

ESE 271  
Fall, 2009

First Exam

Name:  
ID Number:

Do not place your answers on this front page.  
Each problem is worth 25 points.

Prob. 1:

Prob. 2:

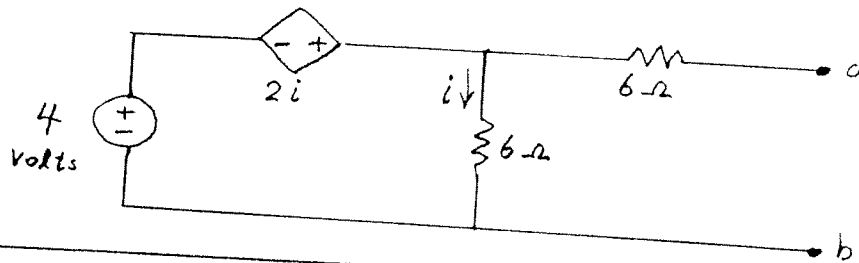
Prob. 3:

Prob. 4:

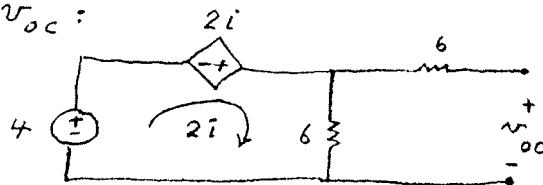
# 1st Exam

Prob. 1:

Find the Thevenin equivalent circuit as seen from the terminals: a,b.



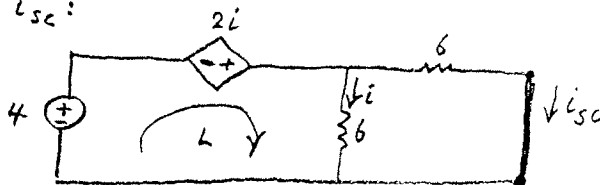
To GET  $V_{oc}$ :



$$\text{KVL: } -4 - 2i + 6i = 0. \text{ So, } i = 1 \text{ A}$$

$$\therefore V_{oc} = 6 \text{ V}$$

To GET  $i_{sc}$ :



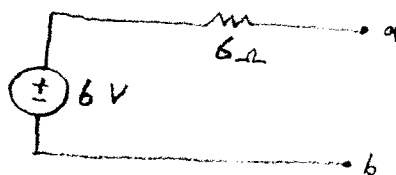
$$i = i_{sc}$$

$$\text{KVL AROUND THE LOOP L: } -4 - 2i_{sc} + 6i_{sc} = 0$$

$$\text{So, } i_{sc} = 1 \text{ A.}$$

$$\text{So, } R_{TH} = \frac{V_{oc}}{i_{sc}} = \frac{6}{1} = 6 \Omega$$

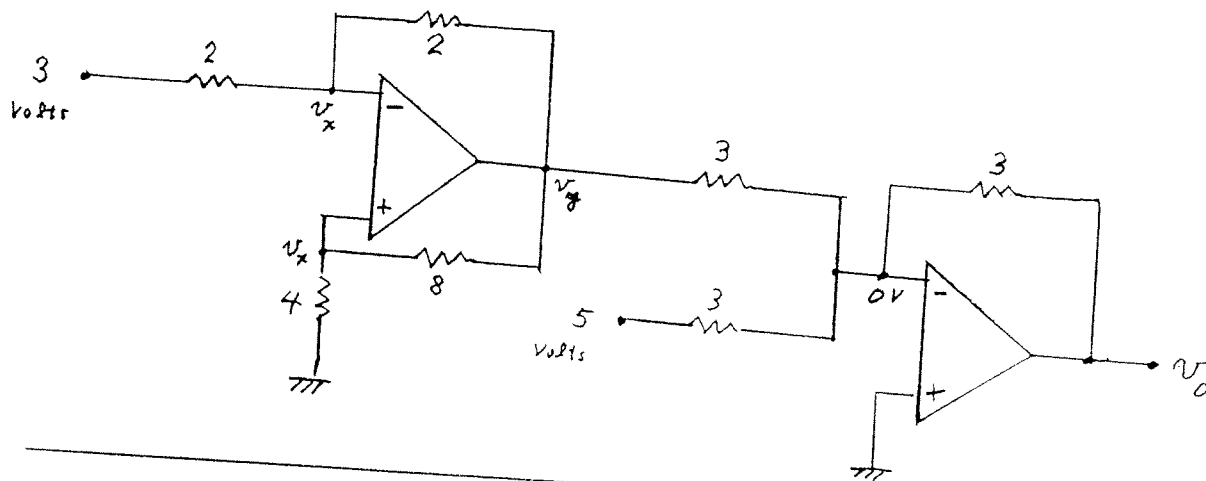
THEVENIN'S CIRCUIT IS:



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Prob. 2:

Find the output voltage  $v_o$ . Use the virtual-short virtual-open model for the op-amps.  
(Resistor values are in  $k\Omega$ .)



$$\left. \begin{aligned} \frac{3 - v_x}{2} + \frac{v_y - v_x}{2} &= 0 \\ v_x &= v_y \frac{4}{4+8} \end{aligned} \right\}$$

HENCE, BY SECOND EQUATION

$$v_y = 3v_x$$

By first equation:

$$v_x = -3 \text{ V}$$

$$\text{So, } v_y = -9 \text{ V}$$

Also

$$\frac{v_y}{3} + \frac{5}{3} + \frac{v_o}{3} = 0$$

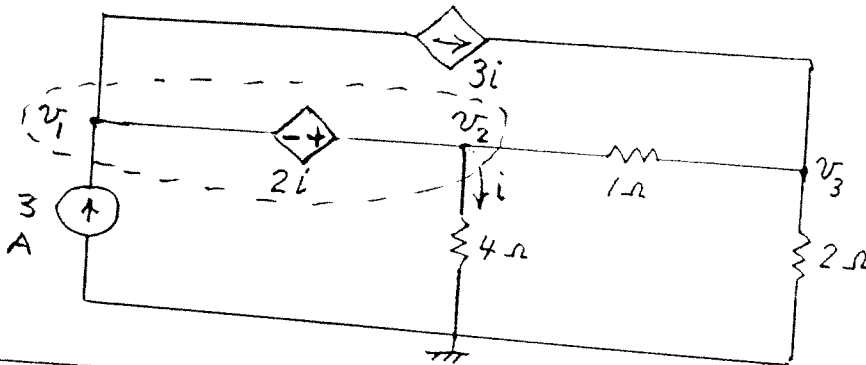
$$\text{So, } v_o = -v_y - 5 = 9 - 5 = 4 \text{ V}$$

$$\begin{aligned} 3 - v_x + 3v_x - v_y &= 0 \\ v_x &= -3 \end{aligned}$$

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Prob. 3:

Using a nodal analysis, determine the node voltage  $v_2$ .



PUT A BALLOON AROUND THE  $2i$  DEPENDENT SOURCE.

INSIDE THAT BALLOON:

$$v_2 - v_1 = 2i = 2 \frac{v_2}{4} = \frac{v_2}{2}, \quad i = \frac{v_2}{4}$$

THUS, 
$$-2v_1 + v_2 = 0$$

KCL ON THE BALLOON:

$$-3 + 3i + \frac{v_2}{4} + \frac{v_2 - v_3}{1} = 0$$

$$-3 + \frac{3}{4}v_2 + \frac{v_2}{4} + v_2 - v_3 = 0 \Rightarrow -3 + v_2 + v_2 - v_3 = 0$$

$$2v_2 - v_3 = 3$$

KCL AT  $v_3$  NODE: 
$$-3i + \frac{v_3 - v_2}{1} + \frac{v_3}{2} = 0$$

$$-7v_2 + 6v_3 = 0$$

$$-3 \cdot \frac{v_2}{4} + v_3 - v_2 + \frac{v_3}{2} = 0$$

$$(4 \times) \Rightarrow -3v_2 + 4v_3 - 4v_2 + 2v_3 = 0$$

SOLVING THE SECOND AND THIRD EQUATIONS:

$$v_2 = \frac{18}{5}$$

From 2nd eqn.  $v_3 = \frac{7}{6}v_2$

Sub in eqn  $2v_2 - \frac{7}{6}v_2 = 3$

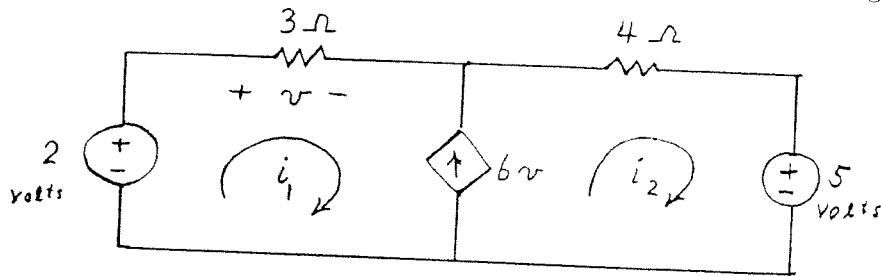
$$12v_2 - 7v_2 = 18$$

$$v_2 = \frac{18}{5}$$

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Prob. 4:

Do a mesh analysis to write two simultaneous equations in  $i_1$  and  $i_2$  as the unknowns. Display your answer by filling in the appropriate numbers in the following matrix equation.



$$\begin{bmatrix} -19 & 1 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} 0 \\ -3 \end{bmatrix}$$

At dependent source

$$i_2 - i_1 = 6V = 6 \times 3i_1 = 18i_1$$

$$\text{Thus, } -19i_1 + i_2 = 0$$

Then, KVL AROUND OUTER LOOPS

$$-2 + 3i_1 + 4i_2 + 5 = 0$$

Thus,

$$3i_1 + 4i_2 = -3$$