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PRN: 2020BTECS00090
Sub: DAA
Assignment no: 6
Topic: Greedy Method

To apply Greedy method to solve problems of

1) Job sequencing with deadlines

1.A) Generate table of feasible, processing sequencing, profit.

1.B) What is the solution generated by the function JS when $n=7$, $(p_1, p_2, \dots, p_7) = (3, 5, 20, 18, 1, 6, 30)$, and $(d_1, d_2, d_3, \dots, d_7) = (1, 3, 4, 3, 2, 1, 2)$?

1.C) **Input:** Five Jobs with following deadlines and profits

JobID	Deadline	Profit
a	2	100
b	1	19
c	2	27
d	1	25
e	3	15

Output: Following is maximum profit sequence of jobs:
c, a, e

1.D) Study and implement Disjoint set algorithm to reduce time complexity of JS from $O(n^2)$ to nearly $O(n)$

2) To implement Fractional Knapsack problem 3 objects ($n=3$).

$(w_1, w_2, w_3) = (18, 15, 10)$

$(p_1, p_2, p_3) = (25, 24, 15)$

$M=20$

With strategy

a) Largest-profit strategy

b) Smallest-weight strategy

c) Largest profit-weight ratio strategy

Solution:

```
// C++ Program to find the maximum profit job sequence  
// from a given array of jobs with deadlines and profits  
#include<bits/stdc++.h>  
using namespace std;  
  
// A structure to represent various attributes of a Job  
struct Job  
{  
    // Each job has id, deadline and profit  
    char id;  
    int deadLine, profit;  
};  
  
// A Simple Disjoint Set Data Structure  
struct DisjointSet  
{  
    int *parent;  
  
    // Constructor  
    DisjointSet(int n)
```

```
{
    parent = new int[n+1];

    // Every node is a parent of itself
    for (int i = 0; i <= n; i++)
        parent[i] = i;
}

// Path Compression
int find(int s)
{
    /* Make the parent of the nodes in the path
    from u--> parent[u] point to parent[u] */
    if (s == parent[s])
        return s;
    return parent[s] = find(parent[s]);
}

// Makes u as parent of v.
void merge(int u, int v)
{
    //update the greatest available
    //free slot to u
    parent[v] = u;
}
};

// Used to sort in descending order on the basis
// of profit for each job
bool cmp(Job a, Job b)
{
    return (a.profit > b.profit);
}

// Functions returns the maximum deadline from the set
// of jobs
int findMaxDeadline(struct Job arr[], int n)
{
    int ans = INT_MIN;
    for (int i = 0; i < n; i++)
        ans = max(ans, arr[i].deadLine);
    return ans;
}

int printJobScheduling(Job arr[], int n)
{
    // Sort Jobs in descending order on the basis
    // of their profit
```

```
sort(arr, arr + n, cmp);

// Find the maximum deadline among all jobs and
// create a disjoint set data structure with
// maxDeadline disjoint sets initially.
int maxDeadline = findMaxDeadline(arr, n);
DisjointSet ds(maxDeadline);

// Traverse through all the jobs
for (int i = 0; i < n; i++)
{
    // Find the maximum available free slot for
    // this job (corresponding to its deadline)
    int availableSlot = ds.find(arr[i].deadLine);

    // If maximum available free slot is greater
    // than 0, then free slot available
    if (availableSlot > 0)
    {
        // This slot is taken by this job 'i'
        // so we need to update the greatest
        // free slot. Note that, in merge, we
        // make first parameter as parent of
        // second parameter. So future queries
        // for availableSlot will return maximum
        // available slot in set of
        // "availableSlot - 1"
        ds.merge(ds.find(availableSlot - 1),
                availableSlot);

        cout << arr[i].id << " ";
    }
}

// Driver code
int main()
{
    Job arr[] = { { '1', 1, 3 }, { '2', 3, 5 },
                  { '3', 4, 20 }, { '4', 3, 18 },
                  { '5', 2, 1 }, { '6', 1, 6 }, { '7', 2, 30 } };
    int n = sizeof(arr) / sizeof(arr[0]);
    cout << "Following jobs need to be "
         << "executed for maximum profit\n";
    printJobScheduling(arr, n);
    return 0;
}
```

OUTPUT:

Following jobs need to be executed for maximum profit
7 3 4 6

1.A) **Input:** Five Jobs with following deadlines and profits

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Output: Following is maximum profit sequence of jobs:
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OUTPUT:

Following jobs need to be executed for maximum profit

a c e

1.B) Study and implement Disjoint set algorithm to reduce time complexity of JS from $O(n^2)$ to nearly $O(n)$

```
// C++ Program to find the maximum profit job sequence
// from a given array of jobs with deadlines and profits
#include<bits/stdc++.h>
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    int deadLine, profit;
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// A Simple Disjoint Set Data Structure
struct DisjointSet
{
    int *parent;

    // Constructor
    DisjointSet(int n)
    {
        parent = new int[n+1];

        // Every node is a parent of itself
        for (int i = 0; i <= n; i++)
            parent[i] = i;
    }

    // Path Compression
    int find(int s)
    {
        /* Make the parent of the nodes in the path
        from u--> parent[u] point to parent[u] */
        if (s == parent[s])
            return s;
        return parent[s] = find(parent[s]);
    }

    // Makes u as parent of v.
    void merge(int u, int v)
    {
        //update the greatest available
        //free slot to u
        parent[v] = u;
    }
};
```

```
// Used to sort in descending order on the basis
// of profit for each job
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// Functions returns the maximum deadline from the set
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int findMaxDeadline(struct Job arr[], int n)
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    int ans = INT_MIN;
    for (int i = 0; i < n; i++)
        ans = max(ans, arr[i].deadLine);
    return ans;
}

int printJobScheduling(Job arr[], int n)
{
    // Sort Jobs in descending order on the basis
    // of their profit
    sort(arr, arr + n, cmp);

    // Find the maximum deadline among all jobs and
    // create a disjoint set data structure with
    // maxDeadline disjoint sets initially.
    int maxDeadline = findMaxDeadline(arr, n);
    DisjointSet ds(maxDeadline);

    // Traverse through all the jobs
    for (int i = 0; i < n; i++)
    {
        // Find the maximum available free slot for
        // this job (corresponding to its deadline)
        int availableSlot = ds.find(arr[i].deadLine);

        // If maximum available free slot is greater
        // than 0, then free slot available
        if (availableSlot > 0)
        {
            // This slot is taken by this job 'i'
            // so we need to update the greatest
            // free slot. Note that, in merge, we
            // make first parameter as parent of
            // second parameter. So future queries
            // for availableSlot will return maximum
            // available slot in set of
```

```
// "availableSlot - 1"
ds.merge(ds.find(availableSlot - 1),
        availableSlot);

    cout << arr[i].id << " ";
}
}
}

// Driver code
int main()
{
    Job arr[] = { { '1', 1, 3 }, { '2', 3, 5 },
                  { '3', 4, 20 }, { '4', 3, 18 },
                  { '5', 2, 1 }, { '6', 1, 6 }, { '7', 2, 30 } };
    int n = sizeof(arr) / sizeof(arr[0]);
    cout << "Following jobs need to be "
          << "executed for maximum profit\n";
    printJobScheduling(arr, n);
    return 0;
}
```

2) To implement Fractional Knapsack problem 3 objects (n=3).

(w1,w2,w3) = (18,15,10)

(p1,p2,p3) = (25,24,15)

M=20

With strategy

a) Largest-profit strategy

b) Smallest-weight strategy

c) Largest profit-weight ratio strategy

```
#include<bits/stdc++.h>
using namespace std;

float greedybyprofit(int weights[3],int profit[3],int M,int N){
    vector<pair<int,int>> vp;
    for(int i=0;i<N;i++){
        vp.push_back({profit[i],weights[i]});
    }
    sort(vp.begin(),vp.end(),greater<pair<int,int>>());
    float ans = 0;
    for(auto x:vp){
        if(M>x.second){
            ans+=x.first;
            M-=x.second;
        }
        else{

```



```
        ans+=(float)((((float)M/x.second)*x.first);
        break;
    }
}
return ans;
}

float greedybyweight(int weights[3],int profit[3],int M,int N){
    vector<pair<int,int>> vp;
    for(int i=0;i<N;i++){
        vp.push_back({weights[i],profit[i]});
    }
    sort(vp.begin(),vp.end());
    float ans = 0.0;
    for(auto x:vp){
        if(M>x.first){
            ans+=x.second;
            M-=x.first;
        }
        else{
            ans+=(float)((((float)M/x.first)*x.second);
            break;
        }
    }
    return ans;
}

float greedybyratio(int weights[3],int profit[3],int M,int N){
    vector<pair<float,int>> vp;
    for(int i=0;i<N;i++){
        vp.push_back({(((float)profit[i]/weights[i])),i});
    }
    sort(vp.begin(),vp.end(),greater<pair<float,int>>());
    float ans = 0.0;
    float sum=0;
    for(auto x:vp){
        if(M>sum+weights[x.second]){
            ans+=profit[x.second];
            M-=weights[x.second];
            sum+=weights[x.second];
        }
        else{
            ans+=(float)((((float)M/weights[x.second])*profit[x.second]));
            break;
        }
    }
}
```

```
    }  
    return ans;  
}  
  
int main(){  
    int weights[3] = {18,15,10};  
    int profit[3] = {25,24,15};  
    int M = 20;  
    cout<<endl;  
    cout<<"Answers using various strategies\n"<<endl;  
    cout<<"Largest profit strategy :  
<<greedybyprofit(weights,profit,M,3)<<endl;  
    cout<<"Smallest weight strategy :  
<<greedybyweight(weights,profit,M,3)<<endl;  
    cout<<"Largest profit-weight ratio strategy :  
<<greedybyratio(weights,profit,M,3)<<endl;  
    cout<<"\n"<<endl;  
  
    return 0;  
}
```

OUTPUT:→

Answers using various strategies

Largest profit strategy :28.2

Smallest weight strategy :31

Largest profit-weight ratio strategy :31.5