Hogebomen

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Abstract

Blablabla

1 Inleiding

AVL-bomen, splay-bomen en treaps zijn klassieke datastructuren die ingezet worden om een verzameling gegevens te faciliteren. Het zijn zelfbalancerende binaire zoekbomen die elk een vorm van ruimte en/of tijd-efficiëntie aanbieden. Er worden experimenten verricht om de prestatie van deze zelf-balancerende zoekbomen te vergelijken aan de hand van ophaaltijd van data, mate van herstructurering en het verwijderen van knopen. Ook wordt de prestatie van deze zoekbomen uitgezet tegen de ongebalanceerde tegenhanger, de binaire zoekboom.

2 Werkwijze

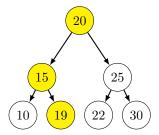
De vier bomen zijn conceptueel eenvoudig en relatief makkelijk te implementeren. Voor alle vier de bomen wordt dezelfde zoekmethode gebruikt. Deze is in het slechtste geval $O(\log n)$.

2.1 Implementatie binaire zoekboom

De binairy zoekboom (BST) vormt de basis voor alle zogeheten zelf-organiserende bomen, zoals de AVL- of SplayTree. Aan de grondslag van de BST ligt de binaire-zoekboom-eigenschap, die zorgt dat de boom op de "gretige" manier kan worden doorzocht in plaats van een exhaustive search. Hierdoor is het mogelijk om een knoop in een boom met hoogte n in hooguit n stappen te vinden, maar gemiddeld genomen sneller, namelijk $\log(n)$. Kort samengevat houdt de bsteigenschap het volgende in:

- Linker-kindknopen en hun kinderen hebben altijd een kleinere waarde dan hun ouder, rechter-kindknopen en al hun kinderen altijd een grotere waarde dan hun ouder.
- Bij een MIN-boom is dit omgekeerd. Onze implementatie is enkel een MAX-boom.
- Toevoegen kan zonder verwisselen worden uitgevoerd (in tegenstelling tot bijv. een heap).

• Voor verwijderen of vervangen moet afhankelijk van de plaats van de knoop wel worden verwisseld.

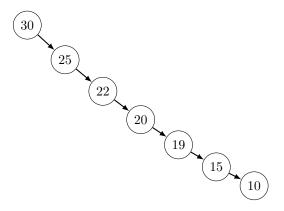


In het voorbeeld is het zoekpad naar de knoop met waarde 19 weergegeven. Dit zoekpad heeft precies complexiteit O(n), namelijk drie stappen/vergelijkingen voordat de gezochte knoop wordt bereikt, dat is dus gelijk aan de hoogte van de boom.

- Het zoekdomein bestaat aanvankelijk uit $2^n 1 = 7$ knopen, want de voorbeeldboom is een volle binaire boom
- Aan het begin van de zoekopdracht is er alleen een pointer naar de wortel (20). We weten dat 19 kleiner is dan de wortel, dus bezoeken we zijn linkerkind. Van de complete rechtersubboom is dus van te voren bekend dat deze niet doorzocht hoeft te worden.
- Het zoekdomein wordt dus ineens van 7 naar $2^n 1 (2^{n-1} 1) = 4$ verkleind. Voor een grote boom zijn dat veel knopen die nooit bezocht hoeven te worden.
- De nieuwe knoop heeft waarde 15. We hebben dus nog geen resultaat, maar er is nu wel bekend dat alleen de rechtersubboom van 15 hoeft te worden doorzocht
- \bullet Het zoekdomein is nu precies n geworden, de "worst case" bij de binair zoeken.
- Het rechterkind van 15 is vervolgens 19, de knoop is gevonden.

Binaire bomen zijn dus sneller dan gewone bomen tijdens het zoeken en correct mits de binaire-zoekboom-eigenschap wordt gehandhaafd. Tijdens een insert operatie kost dat inprinciepe geen extra rekenkracht, maar bij bijvoorbeeld het verwijderen moet de boom soms worden verschoven om de eigenschap te herstellen.

Een ander probleem is dat de binaire zoekboom eigenlijk alleen optimaal presteert als de hoogte zo gering mogelijk is voor het aantal knopen. De hoogte bepaalt namelijk de zoekcomplexiteit, niet het aantal knopen. Een binaire zoekboom met een goede balans tussen de hoogten van de subbomen is *geballanceerd*. Als er tijdens het toevoegen niets bijzonders wordt gedaan, kan een binaire zoekboom heel snel ongebalanceerd raken, afhankelijk van de volgorde waarin knopen worden toegevoegd. Neem bijvoorbeeld de bovenstaande boom. Als men de knopen in de volgorde 10, 15, 19, 20, 25, 22, 30 toegevoegd ontstaat er één lange tak naar rechts. De worst-case zoekdiepte is nu van 3 naar 7 gegaan.

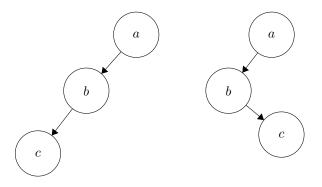


De zelf-organiserende boom is een speciaal soort binaire zoekboom die tijdens verschillende operaties probeert om de boom zo goed mogelijk te (her)belanceren. Uiteraard kosten deze extra operaties ook meer rekenkracht en of dit zich terugbetaald in zoeksnelheid is één van de dingen die wij zullen onderzoeken tijdens deze experimenten.

2.2 Implementatie AVL-bomen

Knopen van een AVL-boom hebben een balansfactor, die altijd -1, 0 of 1 moet zijn. In deze implementatie is de balansfactor de hoogte van de rechtersubboom min de hoogte van de linkersubboom. Dit houdt dus in dat de hoogte van de linkersubboom van de wortel met maar 1 knoop kan verschillen van de hoogte van de rechtersubboom van de wortel. Het moment dat de balansfactor van een knoop minder dan -1 of meer dan 1 wordt, moet de boom geherstructureerd worden, om deze eigenschap te herstellen.

Om de balansfactor voor elke knoop te berekenen, houdt elke knoop zijn eigen hoogte bij. De balansfactor van een knoop wordt hersteld door rotaties. De richting en de hoeveelheid van de rotaties hangt af van de vorm van de betreffende (sub)boom. De volgende twee vormen en hun spiegelbeelden kunnen voorkomen bij het verwijderen of toevoegen van een knoop:



In het eerste geval moet de wortel naar rechts worden geroteerd. In het tweede geval moeten we eerst naar de staat van de eerste subboom komen, door b naar links te roteren. Voor de spiegelbeelden van deze twee vormen geldt hetzelfde alleen in spiegelbeeld.

In deze implementatie van een AVL-boom bedraagt het toevoegen van een knoop in het ergste geval O(logn) tijd, waarbij n staat voor de hoogte van de boom. Eerst moet er gekeken worden of de data niet al in de boom voorkomt (O(logn)) en vervolgens moet de boom op basis van de toevoeging geherstructureerd worden. Dit laatste is in het ergste geval O(logn), omdat dan de gehele boom tot de wortel moeten worden nagelopen.

De complexiteitsgraad van het verwijderen van een knoop is gelijk aan die van het toevoegen van een knoop. In deze implementatie zoeken we in de rechtersubboom het kleinste kind en vervangen we de te verwijderen knoop met deze knoop. Dit heeft een duur van O(logn). Als hij geen rechtersubboom heeft, wordt de node weggegooid en wordt zijn linkersubboom de nieuwe boom.

2.3 Implementatie Splay-bomen

De Splay-boom is een simpele binaire zoekboom die zichzelf herorganiseerd na elke operatie, ook na operaties die alleen lezen, zoals find(). Deze herorganisatiestap heet "splay" (vandaar de naam) en heeft ten doel de laatst aangesproken knoop bovenaan te zetten. Dit wordt dus de wortel. Hieronder is het gedrag kort samengevat:

- Bij zoeken wordt de gevonden knoop de wortel, mits er een zoekresultaat is.
- Bij toevoegen wordt de toegevoegde knoop de wortel
- Bij vervangen wordt de vervangen knoop de wortel
- Bij verwijderen wordt de te verwijderen knoop eerst de wortel, dan wordt deze verwijderd.

Het idee achter dit gedrag is, dat vaak gebruikte knopen hoger in de boom terechtkomen en daarom sneller toegankelijk zijn voor volgende operaties. De splay-operatie zorgt er bovendien voor dat knoop die dicht in de buurt van de gesplayde knoop zitten, ook hoger in de boom worden geplaatst. Dit effect ontstaat doordat splay eigenlijk een serie boom rotaties is. Als men deze rotaties consequent uitvoerd blijft bovendien de binairy-zoekboom-eigenschap behouden.

2.3.1 Splay

De splay-operatie bestaat uit drie operaties en hun spiegelbeelden. We gaan uit van een knoop n, zijn ouderknoop p en diens ouderknoop g. Welke operatie wordt uitgevoerd is afhankelijk van het feit of n en p linker- of rechterkind zijn. We definieren:

- \bullet De Zig stap. Als n linkerkind is van p en p de wortel is, doen we een rotate-right op p.
- \bullet Het spiegelbeeld van Zig is Zag.

- De Zig-Zig stap. Als n linkerkind is van p en p linkerkind is van g, doen we eerst een rotate-right op g en dan een rotate-right op p.
- Het spiegelbeeld van Zig-Zig is Zag-Zag
- De Zig-Zag stap. Als n rechterkind is van p en p linkerkind is van g, doen we eerst een rotate-left op p en dan een rotate-right op g.
- De omgekeerde versie heet Zag-Zig

Onze implementatie splayt op insert(), replace(), remove() en find(). De gebruiker kan eventueel zelf de splay-operatie aanroepen na andere operaties dmv de functie splay().

2.4 Implementatie Treaps

Treap lijkt in veel opzichten op een AVL-boom. De balansfactor per knoop heeft echter plaats gemaakt voor een prioriteit per knoop. Deze prioriteit wordt bij het toevoegen van een knoop willekeurig bepaald. De complexiteit voor het toevoegen en verwijderen van een knoop is hetzelfde als bij de AVL-boom.

Bij het toevoegen van een knoop moet er nog steeds omhoog gelopen worden in de boom, totdat de prioriteit van de toegevoegde knoop kleiner is dan de prioriteit van de ouder. Als dit niet het geval is, blijft de toegevoegde knoop omhoog roteren. In het ergste geval kan het dus weer zo zijn dat we tot de wortel door moeten blijven lopen.

Bij het verwijderen van een knoop blijven we de betreffende knoop roteren naar het kind met de grootste prioriteit. Uiteindelijk belanden we dan in de situatie dat de knoop maar een of geen kinderen heeft. In het eerste geval verwijderen we de knoop en plakken zijn subboom terug aan de boom op zijn plek en in het tweede geval verwijderen we de knoop. In het slechtste geval duurt dit dus ook O(logn) tijd.

3 Onderzoek

Een praktisch voorbeeld van binair zoeken in een grote boom is de spellingscontrole. Een spellingscontrole moet zeer snel voor een groot aantal strings kunnen bepalen of deze wel of niet tot de taal behoren. Aangezien er honderduizenden woorden in een taal zitten, is lineair zoeken geen optie. Voor onze experimenten hebben wij dit als uitgangspunt genomen en hieronder zullen we kort de experimenten toelichten die wij hebben uitgevoerd. In het volgende hoofdstuk staan vervolgens de resultaten beschreven.

3.1 Hooiberg

"Hooiberg" is de naam van het testprogramma dat we hebben geschreven speciaal ten behoeven van onze experimenten. Het is een klein console programma dat woorden uit een bestand omzet tot een boom in het geheugen. Deze boom kan vervolgens worden doorzocht met de input uit een ander bestand: de "naalden". De syntax is alsvolgt:

hooiberg type hooiberg.txt naalden.txt [treap-random-range]

Hierbij is type één van bst, avl, splay, treap, het eerste bestand bevat de invoer voor de boom, het tweede bestand een verzameling strings als zoekopdracht en de vierde parameters is voorbehouden voor het type treap. De bestanden kunnen woorden of zinnen bevatten, gescheiden door regeleinden. De binaire bomen gebruiken lexicografische sortering die wordt geleverd door de operatoren < en > van de klasse std::string. Tijdens het zoeken wordt een exacte match gebruikt (case-sensitive, non-locale-aware).

3.2 Onderzoeks(deel)vragen

Met onze experimenten hebben we gepoogd een aantal eenvoudige vragen te beantwoorden over het gebruik van de verschillende binaire en zelf-organiserende bomen, te weten:

- Hoeveel meer rekenkracht kost het om grote datasets in te voegen in zelforganiserende bomen tov binaire bomen?
- Levert een zelf-organiserende boom betere zoekprestaties en onder welke opstandigheden?
- Hoeveel extra geheugen kost een SOT?
- Wat is de invloed van de random-factor bij de Treap?

3.3 Meetmethoden

Om de bovenstaande vragen te toetsen, hebben we een aantal meetmethoden bedacht.

- Rekenkracht hebben we gemeten in milliseconden tussen aanvang en termineren van een berekening. We hebben de delta's berekend rond de relevante code blokken dmv de C++11 chrono klassen in de Standard Template Library. Alle test zijn volledig sequentieel en single-threaded uitgevoerd. Deze resultaten zijn representatie voor één bepaald systeem, vandaar dat we aantal % 'meer rekenkracht' als eenheid gebruiken.
- Zoekprestatie hebben we zowel met rekenkracht als zoekdiepte gemeten. De zoekdiepte is het aantal stappen dat vanaf de wortel moet worden gemaakt om bij de gewenste knoop te komen. We hebben hierbij naar het totaal aantal stappen gekeken en naar de gemiddelde zoekdiepte.
- Geheugen hebben we gemeten met de valgrind memory profiler. Dit programma wordt gebruikt voor het opsporen van geheugen lekken en houdt het aantal allocaties op de heap bij. Dit is representatie voor het aantal gealloceerde nodes. Aangezien hooiberg nauwelijks een eigen geheugenvoetafdruk heeft, zijn deze waarden representatief.

3.4 Input data

Voor ons experiment hebben we een taalbestand gebruikt van OpenTaal.org met meer dan 164.000 woorden. Dit is een relatief klein taalbestand, maar voldoede om verschillen te kunnen zien. We hebben een aantal testcondities gebruikt:

- Voor het inladen een wel of niet alfabetisch gesoorteerd taalbestand gebruiken.
- Als zoekdocument hebben we een gedicht met 62 woorden gebruikt. Er zitten een aantal dubbele woorden in alsook een aantal woorden die niet in de woordenlijst voorkomen (werkwoordsvervoegingen).
- We hebben ook een conditie waarbij we alle woorden gezocht hebben, zowel in dezelfde, als in een andere volgorde dan dat ze zijn ingevoerd.
- We hebben één conditie waarbij we de random-range van de Treap hebben gevariëerd.

3.5 Hypothesen

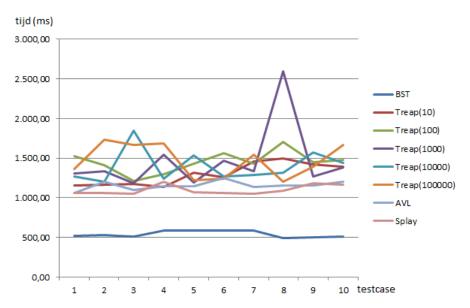
- De binairy search tree zal vermoedelijk het snelst nieuwe data toevoegen. De splay tree heeft veel ingewikkelde rotatie bij een insert, dus deze zal het traagst zijn.
- Bij het gedicht zal de splay boom waarschijnlijk het snelst zijn omdat deze optimaliseert voor herhalingen.
- ..
- De bomen die een aparte node-klasse gebruiken (avl en treap) gebruiken het meeste geheugen.
- De meest efficiënte randomfactor is afhankelijk van de grootte van de boom die geïmplementeerd gaat worden. Bij een kleine boom volstaat een kleine randomfactor, bij een grote boom volstaat een grote randomfactor.

4 Resultaten

4.1 Experiment 1

Hoeveel meer rekenkracht kost het om grote datasets in te voegen in zelforganiserende bomen tov binaire bomen?

Hooiberg: Nederlands_unsorted Naalden: gedicht misschien beter om hier weer gemiddelden te pakken??



figuur 1. Grafiek over het aantal ms voor het construeren van een graaf.

4.2 Experiment 2

Levert een zelf-organiserende boom betere zoekprestaties en onder welke opstandigheden?

??? deze test geeft altijd 0/1 ms bij mij??

4.3 Experiment 3

Hoeveel extra geheugen kost een SOT?

Type	allocs	bytes
Treap	493280	16704426
BST	493278	15389858
AVL	493279	16704390
splay	43260	15389922

4.4 Experiment 4

Wat is de invloed van de random-factor bij de Treap? Hooiberg: Nederlands_unsorted Naalden: gedicht Average search depth

	10	100	1000	10000	10000
	34	36	36	45	38
	31	40	49	34	47
	29	35	26	70	41
	32	40	35	41	42
	33	44	32	38	36
	34	40	49	33	37
	35	47	29	37	35
	36	47	66	36	29
	32	34	36	35	39
	29	36	44	30	46
GEM	32,5	39,9	40,2	39,9	39

Total search depth

	10	100	1000	10000	10000
	1914	2041	2017	2549	2173
	1745	2254	2752	1957	2657
	1652	1982	1511	3954	2312
	1836	2261	1983	2310	2366
	1861	2482	1819	2169	2033
	1925	2253	2783	1852	2092
	2002	2656	1643	2126	1947
	2032	2672	3732	2059	1658
	1798	1917	2021	1999	2211
	1670	2051	2491	1712	2609
GEM	1843,5	2256,9	2275,2	2268,7	2205,8

5 Conclusies

6 Appendix

6.1 main.cc

```
1  /**
2  * main.cc:
3  *
4  * @author Micky Faas (s1407937)
5  * @author Lisette de Schipper (s1396250)
6  * @file main.cc
7  * @date 26-10-2014
8  **/
9
10  #include <iostream>
11  #include "BinarySearchTree.h"
12  #include "AVLTree.h"
13  #include "SplayTree.h"
14  #include "SplayTree.h"
15  #include "Treap.h"
16  #include <<string>
```

```
17
    using namespace std;
18
19
    // Makkelijk voor debuggen, moet nog beter
20
    template < class \  \, \texttt{T} > \  \, \textbf{void} \  \, \texttt{printTree} \left( \  \, \texttt{Tree} < \texttt{T} > \  \, \textbf{tree} \, , \  \, \textbf{int rows} \, \, \right) \, \, \left\{ \right.
21
         typename Tree<T>::nodelist list =tree.row( 0 );
22
         int row =0;
23
         while( !list.empty( ) && row < rows ) {</pre>
24
              string offset;
25
              26
                   offset += ' ';
27
28
29
              for( auto it =list.begin( ); it != list.end( ); ++it ) {
30
                   if( *it )
31
                        \verb|cout| << \verb|offset| << (*it) -> \verb|info()| << " " << \verb|offset|;
32
33
                        \verb"cout" << \verb"offset" << "" << \verb"offset";
34
              cout << endl;</pre>
37
              row++;
              list =tree.row( row );
38
39
40
41
    int main ( int argc, char **argv ) {
42
43
         /* BST hieronder */
44
45
         \verb"cout" << "BST:" << \verb"endl";
         {\tt BinarySearchTree}{<} int{>} \ {\tt bst} \ ;
47
        /* auto root =bst.pushBack( 10 );
49
         bst.pushBack( 5 );
50
         bst.pushBack( 15 );
51
52
         bst.pushBack( 25 );
53
         bst.pushBack( 1 );
54
55
         bst.pushBack( -1 );
         bst.pushBack( 11 );
         bst.pushBack( 12 );*/
         {\tt Tree}{<}{\tt int}{>}{*} bstP =&bst; // Dit werkt gewoon :-)
59
60
         auto root =bstP->pushBack( 10 );
61
         bstP->pushBack(5);
62
         bstP->pushBack(15);
63
64
         bstP->pushBack(25);
65
66
         bstP->pushBack(1);
         bstP->pushBack(-1);
         bstP->pushBack(11);
69
         bstP->pushBack(12);
70
```

```
//printTree<int>( bst, 5 );
71
72
73
         //bst.remove( bst.find( 0, 15 ) );
74
         //bst.replace( -2, bst.find( 0, 5 ) );
75
76
77
         printTree < int > (bst, 5);
78
79
         bst.remove( root );
80
81
82
         printTree < int > (bst, 5);
83
84
         /* Splay Trees hieronder */
85
86
         cout << "Splay Boom:" << endl;</pre>
87
         SplayTree < int > splay;
88
         splay.pushBack(10);
         \mathbf{auto} \ \mathbf{a} = \mathbf{splay.pushBack} (5);
         splay.pushBack(15);
92
93
         \mathtt{splay.pushBack} \left(\begin{array}{c}25\end{array}\right);
94
         auto b = splay.pushBack(1);
95
         {\tt splay.pushBack(} \ -1 \ );
96
         auto c =splay.pushBack( 11 );
97
         splay.pushBack(12);
98
         //printTree<int>( splay, 5 );
         //a->swapWith( b );
         //splay.remove( splay.find( 0, 15 ) );
103
         //splay.replace( -2, splay.find( 0, 5 ) );
104
105
106
         printTree < int > (splay, 5);
107
108
         //splay.remove( root );
109
         splay.splay( c );
         printTree < int > (splay, 5);
113
114
         // Test AVLTree //
115
116
         AVLTree < char > test;
117
         test.insert('a');
118
         auto d =test.insert('b');
119
120
         test.insert('c');
         test.insert('d');
         test.insert('e');
122
         test.insert('f');
123
         test.insert('g');
124
```

```
\verb"cout" << "AVL Boompje:" << \verb"endl";
125
         {\tt printTree}{<}{\tt char}{>}(\ {\tt test}\ ,\ 5\ );
126
         \verb"cout" << \verb"d->info" ( ) << " \ verwijderen: " << \verb"endl";
127
          test.remove( d );
128
         printTree < char > (test, 5);
129
130
         // Test Treap //
131
132
         cout << "Treap" << endl;
         Treap < int > testTreap(5);
          testTreap.insert(2);
136
          {\tt testTreap.insert}(3);
137
         auto e =testTreap.insert(4);
138
          testTreap.insert(5);
139
          printTree < int > (testTreap, 5);
140
          testTreap.remove(e);
141
          printTree < int > (testTreap, 5);
          return 0;
145
    6.2
          hooiberg.cc
      * hooiberg.cc:
      * @author Micky Faas (s1407937)
      * @author Lisette de Schipper (s1396250)
      * Ofile
                   helehogebomen.cc
                    10-12-2014
      * @date
10 #include "BinarySearchTree.h"
    #include "Tree.h"
    #include "AVLTree.h"
    #include "SplayTree.h"
    #include "Treap.h"
    #include <iostream>
    #include <string>
   #include <fstream>
    #include <vector>
    #include <chrono>
20
   // Only works on *nix operating systems
    // Needed for precision timing
    #include <sys/time.h>
    using namespace std;
27
    // Makkelijk voor debuggen, moet nog beter
    template < class \  \, \texttt{T} > \  \, \textbf{void} \  \, \texttt{printTree} \left( \  \, \texttt{Tree} < \texttt{T} > \  \, \textbf{tree} \, \, , \  \, \textbf{int} \  \, \texttt{rows} \, \, \right) \  \, \left\{ \right.
29
         typename Tree<T>::nodelist list =tree.row( 0 );
```

```
int row =0;
31
        \mathbf{while}(\ ! \mathtt{list.empty}(\ ) \&\& \ \mathtt{row} < \mathtt{rows}\ ) \ \{
32
             string offset;
33
             for(int i = 0; i < (1 << (rows - row)) - 1; ++i)
34
                 offset += ';
35
36
37
             for( auto it =list.begin( ); it != list.end( ); ++it ) {
38
                  if( *it )
                      \verb|cout| << \verb|offset| << (*it) -> \verb|info()| << " " << \verb|offset|;
40
41
                 else
                      \verb"cout" << \verb"offset" << "" . " << \verb"offset";
42
43
             cout << endl;</pre>
44
             row++;
45
             list =tree.row( row );
46
        }
47
48
49
   int printUsage( const char* prog ) {
50
        52
             <<~"Usage:~"<<~\operatorname{prog}~<<~"~[type]~[haystack]~[needles]~[treap-random] \\ \backslash n"
53
             << "\ t[type]\ t\ tTree type to use. One of 'splay', 'avl', 'treap', 'bst'\ n"
54
             << "\t[haystack]\tInput file, delimited by newlines\n"
55
             << "\text{t/needles}\\ tFile containing sets of strings to search for, delimited by
56
              << "\t/treap-random]\tOptimal customization of the random factor of Treap\n"
57
              << std::endl;
58
        return 0;
59
60
   }
61
   bool extractNeedles( std::vector<string> &list, std::ifstream &file ) {
62
63
        string needle;
        while( !file.eof( ) ) {
64
             std::getline( file, needle );
65
             if( needle.size( ) )
66
                 list.push_back( needle );
67
68
69
        return true;
70
71
   bool fillTree( BinarySearchTree<string>* tree, std::ifstream &file ) {
72
73
        string word;
        \mathbf{while}(\ !\mathtt{file.eof}(\ )\ )\ \{
74
             std::getline( file, word );
75
             if( word.size( ) )
76
                 tree->pushBack( word );
77
78
        return true;
79
80
   }
81
82
   {\bf void} \  \  {\bf findAll(\  \, std::vector{<}string{>} \& list\,, \  \, BinarySearchTree{<}string{>}* \  \, tree} \  \, ) \  \, \{
83
        int steps =0, found =0, notfound =0;
        for( auto needle : list ) {
84
```

```
if(tree \rightarrow find(0, needle))
85
                      found++;
86
                      steps +=tree->lastSearchStepCount( );
87
                      if(found < 51)
88
                            \mathtt{std}::\mathtt{cout} << "Found" "<< \mathtt{needle} << '\','
89
                           <<~"in~"<<~tree->lastSearchStepCount(~)<<~"steps."<<~std::endl;
90
91
                else if (++notfound < 51)
92
                      std::cout << "Didn't find" << needle << '\',' << std::endl;
94
           if (found > 50)
95
                \mathtt{std}::\mathtt{cout} << \mathtt{found} - 50 << "more results not shown here." << \mathtt{std}::\mathtt{endl};
96
           if( found )
97
                cout << "Total search depth:</pre>
                                                                      " << \ \mathtt{steps} << \ \mathtt{endl}
98
                                                                      " << \mathtt{found} << \mathtt{endl}
                       << "Number of matches:
99
                                                                      "\,<<\,\mathtt{notfound}\,<<\,\mathtt{endl}
                       << "Number of misses:
100
                       << "Average search depth (hits): " << steps/found << endl;</pre>
101
102
103
     int main ( int argc, char **argv ) {
104
105
          enum MODE { NONE =0, BST, AVL, SPLAY, TREAP };
106
           int mode = NONE;
107
108
           if(argc < 4)
109
                return printUsage( argv[0] );
110
111
           if(std::string(argv[1]) = "bst")
112
                mode = BST;
113
           \mathbf{else} \ \mathbf{if} \left( \ \mathbf{std} :: \mathbf{string} \left( \ \mathbf{argv} \left[ 1 \right] \ \right) == "avl" \ \right)
                mode = AVL;
           \mathbf{else} \ \mathbf{if} \big( \ \mathbf{std} :: \mathbf{string} \big( \ \mathbf{argv} \, [\, 1\, ] \ \big) \\ = \ "treap" \ \big)
                mode = TREAP;
117
           \mathbf{if} \left( \begin{array}{c} \mathtt{std} :: \mathtt{string} \left( \begin{array}{c} \mathtt{argv} \left[ 1 \right] \end{array} \right) \\ = \\ \phantom{} "splay " \end{array} \right)
118
                mode =SPLAY;
119
120
           if(!mode)
121
                return printUsage( argv[0] );
122
123
           std::ifstream\ fhaystack(\ argv[2]\ );
           if(!fhaystack.good()) {
                std::cerr << "Could not open" << argv[2] << std::endl;
127
                return -1;
           }
128
129
           std::ifstream fneedles( argv[3] );
130
           if( !fneedles.good( ) ) {
131
                std::cerr << "Could not open" << argv[3] << std::endl;
132
                return -1;
133
          }
134
           if(argc > 4) {
                if (argv[4] \&\& mode != TREAP)  {
137
                      \verb|std::cerr| << "This variable should only be set for Treaps." << \verb|std::endl|;|
138
```

```
return -1;
139
             }
140
             else if (argv[4]) \le 0
141
                 std::cerr << "This variable should only be an integer"
142
                             << " greater than \theta." << std::endl;
143
                 return -1;
144
             }
145
        }
146
        std::vector<string> needles;
        if ( \ ! \texttt{extractNeedles} ( \ \texttt{needles} \ , \ \texttt{fneedles} \ ) \ ) \ \{
             cerr << "Could not read a set of strings to search for." << endl;</pre>
150
             return -1;
151
        }
152
153
        BinarySearchTree<string> *tree;
154
        switch(mode) {
155
             {f case} BST:
156
                  tree = new BinarySearchTree<string>();
                 break:
             case AVL:
                  tree = new AVLTree<string>();
160
                 break:
161
             case SPLAY:
162
                 tree = new SplayTree<string>();
163
                 break;
164
             case TREAP:
165
                  tree = new Treap<string>( argc > 4 ? atoi(argv[4]) : 100 ); // Default wa
166
                 break;
167
        }
170
171
        // Define a start point to time measurement
        auto start = std::chrono::high_resolution_clock::now();
172
173
174
        if ( \ !fillTree( \ tree\,, \ fhaystack \ ) \ ) \ \{
175
             cerr << "Could not read the haystack." << endl;
176
177
             return -1;
        }
        // Determine the duration of the code block
        auto duration =std::chrono::duration_cast<std::chrono::milliseconds>
181
                                    (std::chrono::high_resolution_clock::now() - start);
182
183
        cout << "Filled the binary search tree in " << duration.count() << "ms" << endl;</pre>
184
185
        start = std::chrono::high_resolution_clock::now();
186
        findAll( needles, tree );
187
        auto durationNs =std::chrono::duration_cast<std::chrono::nanoseconds>
188
                                    (std::chrono::high_resolution_clock::now() - start);
        \texttt{cout} << "Searched" the haystack in " << durationNs.count() << "ns, ~" << (float)du
191
192
```

```
// Test pre-order
193
        //for( auto word : *tree ) {
194
        //
              cout << word << '\n';
195
        //}
196
197
        fhaystack.close( );
198
        fneedles.close( );
199
        delete tree;
200
201
        return 0;
202
    6.3
         Tree.h
    * Tree:
                Micky Faas (s1407937)
    * @author
    * @author
                Lisette de Schipper (s1396250)
     * @file
                tree.h
     * @date
                26-10-2014
     **/
  #ifndef TREE_H
10
   #define TREE_H
#include "TreeNodeIterator.h"
13 #include <assert.h>
^{14} #include <list>
   #include <map>
   using namespace std;
17
18
    template < class INFO_T> class SplayTree;
19
20
    template <class INFO_T> class Tree
21
22
23
        public:
            enum ReplaceBehavoir {
                DELETE_EXISTING ,
                ABORT_ON_EXISTING,
                MOVE_EXISTING
27
            };
28
29
            typedef TreeNode<INFO_T> node_t;
30
            typedef TreeNodeIterator<INFO_T> iterator;
31
            typedef TreeNodeIterator_in<INFO_T> iterator_in;
32
            typedef TreeNodeIterator_pre<INFO_T> iterator_pre;
33
            typedef TreeNodeIterator_post<INFO_T> iterator_post;
            typedef list<node_t*> nodelist;
           /**
37
            * @function Tree()
38
            * @abstract Constructor of an empty tree
39
            **/
40
```

```
Tree()
41
                : m_root( 0 ) {
42
43
44
45
            * @function Tree()
46
            * @abstract Copy-constructor of a tree. The new tree contains the nodes
47
                          from the tree given in the parameter (deep copy)
48
            * @param
                          tree, a tree
            **/
50
            Tree( const Tree<INFO_T>& tree )
51
                : m_root( 0 ) {
52
                *this = tree;
53
            }
54
55
            /**
56
            * @function
                          ~Tree( )
57
            * @abstract
                          Destructor of a tree. Timber.
58
            **/
            ~Tree( ) {
              clear( );
61
            }
62
63
           /**
64
            * @function
                         begin_pre( )
65
            * @abstract begin point for pre-order iteration
66
                          interator_pre containing the beginning of the tree in
67
            * @return
                          pre-order
68
            **/
69
            iterator_pre begin_pre( ) {
                \ensuremath{//} Pre-order traversal starts at the root
71
                return iterator_pre( m_root );
72
              }
73
74
           /**
75
            * Ofunction begin()
76
            * @abstract begin point for a pre-order iteration
77
78
            * @return
                          containing the beginning of the pre-Order iteration
79
            **/
80
            iterator_pre begin( ) {
81
                return begin_pre( );
            }
83
           /**
84
            * @function
                          end()
85
            * @abstract
                          end point for a pre-order iteration
86
            * @return
                          the end of the pre-order iteration
87
            **/
88
            iterator_pre end( ) {
89
90
                return iterator_pre( (node_t*)0 );
            }
92
93
           /**
            * Ofunction end_pre()
94
```

```
end point for pre-order iteration
95
             * @abstract
             * @return
                            interator_pre containing the end of the tree in pre-order
96
             **/
97
             iterator_pre end_pre( ) {
98
                  return iterator_pre((node_t*)0);
99
100
101
            /**
102
             * @function
                           begin_in( )
             * @abstract
                            begin point for in-order iteration
             * @return
                            interator_in containing the beginning of the tree in
                            in-order
106
             **/
107
             iterator_in begin_in( ) {
108
                  if( !m_root )
109
                      return end_in( );
110
                  node_t *n =m_root;
111
                  \mathbf{while} \, ( \  \, \mathtt{n-\!\!>} \mathtt{leftChild} \, ( \  \, ) \  \, )
112
                      n = n - > leftChild();
113
                  return iterator_in( n );
116
            /**
117
             * @function
                            end_in()
118
             * @abstract
                            end point for in-order iteration
119
             * @return
                            interator_in containing the end of the tree in in-order
120
             **/
121
             iterator_in end_in( ) {
122
                  return iterator_in( (node_t*)0 );
123
             }
            /**
127
             * @function
                           begin_post( )
             st @abstract begin point for post-order iteration
128
             * @return
                            interator_post containing the beginning of the tree in
129
                            post-order
130
             **/
131
             iterator_post begin_post( ) {
132
133
                  if( !m_root )
                      return end_post( );
                  node_t *n = m_root;
                  while( n->leftChild( ) )
137
                      n = n - leftChild();
                  {\bf return\ iterator\_post(\ n\ )};
138
             }
139
140
            /**
141
             * @function
                            end_post( )
142
                            end point for post-order iteration
             * @abstract
143
             * @return
                            interator_post containing the end of the tree in post-order
144
             **/
             iterator_post end_post( ) {
                  \textbf{return iterator\_post( (node\_t*)0 )};\\
147
             }
148
```

```
149
           /**
150
                         pushBack( )
            * @function
151
                         a new TreeNode containing 'info' is added to the end
              @abstract
152
                          the node is added to the node that :
153
                              - is in the row as close to the root as possible
154
                             - has no children or only a left-child
155
                              - seen from the right hand side of the row
156
                          this is the 'natural' left-to-right filling order
                          compatible with array-based heaps and full b-trees
              @param
                          info, the contents of the new node
            * @post
                          A node has been added.
160
            **/
161
            virtual node_t *pushBack( const INFO_T& info ) {
162
                 node_t *n = new node_t (info, 0);
163
                 if( !m\_root ) { // Empty tree, simplest case }
164
                     m_root =n;
165
166
                 {
m else} { // Leaf node, there are two different scenarios
                     int max =getRowCountRecursive( m_root, 0 );
                     node_t *parent;
                     for ( int i = 1; i <= max; ++i ) {
170
171
                         parent =getFirstEmptySlot( i );
172
                         if( parent ) {
173
                              if( !parent->leftChild( ) )
174
                                  parent->setLeftChild( n );
175
                              else if( !parent->rightChild( ) )
176
                                 parent->setRightChild( n );
                             n->setParent( parent );
                             break;
                         }
                     }
182
                return n;
183
            }
184
185
186
            * @function
                          insert( )
              @abstract
                          inserts node or subtree under a parent or creates an empty
                          root node
              @param
                          info, contents of the new node
                          parent, parent node of the new node. When zero, the root is
              @param
191
192
                          assumed
                          alignRight, insert() checks on which side of the parent
              @param
193
                          node the new node can be inserted. By default, it checks
194
                          the left side first.
195
                          To change this behavior, set preferRight =true.
196
                          replaceBehavior, action if parent already has two children.
              @param
197
                          One of:
198
                          ABORT_ON_EXISTING - abort and return zero
                          MOVE_EXISTING - make the parent's child a child of the new
201
                                           node, satisfies preferRight
                          DELETE_EXISTING - remove one of the children of parent
202
```

```
completely also satisfies preferRight
203
                            pointer to the inserted TreeNode, if insertion was
               @return
204
205
                            successfull
                            If the tree is empty, a root node will be created with info
               @pre
206
                            as it contents
207
                            The instance pointed to by parent should be part of the
               @pre
208
                            called instance of Tree
209
               @post
                            Return zero if no node was created. Ownership is assumed on
210
                            the new node.
                            When DELETE_EXISTING is specified, the entire subtree on
212
213
                            preferred side may be deleted first.
             **/
214
             virtual node_t* insert( const INFO_T& info,
215
216
                               node_t* parent = 0,
                               bool preferRight = false,
217
                               int replaceBehavior =ABORT_ON_EXISTING ) {
218
                  if( !parent )
219
                      parent =m_root;
220
                  if( !parent )
                      return pushBack( info );
224
                  node_t * node = 0;
225
226
                  if( !parent->leftChild( )
227
                        && ( !preferRight || ( preferRight &&
228
                              parent->rightChild( ) ) ) {
229
                      node =new node_t( info, parent );
230
                      parent->setLeftChild( node );
231
                      node->setParent( parent );
                  } else if( !parent->rightChild( ) ) {
235
                      node =new node_t( info, parent );
                      parent->setRightChild( node );
236
                      node->setParent( parent );
237
238
                  \} else if ( replaceBehavior == MOVE_EXISTING ) {
239
                      node =new node_t( info, parent );
240
241
                      if( preferRight ) {
                           {\tt node-\!\!\!>\!\!setRightChild} \left( \begin{array}{c} {\tt parent-\!\!\!>\!\! rightChild} \left( \begin{array}{c} \\ \end{array} \right) \right);
                           node->rightChild( )->setParent( node );
                           parent->setRightChild( node );
                      } else {
245
                           node->setLeftChild( parent->leftChild( ) );
246
                           node->leftChild( )->setParent( node );
247
                           parent->setLeftChild( node );
248
                      }
249
250
                  } else if( replaceBehavior == DELETE_EXISTING ) {
251
                      node =new node_t( info, parent );
252
                      if( preferRight ) {
                           deleteRecursive( parent->rightChild( ) );
255
                           parent->setRightChild( node );
                      } else {
256
```

```
deleteRecursive( parent->leftChild( ) );
257
                         parent->setLeftChild( node );
258
                     }
259
260
261
                 return node;
262
            }
263
264
           /**
                         replace( )
            * @function
            * @abstract
                          replaces an existing node with a new node
                          info, contents of the new node
268
            * @param
                          node, node to be replaced. When zero, the root is assumed
              @param
269
              @param
                          alignRight, only for MOVE_EXISTING. If true, node will be
270
                          the right child of the new node. Otherwise, it will be the
271
                          left.
272
                          replaceBehavior, one of:
               @param
273
                           ABORT_ON_EXISTING - undefined for replace()
                          MOVE_EXISTING - make node a child of the new node,
                                            satisfies preferRight
                          DELETE_EXISTING - remove node completely
              @return
                          pointer to the inserted TreeNode, replace() is always
278
279
                          successful
              @pre
                          If the tree is empty, a root node will be created with info
280
                          as it contents
281
               @pre
                          The instance pointed to by node should be part of the
282
283
                          called instance of Tree
                          Ownership is assumed on the new node. When DELETE_EXISTING
284
               @post
                          is specified, the entire subtree pointed to by node is
                          deleted first.
            **/
            virtual node_t* replace( const INFO_T& info,
289
                              node_t* node = 0,
                               bool alignRight = false,
290
                               int replaceBehavior =DELETE_EXISTING ) {
291
                 assert( replaceBehavior != ABORT_ON_EXISTING );
292
293
                 node_t *newnode =new node_t( info );
294
                 if( !node )
                     node =m_root;
                 if(!node)
                     return pushBack( info );
299
                 if( node->parent( ) ) {
300
                     \verb"newnode->setParent" ( \verb"node->parent" ( ")");
301
                     if( node->parent( )->leftChild( ) == node )
302
                         node->parent( )->setLeftChild( newnode );
303
304
                         node->parent( )->setRightChild( newnode );
305
                 } else
306
                     m_root =newnode;
                 if(replaceBehavior = DELETE_EXISTING) {
309
```

310

```
deleteRecursive( node );
311
                }
312
                 else if ( replaceBehavior = MOVE_EXISTING ) {
313
                     if( alignRight )
314
                         newnode->setRightChild( node );
315
316
                         newnode->setLeftChild( node );
317
                     node->setParent( newnode );
318
                return node;
            }
322
           /**
323
            * @function
                         remove()
324
            * @abstract
                          removes and deletes node or subtree
325
                          n, node or subtree to be removed and deleted
            * @param
326
            * @post
                          after remove(), n points to an invalid address
327
            **/
328
            virtual void remove( node_t *n ) {
                 if(!n)
                     return;
331
                 if(n->parent())
332
                     if(n->parent()->leftChild() == n)
333
                         n->parent()->setLeftChild(0);
334
                     else if( n->parent( )->rightChild( ) == n )
335
                         n->parent()->setRightChild(0);
336
337
                 deleteRecursive( n );
338
            }
           /**
            * @function
                          clear( )
            * @abstract
343
                         clears entire tree
            * @pre
                          tree may be empty
344
            * @post
                          all nodes and data are deallocated
345
346
            void clear( ) {
347
348
                deleteRecursive( m_root );
                m_root = 0;
            }
           /**
            * @function
                          empty( )
353
            * @abstract test if tree is empty
354
            * @return
                          true when empty
355
356
            bool isEmpty( ) const {
357
                return !m_root;
358
            }
359
360
            * Ofunction root()
                         returns address of the root of the tree
363
            * @abstract
            * @return
                          the adress of the root of the tree is returned
364
```

```
* @pre
                          there needs to be a tree
365
            **/
366
            node_t* root( ){
367
                 return m_root;
368
369
370
371
            * Ofunction row()
            * @abstract
                         returns an entire row/level in the tree
            * @param
                          level, the desired row. Zero gives just the root.
            * @return
                          a list containing all node pointers in that row
            * @pre
                          level must be positive or zero
376
            * @post
377
            **/
378
            nodelist row( int level ) {
379
                 nodelist rlist;
380
                 getRowRecursive( m_root, rlist, level );
381
                 return rlist;
382
            }
           /**
                         find()
            * @function
386
             * @abstract
                          find the first occurrence of info and returns its node ptr
387
            * @param
                          haystack, the root of the (sub)tree we want to look in
388
                          null if we want to start at the root of the tree
389
             * @param
                          needle, the needle in our haystack
390
                          a pointer to the first occurrence of needle
391
            * @return
                          there may be multiple occurrences of needle, we only return
392
             * @post
                          one. A null-pointer is returned if no needle is found
            **/
            virtual node_t* find( node_t* haystack, const INFO_T& needle ) {
                 if( haystack == 0 )  {
                         i\,f\,(\ \mathtt{m\_root}\ )
397
                              haystack =m_root;
398
                         else
399
                              return 0;
400
401
                 return findRecursive( haystack, needle );
402
403
            }
           /**
            * @function
                          contains()
            * @abstract
                          determines if a certain content (needle) is found
407
             * @param
                          haystack, the root of the (sub)tree we want to look in
408
                          null if we want to start at the root of the tree
409
                          needle, the needle in our haystack
            * @param
410
                          true if needle is found
            * @return
411
412
            bool contains( node_t* haystack, const INFO_T& needle ) {
413
414
                 return find( haystack, needle );
            }
416
417
           /**
            * Ofunction toDot()
418
```

```
writes tree in Dot-format to a stream
419
              * @abstract
               * @param
                               out, ostream to write to
420
              * @pre
                               out must be a valid stream
421
              * @post
                               out (file or cout) with the tree in dot-notation
422
              **/
423
              void toDot( ostream& out, const string & graphName ) {
424
                    if( isEmpty( ) )
425
                        return;
426
                   {\tt map}{<} {\tt node\_t} \ *, \ {\bf int}{>} \ {\tt adresses} \, ;
                   typename map< node_t *, int >::iterator adrIt;
                   int i = 1;
                   int p;
430
                    iterator_pre it;
431
432
                    iterator_pre tempit;
                    adresses[m\_root] = 0;
433
                   out << "digraph" << graphName << '{ ' << end1 << '" ' << 0 << '" ';
434
                    \begin{tabular}{ll} for ( it = begin_pre( ); it != end_pre( ); ++it ) & ( \\ \end{tabular}
435
                         adrIt = adresses.find( \&(*it) );
436
                         if(adrIt = adresses.end())
                              \mathtt{adresses} \left[ \& \left( \ast \mathtt{it} \right) \right] \ = \!\! \mathtt{i} \, ;
439
                             p = i;
                              i ++;
440
441
                         if((\&(*it))->parent()!=\&(*tempit))
442
                           out << ';' << endl << '"'
443
                                << adresses.find( (\&(*it))->parent( ))->second << '"';
444
                         if((\&(*it)) != m\_root)
445
                             out << " -> \"" << p << '"';
446
                         tempit =it;
447
                   }
                    out << ';' << endl;
                    \mathbf{for} \ ( \ \mathtt{adrIt} \ = \mathtt{adresses.begin} ( \ ); \ \mathtt{adrIt} \ != \ \mathtt{adresses.end} ( \ ); \ +\!\!\!+ \mathtt{adrIt} \ )
                         out << adrIt->second << " [ l\,a\,b\,e\,l=\setminus""
451
                             << adrIt->first->info( ) << "\"]";
452
                   out << '} ';
453
              }
454
455
456
457
              * @function
                               copyFromNode( )
              * @abstract
                               copies the the node source and its children to the node
                               dest
              * @param
                               source, the node and its children that need to be copied
              * @param
461
                               dest, the node who is going to get the copied children
               * @param
                               left, this is true if it's a left child.
462
                               there needs to be a tree and we can't copy to a root.
              * @pre
463
              * @post
                               the subtree that starts at source is now also a child of
464
                               dest
465
466
              void copyFromNode( node_t *source, node_t *dest, bool left ) {
467
                    if (!source)
468
                        return;
470
                   node_t *acorn =new node_t( dest );
                   if(\texttt{left}) \ \{
471
                         i\,f\,(\ \mathtt{dest}\!-\!\!>\!\!\mathtt{leftChild}\,(\ )\,)
472
```

```
473
                             return:
                        dest->setLeftChild( acorn );
474
                   }
475
                   else {
476
                        if( dest->rightChild( ))
477
                             return;
478
                        dest->setRightChild( acorn );
479
480
                   cloneRecursive( source, acorn );
              }
              Tree<INFO_T>& operator=( const Tree<INFO_T>& tree ) {
484
                   {\tt clear}\,(\ )\,;
485
                   if( tree.m_root ) {
486
                        m_{root} = new node_t( (node_t*)0 );
487
                        cloneRecursive( tree.m_root, m_root );
488
489
                   return *this;
490
              }
493
         protected:
             /**
494
              * @function
                             cloneRecursive( )
495
              * @abstract
                              cloning a subtree to a node
496
              * @param
                              source, the node we want to start the cloning process from
497
              * @param
                              dest, the node we want to clone to
498
              * @post
                              the subtree starting at source is cloned to the node dest
499
              **/
500
              void cloneRecursive( node_t *source, node_t* dest ) {
                   dest->info() =source->info();
                   if ( \verb| source-> leftChild( ) ) \ \{\\
                        node_t *left =new node_t( dest );
                        dest->setLeftChild( left );
505
                        {\tt cloneRecursive} \left( \begin{array}{c} {\tt source-}{\gt} {\tt leftChild} \left( \begin{array}{c} \\ \end{array} \right), \begin{array}{c} {\tt left} \end{array} \right);
506
507
                   \mathbf{i}\mathbf{f}( source->rightChild( ) ) \{
508
                        node_t *right =new node_t( dest );
509
                        dest->setRightChild( right );
510
511
                        cloneRecursive( source->rightChild( ), right );
                   }
              }
             /**
515
              * @function
                             deleteRecursive( )
516
              * @abstract
                             delete all nodes of a given tree
517
              * @param
                              root, starting point, is deleted last
518
              * @post
                              the subtree has been deleted
519
              **/
520
              void deleteRecursive( node_t *root ) {
521
                   if( !root )
522
                        return;
                   deleteRecursive( root->leftChild( ) );
525
                   deleteRecursive( root->rightChild( ) );
                   delete root;
526
```

```
}
527
528
            /**
529
             * @function
                          getRowCountRecursive( )
530
             * @abstract
                          calculate the maximum depth/row count in a subtree
531
                           root, starting point
             * @param
532
                           level, starting level
533
             * @param
             * @return
                           maximum depth/rows in the subtree
534
             **/
             int getRowCountRecursive( node_t* root, int level ) {
                 if(!root)
                     return level;
538
                 return max (
539
                          \mathtt{getRowCountRecursive}(\ \mathtt{root}-\!\!>\!\mathtt{leftChild}(\ )\,,\ \mathtt{level}+\!1\ )\,,
540
                          getRowCountRecursive( root->rightChild( ), level+1 ) );
541
             }
542
543
            /**
             * @function
                           getRowRecursive( )
             * @abstract
                           compile a full list of one row in the tree
             * @param
                           root, starting point
                           rlist, reference to the list so far
             * @param
                           level, how many level still to go
             * @param
549
             * @post
                           a list of a row in the tree has been made.
550
             **/
551
             void getRowRecursive( node_t* root, nodelist &rlist, int level ) {
552
553
                 // Base-case
                 if(!level) {
554
                      rlist.push_back( root );
                 } else if( root ){
                     level--;
                      if( level && !root->leftChild( ) )
559
                          for ( int i =0; i < (level <<1); ++i )
                              rlist.push_back(0);
560
                      else
561
                         getRowRecursive( root->leftChild( ), rlist, level );
562
563
                      if( level && !root->rightChild( ) )
564
                          for ( int i =0; i < (level <<1); ++i )
                              rlist.push_back(0);
                      else
                          getRowRecursive( root->rightChild( ), rlist, level );
                 }
569
             }
570
571
572
             * @function
                           findRecursive( )
573
             * @abstract
                           first the first occurrence of needle and return its node
574
575
             * @param
                           haystack, root of the search tree
             * @param
                           needle, copy of the data to find
             * @return
                           the node that contains the needle
579
             **/
             node_t *findRecursive( node_t* haystack, const INFO_T &needle ) {
```

```
if(haystack->info() = needle)
581
                     return haystack;
582
583
                node_t *n = 0;
584
                 if(haystack->leftChild())
585
                     n =findRecursive( haystack->leftChild( ), needle );
586
                 if( !n && haystack->rightChild( ) )
587
                     n =findRecursive( haystack->rightChild( ), needle );
588
                return n;
            }
            friend class TreeNodeIterator_pre<INFO_T>;
592
            {\bf friend \ class \ TreeNodeIterator\_in}{<} {\tt INFO\_T>};
593
            friend class SplayTree<INFO_T>;
594
            TreeNode<INFO_T> *m_root;
595
596
        private:
597
            /**
            * @function
                          getFirstEmptySlot( )
              @abstract when a row has a continuous empty space on the right,
                          find the left-most parent in the above row that has
                          at least one empty slot.
602
            * @param
                          level, how many level still to go
603
            * @return
                          the first empty slot where we can put a new node
604
            * @pre
                          level should be > 1
605
            **/
606
            node_t *getFirstEmptySlot( int level ) {
607
                node_t *p = 0;
608
                nodelist rlist =row( level-1 ); // we need the parents of this level
                 /** changed auto to int **/
                 if(!(*it)->hasChildren())
613
                         p = (*it);
                     \mathbf{else} \ \mathbf{if} (\ !(*\mathit{it}) -> \mathit{rightChild}(\ )\ )\ \{\\
614
                         p = (*it);
615
                         break;
616
                     } else
617
                         break;
618
619
                return p;
            }
622
    };
623
^{624} #endif
         TreeNode.h
    6.4
    /**
 2
    * Treenode:
     * @author Micky Faas (s1407937)
                Lisette de Schipper (s1396250)
     * @author
     * Ofile
                Treenode.h
                26-10-2014
     * @date
```

```
**/
   #ifndef TREENODE.H
10
   #define TREENODE.H
12
   using namespace std;
13
14
   template <class INFO_T> class Tree;
15
    class ExpressionTree;
17
   template < class INFO_T > class TreeNode
19
         public:
20
            /**
21
              * Ofunction TreeNode()
22
              * @abstract
                             Constructor, creates a node
23
                              info, the contents of a node
              * @param
24
              * @param
                              parent, the parent of the node
25
              * @post
                              A node has been created.
              **/
              \label{thm:const_info_T& info_T& info_T} {\tt TreeNode} < {\tt INFO_T} > * \ {\tt parent} \ = 0 \ )
                   : \ \mathtt{m\_lchild} \left( \begin{array}{c} 0 \end{array} \right), \ \mathtt{m\_rchild} \left( \begin{array}{c} 0 \end{array} \right) \ \{
29
                   m_info =info;
30
                   {\tt m\_parent} \ = \! {\tt parent} \ ;
31
             }
32
33
            /**
34
              * Ofunction TreeNode()
35
              * @abstract Constructor, creates a node
              * @param
                              parent, the parent of the node
              * @post
                              A node has been created.
              **/
             {\tt TreeNode} ( \ {\tt TreeNode} {<} {\tt INFO\_T} {>} * \ {\tt parent} \ = 0 \ )
40
                  : m_lchild(0), m_rchild(0) {
41
                   m_parent =parent;
42
              }
43
44
45
46
              * @function
              * @abstract Sets a nodes content to \ensuremath{\mathtt{N}}
              * @param
                              n, the contents you want the node to have
              * @post
                              The node now has those contents.
              **/
50
             void operator =( INFO_T n ) { m_info =n; }
51
52
            /**
53
              * @function INFO_T(), info()
54
              * @abstract Returns the content of a node
55
                              m_info, the contents of the node
56
57
              **/
              operator INFO_T( ) const { return m_info; }
              const INFO_T &info( ) const { return m_info; }
              {\tt INFO\_T \& info( ) \{ return m\_info; } \}
60
              /**
61
```

```
* @function atRow()
 62
                           * @abstract returns the level or row-number of this node
 63
                          * @return
                                                       row, an int of row the node is at
 64
                          **/
 65
                          int atRow( ) const {
 66
                                    const TreeNode < INFO_T > *n = this;
 67
                                    int row = 0;
 68
                                    while( n->parent( ) ) {
 69
                                            n = n->parent();
                                            row++;
 71
 72
                                   {\bf return\ row}\,;
 73
                          }
 74
 75
 76
                          * @function parent(), leftChild(), rightChild()
 77
                                                       returns the adress of the parent, left child and right
                          * @abstract
 78
                                                        child respectively
 79
                                                        the adress of the requested family member of the node
                          * @return
                          **/
                          TreeNode<INFO_T> *parent( ) const { return m_parent; }
                          TreeNode<INFO_T> *leftChild( ) const { return m_lchild; }
 83
                          TreeNode<INFO_T> *rightChild( ) const { return m_rchild; }
 84
 85
 86
                          * @function
                                                      swapWith( )
 87
                          * @abstract Swaps this node with another node in the tree
 88
                                                        n, the node to swap this one with
 89
                           * @param
                          * @pre
                                                        both this node and n must be in the same parent tree
                          * @post
                                                        n will have the parent and children of this node
                                                        and vice verse. Both nodes retain their data.
                          **/
                          {\bf void} swapWith( TreeNode<INFO_T>* n ) {
 94
                                    {\bf bool\ this\_wasLeftChild\ =} {\bf false}\;,\;\; {\bf n\_wasLeftChild\ =} {\bf false}\;;
 95
                                    if(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(pare
 96
                                             this\_wasLeftChild = true;
 97
                                    if(n->parent() \&\& n->parent()->leftChild() == n)
 98
                                            n_wasLeftChild =true;
 99
100
                                    // Swap the family info
                                   TreeNode < INFO_T > * newParent =
                                            (n->parent() = this)? n : n->parent();
                                    {\tt TreeNode}{<}{\tt INFO\_T}{>}{*}\ {\tt newLeft}\ =
104
                                            (n->leftChild() = this)? n:n->leftChild();
105
                                    TreeNode<INFO_T>* newRight =
106
                                               (n\rightarrow rightChild() = this)? n:n\rightarrow rightChild();
107
108
                                   n->setParent( parent( ) == n ? this : parent( ) );
109
                                   n->setLeftChild( leftChild( ) == n ? this : leftChild( ) );
110
111
                                   n->setRightChild( rightChild( ) == n ? this : rightChild( ) );
113
                                    setParent( newParent );
114
                                    setLeftChild( newLeft );
                                    setRightChild( newRight );
115
```

```
116
                  // Restore applicable pointers
117
                  if(n->leftChild())
118
                      {\tt n->leftChild(\ )->setParent(\ n\ );}
119
                  if( n->rightChild( ) )
120
                      n->rightChild( )->setParent( n );
121
                  if( leftChild( ) )
122
                      leftChild( )->setParent( this );
123
                  if( rightChild( ) )
                      rightChild()->setParent(this);
                  if(n->parent())
                       if( this_wasLeftChild )
127
                           {\tt n-\!\!>\!\!parent(\ )-\!\!>\!\!setLeftChild(\ n\ );}
128
                       else
129
                           n->parent( )->setRightChild( n );
130
131
                  if( parent( ) ) {
132
                       if( n_wasLeftChild )
133
                           \verb|parent( )-> \verb|setLeftChild( this );||
                       else
                           parent( )->setRightChild( this );
                  }
137
             }
138
139
140
             * @function
                            replace()
141
                            Replaces the node with another node in the tree
142
             * @abstract
                            n, the node we replace the node with, this one gets deleted
143
              * @param
             * @pre
                            both this node and n must be in the same parent tree
             * @post
                            The node will be replaced and n will be deleted.
             **/
             void replace( TreeNode<INFO_T>* n ) {
                  {\bf bool\ n\_wasLeftChild\ =} {\bf false}\;;
148
149
                  if(n->parent() \& n->parent()->leftChild() == n)
150
                      n_{wasLeftChild} = true;
151
152
                  // Swap the family info
153
                  TreeNode<INFO_T>* newParent =
154
                       ( n->parent( ) == this ) ? n : n->parent( );
                  TreeNode < INFO_T > * newLeft =
                      (n->leftChild() = this)? n:n->leftChild();
                  TreeNode<INFO_T>* newRight =
158
                        ( \  \, \text{n->} \text{rightChild} ( \ ) == \ this \ ) \ ? \ n \ : \text{n->} \text{rightChild} ( \ );
159
160
                  setParent( newParent );
161
                  setLeftChild( newLeft );
162
                  setRightChild( newRight );
163
                  m_info = n->m_info;
164
165
                  // Restore applicable pointers
167
                  if( leftChild( ) )
                       leftChild( )->setParent( this );
168
                  if( rightChild( ) )
169
```

```
rightChild( )->setParent( this );
170
171
                                      if( parent( ) ) {
172
                                               if( n_wasLeftChild )
173
                                                        parent( )->setLeftChild( this );
174
175
                                                         parent( )->setRightChild( this );
176
177
                                      delete n;
                            }
179
                            /**
181
                            * Ofunction
                                                         sibling( )
182
                                                          returns the address of the sibling
183
                            * @abstract
                            * @return
                                                           the address to the sibling or zero if there is no sibling
184
                            **/
185
                            {\tt TreeNode}{<} {\tt INFO\_T}{>}{*} \ {\tt sibling} (\ ) \ \{
186
                                      if(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(pare
187
                                               return parent( )->rightChild( );
                                      else if( parent( )->rightChild( ) == this )
                                               return parent( )->leftChild( );
                                      else
191
                                               return 0;
192
                            }
193
194
195
                                                         hasChildren(), hasParent(), isFull()
196
                            * @function
                                                         Returns whether the node has children, has parents or is
197
                                                           full (has two children) respectively
198
                            * @param
                            * @return
                                                           true or false, depending on what is requested from the node.
                                                           if hasChildren is called and the node has children, it will
                                                           \hbox{return true, otherwise false.}\\
202
                                                           If hasParent is called and the node has a parent, it will
203
                                                           return true, otherwise false.
204
                                                           If is Full is called and the node has two children, it will
205
                                                           return true, otherwise false.
206
207
                            bool hasChildren( ) const { return m_lchild || m_rchild; }
208
                            bool hasParent( ) const { return m_parent; }
                            bool isFull( ) const { return m_lchild && m_rchild; }
                   protected:
212
                            friend class Tree<INFO_T>;
213
                            {\bf friend} \ \ {\bf class} \ \ {\tt ExpressionTree} \, ;
214
215
                          /**
216
                            * @function
                                                           setParent(), setLeftChild(), setRightChild()
217
                                                           sets the parent, left child and right child of the
218
219
                                                           particular node respectively
                            * @param
                                                           p, the node we want to set a certain family member of
                            * @return
                                                           void
222
                            * @post
                                                           The node now has a parent, a left child or a right child
                                                           respectively.
223
```

```
**/
224
                void setParent( TreeNode<INFO_T> *p ) { m_parent =p; }
225
                 \mathbf{void} \ \mathtt{setLeftChild} ( \ \mathtt{TreeNode} {<} \mathtt{INFO}_\mathtt{T} {>} \ *p \ ) \ \{ \ \mathtt{m\_lchild} \ {=} \mathtt{p} \, ; \ \}
226
                 void setRightChild( TreeNode<INFO_T> *p ) { m_rchild =p; }
227
228
           private:
229
                 INFO_T m_info;
230
                 TreeNode<INFO_T> *m_parent;
231
                 TreeNode<INFO_T> *m_lchild;
                TreeNode<INFO_T> *m_rchild;
233
234
     };
235
236
     * @function
237
     * @abstract
                       the contents of the node are returned
238
     * @param
                       out, in what format we want to get the contents
239
                       rhs, the node of which we want the contents
     * @param
240
     * @return
                       the contents of the node.
241
     **/
     \textbf{template} < \textbf{class} \hspace{0.2cm} \texttt{INFO\_T} > \hspace{0.2cm} \texttt{ostream} \hspace{0.2cm} \& \hspace{0.2cm} \texttt{operator} \hspace{0.2cm} << \hspace{-0.2cm} (\texttt{ostream} \& \hspace{0.2cm} \texttt{out} \hspace{0.2cm}, \hspace{0.2cm} \textbf{const} \hspace{0.2cm} \texttt{TreeNode} < \texttt{INFO\_T} > \hspace{0.2cm} \& \hspace{0.2cm} \texttt{r} = \hspace{-0.2cm} \texttt{out} \hspace{0.2cm} .
           out << rhs.info( );</pre>
           return out;
245
     }
246
247
_{248} #endif
            TreeNodeIterator.h
     6.5
     /**
      * TreeNodeIterator: Provides a set of iterators that follow the STL-standard
      * @author Micky Faas (s1407937)
      * Cauthor Lisette de Schipper (s1396250)
      * @file
                      TreeNodeIterator.h
       * @date
                      26-10-2014
 10 #include <iterator>
     #include "TreeNode.h"
     template < class \  \, \texttt{INFO\_T} \! > \  \, class \  \, \texttt{TreeNodeIterator}
 13
                                        : public std::iterator<std::forward_iterator_tag,
 14
                                                                        TreeNode<INFO_T>>> {
 15
           public:
 16
                 typedef TreeNode<INFO_T> node_t;
 17
 18
 19
                 * Ofunction TreeNodeIterator()
 20
                 * @abstract (copy)constructor
                 * @pre
                                   TreeNodeIterator is abstract and cannot be constructed
                **/
                TreeNodeIterator( node_t* ptr =0 ) : p( ptr ) { }
                {\tt TreeNodeIterator(\ const\ TreeNodeIterator\&\ it\ )\ :\ p(\ it.p\ )\ \{\ \}}
 25
```

26

```
/**
27
             * @function
                             (in)equality operator overload
28
             * @abstract
                             Test (in)equality for two TreeNodeIterators
29
                             rhs, right-hand side of the comparison
              * @param
30
              * @return
                             true if both iterators point to the same node (==)
31
                             false if both iterators point to the same node (!=)
32
             **/
33
             bool operator == (const TreeNodeIterator& rhs) { return p=rhs.p; }
             37
             * @function
                             operator*( )
38
             * @abstract
                             Cast operator to node_t reference
39
                             The value of the current node
40
             * @return
              * @pre
                             Must point to a valid node
41
             **/
42
             node_t& operator*( ) { return *p; }
43
44
             * Ofunction operator++()
                             pre- and post increment operators
             * @abstract
             * @return
                             {\tt TreeNodeIterator\ that\ has\ iterated\ one\ step}
48
49
             {\tt TreeNodeIterator~\& operator} ++(~)~\{~{\tt next(~)};~{\tt return~*this}\,;~\}
50
             TreeNodeIterator operator++( int )
51
                  { TreeNodeIterator tmp(*this); operator++(); return tmp; }
52
53
         protected:
54
            /**
55
             * Ofunction next() //(pure virtual)
             * @abstract Implement this function to implement your own iterator
             virtual bool next( ){ return false; }// =0;
59
60
             node_t *p;
    };
61
62
    template <class INFO_T> class TreeNodeIterator_pre
63
                                 : public TreeNodeIterator<INFO_T> {
64
65
         public:
             {f typedef} TreeNode<INFO_T> node_t;
             TreeNodeIterator_pre( node_t* ptr =0 )
                  : TreeNodeIterator<INFO_T>( ptr ) { }
69
             {\tt TreeNodeIterator\_pre} \left( \begin{array}{ccc} {\tt const} & {\tt TreeNodeIterator}{<} {\tt INFO\_T}{>} \& \ {\tt it} \end{array} \right)
70
                  : TreeNodeIterator<INFO_T>( it ) { }
71
             {\tt TreeNodeIterator\_pre} \left( \begin{array}{c} {\bf const} \end{array} \right. {\tt TreeNodeIterator\_pre} \& \ {\tt it} \  \  \, )
72
                  : TreeNodeIterator<INFO_T>( it.p ) \{ \}
73
74
             TreeNodeIterator_pre &operator++( ) { next( ); return *this; }
75
             TreeNodeIterator_pre operator++( int )
76
                   \{ \  \, \texttt{TreeNodeIterator\_pre} \  \, \texttt{tmp(} \  \, *\textbf{this} \  \, ); \  \, \textbf{operator} + + ( \  \, ); \  \, \textbf{return} \  \, \texttt{tmp;} \  \, \} 
77
79
         protected:
             \mathbf{using} \ \mathsf{TreeNodeIterator} {<} \mathsf{INFO\_T} {>} {::} \mathsf{p} \, ;
```

```
81
             /**
82
               * Ofunction next()
83
               * @abstract
                              Takes one step in pre-order traversal
84
               * @return
                               returns true if such a step exists
85
               */
86
               bool next( ) {
87
                    if(!p)
88
                         return false;
                    if( p->hasChildren( ) ) \{ // a possible child that can be the next
                         p = p -> leftChild( ) ? p -> leftChild( ) : p -> rightChild( );
91
                         return true;
92
93
                    \mathbf{else} \ \mathbf{if} \left( \ \mathbf{p} \!\!\!\! - \!\!\!\! \mathsf{>} \!\! \mathsf{hasParent} \left( \ \right) \ / / \ \mathsf{we have a right brother} \right.
94
                              && p->parent()->rightChild()
95
                             && p->parent( )->rightChild( ) != p ) {
96
                         {\tt p} = \!\! {\tt p-\!\!>} {\tt parent} \, ( \ ) - \!\! > \!\! {\tt rightChild} \, ( \ ) \, ;
97
                         return true;
98
                    else if ( p->hasParent( ) ) \{ // just a parent, thus we go up
                         TreeNode < INFO_T > *tmp = p -> parent();
                         while( tmp->parent( ) ) {
102
                              if ( tmp->parent( )->rightChild( )
103
                                        && tmp->parent(\ )->rightChild(\ ) != tmp ) {
104
                                   p =tmp->parent( )->rightChild( );
105
                                   return true;
106
107
                              tmp =tmp->parent( );
108
                         }
109
                    // Nothing left
                    p = 0;
113
                    return false;
               }
114
115
     };
116
117
     template <class INFO_T> class TreeNodeIterator_in
118
119
                                   : public TreeNodeIterator<INFO_T>{
          public:
              typedef TreeNode<INFO_T> node_t;
               TreeNodeIterator_in( node_t* ptr =0 )
123
                   : TreeNodeIterator<INFO_T>( ptr ) \{ \}
124
               TreeNodeIterator_in( const TreeNodeIterator<INFO_T>& it )
125
                    : TreeNodeIterator<INFO_T>( it ) { }
126
               TreeNodeIterator_in( const TreeNodeIterator_in& it )
127
                    : TreeNodeIterator<INFO_T>( it.p ) \{ \}
128
129
               TreeNodeIterator_in & operator++( ) { next( ); return *this; }
130
               TreeNodeIterator_in operator++( int )
                     \{ \  \, {\tt TreeNodeIterator\_in} \  \, {\tt tmp(\ *this\ )}; \  \, {\tt operator} + + (\ ); \  \, {\tt return} \  \, {\tt tmp;} \  \, \} 
132
133
          protected:
134
```

```
using TreeNodeIterator<INFO_T>::p;
135
             /**
136
              * @function
                             next()
137
              * @abstract
                              Takes one step in in-order traversal
138
              * @return
                              returns true if such a step exists
139
              */
140
              bool next( ) {
141
                   if( p->rightChild( ) ) {
142
                        p =p->rightChild( );
                        \mathbf{while}(\ p \rightarrow \mathtt{leftChild}(\ )\ )
144
                            p =p->leftChild( );
                        return true;
146
147
                   {\tt else \ if(\ p->parent(\ )} \ \&\& \ p->parent(\ )->{\tt leftChild(\ )} \ \Longrightarrow \ p \ ) \ \{
148
                        p =p->parent( );
149
                        return true;
150
                   } else if( p->parent( ) && p->parent( )->rightChild( ) = p ) {
151
                        p = p->parent();
152
                        \mathbf{while}(\ p\text{--}\mathsf{parent}(\ )\ \&\&\ p\ \Longrightarrow\ p\text{--}\mathsf{parent}(\ )\text{--}\mathsf{rightChild}(\ )\ )\ \{
                            p = p->parent();
                        if( p )
156
                            p = p->parent();
157
                        if( p )
158
                             return true:
159
                        else
160
                             return false;
161
162
                   // Er is niks meer
163
                   p = 0;
                   return false;
165
              }
166
167
    };
168
    template <class INFO_T> class TreeNodeIterator_post
169
                                  : public TreeNodeIterator<INFO_T>{
170
         public:
171
              typedef TreeNode<INFO_T> node_t;
172
173
              TreeNodeIterator_post( node_t* ptr =0 )
                   : TreeNodeIterator<INFO_T>( ptr ) { }
              TreeNodeIterator_post( const TreeNodeIterator<INFO_T>& it )
177
                   : TreeNodeIterator<INFO_T>( it ) { }
              {\tt TreeNodeIterator\_post(\ const\ TreeNodeIterator\_post\&\ it\ )}
178
                   : TreeNodeIterator<INFO_T>( it.p ) \{ \}
179
180
              TreeNodeIterator_post & operator++( ) { next( ); return *this; }
181
              TreeNodeIterator_post operator++( int )
182
                   { TreeNodeIterator_post tmp( *this ); operator++( ); return tmp; }
183
184
         protected:
              using TreeNodeIterator<INFO_T>::p;
187
             /**
              * @function next()
188
```

```
* @abstract Takes one step in post-order traversal
189
             * @return
                           returns true if such a step exists
190
             */
191
             bool next( ) {
192
193
                 if( p->hasParent( ) // We have a right brother
194
                          && p->parent()->rightChild()
195
                          && p->parent( )->rightChild( ) != p ) {
196
                      p =p->parent( )->rightChild( );
                      while( p->leftChild( ) )
                          p = p->leftChild();
                      return true;
200
                 } else if( p->parent( ) ) {
201
                      p = p->parent();
202
                      return true;
203
204
                 // Nothing left
205
                 p = 0;
                 return false;
             }
    };
209
    6.6
          SelfOrganizingTree.h
     * SelfOrganizingTree - Abstract base type inheriting from Tree
                Micky Faas (s1407937)
     * @author
                 Lisette de Schipper (s1396250)
     * @author
     * @file
                 SelfOrganizingTree.h
     * @date
                 3-11-2014
     **/
   #ifndef SELFORGANIZINGTREE_H
10
   #define SELFORGANIZINGTREE_H
11
12
   #include "BinarySearchTree.h"
13
    	ext{template} < 	ext{class} 	ext{ INFO_T} > 	ext{class SelfOrganizingTree} : 	ext{public BinarySearchTree} < 	ext{INFO_T} > \{
        public:
16
             typedef BSTNode<INFO_T> node_t;
17
             {\bf typedef~BinarySearchTree}{<} {\tt INFO\_T}{>}~{\tt S}~;~{\tt //~super~class}
18
19
20
                           SelfOrganizingTree() : S()
             * @function
21
             * @abstract
                          Constructor
22
23
             SelfOrganizingTree( ) : S( ) { }
24
             * @function
                          rotateLeft( ) and rotateRight( )
28
             * @abstract
                           Performs a rotation with the given node as root of the
                           rotating subtree, either left of right.
29
                           The tree's root pointer will be updated if neccesary.
30
```

```
{\tt node}, the {\tt node} to {\tt rotate}
31
            * @param
            * @pre
                          The node must be a node in this tree
32
                          The node may be be the new root of the tree
            * @post
33
                          No nodes will be invalided and no new memory is
34
                          allocated. Iterators may become invalid.
35
            **/
36
            virtual node_t *rotateLeft( node_t * node ){
37
                if(this->root() = node)
38
                    return static_cast<node_t *>( S::m_root = node->rotateLeft( ) );
                else
40
                    return node->rotateLeft( );
41
            }
42
43
            virtual node_t *rotateRight( node_t * node ){
44
                if(this->root() = node)
45
                    return static_cast<node_t *>( S::m_root = node->rotateRight( ) );
46
47
                    return node->rotateRight( );
48
            }
       private:
51
52
   };
53
54
55
  #endif
         BinarySearchTree.h
   6.7
    * BinarySearchTree - BST that inherits from Tree
2
    * @author Micky Faas (s1407937)
    * @author
               Lisette de Schipper (s1396250)
    * @file
                BinarySearchTree.h
    * @date
                3-11-2014
   #ifndef BINARYSEARCHTREE_H
   #define BINARYSEARCHTREE.H
11
12
   #include "Tree.h"
13
   \#include "BSTNode.h"
14
15
   template <class INFO_T> class BinarySearchTree : public Tree<INFO_T> {
16
       public:
17
            typedef BSTNode<INFO_T> node_t;
18
            typedef Tree<INFO_T> S; // super class
19
            BinarySearchTree( ) : S( ) { }
            {\tt BinarySearchTree(\ const\ BinarySearchTree\&\ cpy\ )\ :\ S(\ cpy\ )\ \{\ \}}
            virtual ~BinarySearchTree( ) { }
24
```

```
/**
26
             * Ofunction pushBack()
27
                           reimplemented virtual function from Tree <>
             * @abstract
28
                            this function is semantically identical to insert()
29
             * @param
                            info, the contents of the new node
30
             **/
31
             virtual node_t *pushBack( const INFO_T& info ) {
32
                 return insert( info );
33
             }
           /**
37
             * @function
                          insert( )
             * @abstract
                           reimplemented virtual function from Tree<>
38
                            the exact location of the new node is determined
39
                            by the rules of the binary search tree.
40
             * @param
                            info, the contents of the new node
41
                            parent, ignored
             * @param
42
             * @param
                            preferRight, ignored
43
             * @param
                           replaceBehavior, ignored
             * @return
                           returns a pointer to the inserted node
46
             **/
             virtual node_t* insert( const INFO_T& info,
47
                                    {\tt TreeNode}{<}{\tt INFO\_T}{>}{*} {\tt parent} \ = 0, \ // \ {\tt Ignored}
48
                                    {\bf bool\ preferRight\ =} {\bf false}\;, \qquad \  \  //\ {\tt Ignored}
49
                                    int replaceBehavior =S::ABORT_ON_EXISTING ) { // Ignored}
50
                 node_t *n =new node_t( );
51
                 return insertInto( info, n );
52
            }
53
54
           /**
             * Ofunction replace()
             * @abstract reimplemented virtual function from Tree<>
57
58
                            replaces a given node or the root
                            the location of the replaced node may be different
59
                            due to the consistency of the binary search tree
60
             * @param
                            info, the contents of the new node
61
             * @param
                            node, node to be replaced
62
              @param
                            alignRight, ignored
63
64
             * @param
                            replaceBehavior, ignored
             * @return
                            returns a pointer to the new node
             * @pre
                            node should be in this tree
             * @post
                            replace() will delete and/or remove node.
                            if node is 0, it will take the root instead
68
69
             \mathbf{virtual} \ \ \mathtt{node\_t*} \ \ \mathtt{replace} \big( \ \ \mathbf{const} \ \ \mathtt{INFO\_T} \& \ \ \mathtt{info} \ ,
70
                                     TreeNode < INFO_T > * node = 0,
71
                                     bool alignRight = false,
72
                                     int replaceBehavior =S::DELETE_EXISTING ) {
73
                 node_t *newnode;
74
                 if( !node )
75
                      \verb"node =S::m_root";
77
                 if (!node)
                      return pushBack( info );
78
```

```
bool swap =false;
80
                 // We can either just swap the new node with the old and remove
81
                 // the old, or we can remove the old and add the new node via
82
                 // pushBack(). This depends on the value of info
83
                 if ( \ ! {\tt node} {\tt ->} {\tt hasChildren} ( \ ) \ ) \ \{
84
                      swap = true;
85
86
                 else if( !(node->leftChild( )
87
                          && node->leftChild( )->info( ) > info )
                          && !(node->rightChild()
89
                          && node->rightChild( )->info( ) < info ) ) {
90
                      swap = true;
91
92
                  if(swap) {
93
                      newnode =new node_t( info );
94
                      if ( node == S::m_root )
95
                           S::m_root =newnode;
96
                      node->swapWith( newnode );
                      delete node;
                 } else {
                      remove( node );
                      newnode =pushBack( info );
101
102
103
                 return newnode;
104
             }
105
106
107
             * @function
                           remove()
108
             * @abstract
                           reimplemented virtual function from Tree<>
                           removes a given node or the root and restores the
                           BST properties
112
             * @param
                           node, node to be removed
             * @pre
                           node should be in this tree
113
             * @post
                           memory for node will be deallocated
114
115
             virtual void remove( TreeNode<INFO_T> *node ) {
116
                 node_t *n =static_cast<node_t*>( node );
117
118
                 while ( n->isFull( ) ) {
                      // the difficult case
                      // we could take either left of right here
                      {\tt TreeNode}{<} {\tt INFO\_T}{>} \ *{\tt temp} \ ;
122
                      temp =n->leftChild( );
123
                      while( temp->rightChild( ) ) {
124
                          temp =temp->rightChild( );
125
126
                      if( n == S::m_root )
127
                          S::m_root =temp;
128
129
                      n->swapWith( temp );
                 }
131
132
                 // Assume the above is fixed
133
```

```
while( n->hasChildren( ) ) {
134
                     if(n->leftChild())
135
                         if( n == S::m_root )
136
                             S::m_root =n->leftChild();
137
                         n->swapWith( n->leftChild( ) );
138
                     }
139
                     else {
140
                         if( n == S::m_root )
141
                              S::m_root =n->rightChild();
                         n->swapWith( n->rightChild( ) );
                     }
                }
145
146
                 if(n->parent() \& n->parent()->leftChild() == n)
147
                     static\_cast < node\_t*> (n->parent())-> setLeftChild(0);
148
                 {\tt else \ if(\ n->parent(\ ) \&\&\ n->parent(\ )->rightChild(\ ) == n\ )}
149
                     static\_cast < node\_t*> (n->parent())-> setRightChild(0);
150
                 delete n;
151
            }
           /**
            * @function
                          find()
155
            * @abstract
                          reimplemented virtual function from Tree<>
156
                          performs a binary search in a given (sub)tree
157
              @param
                          haystack, the subtree to search. Give 0 for the entire tree
158
              @param
                          needle, key/info-value to find
159
            * @return
                          returns a pointer to node, if found
160
             * @pre
                          haystack should be in this tree
161
            * @post
                          may return 0
162
            **/
            virtual TreeNode<INFO_T>* find( TreeNode<INFO_T>* haystack,
                                               const INFO_T& needle ) {
                 m_searchStepCounter = 0;
166
167
                 if( !haystack )
168
                     haystack =S::m_root;
169
                 while( haystack && haystack->info( ) != needle ) {
170
                     m_searchStepCounter++;
171
172
                     if( haystack->info( ) > needle )
                         haystack =haystack->leftChild( );
                     else
                         haystack =haystack->rightChild( );
176
                 if( !haystack )
177
                     m_searchStepCounter = -1;
178
                 return haystack;
179
            }
180
181
           /**
182
            * @function
                          lastSearchStepCount( )
183
            * @abstract
                          gives the amount of steps needed to complete the most
                          recent call to find()
186
              @return
                          positive amount of steps on a defined search result,
                          -1 on no search result
187
```

```
188
            virtual int lastSearchStepCount( ) const {
189
                 return m_searchStepCounter;
190
            }
191
192
           /**
193
            * @function
                              min()
194
             * @abstract
                              Returns the node with the least value in a binary search
195
                              tree. This is achieved through recursion.
            * @param
                              node - the node from which we start looking
              @return
                              Eventually, at the end of the recursion, we return the
199
                              adress of the node with the smallest value.
            * @post
                              The node with the smallest value is returned.
200
            **/
201
            node_t* min( node_t* node ) const {
202
                 return node->leftChild( ) ?
203
                        min(static_cast<node_t*>( node->leftChild( ) ) ) : node;
204
            }
            /**
                              min()
            * @function
             * @abstract
                              We call the function mentioned above and then
209
                              return the node with the least value in a binary search
210
211
                              tree.
            * @return
                              We return the adress of the node with the smallest value.
212
            * @post
                              The node with the smallest value is returned.
213
            **/
214
            node_t* min( ) const {
215
                 return min( static_cast < node_t*>( this->root( ) ) );
216
            }
            /**
            * @function
220
                              max()
              @abstract
                              Returns the node with the highest value in a binary
221
                              search tree. This is achieved through recursion.
222
            * @param
                              node - the node from which we start looking
223
              @return
                              Eventually, at the end of the recursion, we return the
224
225
                              adress of the node with the highest value.
226
            * @post
                              The node with the highest value is returned.
            **/
            node_t* max( node_t* node ) const
                 return node->rightChild( ) ?
                        \verb|max(static_cast| < \verb|node_t*| < \verb|node_rightChild( ) ) ) : \verb|node|;
230
            }
231
232
233
             * @function
                              max()
234
                              We call the function mentioned above and then
235
                              return the node with the highest value in a binary
236
237
                              search tree.
            * @return
                              We return the adress of the node with the highest value.
239
            * @post
                              The node with the highest value is returned.
            **/
240
            node_t* max( ) const {
241
```

```
return max( static_cast < node_t *>( this -> root( ) ) );
242
             }
243
244
        protected:
245
             /**
246
             * @function
                          insertInto( )
247
               @abstract Inserts new node into the tree following BST rules
248
                           Assumes that the memory for the node is already allocated
                           This function exists mainly because of derived classes
                           want to insert nodes of a derived type.
             * @param
                           info, the contents of the new node
             * @param
                           n, node pointer, should be already allocated
253
             * @return
                           returns a pointer to the inserted node
254
             **/
255
             virtual node_t* insertInto( const INFO_T& info,
256
                                   node_t*n ) { // Preallocated
257
                 n->info() =info;
258
259
                 if( !S::m_root )
                      S:=m_root =n;
                  else {
                      node_t *parent = 0;
263
                      node_t *sub =static_cast < node_t*>( S::m_root );
264
                      do {
265
                           if(*n < *sub) {
266
                               parent =sub;
267
                               sub =static_cast < node_t*>( parent->leftChild( ) );
268
269
                          else {
                               parent =sub;
                               sub =static_cast < node_t*>( parent -> rightChild( ) );
                      } while( sub );
274
                      i\,f\,(\ *\mathtt{n}\ <\ *\mathtt{parent}\ )
275
                          parent->setLeftChild( n );
276
277
                          parent->setRightChild( n );
278
                      n->setParent( parent );
279
280
                 return n;
             }
             int \  \, \texttt{m\_searchStepCounter} \, ;
284
    };
285
286
_{287} #endif
    6.8
          BSTNode.h
    /**
 2
     * BSTNode - Node atom for BinarySearchTree
 3
     * @author Micky Faas (s1407937)
 4
     * @author Lisette de Schipper (s1396250)
```

```
* @file
                BSTNode.h
    * @date
                3-11-2014
  #ifndef BSTNODE_H
10
  #define BSTNODE_H
11
12
  #include "TreeNode.h"
13
14
   template <class INFO_T> class BinarySearchTree;
15
16
   template <class INFO_T> class BSTNode : public TreeNode<INFO_T>
17
18
       public:
19
            typedef TreeNode<INFO_T> S; // super class
20
21
22
            * Ofunction BSTNode()
23
            * @abstract Constructor, creates a node
            * @param
                          info, the contents of a node
                          parent, the parent of the node
            * @param
            * @post
                          A node has been created.
27
            **/
28
            BSTNode( const INFO_T& info, BSTNode<INFO_T>* parent =0 )
29
                : S( info, parent ) { }
30
31
           /**
32
            * @function BSTNode()
33
            * @abstract Constructor, creates a node
            * @param
                          parent, the parent of the node
            * @post
                          A node has been created.
37
            **/
            {\tt BSTNode} \left( \begin{array}{ccc} {\tt BSTNode} {<} {\tt INFO\_T} {>} * \begin{array}{c} {\tt parent} \end{array} = 0 \end{array} \right)
38
                : S( (S)parent ) { }
39
40
            // Idea: rotate this node left and return the node that comes in its place
41
            BSTNode *rotateLeft( ) {
42
43
                if( !this \rightarrow prightChild( ) ) // Cannot rotate
44
                    return this;
                bool isLeftChild =this->parent( ) && this == this->parent( )->leftChild(
47
48
                // new root of tree
49
                50
                // new rightchild of the node that is rotated
51
                BSTNode *newRight =static_cast <BSTNode *>(newTop->leftChild( ));
52
                // the parent under which all of the magic is happening
53
                BSTNode *topParent =static_cast <BSTNode *>(this->parent( ));
54
55
                // We become left-child of our right-child
                // newTop takes our place with our parent
57
                newTop->setParent( topParent );
58
                if( isLeftChild && topParent )
59
```

```
topParent->setLeftChild( newTop );
60
                 else if( topParent )
61
                     topParent->setRightChild( newTop );
62
63
                newTop->setLeftChild( this );
64
                 this->setParent( newTop );
65
66
                // We take the left-child of newTop as our right-child
                 this->setRightChild( newRight );
                 if( newRight )
69
                     newRight->setParent( this );
70
71
                {\bf return\ newTop}\,;
72
            }
73
74
            // Idea: rotate this node right and return the node that comes in its place
75
            BSTNode *rotateRight( ) {
76
                 if( !this->leftChild( ) ) // Cannot rotate
77
                     return this;
                 bool isRightChild =this->parent( ) && this == this->parent( )->rightChild
81
                 // new root of tree
82
                BSTNode *newTop =static_cast <BSTNode *>(this->leftChild( ));
83
                 // new leftchild of the node that is rotated
84
                BSTNode *newLeft =static_cast < BSTNode *>(newTop->rightChild( ));
85
                 // the parent under which all of the magic is happening
86
                BSTNode *topParent =static_cast <BSTNode *>(this->parent( ));
87
88
                // We become left-child of our right-child
                 // newTop takes our place with our parent
                newTop->setParent( topParent );
92
                 if( isRightChild && topParent )
                     topParent->setRightChild( newTop );
93
                 else if( topParent )
94
                     topParent->setLeftChild( newTop );
95
96
                newTop->setRightChild( this );
97
                 this->setParent( newTop );
98
                 // We take the left-child of newTop as our right-child
                 this->setLeftChild( newLeft );
                 if( newLeft )
102
                     newLeft->setParent( this );
103
104
                return newTop;
105
            }
106
107
            bool operator <( const BSTNode<INFO_T> &rhs ) {
108
                return S::info() < rhs.info();</pre>
109
            }
112
            bool operator <=( const BSTNode<INFO_T> &rhs ) {
                return S::info() <= rhs.info();
113
```

```
}
114
115
             bool operator >( const BSTNode<INFO_T> &rhs ) {
116
                  return S::info() > rhs.info();
117
118
119
             bool operator >=( const BSTNode<INFO_T> &rhs ) {
120
                  return S::info() >= rhs.info();
121
             }
         protected:
123
             friend class BinarySearchTree<INFO_T>;
124
    };
125
126
_{127} #endif
          AVLTree.h
    6.9
    /**
     * \ \texttt{AVLTree} \ - \ \texttt{AVL-SelfOrganizingTree} \ \ \texttt{that} \ \ \texttt{inherits} \ \ \texttt{from} \ \ \texttt{SelfOrganizingTree}
 2
     * @author Micky Faas (s1407937)
     * @author Lisette de Schipper (s1396250)
     * @file
                  AVLTree.h
     * @date
                  9-12-2014
   #ifndef AVLTREE_H
10
    #define AVLTREE_H
    \#include "SelfOrganizingTree.h"
    \#include "AVLNode.h"
14
15
    template <class INFO_T> class AVLTree : public SelfOrganizingTree<INFO_T> {
16
         public:
17
             typedef AVLNode<INFO_T> node_t;
18
             typedef SelfOrganizingTree<INFO_T> S; // super class
19
20
            /**
             * Ofunction
                                AVLTree( )
             * @abstract
                                constructor
                                An AVLTree is created
             * @post
             **/
25
             AVLTree( ) : S( ) { }
26
27
            /**
28
             * @function
                                AVLTree( )
29
             * @abstract
                                constructor
30
             * @param
31
                                сру
             * @post
                                An AVLTree is created
             {\tt AVLTree(\ const\ AVLTree\&\ cpy\ )\ :\ S(\ cpy\ )\ \{\ \}}
35
            /**
36
             * @function
                                insert()
37
```

```
A node with label 'info' is inserted into the tree and
38
            * @abstract
                              put in the right place. A label may not appear twice in
39
                              a tree.
40
            * @param
                              info - the label of the node
41
            * @return
                              the node we inserted
42
            * @post
                              The tree now contains a node with 'info'
43
            **/
44
            node_t* insert( const INFO_T& info,
45
                              {\tt TreeNode}{<}{\tt INFO\_T}{>}{*} \ {\tt parent} \ =0, \ // \ {\tt Ignored}
                              \mathbf{bool} \ \mathbf{preferRight} = \mathbf{false} \;,
                                                               // Ignored
47
                              {f int} replaceBehavior =0 ) { // Ignored
48
                 if(S::find(this->root(), info))
49
                     return 0;
50
                 node_t *node =new node_t( );
51
                 S::insertInto( info, node );
52
                 rebalance( node );
53
                 return node;
54
            }
55
           /**
                              remove()
            * @function
            * @abstract
                              A node is removed in such a way that the properties of
59
                              an AVL tree remain intact.
60
              @param
                              node - the node we're going to remove
61
              @post
                              The node has breen removed, but the remaining tree still
62
                              contains all of its other nodes and still has all the
63
64
                              AVL properties.
            **/
65
            void remove( node_t* node ) {
66
                 // if it's a leaf
                 if( !node->leftChild( ) \&\& !node->rightChild( ) )
                     S::remove( node );
                 // internal node with kids
70
                 else {
71
                     if( node->rightChild( ) ) {
72
                          node =static_cast<node_t*>( S::replace(
73
                                 S::min( static_cast < node_t *>(
74
                                 {\tt node-\!\!\!>\!\!rightChild(\ )\ )-\!\!\!>\!\!info(\ )\,,\ node\ )\ );}
75
76
                          removeMin( static_cast < node_t *> ( node -> rightChild( ) ) );
                          node->setRightChild( node->rightChild( ));
                     }
                     else
79
                          // just delete the node and replace it with its leftChild
80
                          node->replace( node->leftChild( ) );
81
                 }
82
            }
83
84
        private:
85
86
87
           /**
            * @function
                              removeMin()
                              Recursively we go through the tree to find the node with
89
            * @abstract
90
                              the smallest value in the subtree with root node. Then we
                              restore the balance factors of all its parents.
91
```

```
node - the root of the subtree we're looking in
92
            * @param
            * @return
                             At the end of the recursion we return the parent of the
93
                             node with the smallest value. Then we go up the tree and
94
                             rebalance every parent from this upwards.
95
              @post
                             The node with the smallest value is deleted and every
96
                             node still has the correct balance factor.
97
            **/
98
            node_t* removeMin( node_t* node ) {
                node_t* temp;
                if( node->leftChild( ) )
101
                     temp =removeMin( static_cast<node_t*>( node->leftChild( ) );
                 else {
103
                     temp =static_cast<node_t*>( node->parent( ) );
104
                     S::remove( node );
105
106
                rebalance( temp );
107
                return temp;
108
            }
109
           /**
112
            * @function
                             removeMax()
              @abstract
                             Recursively we go through the tree to find the node with
113
                             the highest value in the subtree with root node. Then we
114
                             restore the balance factors of all its parents.
115
              @param
                             node - the root of the subtree we're looking in
116
              @return
                             At the end of the recursion we return the parent of the
117
                             node with the highest value. Then we go up the tree and
118
                             rebalance every parent from this upwards.
119
            * @post
                             The node with the highest value is deleted and every
120
                             node still has the correct balance factor.
            **/
            node_t* removeMax( node_t* node ) {
                node_t* temp;
124
                if( node->rightChild( ) )
125
                     temp =removeMin( static_cast < node_t*>( node->rightChild( ) ) );
126
                else {
127
                     temp =static_cast<node_t*>( node->parent( ) );
128
                     S::remove( node );
129
130
                rebalance( temp );
                return temp;
            }
134
           /**
135
136
            * @function
                             rotateLeft()
            * @abstract
                             We rotate a node left and make sure all the internal
137
                             heights of the nodes are up to date.
138
                             node - the node we're going to rotate left
              @param
139
              @return
                             we return the node that is now at the top of this
140
                             particular subtree.
141
            * @post
                             The node is rotated to the left and the heights are up
143
                             to date.
144
            **/
            node_t* rotateLeft( node_t* node ) {
145
```

```
{\tt node\_t} \ *{\tt temp} \ = \! static\_cast < \! {\tt node\_t*} > \! ( \ S::rotateLeft( \ node \ ) \ );
146
                  temp->updateHeight( );
147
                  if( temp->leftChild( ) )
148
                      {\tt static\_cast} < {\tt node\_t} \ *> ( \ {\tt temp-} > {\tt leftChild} ( \ ) \ )-> {\tt updateHeight} ( \ ) ;
149
                  return temp;
150
             }
151
152
            /**
153
             * @function
                               rotateRight()
             * @abstract
                               We rotate a node right and make sure all the internal
                               heights of the nodes are up to date.
             * @param
                               {\tt node} \ {\tt -} \ {\tt the} \ {\tt node} \ {\tt we're} \ {\tt going} \ {\tt to} \ {\tt rotate} \ {\tt right}
157
               @return
                               we return the node that is now at the top of this
158
159
                               particular subtree.
               @post
                               The node is rotated to the right and the heights are up
160
                               to date.
161
162
             node_t* rotateRight( node_t* node ) {
163
                  node_t* temp =static_cast<node_t*>( S::rotateRight( node ) );
                  temp->updateHeight( );
                  if ( temp->rightChild( ) )
                      static\_cast < node\_t*> (temp->rightChild())->updateHeight();
167
168
                  return temp;
             }
169
170
171
                               rebalance()
172
             * @function
                               The tree is rebalanced. We do the necessary rotations
173
               @abstract
                               from the bottom up to make sure the AVL properties are
174
                                still intact.
                               node - the node we're going to rebalance
             * @param
             * @post
177
                               The tree is now perfectly balanced.
             **/
178
             void rebalance( node_t* node ) {
179
                 node->updateHeight( );
180
181
                  node_t* temp =node;
182
                  while( temp->parent( ) ) {
183
                      temp =static_cast < node_t*>( temp->parent( ) );
184
                      temp->updateHeight();
                      // right subtree too deep
                      if(temp->balanceFactor() == 2) {
                           if(temp->rightChild())
188
                                189
                                    ->balanceFactor( ) < 0 )
190
                                    this->rotateRight(
191
                                    static_cast < node_t*>( temp->rightChild( ) );
192
193
                           this->rotateLeft( temp );
194
195
                      // left subtree too deep
                      else if ( temp->balanceFactor( ) == -2 ) {
198
                           if( temp->leftChild( ) ) {
                                if(static\_cast < node\_t*> (temp->leftChild())->
199
```

```
balanceFactor(\ )>0\ )
200
                                    this->rotateLeft(
201
                                    static\_cast < node\_t*> ( temp->leftChild( ) ) );
202
203
                           this->rotateRight( temp );
204
                      }
205
                  }
206
             }
207
    };
208
209
   #endif
    6.10
           AVLNode.h
     * AVLNode - Node atom type for AVLTree
                  Micky Faas (s1407937)
     * @author
                 Lisette de Schipper (s1396250)
     * @author
     * @file
                  AVLNode.h
     * @date
                  9-11-2014
     **/
   #ifndef AVLNODE_H
10
    #define AVLNODE_H
11
12
    #include "BSTNode.h"
13
    template <class INFO_T> class AVLTree;
15
16
    template < class \  \, \texttt{INFO\_T} > \  \, class \  \, \texttt{AVLNode} \  \, : \  \, \texttt{public} \  \, \texttt{BSTNode} < \texttt{INFO\_T} >
17
18
         public:
19
             typedef BSTNode<INFO_T> S; // super class
20
21
             /**
22
             * @function
                                AVLNode()
23
                                Constructor, creates a node
             * @abstract
             * @param
                                info, the contents of a node
             * @param
                               parent, the parent of the node
             * @post
                               A node has been created.
27
28
             29
                  : S(info, parent) {
30
31
32
            /**
33
             * @function
                                AVLNode()
34
             * @abstract
                               Constructor, creates a node
36
             * @param
                               parent, the parent of the node
37
             * @post
                                A node has been created.
             **/
38
             {\tt AVLNode} ( \ {\tt AVLNode} {<} {\tt INFO\_T} {>} * \ {\tt parent} \ = 0 \ )
39
                  : S((S)parent) {
40
```

```
}
41
42
           /**
43
            * @function
                             balanceFactor( )
44
                             we return the height of the rightchild subtracted with
            * @abstract
45
                             the height of the left child. Because of the properties
46
                             of an AVLtree, this should never be less than -1 or more
47
                             than 1.
48
             @return
                             we return the difference between the height of the
                             rightchild and the leftchild.
            * @post
                             The difference between the two child nodes is returned.
51
            **/
52
            int balanceFactor( ){
53
                \tt return \ static\_cast < AVLNode \ *>( \ this -> rightChild( \ ) \ )-> getHeight( \ ) \ -
54
                        static\_cast < AVLNode *> ( this-> leftChild( ) )-> getHeight( );
55
           }
56
57
           /**
58
            * @function
                             updateHeight()
                             we update the height of the node.
            * @abstract
                             The children of the node need to have the correct height.
            * @pre
            * @post
                             The node now has the right height.
62
            **/
63
            void updateHeight( ) {
64
                int lHeight =static_cast<AVLNode *>( this->leftChild( ) )
65
                              ->getHeight( );
66
                int rHeight =static_cast<AVLNode *>( this->rightChild( ) )
67
68
                              ->getHeight( );
69
                this->height = ( 1 + ( ( lHeight > rHeight ) ? lHeight : rHeight ) );
           }
71
72
           /**
73
            * @function
                             getHeight( )
74
                             we want to know the height of the node.
            * @abstract
75
            * @return
                             we return the height of the node.
76
            * @post
                             The current height of the node is returned.
77
            **/
78
79
            int getHeight( )
                return (this ? this->height : 0);
80
            bool operator <( const AVLNode<INFO_T> &rhs ) {
83
                return S::info() < rhs.info();
84
            }
85
86
            bool operator <=( const AVLNode<INFO_T> &rhs ) {
87
                return S::info() <= rhs.info();
88
            }
89
90
            bool operator >( const AVLNode<INFO_T> &rhs ) {
92
                return S::info() > rhs.info();
            }
93
```

```
\bool operator >= ( \boo
 95
                                           return S::info() >= rhs.info();
 96
                                }
 97
 98
                     protected:
 99
                                friend class AVLTree<INFO_T>;
100
101
                     private:
102
                                int height;
104
          };
105
106
       #endif
          6.11
                            SplayTree.h
          /**
            * SplayTree - Splay-tree implementation
   2
   3
            * @author Micky Faas (s1407937)
            * @author
                                          Lisette de Schipper (s1396250)
                                           SplayTree.h
            * Ofile
                                           3-11-2014
             * @date
       #ifndef SPLAYTREE_H
 10
         #define SPLAYTREE_H
 11
 12
         #include "SelfOrganizingTree.h"
 13
 14
          template < class \  \, \texttt{INFO\_T} > \  \, class \  \, \texttt{SplayTree} \  \, : \  \, \textbf{public} \  \, \texttt{SelfOrganizingTree} < \texttt{INFO\_T} > \, \{
 15
                     public:
 16
                                typedef BSTNode<INFO_T> node_t;
 17
                                typedef SelfOrganizingTree<INFO_T> S; // super class
 18
 19
                                SplayTree( ) : SelfOrganizingTree<INFO_T>( ) { }
 20
 21
                                SplayTree( const SplayTree& copy )
                                            : SelfOrganizingTree<INFO_T>( copy ) { }
                                /**
 25
                                * @function insert()
 26
                                                                   reimplemented virtual function from BinarySearchTree<>
                                * @abstract
 27
                                                                     the new node will always be the root
 28
                                * @param
                                                                     info, the contents of the new node
 29
                                * @param
                                                                    parent, ignored
 30
                                * @param
                                                                    preferRight, ignored
 31
                                * @param
                                                                    replaceBehavior, ignored
 32
                                * @return
                                                                    returns a pointer to the inserted node (root)
 34
                                **/
 35
                                virtual node_t* insert( const INFO_T& info,
                                                                                         {\tt TreeNode}{<}{\tt INFO\_T}{>}{*} {\tt parent} \ = 0, \ // \ {\tt Ignored}
 36
                                                                                         \bool preferRight = false \ , \ // \ Ignored
 37
                                                                                         {f int} replaceBehavior =0 ) { // Ignored
 38
```

```
return splay( S::insert( info, parent, preferRight ) );
39
            }
40
41
            /**
42
            * Ofunction replace()
43
                        reimplemented virtual function from BinarySearchTree<>
            * @abstract
44
                          replaces a given node or the root
45
                          the resulting node will be propagated to location of the root
46
            * @param
                          info, the contents of the new node
47
            * @param
                         node, node to be replaced
49
            * @param
                          alignRight, ignored
                         replaceBehavior, ignored
50
            * @param
            * @return
                         returns a pointer to the new node (=root)
51
                          node should be in this tree
52
            * @pre
            * @post
                          replace() will delete and/or remove node.
53
                          if node is 0, it will take the root instead
54
55
            virtual node_t* replace( const INFO_T& info,
56
                                  TreeNode < INFO_T > * node = 0,
                                  bool alignRight = false
                                  \mathbf{int} \ \mathtt{replaceBehavior} \ = \!\! 0 \ ) \ \{
                return splay( S::replace( info, node, alignRight ) );
60
            }
61
62
63
            * @function
                        remove()
64
                         reimplemented virtual function from BinarySearchTree<>
65
            * @abstract
                          removes a given node or the root and restores the
66
                          BST properties. The node-to-be-removed will be spayed
67
                          before removal.
            * @param
                          node, node to be removed
70
            * @pre
                          node should be in this tree
                          memory for node will be deallocated
71
            * @post
72
            virtual void remove( TreeNode<INFO_T> *node ) {
73
                S::remove( splay( static_cast < node_t *> (node) ));
74
75
76
           /**
77
            * @function find()
            * @abstract
                         reimplemented virtual function from Tree<>
                          performs a binary search in a given (sub)tree
                          splays the node (if found) afterwards
81
            * @param
                          haystack, the subtree to search. Give 0 for the entire tree
82
            * @param
                          needle, key/info-value to find
83
                          returns a pointer to node, if found
            * @return
84
            * @pre
                          haystack should be in this tree
85
            * @post
                          may return 0, the structure of the tree may change
86
            **/
87
            virtual TreeNode<INFO_T>* find( TreeNode<INFO_T>* haystack,
88
                                              const INFO_T& needle ) {
90
                return splay( static_cast<node_t*>( S::find( haystack, needle ) ) );
            }
91
```

```
/**
93
            * @function
                          splay()
94
              @abstract
                          Performs the splay operation on a given node.
95
                           'Splay' means a certain amount of rotations in order
96
                          to make the given node be the root of the tree while
97
                          maintaining the binary search tree properties.
98
              @param
                          node, the node to splay
99
            * @pre
                          The node must be a node in this tree
100
            * @post
                          The node will be the new root of the tree
                          No nodes will be invalided and no new memory is
                          allocated. Iterators may become invalid.
            **/
104
            {\tt node\_t*\ splay(\ node\_t*\ node\ )\ \{}
105
106
                enum MODE {
107
                     LEFT =0x1, RIGHT =0x2,
108
                     PLEFT =0x4, PRIGHT =0x8 };
109
110
                 // Can't splay the root (or null)
                 if(!node||S::m_root == node)
113
                     return node;
114
                 node_t *p =static_cast<node_t*>( node->parent( ) );
115
                 int mode;
116
117
                 while( p != S::m_root ) {
118
                     if( p->leftChild( ) == node )
119
                         mode =RIGHT;
120
                     else
121
                         mode = LEFT;
                     assert( p->parent( ) != nullptr );
125
                     // Node's grandparent
126
                     node_t* g =static_cast<node_t*>( p->parent( ) );
127
128
                     if(g\rightarrow p) = p
129
                         mode |= PRIGHT;
130
131
                     else
                         mode |= PLEFT;
                     // True if either mode is LEFT|PLEFT or RIGHT|PRIGHT
                     if( (mode >> 2) == (mode & 0x3) ) {
135
                          // the 'zig-zig' step
136
                         // first rotate g-p then p-node
137
138
                          if( mode & PLEFT )
139
                              this->rotateLeft( g );
140
                          else
141
142
                              this->rotateRight( g );
144
                          if( mode & LEFT )
                              this->rotateLeft( p );
145
                          else
146
```

```
this->rotateRight( p );
147
                        }
148
                        else {
149
                             // the 'zig-zag' step
150
                             // first rotate p-node then g-p
151
152
                             if( mode & LEFT )
153
                                  \mathbf{this} \! - \! \! > \! \! \mathsf{rotateLeft} \left( \begin{array}{c} \mathtt{p} \end{array} \right);
154
                             else
                                  this->rotateRight( p );
156
157
                             if( mode & PLEFT )
158
                                  this->rotateLeft( g );
159
                             else
160
                                  this->rotateRight( g );
161
                        }
162
163
                        // perhaps we're done already...
164
                        if(node = this - > root())
                             {\bf return\ node}\,;
                        _{
m else}
167
                             p = static\_cast < node\_t*> (node->parent());
168
                   }
169
170
                   // The 'zig-step': parent of node is the root
171
172
                   if( p->leftChild( ) == node )
173
                        this->rotateRight( p );
                   else
                        this->rotateLeft( p );
177
                   {\bf return\ node}\,;
178
              }
179
    };
180
181
182 #endif
    6.12
            Treap.h
     * Treap - Treap that inherits from SelfOrganizingTree
 2
     * @author Micky Faas (s1407937)
                  Lisette de Schipper (s1396250)
     * @author
      * @file
                   Treap.h
      * @date
                   9-12-2014
   #ifndef TREAP_H
   #define TREAP_H
11
   #include "SelfOrganizingTree.h"
   #include "TreapNode.h"
15
```

```
template < class \  \, \texttt{INFO\_T} > \  \, class \  \, \texttt{Treap} \ : \  \, \textbf{public} \  \, \texttt{SelfOrganizingTree} < \texttt{INFO\_T} > \  \, \{
16
                           public:
17
                                           typedef TreapNode<INFO_T> node_t;
18
                                           {\bf typedef~SelfOrganizingTree}{<} {\tt INFO\_T>~S;~//~super~class}
19
20
                                        /**
21
                                           * @function
                                                                                                         Treap( )
22
                                           * @abstract
                                                                                                         constructor
23
                                           * @post
                                                                                                         A Treap is created
                                           **/
25
                                           Treap( int randomRange =100 ) : S( ) {
26
                                                          random = randomRange;
27
                                                          srand( time( NULL ) );
28
                                           }
29
30
                                        /**
31
                                           * @function
                                                                                                         Treap( )
32
                                           * @abstract
                                                                                                         constructor
33
                                           * @param
                                                                                                         сру
                                           * @post
                                                                                                         A Treap is created
                                           **/
36
                                           {\tt Treap(\ const\ Treap\&\ cpy,\ int\ randomRange\ =}100\ )} : {\tt S(\ cpy)} {
37
                                                          random = randomRange;
38
                                                          srand( time( NULL ) );
39
                                           }
40
41
                                        /**
42
                                           * @function
                                                                                                         insert()
43
                                           * @abstract
                                                                                                         A node with label 'info' is inserted into the tree and
44
                                                                                                         put in the right place. A label may not appear twice in
46
                                                                                                         a tree.
                                           * @param
                                                                                                         info - the label of the node
47
48
                                           * @return
                                                                                                         the node we inserted
                                                                                                         The tree now contains a node with 'info'
                                           * @post
49
50
                                           node_t* insert( const INFO_T& info,
51
                                                                                                         {\tt TreeNode}{<}{\tt INFO\_T}{>}{*} {\tt parent} \ = 0, \ // \ {\tt Ignored}
52
                                                                                                         bool preferRight =false ,
53
54
                                                                                                         int replaceBehavior =0 ) { // Ignored
                                                          // Prevent duplicates
                                                           \hspace{0.1cm} \textbf{if} \hspace{0.1cm} ( \hspace{0.1cm} \mathtt{S} \hspace{-0.1cm} :: \hspace{0.1cm} \hspace{
58
                                                                         return 0;
                                                          node_t *node =new node_t( );
59
                                                          S::insertInto( info, node );
60
                                                          \verb"node->priority = \verb"rand"(") \% \verb" random" + 1;
61
                                                          rebalance( node );
62
63
                                                          return node;
64
65
                                           }
67
                                        /**
                                                                                                         remove()
68
                                           * @function
                                           * @abstract
                                                                                                         the node provided with the parameter is deleted from the
69
```

```
tree by rotating it down until it becomes a leaf or has
70
                                 only one child. In the first case it's just deleted,
71
                                 in the second it's replaced by its subtree.
72
              * @param
                                 node - the node to be deleted
73
              * @post
                                 The node is deleted from the tree which still retains
74
                                 the Treap properties.
75
76
              void remove( node_t* node ) {
77
                  node_t *temp = node;
                   // rotating it down until the condition no longer applies.
79
                  while( temp->leftChild( ) && temp->rightChild( ) )
80
81
                   {
                       if(\ static\_cast < \verb"node\_t" *> (\ temp-> \verb"rightChild"(\ )\ )-> \verb"priority">
82
                            static\_cast < node\_t*> (temp->leftChild())->priority)
83
                            this->rotateLeft( temp );
84
                       else
85
                            this->rotateRight( temp );
86
87
                   // if it's a leaf
                   if ( \ !\texttt{temp-}\!\!>\!\! \texttt{leftChild}( \ ) \ \&\& \ !\texttt{temp-}\!\!>\!\! \texttt{rightChild}( \ ) \ )
                       S::remove( temp );
                   // if it only has a right child
91
                   \mathbf{else} \ \mathbf{if} \left( \ ! \mathtt{temp-} \!\! > \!\! \mathtt{leftChild} \left( \ \right) \ \right)
92
                       \label{lemp-replace} \verb|temp->replace(static_cast<| node_t*>(temp->rightChild());|
93
                   // if it only has a left child
94
                   else if( !node->rightChild( ) )
95
                       temp->replace( static_cast<node_t*>( temp->leftChild( ) ) );
96
              }
97
         private:
             int random;
             /**
102
              * @function
                                 rebalance()
103
                                 The tree is rebalanced. We do the necessary rotations
              * @abstract
104
                                 from the bottom up to make sure the Treap properties are
105
                                 still intact.
106
               @param
                                 info - the label of the node
107
              * @return
                                 the node we inserted
108
              * @post
                                 The tree is now perfectly balanced.
              **/
              void rebalance( node_t* node ) {
                   if (!node)
112
113
                       return:
                  node_t* temp =node;
114
                  int myPriority =node->priority;
115
                   while ( temp->parent( ) &&
116
                           myPriority >
117
                           static_cast<node_t*>( temp->parent( ) )->priority ) {
118
                       temp =static_cast<node_t*>( temp->parent( ) );
119
                        if(temp->leftChild() == node)
121
                            this->rotateRight( temp );
                       else
122
                            this->rotateLeft( temp );
123
```

```
}
124
             }
125
126
    };
127
128
129 #endif
            TreapNode.h
    6.13
    /**
     * TreapNode - Node atom type for Treap
     * @author Micky Faas (s1407937)
                  Lisette de Schipper (s1396250)
     * @author
 5
     * @file
                  TreapNode.h
     * @date
                  9-11-2014
    #ifndef TREAPNODE.H
10
    #define TREAPNODE.H
11
12
    #include "BSTNode.h"
13
14
    template <class INFO_T> class Treap;
15
16
    template <class INFO_T> class TreapNode : public BSTNode<INFO_T>
17
18
         public:
19
             typedef BSTNode<INFO_T> S; // super class
20
21
             /**
22
             * @function
                                TreapNode( )
23
             * @abstract
                                Constructor, creates a node
24
             * @param
                                info, the contents of a node
25
             * @param
                                parent, the parent of the node
26
             * @post
                                A node has been created.
27
             **/
28
             {\tt TreapNode}(\  \, \mathbf{const}\  \, {\tt INFO\_T\&}\  \, \mathtt{info}\,,\  \, {\tt TreapNode}{<} \mathtt{INFO\_T}{>}{*}\,\,\, \mathtt{parent}\,\,=\!\!0\,\,\,)
                  : S(info, parent), priority(0)
31
32
            /**
33
             * @function
                                TreapNode( )
34
             * @abstract
                                Constructor, creates a node
35
                                parent, the parent of the node
              * @param
36
             * @post
                                A node has been created.
37
             **/
38
             TreapNode( TreapNode<INFO_T>* parent =0 )
39
                  : S((S)parent), priority(0)
             }
41
42
             /**
43
             * Ofunction replace()
44
             * @abstract Replaces the node with another node in the tree
45
```

```
\ensuremath{\mathbf{n}}\xspace , the node we replace the node with, this one gets deleted
46
              * @param
              * @pre
                               both this node and \boldsymbol{n} must be in the same parent tree
47
              * @post
                               The node will be replaced and n will be deleted.
48
              **/
49
              void replace( TreapNode<INFO_T>* n ) {
50
                   priority = n->priority;
51
                   this \rightarrow S::replace(n);
52
              }
53
              {\bf bool\ operator}\ <(\ {\bf const}\ {\tt TreapNode}{<} {\tt INFO\_T}{>}\ \&{\tt rhs}\ )\ \{
                   return S::info() < rhs.info();</pre>
              }
57
58
              bool operator <=( const TreapNode<INFO_T> &rhs ) {
59
                   return S::info() \le rhs.info();
60
61
62
              bool operator >( const TreapNode<INFO_T> &rhs ) {
63
                   return S::info() > rhs.info();
              \bool operator >= (const TreapNode < INFO_T > \&rhs) \{
67
                   \mathbf{return} \ \mathtt{S}:: \mathtt{info}\,(\,) >= \mathtt{rhs.info}\,(\,)\,;
68
              }
69
70
              int priority;
71
72
         protected:
73
              friend class Treap<INFO_T>;
74
    };
75
76
77
78 #endif
```