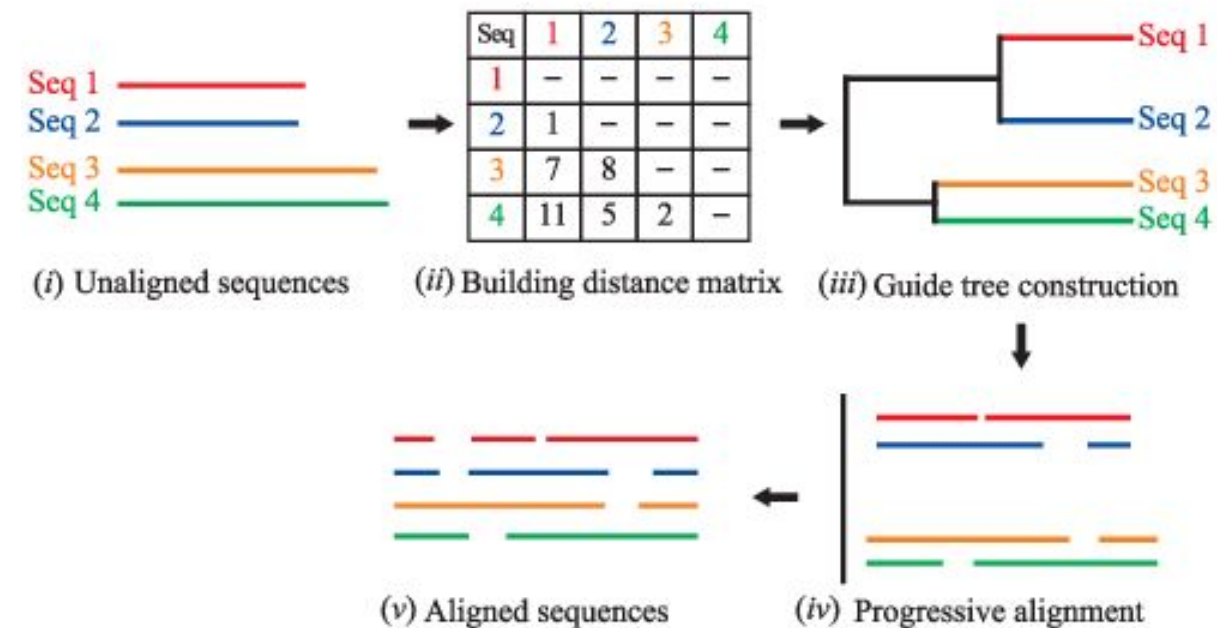
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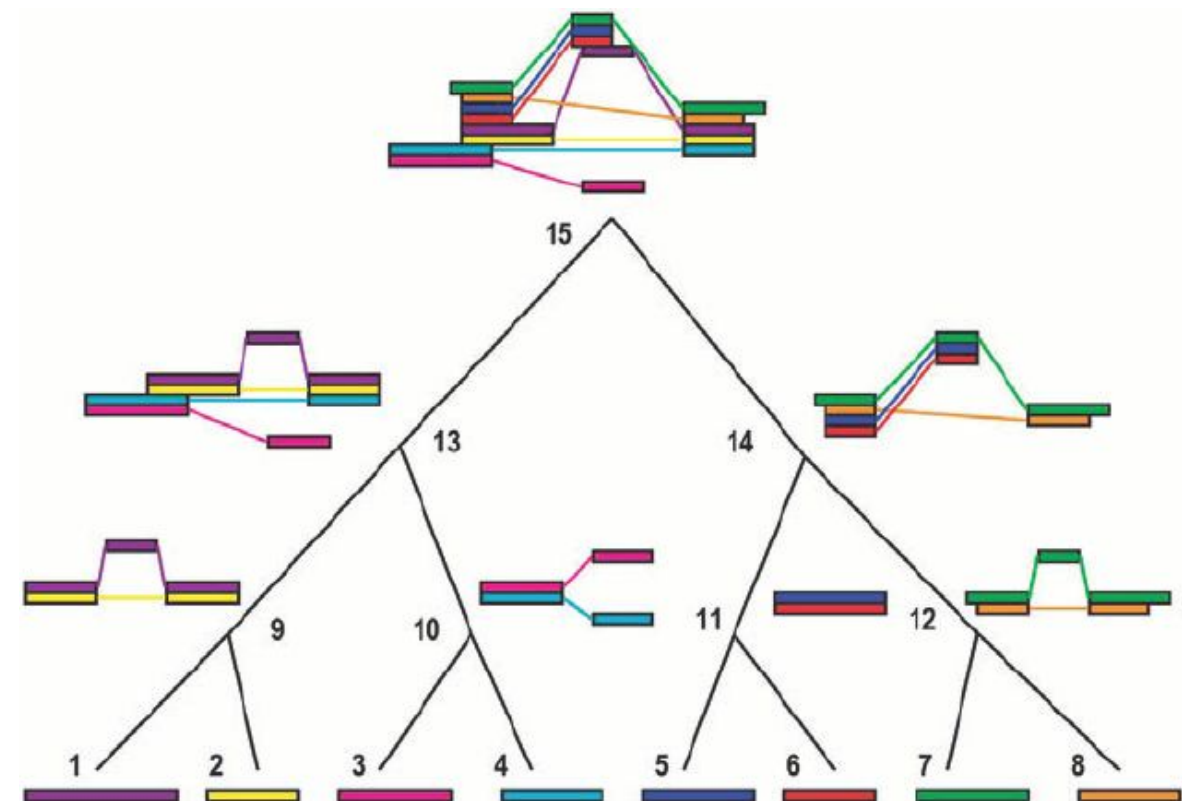


# Progressive alignments

1. Pairwise alignments (each pair of sequences)
2. Builds a distance matrix
3. Finds a guiding tree using one of clustering methods
4. Builds a multiple alignment progressively, starting from most similar sequences, stacking them as in the guiding tree



- + efficient enough to work with up to 1000 sequences
- does not provide a global optimal alignment
- errors in the first steps (e.g. erroneous gaps) do propagate to the final alignment



# Iterative methods

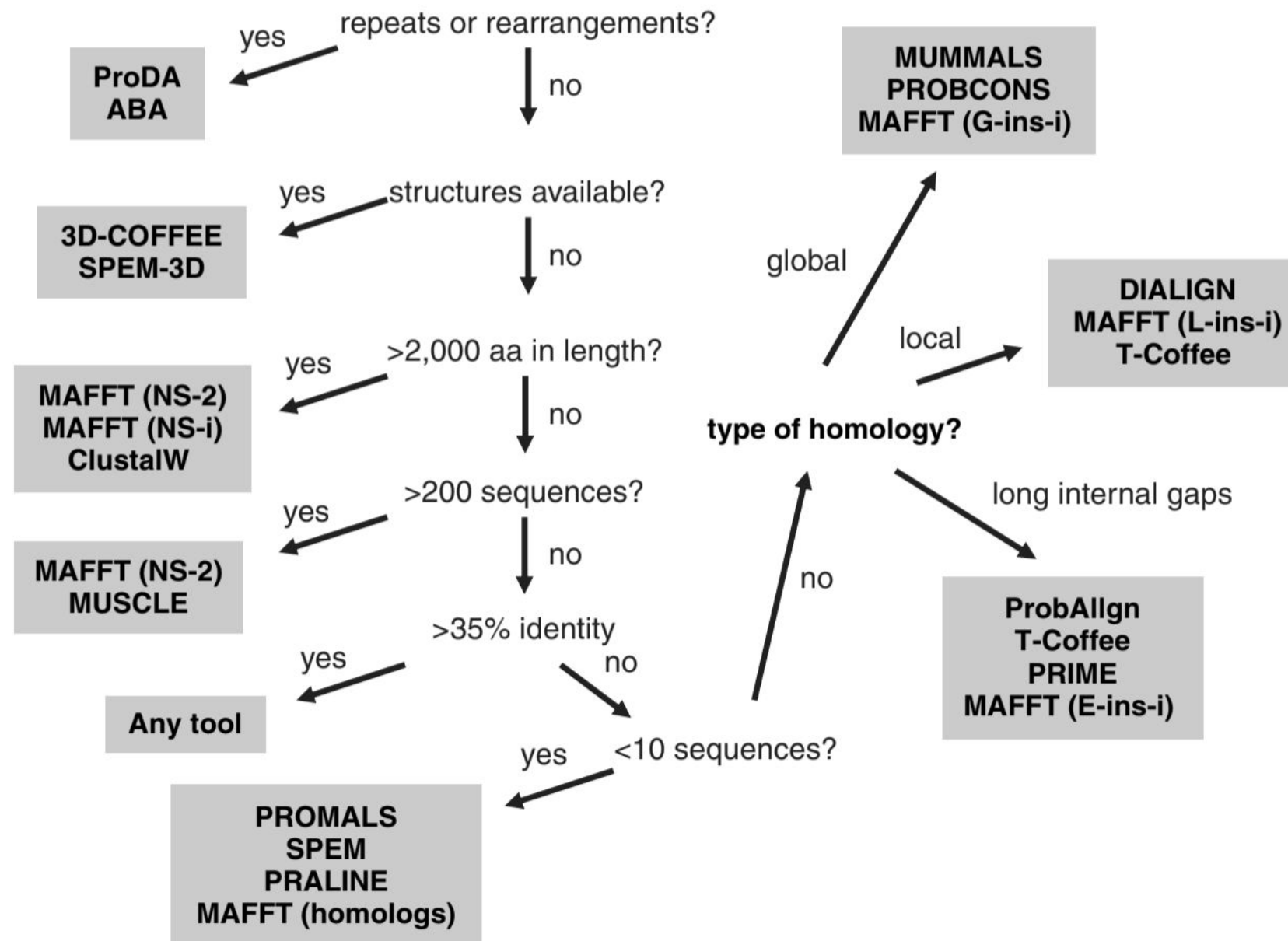
- works similar to progressive algorithms, but allows to realign the sequences in the alignment on each step
- optimizes a global metric
  - + less prone to error propagation, provides a more accurate result
  - + works fine with pairwise distant sequences
  - still heuristic
  - not as efficient as progressive algorithms

# Popular aligners

Aligner Algorithm	Type	Input	Comments
MUSCLE	Iterative	DNA, RNA, proteins	Widely used. Allows a lot of options
CLUSTAL Omega	Progressive	DNA, RNA, proteins	$O(N \log N)$ guide tree production allows over 100 000 sequences to be aligned. Can reuse existing alignment and append new sequences to them
T-Coffee	Progressive	DNA, RNA, proteins, structures	Wide range of flavors for different situations, e.g. DNA, RNA, proteins. Different modes for fast, accurate, memory-efficient aligning
MAFFT	Iterative	DNA, RNA, proteins	One of the most accurate algorithms for less than 100 sequences. Allows large gaps, making it suitable for rRNA alignments



# How to select your aligner?



# Popular aligners

- **ClustalW and ClustalO**

- documentation, servers and download page: <http://www.clustal.org/>
- try: `clustalw -INFILE=<fasta>` and `clustalo --auto --in <fasta>` in terminal

- **MUSCLE**

- documentation and download page: <http://www.drive5.com/muscle/>
- server: <https://www.ebi.ac.uk/Tools/msa/muscle/>
- try: `muscle -in <fasta>` in terminal

- **T-Coffee**

- Coffee family: <http://www.tcoffee.org/homepage.html>
- documentation, servers and download page: <http://www.tcoffee.org/Projects/tcoffee/>

- **MAFFT**

- documentation, servers and download page: <https://mafft.cbrc.jp/alignment/software/>

# How to run aligners?

- Online Tools through **Web Interface**, for small tasks for manual curation:
  - <https://www.ebi.ac.uk/Tools/msa/>
- **Standalone programs** for larger tasks and manual curation:
  - JalView: <https://www.jalview.org/>
  - MEGA
- From **bash terminal**: Command Line Interface (CLI), for the large and time-consuming tasks
- From **programming languages**, for full control over input/output:
  - BioPython in Python
  - SciKit-Bio for simple alignments and files parsing in Python
  - msa package for R

# Task 1 (Multiple Alignment)

## Instructions:

[https://github.com/rybinaanya/2022\\_Skoltech\\_Bioinformatics\\_course\\_seminar\\_4](https://github.com/rybinaanya/2022_Skoltech_Bioinformatics_course_seminar_4)

## Outline:

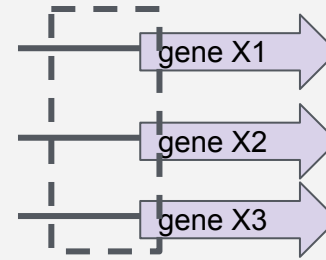
Download file with upstream regions of bacterial orthologs `upstreams.fasta`.  
Create multiple alignment with T-COFFEE, MUSCLE and CLUSTALW.  
Manually select the **most conserved gapless** region and save it into .fasta file.

# Motif discovery problem: flowchart

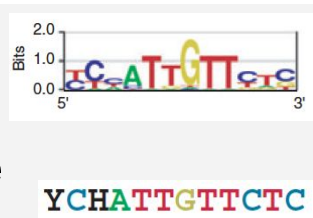
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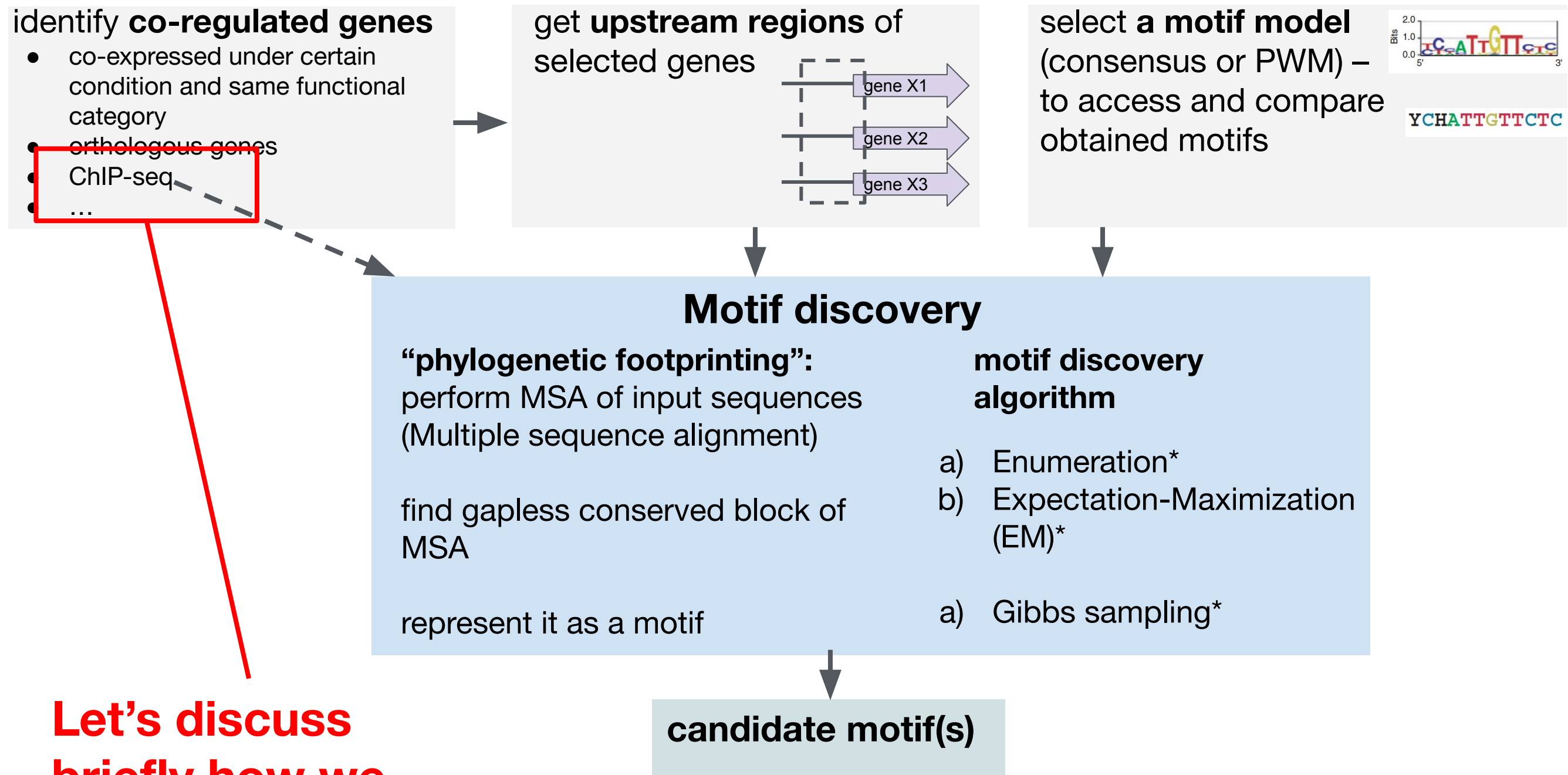
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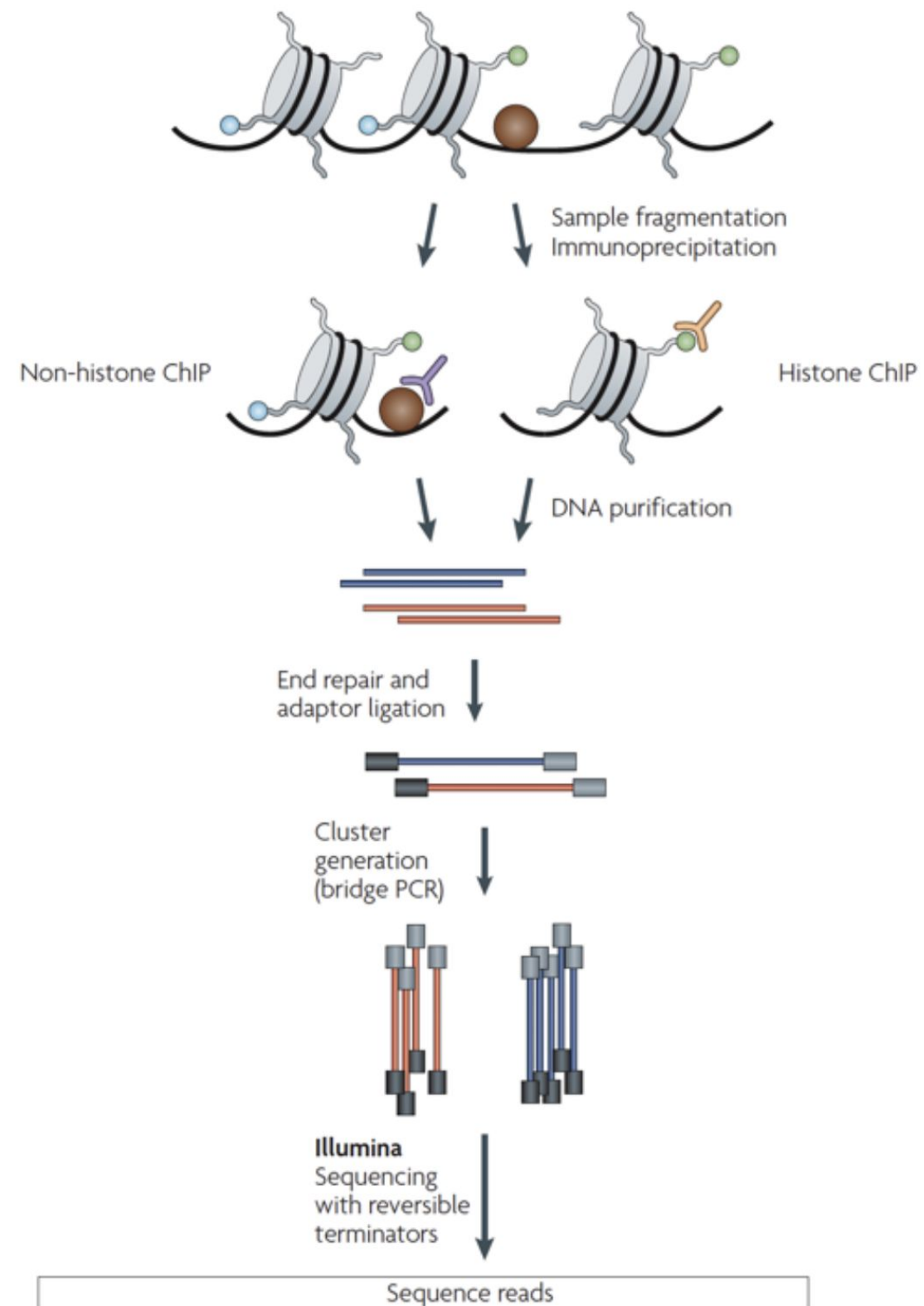
# Motif discovery problem: flowchart



**Let's discuss briefly how we may prepare a set of input sequences using ChIP-seq**

# ChIP-seq basics: sample preparation for NGS

Chromatin-immunoprecipitation followed by sequencing:

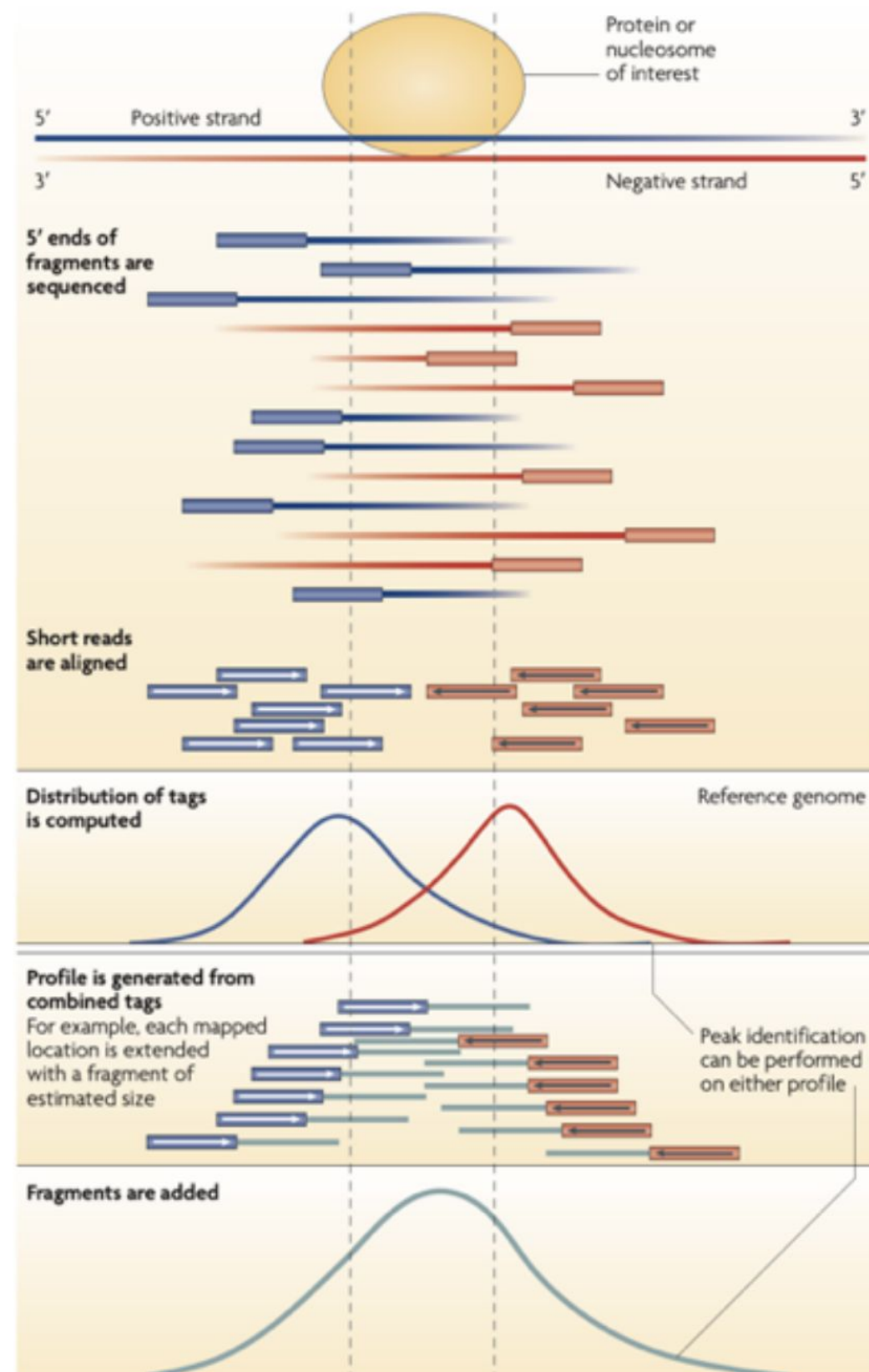




# ChIP-seq basics: NGS data analysis

Binding events:

Read alignments:



Peak calling:



# Motif search problem

Given a set of sequences find the motif (number of motifs, the width of each motif and its location in input sequences)

# Motif search: training attention

- Try to predict what is the regulatory motif in the following set of sequences:

```
atgaccgggatactgataaaaaaaagggggggggcggtacacattagataaacgtatgaagtacgttagactcggcgccgccg
accctatTTTTTgagcagatttagtgacctggaaaaaaaatttgagtacaaaactTTTccgaataaaaaaaaaaggggggga
tgagtatccctgggatgacttaaaaaaaaggggggggtgctctcccgattTTTgaatatgtaggatcattcgccaggggtccga
gctgagaattggatgaaaaaaaaggggggggtccacgcaatcgcgaaaccaacgcggacccaaaggcaagaccgataaaggaga
tccctTTTgcggtaatgtgccgggaggctgggttacgtaggggaagccctaacggacttaataaaaaaaaggggggggcttatag
gtcaatcatgttcttgtgaatggatttaaaaaaaagggggggggaccgcttggcgcacccaaattcagtggtgggcgagcgcaa
cggTTTTggcccttgtagaggcccccgtaaaaaaaaggggggggcaattatgagagagctaattctatcgcggtgcgtgttcat
aacttgagttaaaaaaaaggggggggctggggcacatacaagaggagtcttccttatcagttaatgctgtatgacactatgta
ttggcccattggctaaaagcccaacttgacaaatggaagatagaatccttgcataaaaaaaaggggggggaccgaaagggaag
ctggtgagcaacgacagattcttacgtgcattagctcgcttccgggggatctaatagcacgaagcttaaaaaaaagggggggga
```

# Motif search: training attention

- Seems to be easy:

atgaccgggatactgatAAAAAAAAAGGGGGGGggcggtacacattagataaacgtatgaagtacgttagactcggcgccgccg  
accctatTTTTTgagcagatttagtgacctggaaaaaaaatttgagtacaaaactTTTccgaataAAAAAAAAAGGGGGGGa  
tgagtatccctgggatgacttAAAAAAAAAGGGGGGGtgctctcccgattTTTgaatatgtaggatcattcgccagggtccga  
gctgagaattggatgAAAAAAAAAGGGGGGGtccacgcaatcgcgaaaccaacgcggacccaaaggcaagaccgataaaggaga  
tccctTTTgcggtaatgtgccgggaggctggttacgtaggggaagccctaacggacttaatAAAAAAAAAGGGGGGGcttatag  
gtcaatcatgttcttgtgaatggatttAAAAAAAAAGGGGGGGgaccgcttggcgcacccaaattcagtggtggcgagcgcaa  
cggTTTTggcccttggttagaggcccccgAAAAAAAAAGGGGGGGcaattatgagagagctaatactatcgcggtgcgtgttcat  
aacttgagttAAAAAAAAAGGGGGGGctggggcacatacaagaggagtcttccttatcagttaatgctgtatgacactatgta  
ttggcccattggctaaaagcccaacttgacaaatggaagatagaatccttgcatAAAAAAAAAGGGGGGGaccgaaagggaag  
ctggtgagcaacgacagattcttacgtgcattagctcgcttccgggggatctaatagcacgaagcttAAAAAAAAAGGGGGGGa



# Motif search: training attention

- Let's introduce some substitutions:

atgaccgggatactgatAgAAgAAAGGttGGGggcggtacacattagataaacgtatgaagtacgtttagactcggcgccgcccg  
accctatTTTTTgagcagatttagtgacctggaaaaaaaaatttgagtacaaaactTTTccgaataCAAtAAAAcGGcGGGa  
tgagtatccctgggatgacttAAAAtAAtGGaGtGGtgctctcccgattTTTgaatatgtaggatcattcgccaggggtccga  
gctgagaattggatgCAAAAAAGGGattGtccacgcaatcgcgaaaccaacgcggacccaaaggcaagaccgataaaggaga  
tccctTTTgcggtaatgtgccgggaggctggttacgtagggaagccctaacggacttaatAtAAtAAAGGaGgGccttatag  
gtcaatcatgttcttgtgaatggatttAAcAAtAAGGGctGGgaccgcttggcgcacccaaattcagtgtgggcgagcgcaa  
cggTTTTggcccttgtagaggcccccgAtAAAcAAGGaGGGccaattatgagagagctaatactatcgcggtgcgtgttcat  
aacttgagttAAAAAtAGGGaGccctggggcacatacaagaggagtcttccttatcagttaatgctgtatgacactatgta  
ttggcccatTggctaaaagcccaacttgacaaatggaagatagaatccttgcatActAAAAAGGaGcGGaccgaaagggaag  
ctggtgagcaacgacagattcttacgtgcattagctcgcttccggggatctaatagcacgaagcttActAAAAAGGaGcGGa

# Motif search: training attention

- Is everything easy if you know the answer?

atgaccgggatactgatagaagaaagggttggggggcgtagacattagataaacgtatgaagtacgtttagactcggcgccgcccg  
accctatTTTTTgagcagatttagtgacctggaaaaaaaaatttgagtacaaaacttttccgaatacaataaaacggcgggga  
tgagtatccctgggatgacttaaaataatggagtggtgctctcccgatttttgaatatgtaggatcattcgccaggggtccga  
gctgagaattggatgcaaaaaaagggttgtccacgcaatcgcgaaaccaacgcggacccaaaggcaagaccgataaaggaga  
tcccttttgcggtaatgtgccgggaggctgggttacgtagggaagccctaacggacttaataataaaggaagggcttatag  
gtcaatcatgttcttgtgaatggatttaacaataagggctgggaccgcttggcgcacccaaattcagtggtggcgagcgcaa  
cggttttggcccttgtagaggcccccgataaacaaggaggggccaattatgagagagctaatactatcgcggtgcgtgttcat  
aacttgagttaaaaaataggagaccctggggcacatacaagaggagtcttccttatcagttaatgctgtatgacactatgta  
ttggcccattggctaaaagcccaacttgacaaatggaagatagaatccttgcataactaaaaggagcggaccgaaagggaag  
ctggtgagcaacgacagattcttacgtgcattagctcgcttccgggggatctaatagcacgaagcttactaaaaaggagcgga

# Motif search problem

Given a set of sequences find the motif (number of motifs, the width of each motif and its location in input sequences)

## **Challenge:**

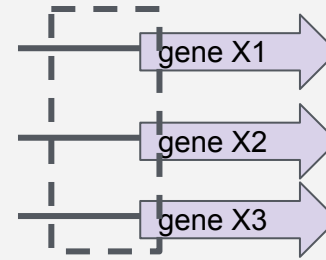
- input sequences could be long (up to thousands and millions)
- motifs are short and could be only slightly similar (due to substitutions)
- we need to distinguish a motif (“signal”) from genomic noise (uninformative background DNA)

# Motif discovery problem: flowchart

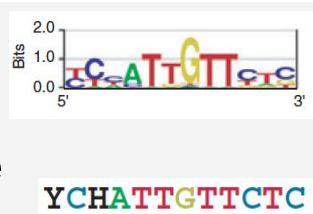
## identify **co-regulated genes**

- co-expressed under certain condition and same functional category
- orthologous genes
- ChIP-seq
- ...

## get **upstream regions** of selected genes



## select a **motif model** (consensus or PWM) – to access and compare obtained motifs



## Motif discovery

### “**phylogenetic footprinting**”:

perform MSA of input sequences  
(Multiple sequence alignment)

find gapless conserved block of  
MSA

represent it as a motif

### **motif discovery algorithm**

- a) Enumeration\*
- b) Expectation-Maximization (EM)\*
- a) Gibbs sampling\*

**candidate motif(s)**

**To compare, assess, rank motifs, we need a scoring metric and model (way of representation) for motifs**



# Motif representation (motif models)

TATAAT

TAAAAT

TAATAT – set of candidate motifs

TGTAAT

TATACT

- consensus sequence – T [AG] [AT] [AT] [AC] T

- position frequency matrix (PFM), or position count matrix (PCM) –

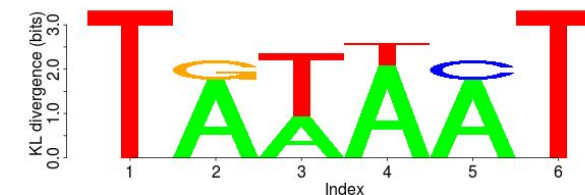
	1	2	3	4	5	6
A	0	4	2	4	4	0
C	0	0	0	0	1	0
G	0	1	0	0	0	0
T	5	0	3	1	0	5

- position probability matrix (PPM) –

	1	2	3	4	5	6
A	0.0	0.8	0.4	0.8	0.8	0.0
C	0.0	0.0	0.0	0.0	0.2	0.0
G	0.0	0.2	0.0	0.0	0.0	0.0
T	1.0	0.0	0.6	0.2	0.0	1.0

- position-specific weight matrix (PWM)

- information content matrix, or sequence logo –





# Motif representation: consensus sequence

**Consensus sequence** lists nucleotides that are allowed in given position.  
Consider following **gapless block of an alignment**:

TATAAT

TAAAAT

TAATAT

TGTAAT

TATACT

**Its consensus:**    T [AG] [AT] [AT] [AC] T

## **Problems:**

- Doesn't allow to incorporate different preferences for different nucleotides,
- Doesn't allow to account for background nucleotides frequencies.

# Motif representation

```
123456  
TATAAT  
TAAAAT  
TAATAT  
TGTAAT  
TATACT
```

Consider a set of  
candidate motifs obtained  
from multiple sequence  
alignment



# Motif representation: position **probability** matrix

123456	position <b>count</b> matrix PCM (position <b>frequency</b> matrix PFM)							position <b>probability</b> matrix PPM						
		1	2	3	4	5	6		1	2	3	4	5	6
TATAAT	A	0	4	2	4	4	0	A	0.0	0.8	0.4	0.8	0.8	0.0
TAAAAT	C	0	0	0	0	1	0	C	0.0	0.0	0.0	0.0	0.2	0.0
TAATAT	G	0	1	0	0	0	0	G	0.0	0.2	0.0	0.0	0.0	0.0
TGTAAT	T	5	0	3	1	0	5	T	1.0	0.0	0.6	0.2	0.0	1.0
TATACT														

count / (number of input sequences)

😊 PPM **normalizes** the count matrix by the **number of observations**, resulting in an estimate for the probability of observing each letter at a given position  $\Rightarrow$  Motif representation **no longer depends on the number of sequences aligned**

# Motif representation: position **probability** matrix

123456	position <b>count</b> matrix PCM (position <b>frequency</b> matrix PFM)							position <b>probability</b> matrix PPM						
		1	2	3	4	5	6		1	2	3	4	5	6
TATAAT	A	0	4	2	4	4	0	A	0.0	0.8	0.4	0.8	0.8	0.0
TAAAAT	C	0	0	0	0	1	0	C	0.0	0.0	0.0	0.0	0.2	0.0
TAATAT	G	0	1	0	0	0	0	G	0.0	0.2	0.0	0.0	0.0	0.0
TGTAAT	T	5	0	3	1	0	5	T	1.0	0.0	0.6	0.2	0.0	1.0
TATACT														

count / (number of input sequences)

😊 PPM **normalizes** the count matrix by the **number of observations**, resulting in an estimate for the probability of observing each letter at a given position  $\Rightarrow$  Motif representation **no longer depends on the number of sequences aligned**

😓 it does not give us any idea of how “surprising” it would be to observe any given sequence that matches the motif. We need estimate the probability that this observed pattern can be found by chance in the genome. **We need to distinguish informative pattern** (e.g. specific binding, recognized by TF) **from “uninformative” genomic “noise”** (non-specific sites, e.g. not recognized by TF). We need to consider this noise



# Motif representation: position **weight** matrix

	position <b>count</b> matrix PCM (position <b>frequency</b> matrix PFM)							position <b>probability</b> matrix PPM						
123456		1	2	3	4	5	6		1	2	3	4	5	6
TATAAT	A	0	4	2	4	4	0	A	0.0	0.8	0.4	0.8	0.8	0.0
TAAAAT	C	0	0	0	0	1	0	C	0.0	0.0	0.0	0.0	0.2	0.0
TAATAT	G	0	1	0	0	0	0	G	0.0	0.2	0.0	0.0	0.0	0.0
TGTAAT	T	5	0	3	1	0	5	T	1.0	0.0	0.6	0.2	0.0	1.0
TATACT														

$$M_{p,n} = \log_2 \left( \frac{p_{p,n}}{b_n} \right)$$

$p_{p,n}$  is probability of nucleotide  $n$  in position  $p$  (column)

$b_n$  is probability of nucleotide  $n$  in background

“**Background**” refers here to the base composition at **non-specific** sites (i.e. here, sequences that do not necessarily bind the TF). Background is **uniform** ( $b_n = 1/4$ ) or **genome-wide frequencies**

	1	2	3	4	5	6
A	-Inf	1.6	0.6	1.6	1.6	-Inf
C	-Inf	-Inf	-Inf	-Inf	-0.3	-Inf
G	-Inf	-0.3	-Inf	-Inf	-Inf	-Inf
T	2	-Inf	1.2	-0.3	-Inf	2

# Motif representation: position **weight** matrix

	position <b>count</b> matrix PCM (position <b>frequency</b> matrix PFM)							position <b>probability</b> matrix PPM						
123456		1	2	3	4	5	6		1	2	3	4	5	6
TATAAT	A	0	4	2	4	4	0	A	0.0	0.8	0.4	0.8	0.8	0.0
TAAAAT	C	0	0	0	0	1	0	C	0.0	0.0	0.0	0.0	0.2	0.0
TAATAT	G	0	1	0	0	0	0	G	0.0	0.2	0.0	0.0	0.0	0.0
TGTAAT	T	5	0	3	1	0	5	T	1.0	0.0	0.6	0.2	0.0	1.0
TATACT														

$$M_{p,n} = \log_2 \left( \frac{p_{p,n}}{b_n} \right)$$

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	1	2	3	4	5	6
A	-Inf	1.6	0.6	1.6	1.6	-Inf
C	-Inf	-Inf	-Inf	-Inf	-0.3	-Inf
G	-Inf	-0.3	-Inf	-Inf	-Inf	-Inf
T	2	-Inf	1.2	-0.3	-Inf	2



But we've got infinity in the matrix!

In small datasets, there is always a chance that a possible event does not occur (zeros in count/frequency matrix -> infinity in weight matrix).

To consider rare events and eliminate empirical zero frequencies, we use **pseudocounts**. We will add **pseudocount to each count** in count matrix



# Motif representation: position weight matrix

		position <b>count</b> matrix PCM (position <b>frequency</b> matrix PFM)							position <b>probability</b> matrix PPM					
123456		1	2	3	4	5	6		1	2	3	4	5	6
TATAAT	A	0	4	2	4	4	0	A	0.0	0.8	0.4	0.8	0.8	0.0
TAAAAT	C	0	0	0	0	1	0	C	0.0	0.0	0.0	0.0	0.2	0.0
TAATAT	G	0	1	0	0	0	0	G	0.0	0.2	0.0	0.0	0.0	0.0
TGTAAT	T	5	0	3	1	0	5	T	1.0	0.0	0.6	0.2	0.0	1.0
TATACT														

$$M_{p,n} = \log_2 \left( \frac{p_{p,n}}{b_n} \right)$$

$p_{p,n}$  is probability of nucleotide  $n$  in position  $p$  (column)

$b_n$  is probability of nucleotide  $n$  in background

“**Background**” refers here to the base composition at **non-specific** sites (i.e. here, sequences that do not necessarily bind the TF). Background is **uniform** ( $b_n = 1/4$ ) or **genome-wide frequencies**

Add pseudocounts (for example, 1), to frequency matrix to evade infinity in PWMs. Pseudocounts reflect the fact, that any sequence can be bound by the protein. But some of them are bound with very low probability

	1	2	3	4	5	6
A	-Inf	1.6	0.6	1.6	1.6	-Inf
C	-Inf	-Inf	-Inf	-Inf	-0.3	-Inf
G	-Inf	-0.3	-Inf	-Inf	-Inf	-Inf
T	2	-Inf	1.2	-0.3	-Inf	2

	1	2	3	4	5	6
A	-1.2	1.2	0.4	1.2	1.2	-1.2
C	-1.2	-1.2	-1.2	-1.2	-0.2	-1.2
G	-1.2	-0.2	-1.2	-1.2	-1.2	-1.2
T	1.4	-1.2	0.8	-0.2	-1.2	1.4

position **weight**  
matrix PWM

# Motif representation: sequence logo

**Relative entropy** (Kullback-Leibler distance) of the binding site with respect to the background frequencies:

$$I_{seq}(i) = -\sum_b f_{b,i} \log_2 \frac{f_{b,i}}{p_b}$$

the frequency of base b at position i

the background frequency of base b in the genome

Relative entropy measures the degree of disagreement (**dissimilarity**) **between the observed and background base frequencies**, and thus can be used to calculate the significance of the motif itself

# Motif representation: sequence logo

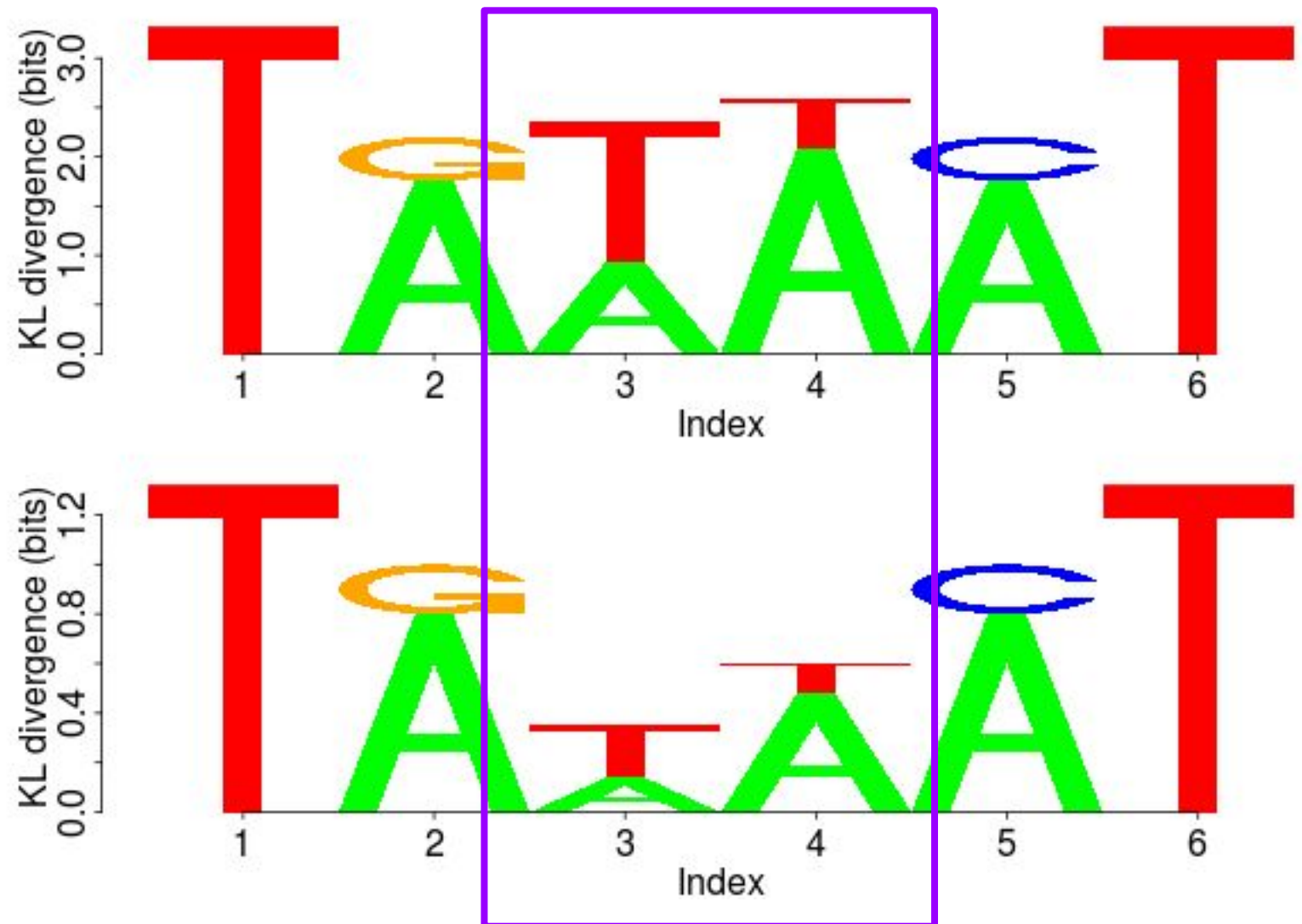
Height of each column is significance of the position (dissimilarity to background).

Relative size of the letter is a frequency of the nucleotide.

$$I_{seq}(i) = -\sum_b f_{b,i} \log_2 \frac{f_{b,i}}{p_b}$$

GC-rich  
background:  
  
appearance of T and A is more  
significant in the GC-rich  
background than in the AT-rich  
(=low-GC) background

AT-rich  
background:





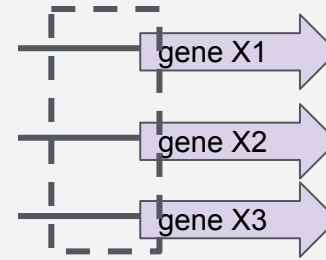
# Motif discovery problem: flowchart

## identify **co-regulated genes**

- co-expressed under certain condition and same functional category
- orthologous genes
- ChIP-seq
- ...



## get **upstream regions** of selected genes



## select a **motif model** (consensus or PWM) – to access and compare obtained motifs



YCHATTGTTCTC



## Motif discovery

### “**phylogenetic footprinting**”:

perform MSA of input sequences  
(Multiple sequence alignment)

find gapless conserved block of  
MSA

represent it as a motif

### **motif discovery algorithm**

- a) Enumeration\*
- b) Expectation-Maximization (EM)\*
- a) Gibbs sampling\*

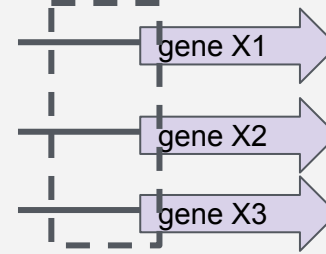
**candidate motif(s)**

# Motif discovery problem: flowchart

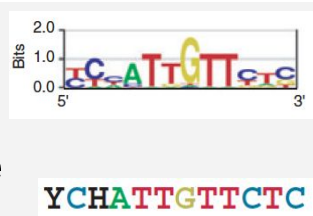
## identify **co-regulated genes**

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- ...

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## Motif discovery

**“phylogenetic footprinting”:**  
perform MSA of input sequences  
(Multiple sequence alignment)

find gapless conserved block of  
MSA

represent it as a motif

## motif discovery algorithm

- a) Enumeration\*
- b) Expectation-Maximization (EM)\*
- a) Gibbs sampling\*

database(s) of  
known motifs

**candidate motif(s)**

## Motif comparison

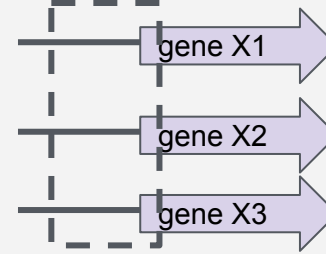
compare candidate  
motif with known motifs

# Motif discovery problem: flowchart

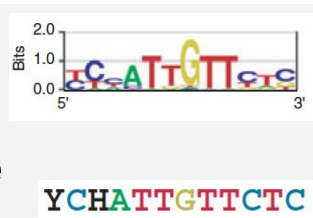
## identify **co-regulated genes**

- co-expressed under certain condition and same functional category
- orthologous genes
- ChIP-seq
- ...

## get **upstream regions** of selected genes



## select a **motif model** (consensus or PWM) – to access and compare obtained motifs



## Motif discovery

**“phylogenetic footprinting”:**  
perform MSA of input sequences  
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MSA

represent it as a motif

## motif discovery algorithm

- a) Enumeration\*
- b) Expectation-Maximization (EM)\*
- a) Gibbs sampling\*

database(s) of  
known motifs

**candidate motif(s)**

**Motif comparison**  
compare candidate  
motif with known motifs

**Tasks 2 – 4**

# Some tools for motifs search and manipulation

## Web server tools:

- <http://rsat.eu/>
- <http://meme-suite.org/>

## Console tools:

- <https://gimmemotifs.readthedocs.io/en/master/>
- <http://autosome.ru/>

## Tools embedded in **programming languages**:

- BioPython motifs



# Task 2-4 (Motif search)

All the **materials** for this seminar are located in Canvas and on GitHub:

[https://github.com/rybinaanya/2022\\_Skoltech\\_Bioinformatics\\_course\\_seminar\\_4](https://github.com/rybinaanya/2022_Skoltech_Bioinformatics_course_seminar_4)

Go to **instructions**:

[https://github.com/rybinaanya/2022\\_Skoltech\\_Bioinformatics\\_course\\_seminar\\_4](https://github.com/rybinaanya/2022_Skoltech_Bioinformatics_course_seminar_4)

## Outline

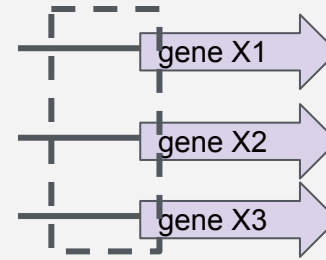
- Create counts, frequencies, weights matrices and logo from gapless alignment with RSAT tools: <http://embnet.ccg.unam.mx/rsat/> -> Matrix tools.
- Process the same set of sequences `upstreams.fasta` with MEME: <http://meme-suite.org/>. Set possible length of motif from 5 to 15. Is the result similar to what you found manually?
- Download file with peaks sequences from the given **chicken** ChIP-Seq (`peaks.fasta`).  
Find motifs with MEME-ChIP (<http://meme-suite.org/> -> MEME-ChIP).  
What was the protein used for ChIP-Seq?
- Repeat for **your peak file** assigned to you in Canvas (see Files for this seminar).

# Motif discovery problem: flowchart

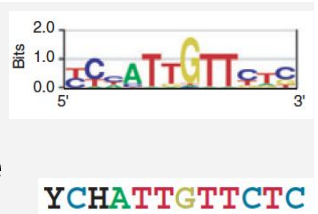
## identify **co-regulated genes**

- co-expressed under certain condition and same functional category
- orthologous genes
- ChIP-seq
- ...

## get **upstream regions** of selected genes



## select a **motif model** (consensus or PWM) – to access and compare obtained motifs



## Motif discovery

**“phylogenetic footprinting”:**  
perform MSA of input sequences  
(Multiple sequence alignment)

find gapless conserved block of MSA

represent it as a motif

## motif discovery algorithm

- a) Enumeration\*
- b) Expectation-Maximization (EM)\*
- a) Gibbs sampling\*

set of input sequences

database(s) of known motifs

**candidate motif(s)**

sequence (e.g. genome)

## Motif enrichment

find which known motifs might be overrepresented in an input set of sequences

## Motif comparison

compare candidate motif with known motifs

## Motif scanning

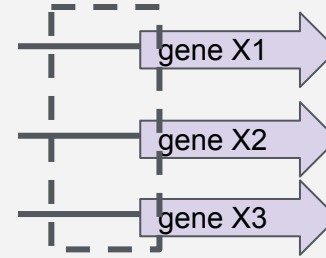
scan input sequence to find occurrences of the motif

# Motif discovery problem: flowchart

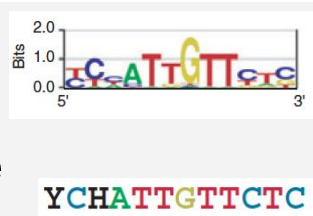
## identify **co-regulated genes**

- co-expressed under certain condition and same functional category
- orthologous genes
- ChIP-seq
- ...

## get **upstream regions** of selected genes



## select a **motif model** (consensus or PWM) – to access and compare obtained motifs



## Motif discovery

**“phylogenetic footprinting”:**  
perform MSA of input sequences  
(Multiple sequence alignment)  
  
find gapless conserved block of MSA  
  
represent it as a motif

### motif discovery algorithm

- a) Enumeration\*
- b) Expectation-Maximization (EM)\*
- a) Gibbs sampling\*

**Let's discuss general idea**

set of input sequences

database(s) of known motifs

**candidate motif(s)**

sequence (e.g. genome)

## Motif enrichment

find which known motifs might be overrepresented in an input set of sequences

## Motif comparison

compare candidate motif with known motifs

## Motif scanning

scan input sequence to find occurrences of the motif

# Motif scanning: estimate how well input sequence matches the motif

- Let's imagine that we know particular motif and its PWM for some protein. How can we find the binding sites of this protein in the genome?

input data:



motif logo

given sequence  
(e.g. genome)

# Motif scanning: estimate how well input sequence matches the motif

- Let's imagine that we know particular motif and its PWM for some protein. How can we find the binding sites of this protein in the genome?

input data:



motif logo

given sequence  
(e.g. genome)

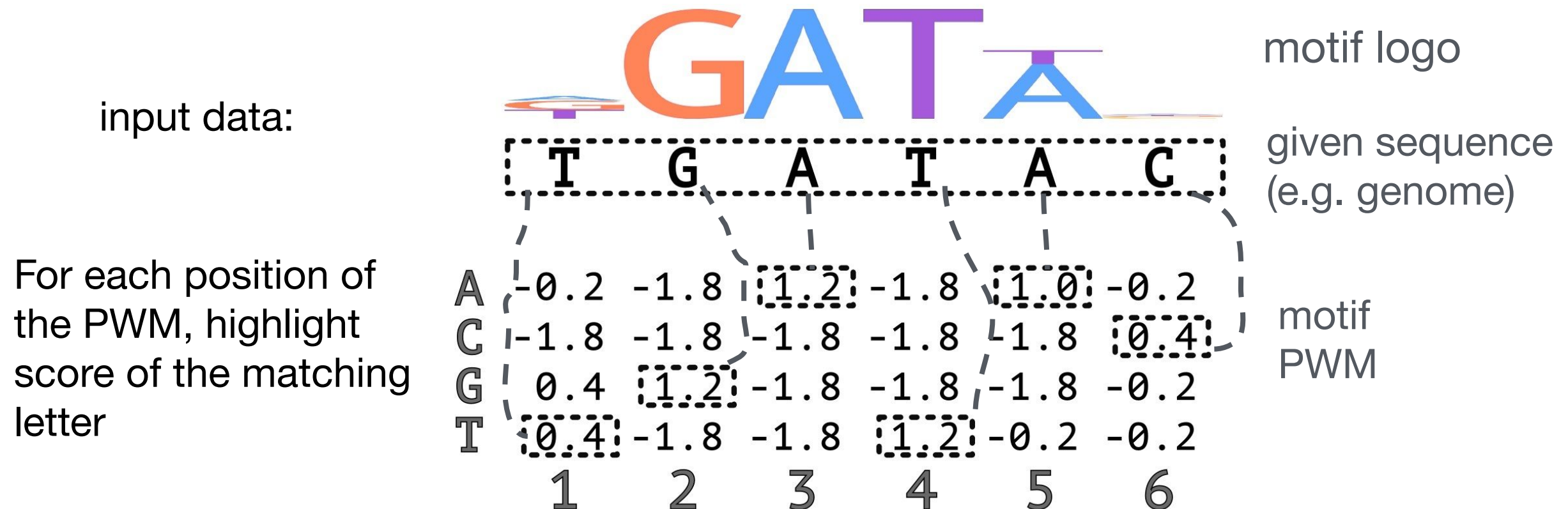
For each position of the PWM, highlight score of the matching letter

A	-0.2	-1.8	[1.2]	-1.8	[1.0]	-0.2
C	-1.8	-1.8	-1.8	-1.8	-1.8	[0.4]
G	0.4	[1.2]	-1.8	-1.8	-1.8	-0.2
T	[0.4]	-1.8	-1.8	[1.2]	-0.2	-0.2
	1	2	3	4	5	6

motif  
PWM

# Motif scanning: estimate how well input sequence matches the motif

- Let's imagine that we know particular motif and its PWM for some protein. How can we find the binding sites of this protein in the genome?





# Motif scanning: estimate how well input sequence matches the motif

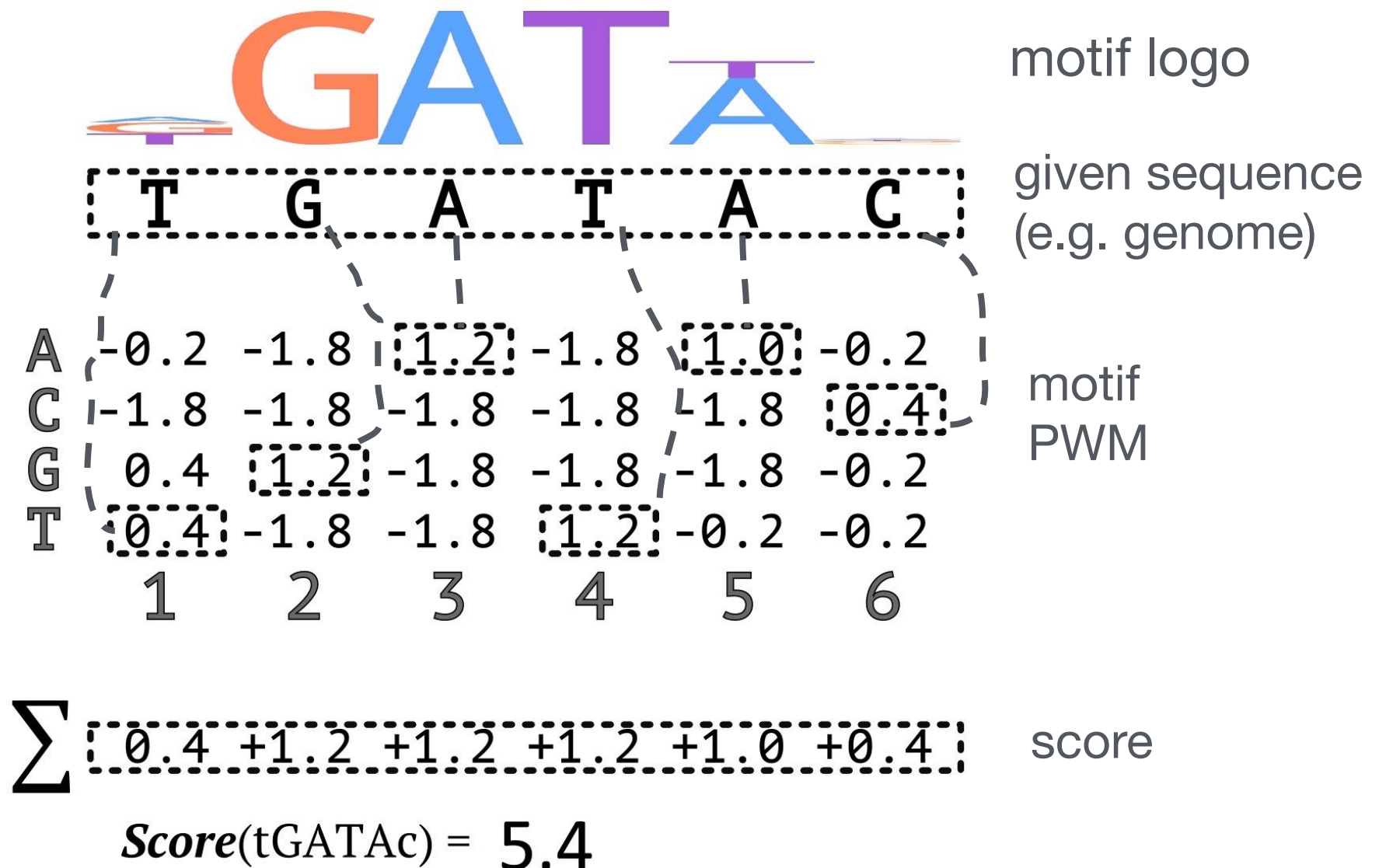
- Let's imagine that we know particular motif and its PWM for some protein. How can we find the binding sites of this protein in the genome?

input data:

For each position of the PWM, highlight score of the matching letter

A sequence's score for a given motif represents how well the sequence matches the motif


- Additivity assumption: score is larger for longer sequences!





# Motif scanning: select the score threshold to mark candidate binding sites

## Motif model (e.g. positional weight matrix, PWM)

	1	2	3	4	5	6	
A	-1.6	-1.6	0.96	-1.6	-1.6	0.96	 PWM GGATTA → $S_{\text{GGATTA}} = 1.22 + 1.22 + 0.96 + 1.22 + 1.22 + 0.96 = \mathbf{6.8}$ $S_{\text{GGGGGG}} = 2.44 - 6.4 = \mathbf{-3.96}$ $S = \mathbf{-9.6}$ the worst score the best score
C	-1.6	-1.6	0.00	-1.6	-1.6	-1.6	
G	1.22	1.22	-1.6	-1.6	-1.6	-1.6	
T	-1.6	-1.6	-1.6	1.22	1.22	0.00	

a) **S<sub>min</sub>** as threshold:

**False positive:**  $S_{\text{GGGGGG}} = -3.96 > S_{\text{min}} = -9.6 \Rightarrow$   
 $S_{\text{GGGGGG}}$  has passed but it is not a true motif! not cool

a) **S<sub>max</sub>** as threshold:

$S_{\text{GGGGGG}} = -3.96 < S_{\text{max}} = 6.8 \Rightarrow S_{\text{GGGGGG}}$  is rejected  
and it is not true motif, everything is ok

# Motif scanning: select the score threshold to mark candidate binding sites

## Motif model (e.g. positional weight matrix, PWM)

	1	2	3	4	5	6
A	-1.6	-1.6	0.96	-1.6	-1.6	0.96
C	-1.6	-1.6	0.00	-1.6	-1.6	-1.6
G	1.22	1.22	-1.6	-1.6	-1.6	-1.6
T	-1.6	-1.6	-1.6	1.22	1.22	0.00



PWM

GGATTA

$$S_{\text{GGATTA}} = 1.22 + 1.22 + 0.96 + 1.22 + 1.22 + 0.96 = \mathbf{6.8}$$

$$S_{\text{GGGGGG}} = 2.44 - 6.4 = \mathbf{-3.96}$$

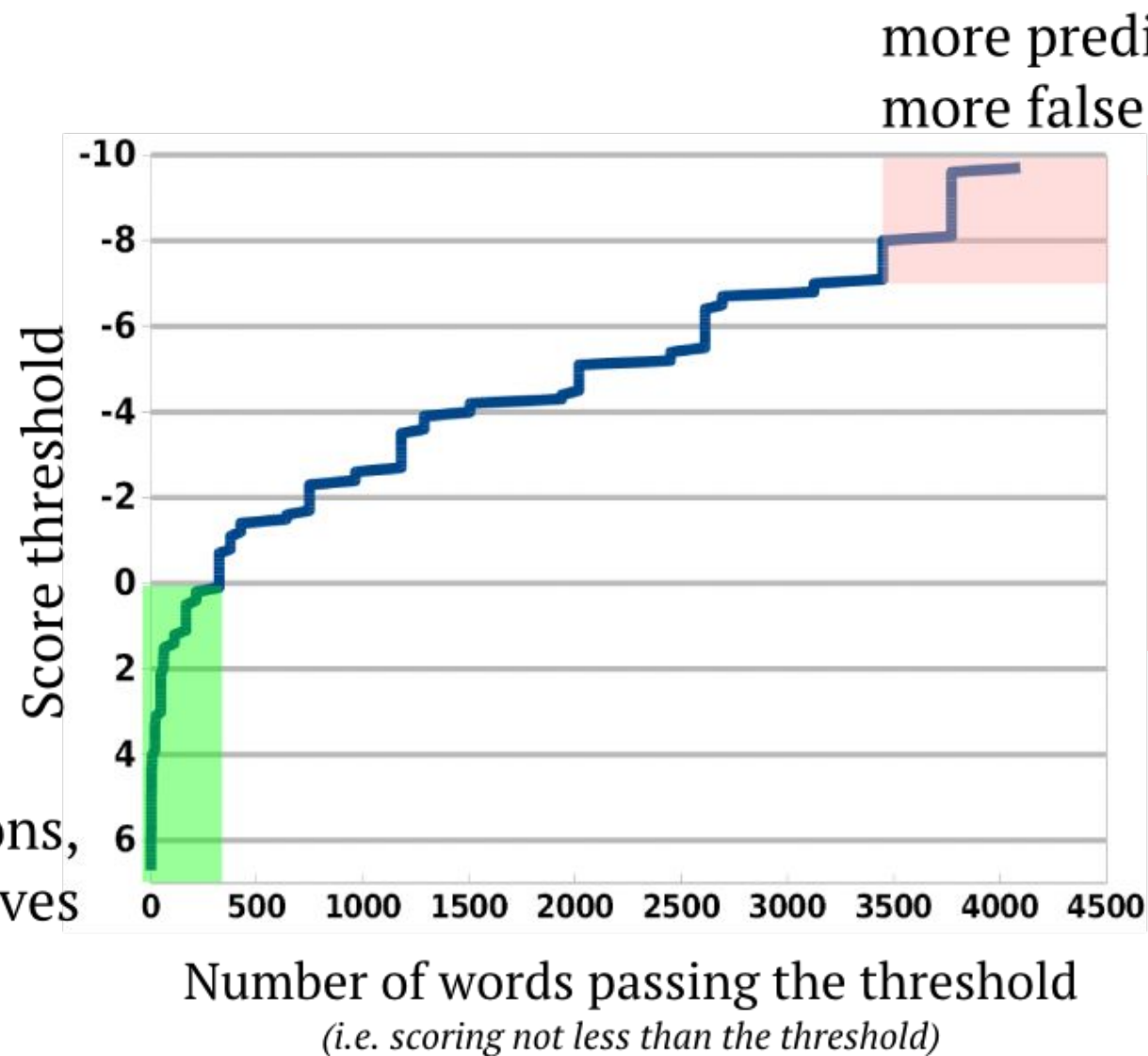
$$S = \mathbf{-9.6}$$

the worst score

the best score

**threshold is too strict, too high**  
a lot of patterns that are real motifs do not pass the threshold and we lose them

less TFBS predictions,  
less true positives



**threshold is too negative, too low**  
a lot of patterns pass a threshold and are reported as motifs but they are not real motifs

Score threshold turns a motif model into a binary "yes/no" classifier!

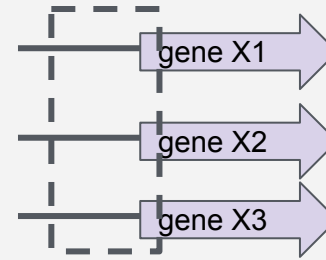


# Motif discovery problem: flowchart

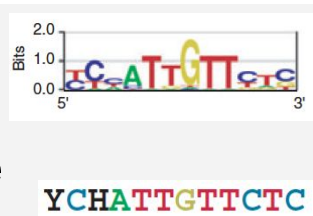
## identify **co-regulated genes**

- co-expressed under certain condition and same functional category
- orthologous genes
- ChIP-seq
- ...

## get **upstream regions** of selected genes



## select a **motif model** (consensus or PWM) – to access and compare obtained motifs



## Motif discovery

**“phylogenetic footprinting”:**  
perform MSA of input sequences  
(Multiple sequence alignment)  
  
find gapless conserved block of  
MSA  
  
represent it as a motif

### motif discovery algorithm

- a) Enumeration\*
- b) Expectation-Maximization (EM)
- a) Gibbs sampling\*

set of input  
sequences

database(s) of  
known motifs

**candidate motif(s)**

sequence  
(e.g. genome)

## Motif enrichment

find which known motifs  
might be overrepresented in  
an input set of sequences

## Motif comparison

compare candidate  
motif with known motifs

## Motif scanning

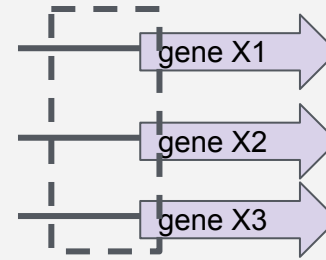
scan input sequence to find  
occurrences of the motif

# Search for regulatory DNA motifs: computational approach

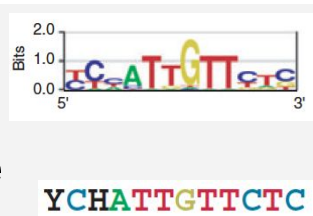
## identify **co-regulated genes**

- co-expressed under certain condition and same functional category
- orthologous genes
- ChIP-seq
- ...

## get **upstream regions** of selected genes



## select a **motif model** (consensus or PWM) – to access and compare obtained motifs



## Motif discovery

**“phylogenetic footprinting”:**  
perform MSA of input sequences  
(Multiple sequence alignment)

find gapless conserved block of MSA

represent it as a motif

## motif discovery algorithm

- Enumeration\*
  - Expectation-Maximization (EM)
- 
- Gibbs sampling\*

MSA:  
Muscle/T-coffee/ClustalW  
Visualization: MView

RSAT

set of input sequences

database(s) of known motifs

**candidate motif(s)**

sequence (e.g. genome)

## Motif enrichment

find which known motifs might be overrepresented in an input set of sequences



## Motif comparison

compare candidate motif with known motifs

## Motif scanning

scan input sequence to find occurrences of the motif

# Homework

**Assignment** is in Canvas (quizz format)

**Files** for assignment – Canvas and github

**Instructions:**

[https://github.com/rybinaanya/2022\\_Skoltech\\_Bioinformatics\\_course\\_seminar\\_4](https://github.com/rybinaanya/2022_Skoltech_Bioinformatics_course_seminar_4)

**Deadline:** 12:00 (midday), 23 November Wed

If you have questions, please e-mail me [anna.rybina@skoltech.ru](mailto:anna.rybina@skoltech.ru)



# Useful links for future learning

Multiple Sequence Alignment Methods Edited by David J. Russell.

<https://doi.org/10.1007/978-1-62703-646-7>

Multiple Sequence Alignment Edited by Kazutaka Katoh.

<https://link.springer.com/book/10.1007/978-1-0716-1036-7>

Kharchenko, P., Tolstorukov, M. & Park, P. Design and analysis of ChIP-seq experiments for DNA-binding proteins. Nat Biotechnol 26, 1351–1359 (2008).

<https://doi.org/10.1038/nbt.1508>

ChIP-seq guidelines and practices of the ENCODE and modENCODE consortia

<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC3431496/>

About motif representation: D'haeseleer, P. What are DNA sequence motifs?. Nat Biotechnol 24, 423–425 (2006). <https://doi.org/10.1038/nbt0406-423>

General strategies for motif discovery (relatively old paper but gives a good general description of approaches)

<https://journals.plos.org/ploscompbiol/article?id=10.1371/journal.pcbi.0020036>

Review of motif discovery algorithms

<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC6490410/>

Pavel Pevzner's course on bioinformatics algorithms: motif discovery problem

<https://youtube.com/playlist?list=PLQ-85IQIPqFMEcdAi0yF015RgmowtsvwT>