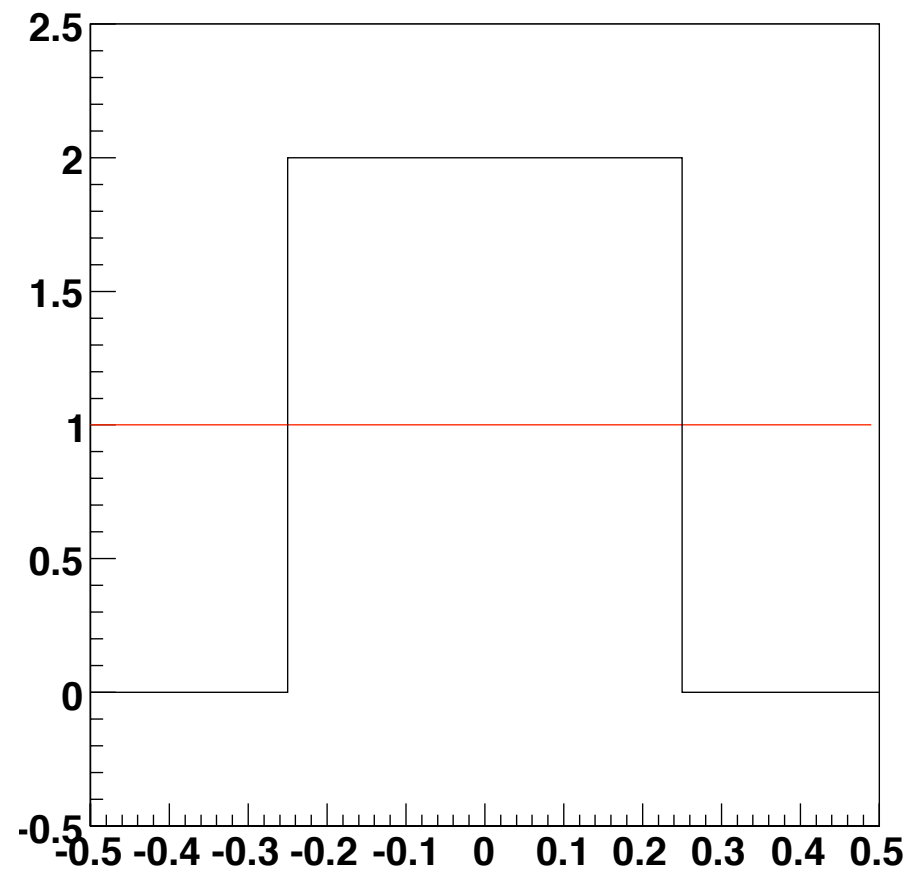


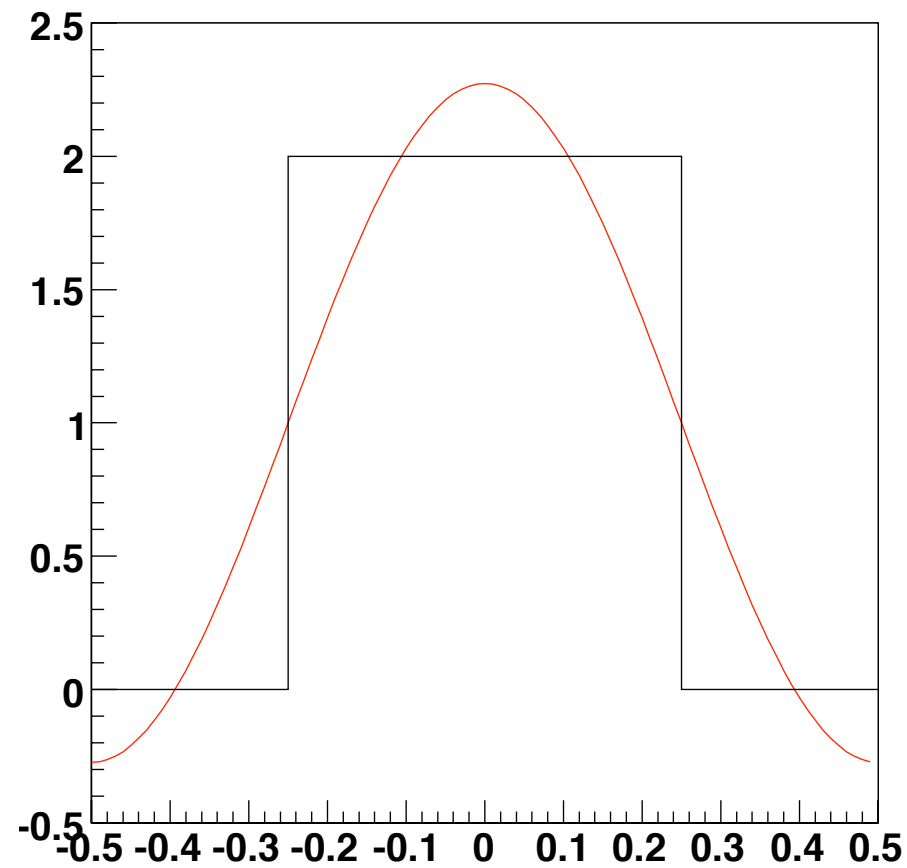
## Zero-th Approximation



Approximate function by its average

$$f(x) \simeq 1$$

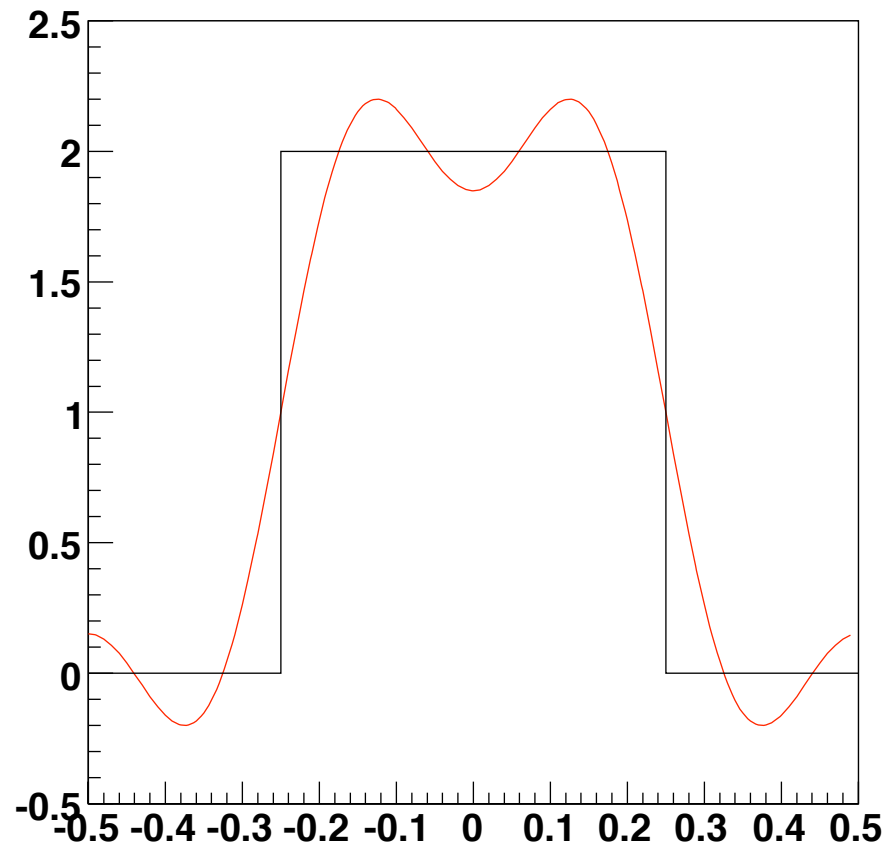
## 1st Approximation



Approximate function by its average +  $\cos(x)$

$$f(x) \simeq 1 + \frac{2}{\pi} \cos(2\pi x)$$

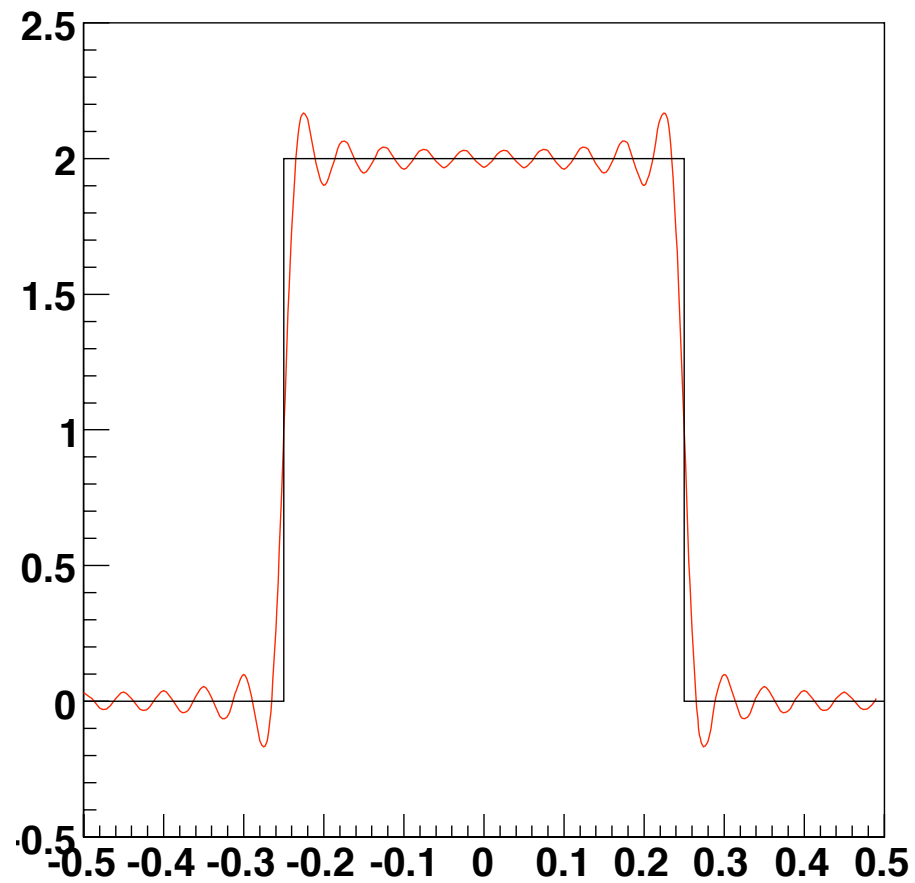
## 3 term Approximation



Approximate function by its average +  $\cos(x)$

$$f(x) \simeq 1 + \frac{2}{\pi} \cos(2\pi x) - \frac{2}{3\pi} \cos(2\pi \cdot 3x)$$

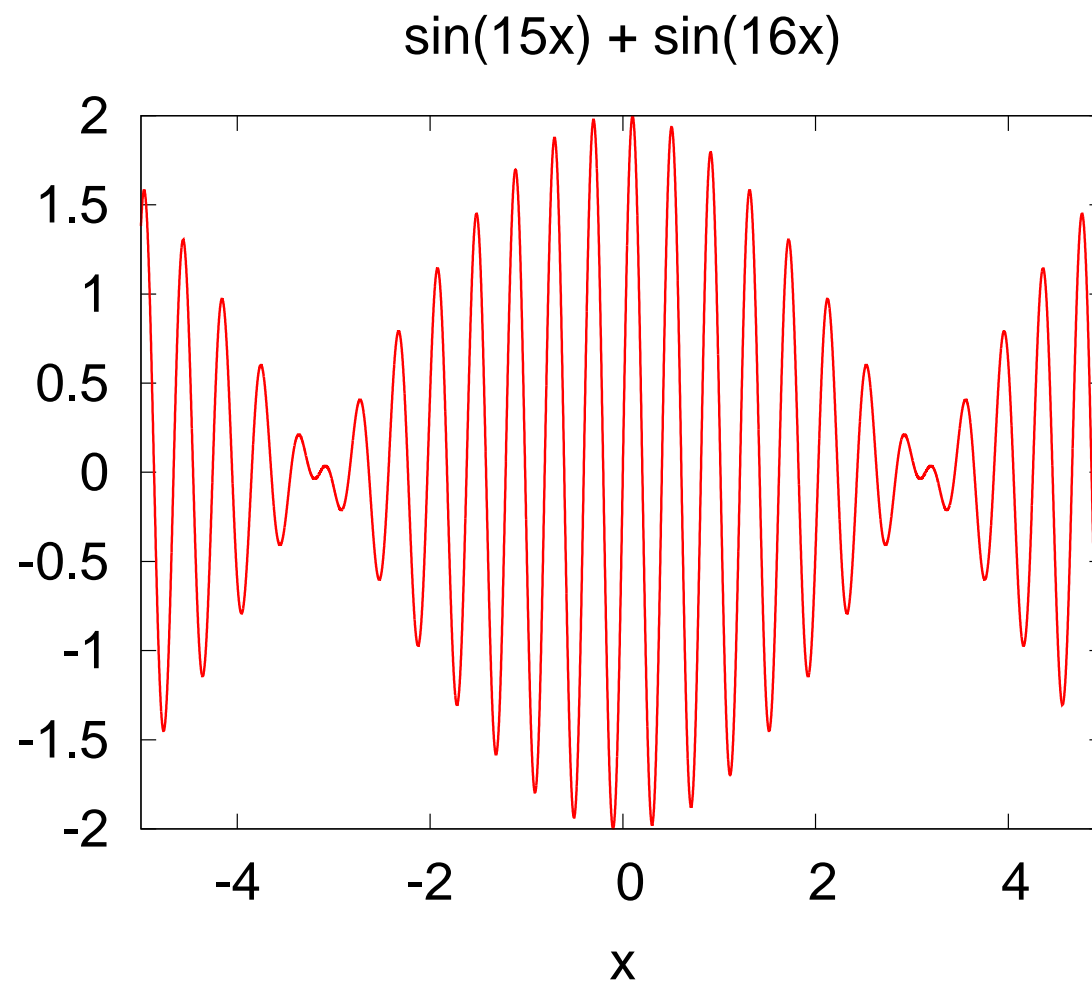
## 10 term Approximation



Approximate function by its average + cos(x)

$$f(x) \simeq 1 + \frac{2}{\pi} \cos(2\pi x) - \frac{2}{3\pi} \cos(2\pi \cdot 3x) + \frac{2}{5\pi} \cos(2\pi \cdot 5x) + \dots$$

## Adding two sin waves



Adding two waves of similar frequency makes "beats"

Group velocity – see Michael Fowler's applet

