Hogebomen

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Abstract

Blablabla

1 Inleiding

AVL-bomen, splay-bomen en treaps zijn klassieke datastructuren die ingezet worden om een verzameling gegevens te faciliteren. Het zijn zelfbalancerende binaire zoekbomen die elk een vorm van ruimte en/of tijd-efficiëntie aanbieden. Er worden experimenten verricht om de prestatie van deze zelf-balancerende zoekbomen te vergelijken aan de hand van ophaaltijd van data, mate van herstructurering en het verwijderen van knopen. Ook wordt de prestatie van deze zoekbomen uitgezet tegen de ongebalanceerde tegenhanger, de binaire zoekboom.

2 Werkwijze

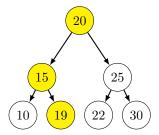
De vier bomen zijn conceptueel eenvoudig en relatief makkelijk te implementeren. Voor alle vier de bomen wordt dezelfde zoekmethode gebruikt. Deze is in het slechtste geval $O(\log n)$.

2.1 Implementatie binaire zoekboom

De binairy zoekboom (BST) vormt de basis voor alle zogeheten zelf-organiserende bomen, zoals de AVL- of SplayTree. Aan de grondslag van de BST ligt de binaire-zoekboom-eigenschap, die zorgt dat de boom op de "gretige" manier kan worden doorzocht in plaats van een exhaustive search. Hierdoor is het mogelijk om een knoop in een boom met hoogte n in hooguit n stappen te vinden, maar gemiddeld genomen sneller, namelijk $\log(n)$. Kort samengevat houdt de bsteigenschap het volgende in:

- Linker-kindknopen en hun kinderen hebben altijd een kleinere waarde dan hun ouder, rechter-kindknopen en al hun kinderen altijd een grotere waarde dan hun ouder.
- Bij een MIN-boom is dit omgekeerd. Onze implementatie is enkel een MAX-boom.
- Toevoegen kan zonder verwisselen worden uitgevoerd (in tegenstelling tot bijv. een heap).

• Voor verwijderen of vervangen moet afhankelijk van de plaats van de knoop wel worden verwisseld.

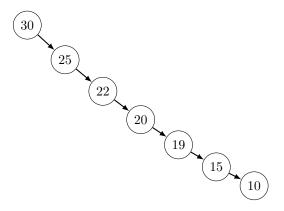


In het voorbeeld is het zoekpad naar de knoop met waarde 19 weergegeven. Dit zoekpad heeft precies complexiteit O(n), namelijk drie stappen/vergelijkingen voordat de gezochte knoop wordt bereikt, dat is dus gelijk aan de hoogte van de boom.

- Het zoekdomein bestaat aanvankelijk uit $2^n 1 = 7$ knopen, want de voorbeeldboom is een volle binaire boom
- Aan het begin van de zoekopdracht is er alleen een pointer naar de wortel (20). We weten dat 19 kleiner is dan de wortel, dus bezoeken we zijn linkerkind. Van de complete rechtersubboom is dus van te voren bekend dat deze niet doorzocht hoeft te worden.
- Het zoekdomein wordt dus ineens van 7 naar $2^n 1 (2^{n-1} 1) = 4$ verkleind. Voor een grote boom zijn dat veel knopen die nooit bezocht hoeven te worden.
- De nieuwe knoop heeft waarde 15. We hebben dus nog geen resultaat, maar er is nu wel bekend dat alleen de rechtersubboom van 15 hoeft te worden doorzocht
- \bullet Het zoekdomein is nu precies n geworden, de "worst case" bij de binair zoeken.
- Het rechterkind van 15 is vervolgens 19, de knoop is gevonden.

Binaire bomen zijn dus sneller dan gewone bomen tijdens het zoeken en correct mits de binaire-zoekboom-eigenschap wordt gehandhaafd. Tijdens een insert operatie kost dat inprinciepe geen extra rekenkracht, maar bij bijvoorbeeld het verwijderen moet de boom soms worden verschoven om de eigenschap te herstellen.

Een ander probleem is dat de binaire zoekboom eigenlijk alleen optimaal presteert als de hoogte zo gering mogelijk is voor het aantal knopen. De hoogte bepaalt namelijk de zoekcomplexiteit, niet het aantal knopen. Een binaire zoekboom met een goede balans tussen de hoogten van de subbomen is *geballanceerd*. Als er tijdens het toevoegen niets bijzonders wordt gedaan, kan een binaire zoekboom heel snel ongebalanceerd raken, afhankelijk van de volgorde waarin knopen worden toegevoegd. Neem bijvoorbeeld de bovenstaande boom. Als men de knopen in de volgorde 10, 15, 19, 20, 25, 22, 30 toegevoegd ontstaat er één lange tak naar rechts. De worst-case zoekdiepte is nu van 3 naar 7 gegaan.

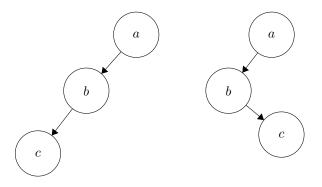


De zelf-organiserende boom is een speciaal soort binaire zoekboom die tijdens verschillende operaties probeert om de boom zo goed mogelijk te (her)belanceren. Uiteraard kosten deze extra operaties ook meer rekenkracht en of dit zich terugbetaald in zoeksnelheid is één van de dingen die wij zullen onderzoeken tijdens deze experimenten.

2.2 Implementatie AVL-bomen

Knopen van een AVL-boom hebben een balansfactor, die altijd -1, 0 of 1 moet zijn. In deze implementatie is de balansfactor de hoogte van de rechtersubboom min de hoogte van de linkersubboom. Dit houdt dus in dat de hoogte van de linkersubboom van de wortel met maar 1 knoop kan verschillen van de hoogte van de rechtersubboom van de wortel. Het moment dat de balansfactor van een knoop minder dan -1 of meer dan 1 wordt, moet de boom geherstructureerd worden, om deze eigenschap te herstellen.

Om de balansfactor voor elke knoop te berekenen, houdt elke knoop zijn eigen hoogte bij. De balansfactor van een knoop wordt hersteld door rotaties. De richting en de hoeveelheid van de rotaties hangt af van de vorm van de betreffende (sub)boom. De volgende twee vormen en hun spiegelbeelden kunnen voorkomen bij het verwijderen of toevoegen van een knoop:



In het eerste geval moet de wortel naar rechts worden geroteerd. In het tweede geval moeten we eerst naar de staat van de eerste subboom komen, door b naar links te roteren. Voor de spiegelbeelden van deze twee vormen geldt hetzelfde alleen in spiegelbeeld.

In deze implementatie van een AVL-boom bedraagt het toevoegen van een knoop in het ergste geval O(logn) tijd, waarbij n staat voor de hoogte van de boom. Eerst moet er gekeken worden of de data niet al in de boom voorkomt (O(logn)) en vervolgens moet de boom op basis van de toevoeging geherstructureerd worden. Dit laatste is in het ergste geval O(logn), omdat dan de gehele boom tot de wortel moeten worden nagelopen.

De complexiteitsgraad van het verwijderen van een knoop is gelijk aan die van het toevoegen van een knoop. In deze implementatie zoeken we in de rechtersubboom het kleinste kind en vervangen we de te verwijderen knoop met deze knoop. Dit heeft een duur van O(logn). Als hij geen rechtersubboom heeft, wordt de node weggegooid en wordt zijn linkersubboom de nieuwe boom.

2.3 Implementatie Splay-bomen

De Splay-boom is een simpele binaire zoekboom die zichzelf herorganiseerd na elke operatie, ook na operaties die alleen lezen, zoals find(). Deze herorganisatiestap heet "splay" (vandaar de naam) en heeft ten doel de laatst aangesproken knoop bovenaan te zetten. Dit wordt dus de wortel. Hieronder is het gedrag kort samengevat:

- Bij zoeken wordt de gevonden knoop de wortel, mits er een zoekresultaat is.
- Bij toevoegen wordt de toegevoegde knoop de wortel
- Bij vervangen wordt de vervangen knoop de wortel
- Bij verwijderen wordt de te verwijderen knoop eerst de wortel, dan wordt deze verwijderd.

Het idee achter dit gedrag is, dat vaak gebruikte knopen hoger in de boom terechtkomen en daarom sneller toegankelijk zijn voor volgende operaties. De splay-operatie zorgt er bovendien voor dat knoop die dicht in de buurt van de gesplayde knoop zitten, ook hoger in de boom worden geplaatst. Dit effect ontstaat doordat splay eigenlijk een serie boom rotaties is. Als men deze rotaties consequent uitvoerd blijft bovendien de binairy-zoekboom-eigenschap behouden.

2.3.1 Splay

De splay-operatie bestaat uit drie operaties en hun spiegelbeelden. We gaan uit van een knoop n, zijn ouderknoop p en diens ouderknoop g. Welke operatie wordt uitgevoerd is afhankelijk van het feit of n en p linker- of rechterkind zijn. We definieren:

- \bullet De Zig stap. Als n linkerkind is van p en p de wortel is, doen we een rotate-right op p.
- \bullet Het spiegelbeeld van Zig is Zag.

- De Zig-Zig stap. Als n linkerkind is van p en p linkerkind is van g, doen we eerst een rotate-right op g en dan een rotate-right op p.
- Het spiegelbeeld van Zig-Zig is Zag-Zag
- De Zig-Zag stap. Als n rechterkind is van p en p linkerkind is van g, doen we eerst een rotate-left op p en dan een rotate-right op g.
- De omgekeerde versie heet Zag-Zig

Onze implementatie splayt op insert(), replace(), remove() en find(). De gebruiker kan eventueel zelf de splay-operatie aanroepen na andere operaties dmv de functie splay().

2.4 Implementatie Treaps

Treap lijkt in veel opzichten op een AVL-boom. De balansfactor per knoop heeft echter plaats gemaakt voor een prioriteit per knoop. Deze prioriteit wordt bij het toevoegen van een knoop willekeurig bepaald. De complexiteit voor het toevoegen en verwijderen van een knoop is hetzelfde als bij de AVL-boom.

Bij het toevoegen van een knoop moet er nog steeds omhoog gelopen worden in de boom, totdat de prioriteit van de toegevoegde knoop kleiner is dan de prioriteit van de ouder. Als dit niet het geval is, blijft de toegevoegde knoop omhoog roteren. In het ergste geval kan het dus weer zo zijn dat we tot de wortel door moeten blijven lopen.

Bij het verwijderen van een knoop blijven we de betreffende knoop roteren naar het kind met de grootste prioriteit. Uiteindelijk belanden we dan in de situatie dat de knoop maar een of geen kinderen heeft. In het eerste geval verwijderen we de knoop en plakken zijn subboom terug aan de boom op zijn plek en in het tweede geval verwijderen we de knoop. In het slechtste geval duurt dit dus ook O(logn) tijd.

3 Onderzoek

Een praktisch voorbeeld van binair zoeken in een grote boom is de spellingscontrole. Een spellingscontrole moet zeer snel voor een groot aantal strings kunnen bepalen of deze wel of niet tot de taal behoren. Aangezien er honderduizenden woorden in een taal zitten, is lineair zoeken geen optie. Voor onze experimenten hebben wij dit als uitgangspunt genomen en hieronder zullen we kort de experimenten toelichten die wij hebben uitgevoerd. In het volgende hoofdstuk staan vervolgens de resultaten beschreven.

3.1 Hooiberg

"Hooiberg" is de naam van het testprogramma dat we hebben geschreven speciaal ten behoeven van onze experimenten. Het is een klein console programma dat woorden uit een bestand omzet tot een boom in het geheugen. Deze boom kan vervolgens worden doorzocht met de input uit een ander bestand: de "naalden". De syntax is alsvolgt:

hooiberg type hooiberg.txt naalden.txt [treap-random-range]

Hierbij is type één van bst, avl, splay, treap, het eerste bestand bevat de invoer voor de boom, het tweede bestand een verzameling strings als zoekopdracht en de vierde parameters is voorbehouden voor het type treap. De bestanden kunnen woorden of zinnen bevatten, gescheiden door regeleinden. De binaire bomen gebruiken lexicografische sortering die wordt geleverd door de operatoren < en > van de klasse std::string. Tijdens het zoeken wordt een exacte match gebruikt (case-sensitive, non-locale-aware).

3.2 Onderzoeks(deel)vragen

Met onze experimenten hebben we gepoogd een aantal eenvoudige vragen te beantwoorden over het gebruik van de verschillende binaire en zelf-organiserende bomen, te weten:

- Hoeveel meer rekenkracht kost het om grote datasets in te voegen in zelforganiserende bomen tov binaire bomen?
- Levert een zelf-organiserende boom betere zoekprestaties en onder welke opstandigheden?
- Hoeveel extra geheugen kost een SOT?
- Wat is de invloed van de random-factor bij de Treap?

3.3 Meetmethoden

Om de bovenstaande vragen te toetsen, hebben we een aantal meetmethoden bedacht.

- Rekenkracht hebben we gemeten in milliseconden tussen aanvang en termineren van een berekening. We hebben de delta's berekend rond de relevante code blokken dmv de C++11 chrono klassen in de Standard Template Library. Alle test zijn volledig sequentieel en single-threaded uitgevoerd. Deze resultaten zijn representatie voor één bepaald systeem, vandaar dat we aantal % 'meer rekenkracht' als eenheid gebruiken.
- Zoekprestatie hebben we zowel met rekenkracht als zoekdiepte gemeten. De zoekdiepte is het aantal stappen dat vanaf de wortel moet worden gemaakt om bij de gewenste knoop te komen. We hebben hierbij naar het totaal aantal stappen gekeken en naar de gemiddelde zoekdiepte.
- Geheugen hebben we gemeten met de valgrind memory profiler. Dit programma wordt gebruikt voor het opsporen van geheugen lekken en houdt het aantal allocaties op de heap bij. Dit is representatie voor het aantal gealloceerde nodes. Aangezien hooiberg nauwelijks een eigen geheugenvoetafdruk heeft, zijn deze waarden representatief.

3.4 Input data

Voor ons experiment hebben we een taalbestand gebruikt van OpenTaal.org met meer dan 164.000 woorden. Dit is een relatief klein taalbestand, maar voldoede om verschillen te kunnen zien. We hebben een aantal testcondities gebruikt:

- Voor het inladen een wel of niet alfabetisch gesoorteerd taalbestand gebruiken.
- Als zoekdocument hebben we een gedicht met 62 woorden gebruikt. Er zitten een aantal dubbele woorden in alsook een aantal woorden die niet in de woordenlijst voorkomen (werkwoordsvervoegingen).
- We hebben ook een conditie waarbij we alle woorden gezocht hebben, zowel in dezelfde, als in een andere volgorde dan dat ze zijn ingevoerd.
- We hebben één conditie waarbij we de random-range van de Treap hebben gevariëerd.

3.5 Hypothesen

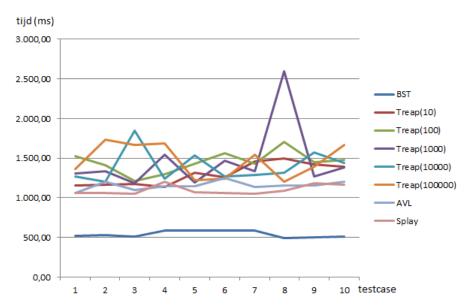
- De binairy search tree zal vermoedelijk het snelst nieuwe data toevoegen. De splay tree heeft veel ingewikkelde rotatie bij een insert, dus deze zal het traagst zijn.
- Bij het gedicht zal de splay boom waarschijnlijk het snelst zijn omdat deze optimaliseert voor herhalingen.
- ..
- De bomen die een aparte node-klasse gebruiken (avl en treap) gebruiken het meeste geheugen.
- De meest efficiënte randomfactor is afhankelijk van de grootte van de boom die geïmplementeerd gaat worden. Bij een kleine boom volstaat een kleine randomfactor, bij een grote boom volstaat een grote randomfactor.

4 Resultaten

4.1 Experiment 1

In dit experiment hebben we voor elke soort boom gemeten hoe lang het duurt de boom op te bouwen met het bestand Nederlands_unsorted.txt om deze tijden te kunnen vergelijken. Dit hebben we gemeten in miliseconden. De volgende gegevens kwamen eruit. Deze hebben we vervolgens verwerkt in een grafiek.

	BST	Treap(10)	Treap(100)	Treap(1000)	Treap(10000)	Treap(100000)	AVL	Splay
	525	1160	1526	1307	1272	1368	1063	1065
	527	1162	1409	1332	1202	1736	1207	1059
	511	1173	1215	1181	1846	1669	1102	1053
	585	1141	1298	1547	1246	1688	1150	1202
	589	1319	1427	1190	1538	1221	1146	1067
	588	1265	1560	1472	1271	1238	1251	1063
	592	1464	1428	1338	1286	1543	1136	1050
	492	1501	1704	2594	1316	1206	1155	1092
	506	1425	1449	1269	1571	1389	1153	1183
	512	1391	1474	1384	1440	1663	1203	1162
GEM	542,7	1300,1	1449	1461,4	1398,8	1472,1	1156,6	1099,6



figuur 1. Grafiek over het aantal ms voor het construeren van een graaf.

4.2 Experiment 2

Om de zoekprestaties van de verschillende soorten bomen te vergelijken kijken we naar zowel de totale zoekdiepte van de boom, de gemiddelde zoekdiepte van een woord in gedicht.txt en naar het aantal miliseconden die de gemiddelde zoekoperatie nodig had. Onze boom is opgebouwd uit nederlands_unsorted.txt. De gehele hoogte van de boom die dit opleverd en de gemiddelde zoekdiepte van een woord uit gedicht.txt staan in onderstaande tabel weergegeven. Het gemiddelde aantal miliseconden dat nodig was voor de zoekoperaties van elk woord bedroeg nooit meer dan 1 miliseconden en dook zelfs vaak onder de halve miliseconde.

Type	totale zoekdiepte	gemiddelde zoekdiepte
Treap(10)	1843,5	32,5
Treap(100)	2256,9	39,9
Treap(1000)	2275,2	40,2
Treap(10000)	2268,7	39,9
Treap(100000)	2205,8	39
BST	1106	19
AVL	880	15
splay	997	17

Ditzelfde experiment voerden we uit op dezelfde boom met als zoekopdrachten elk element in die boom. Daar kwamen de volgende resultaten uit.

Type	totale zoekdiepte	gemiddelde zoekdiepte	tijd (ms)
Treap(10)	5783309	34,67	882.005
Treap(100)	7034043	$42,\!22$	956.880
Treap(1000)	7162473	44.11	1067.861
Treap(10000)	7253419	$44,\!67$	1053.257
BST	3369405	20	557.934
AVL	2576171	15	450.390
splay	3922834	23	1378,197

4.3 Experiment 3

Hieronder staan de hoeveelheden geheugen en het aantal allocaties weergegeven voor elke boom. De metingen zijn van heap dynamisch gealloceerd geheugen alleen en zijn uitgevoerd met Valgrind. De onderlinge verschillen zijn, zelfs met een wat grotere data set, verwaarloosbaar. Niet geheel verassend nemen de nodes van Treap en AVL iets meer ruimte in omdat deze een prioriteit resp. balansfactor bijhouden.

Het feit dat het invoer bestand slechts 2,1 Mb groot is, zegt wel iets over de efficiëntie van het geheugengebruik in het algemeen, zowel van onze implementatie als van dit soort boom datatypen in het algemeen. Ontwerpkeuzen spelen hier een grote rol: als we bijvoorbeeld ervoor hadden gekozen om geen 'ouderpointers' te gebruiken, hadden we tussen 0,6 en 1,2 Mb op deze cijfers kunnen besparen.

Type	allocs	bytes
Treap	493280	16704426 (15,9 Mb)
BST	493278	15389858 (14,7 Mb)
AVL	493279	16704390 (15,9 Mb)
splay	493260	15389922 (14,7 Mb)

4.4 Experiment 4

Wat is de invloed van de random-factor bij de Treap? Hooiberg: Nederlands_unsorted Naalden: gedicht Average search depth

	10	100	1000	10000	10000
	34	36	36	45	38
	31	40	49	34	47
	29	35	26	70	41
	32	40	35	41	42
	33	44	32	38	36
	34	40	49	33	37
	35	47	29	37	35
	36	47	66	36	29
	32	34	36	35	39
	29	36	44	30	46
GEM	32,5	39,9	40,2	39,9	39

Total search depth

	10	100	1000	10000	10000
	1914	2041	2017	2549	2173
	1745	2254	2752	1957	2657
	1652	1982	1511	3954	2312
	1836	2261	1983	2310	2366
	1861	2482	1819	2169	2033
	1925	2253	2783	1852	2092
	2002	2656	1643	2126	1947
	2032	2672	3732	2059	1658
	1798	1917	2021	1999	2211
	1670	2051	2491	1712	2609
GEM	1843,5	2256,9	2275,2	2268,7	2205,8

De volgende tabel geeft de uitersten aan van de resultaten die we tegenkwamen in deelexperiment 2 van experiment 2.

	Totale zoekdiepte		Gemiddelde zoekdiepte		Tijd	
bereik	minimum	maximum	minimum	maximum	minimum	maximum
10	5194145	6826579	31	41	778.449	992.709
100	5321940	10137343	32	61	823.003	1379.380
1000	592787 2	9952377	32	60	873.975	1300.820
10000	5841811	10283676	35	62	940.451	1270.090

5 Conclusies

6 Appendix

6.1 main.cc

```
* main.cc:
     * @author Micky Faas (s1407937)
     * @author Lisette de Schipper (s1396250)
     * @file
                    main.cc
     * @date
                    26-10-2014
10 #include <iostream>
#include "BinarySearchTree.h"
#include "Tree.h"
#include "AVLTree.h"
#include "SplayTree.h"
#include "Treap.h"
16 #include <string>
   using namespace std;
   // Makkelijk voor debuggen, moet nog beter
    template < class \  \, \texttt{T} > \  \, \textbf{void} \  \, \texttt{printTree} \left( \  \, \texttt{Tree} < \texttt{T} > \  \, \textbf{tree} \, , \  \, \textbf{int rows} \, \, \right) \, \, \left\{ \right.
```

```
 \textbf{typename Tree} < \texttt{T} > :: \texttt{nodelist list =} \texttt{tree.row} ( \ 0 \ ); 
22
        int row =0;
23
        \mathbf{while}(\ ! \mathtt{list.empty}(\ ) \&\& \ \mathtt{row} < \mathtt{rows}\ ) \ \{
24
             string offset;
25
             for(int i = 0; i < (1 << (rows - row)) - 1; ++i)
26
                  offset += ';
27
28
29
             for( auto it =list.begin( ); it != list.end( ); ++it ) {
                  if( *it )
31
                       \verb|cout| << \verb|offset| << (*it) -> \verb|info()| << " " << \verb|offset|;
                  else
33
                       cout << offset << ". " << offset;</pre>
34
             }
35
             cout << endl;</pre>
36
             row++;
37
             list =tree.row( row );
38
        }
39
40
41
   int main ( int argc, char **argv ) {
42
43
        /* BST hieronder */
44
45
        cout << "BST:" << endl;
46
        {\tt BinarySearchTree}{<}{\tt int}{>} bst;
47
48
       /* auto root =bst.pushBack( 10 );
49
        bst.pushBack( 5 );
50
51
        bst.pushBack( 15 );
52
        bst.pushBack( 25 );
53
        bst.pushBack( 1 );
54
        bst.pushBack( -1 );
55
        bst.pushBack( 11 );
56
        bst.pushBack( 12 ); */
57
58
59
        Tree<int>* bstP =\&bst; // Dit werkt gewoon :-)
60
        auto root =bstP->pushBack( 10 );
        bstP->pushBack(5);
        bstP->pushBack(15);
63
64
        bstP->pushBack(25);
65
        bstP->pushBack(1);
66
        bstP->pushBack(-1);
67
        bstP->pushBack(11);
68
        bstP->pushBack(12);
69
70
71
        //printTree<int>( bst, 5 );
72
73
        //bst.remove( bst.find( 0, 15 ) );
74
        //bst.replace( -2, bst.find( 0, 5 ) );
75
```

```
76
 77
          {\tt printTree}{<}{\tt int}{>}({\tt bst}\;,\;\;5\;\;);
 78
 79
          bst.remove( root );
 80
 81
 82
          printTree < int > (bst, 5);
 83
          /* Splay Trees hieronder */
 85
 86
          \verb"cout" << "Splay Boom:" << \verb"endl";
 87
          {\tt SplayTree}{<} {\tt int}{>} \ {\tt splay} \, ;
 88
 89
          splay.pushBack(10);
 90
          auto a = splay.pushBack(5);
 91
          splay.pushBack(15);
 92
 93
          {\tt splay.pushBack(25)};
          \mathbf{auto} \ \mathbf{b} = \mathbf{splay.pushBack} ( 1 );
          {\tt splay.pushBack(} \ -1 \ );
          \mathbf{auto} \ \mathtt{c} \ \mathtt{=splay.pushBack} \, ( \ 11 \ ) \, ;
 97
          {\tt splay.pushBack} \, (\ 12\ ) \, ;
98
99
          //printTree<int>( splay, 5 );
100
101
          //a->swapWith( b );
102
          //splay.remove( splay.find( 0, 15 ) );
103
          //splay.replace( -2, splay.find( 0, 5 ) );
104
          printTree < int > (splay, 5);
108
          //splay.remove( root );
109
110
          splay.splay( c );
111
112
          printTree < int > (splay, 5);
113
114
          // Test AVLTree //
          AVLTree<char> test;
          test.insert('a');
118
          auto d =test.insert('b');
119
          test.insert('c');
120
          test.insert(',d');
121
          test.insert('e');
122
          test.insert('f');
123
          test.insert('g');
124
          cout << "AVL Boompje:" << endl;</pre>
125
          printTree < char > (test, 5);
          \verb|cout| << \verb|d->info|(  ) << "  verwijderen: " << \verb|endl|; 
128
          test.remove( d );
          printTree < char > (test, 5);
129
```

```
// Test Treap //
131
132
        cout << "Treap" << endl;
133
134
        Treap < int > testTreap(5);
135
        testTreap.insert(2);
136
        testTreap.insert(3);
137
        \mathbf{auto} \ \mathtt{e} \ \mathtt{=} \mathtt{testTreap.insert} \left( \, 4 \, \right);
        testTreap.insert(5);
        printTree < int > (testTreap, 5);
        testTreap.remove(e);
141
        {\tt printTree}{<} {\tt int}{>}( \ {\tt testTreap} \ , \ 5 \ );
142
143
        return 0;
144
145
         hooiberg.cc
     * hooiberg.cc:
     * @author Micky Faas (s1407937)
     * @author Lisette de Schipper (s1396250)
     * @file
                 helehogebomen.cc
     * @date
                 10-12-2014
10 #include "BinarySearchTree.h"
#include "Tree.h"
#include "AVLTree.h"
   #include "SplayTree.h"
   #include "Treap.h"
15
   #include <iostream>
16
   #include <string>
   #include <fstream>
   #include <vector>
   #include <chrono>
    // Only works on *nix operating systems
    // Needed for precision timing
   #include <sys/time.h>
25
    using namespace std;
26
27
    // Makkelijk voor debuggen, moet nog beter
28
    template<class T> void printTree( Tree<T> tree, int rows ) {
29
        typename Tree<T>::nodelist list =tree.row( 0 );
31
        int row =0;
32
        while( !list.empty( ) && row < rows ) {</pre>
33
            string offset;
            34
                 offset += ';
35
```

130

```
36
37
             for( auto it =list.begin( ); it != list.end( ); ++it ) {
38
                  if( *it )
39
                      cout << offset << (*it)->info() << " " << offset;</pre>
40
41
                      cout << offset << ". " << offset;</pre>
42
             }
43
             cout << endl;</pre>
             row++;
45
             list =tree.row( row );
46
        }
47
48
49
   int printUsage( const char* prog ) {
50
51
        52
              << "Usage:" << proj << " [type] [haystack] [needles] [treap-random] \\  << " \\ t[type] \\ t \\ tTree type to use. One of 'splay', 'avl', 'treap', 'bst' \\ "" 
53
              <<\ "\ t\,[\,h\,aystack\,]\ \backslash\ tInput\ file\ ,\ delimited\ by\ newlines\ \backslash n"
             << "\tilde{t}[needles]\text{\chi}tFile containing sets of strings to search for, delimited by
              << "\ t[treap-random]\ tOptimal customization of the random factor of Treap\n"
57
             << std::endl;
58
        return 0;
59
   }
60
61
   bool extractNeedles( std::vector<string> &list, std::ifstream &file ) {
62
63
        string needle;
        while( !file.eof( ) ) {
64
             std::getline( file, needle );
             if( needle.size( ) )
67
                 list.push_back( needle );
68
        return true;
69
70
71
   bool fillTree( BinarySearchTree<string>* tree, std::ifstream &file ) {
72
        string word;
73
        while( !file.eof( ) ) {
74
             std::getline( file, word );
             if( word.size( ) )
                 tree->pushBack( word );
78
        return true;
79
80
81
   {f void} findAll( std::vector<string> &list, BinarySearchTree<string>* tree ) {
82
        int steps =0, found =0, notfound =0;
83
        for( auto needle : list ) {
84
             if(tree -> find(0, needle))
85
                 found++;
87
                 steps +=tree->lastSearchStepCount( );
88
                 if (found < 51)
                      \mathtt{std} :: \mathtt{cout} << "Found" `" << \mathtt{needle} << " \setminus " "
89
```

```
<< " in " << tree->lastSearchStepCount( ) << " steps." << std::endl;
90
               }
91
               else if (++notfound < 51)
92
                    std::cout << "Didn't find" << needle << '\'' << std::endl;
93
94
          if(found > 50)
95
               std::cout << found - 50 << " more results not shown here." << std::endl;
96
          if( found )
97
               cout << "Total search depth:</pre>
                                                                 "\,<<\,\mathtt{steps}\,<<\,\mathtt{endl}
                                                                 " << \mathtt{found} << \mathtt{endl}
                     << "Number of matches:
99
                                                                 " << \ \mathtt{notfound} << \ \mathtt{endl}
                     << "Number of misses:
100
                     << "Average search depth (hits): " << steps/found << endl;</pre>
101
102
103
     int main ( int argc, char **argv ) {
104
105
          enum MODE { NONE =0, BST, AVL, SPLAY, TREAP };
106
107
          int mode =NONE;
          if(argc < 4)
               return printUsage( argv[0] );
111
          \mathbf{if} \, ( \ \mathtt{std} :: \mathtt{string} \, ( \ \mathtt{argv} \, [\, 1 \, ] \ ) \, = \, "\, b \, s \, t \, " \ )
112
               mode = BST;
113
          else if ( std::string( argv[1] ) == "avl" )
114
               mode = AVL;
115
          \mathbf{else} \ \mathbf{if} ( \ \mathbf{std} :: \mathbf{string} ( \ \mathbf{argv} [1] \ ) == "treap" \ )
116
               mode = TREAP;
117
          \mathbf{if} \, ( \ \mathtt{std} :: \mathtt{string} \, ( \ \mathtt{argv} \, [\, 1\, ] \ ) \, = \, "\mathit{splay} \, " \ )
118
               mode =SPLAY;
120
          if(!mode)
121
               return printUsage( argv[0] );
122
123
          std::ifstream fhaystack(argv[2]);
124
          if( !fhaystack.good( ) ) {
125
               std::cerr << "Could not open" << argv[2] << std::endl;
126
127
               return -1;
128
          std::ifstream fneedles( argv[3] );
          if( !fneedles.good( ) ) {
131
               \mathtt{std}::\mathtt{cerr} << "Could not open" << \mathtt{argv}[3] << \mathtt{std}::\mathtt{endl};
132
               return -1;
133
          }
134
135
          if(argc > 4)
136
               if (argv [4] \&\& mode != TREAP) 
137
                    std::cerr << "This variable should only be set for Treaps." << std::endl;</pre>
138
                    return -1;
139
141
               else if (argv[4]) \le 0
                    {\tt std}::{\tt cerr} << "This variable should only be an integer"
142
                                 << " greater than \theta." << std::endl;
143
```

```
return -1;
144
             }
145
        }
146
147
        std::vector<string> needles;
148
        if( !extractNeedles( needles, fneedles ) ) {
149
             cerr << "Could not read a set of strings to search for." << endl;</pre>
150
             return -1;
151
        }
153
        BinarySearchTree<string> *tree;
154
        switch(mode) {
155
             case BST:
156
                  tree = new BinarySearchTree<string>();
157
                 break;
158
             case AVL:
159
                  tree = new AVLTree<string>();
160
                 break;
161
             case SPLAY:
                  {\tt tree} \; = \; \mathbf{new} \; \; {\tt SplayTree} {<} {\tt string} \, {>} (\,) \, ;
                 break:
165
             case TREAP:
                  tree = new Treap < string > (argc > 4 ?atoi(argv[4]) : 100 ); // Default was
166
                 break;
167
        }
168
169
170
        // Define a start point to time measurement
171
        auto start = std::chrono::high_resolution_clock::now();
172
174
        if( !fillTree( tree, fhaystack ) ) {
             cerr << "Could not read the haystack." << endl;</pre>
176
             return -1;
177
178
179
        // Determine the duration of the code block
180
        auto duration =std::chrono::duration_cast<std::chrono::milliseconds>
181
                                    (std::chrono::high_resolution_clock::now() - start);
182
        \texttt{cout} << "Filled the binary search tree in" << duration.count() << "ms" << endl;
        start = std::chrono::high_resolution_clock::now();
        findAll( needles, tree );
187
        auto durationNs =std::chrono::duration_cast<std::chrono::nanoseconds>
188
                                    (std::chrono::high_resolution_clock::now() - start);
189
190
        cout << "Searched the haystack in " << durationNs.count() << "ns, ~" << (float)du
191
192
        // Test pre-order
193
        //for( auto word : *tree ) {
        //
               cout << word << '\n';
        //}
196
197
```

```
fhaystack.close( );
198
          fneedles.close( );
199
          delete tree;
200
201
          return 0;
202
203
     6.3
            Tree.h
     /**
      * Tree:
      * @author Micky Faas (s1407937)
                     Lisette de Schipper (s1396250)
      * @author
      * @file
                     tree.h
                     26-10-2014
      * @date
      **/
    #ifndef TREE_H
 10
    #define TREE_H
    \#include "TreeNodeIterator.h"
    #include <assert.h>
    #include <list>
 14
    #include <map>
 15
 16
     using namespace std;
 17
 18
     {\bf template} \ <\! {\bf class} \ \ {\tt INFO\_T}\! > \ {\bf class} \ \ {\tt SplayTree} \ ;
20
     template < class \  \, \texttt{INFO\_T} \! > \  \, class \  \, \texttt{Tree}
21
22
          public:
23
               enum ReplaceBehavoir {
 24
                     DELETE_EXISTING,
 25
                     ABORT_ON_EXISTING,
 26
                     MOVE_EXISTING
 27
 28
                };
                {f typedef} TreeNode<INFO_T> node_t;
                typedef TreeNodeIterator<INFO_T> iterator;
                {\bf typedef} \  \, {\tt TreeNodeIterator\_in}{<\tt INFO\_T>} \  \, {\tt iterator\_in}\,;
 32
                {\bf typedef} \  \, {\tt TreeNodeIterator\_pre} {<\tt INFO\_T>} \  \, {\tt iterator\_pre} \, ;
 33
                {\bf typedef\ TreeNodeIterator\_post}{<} {\tt INFO\_T}{>}\ {\tt iterator\_post};
 34
                \mathbf{typedef} \ \mathtt{list} < \mathtt{node\_t} *> \ \mathtt{nodelist} \; ;
 35
36
37
                * @function Tree()
38
                * @abstract Constructor of an empty tree
 39
                **/
                Tree()
 41
                     : m_root( 0 ) {
 42
                }
 43
 44
               /**
 45
```

```
* @function Tree()
46
            \boldsymbol{\ast} @abstract Copy-constructor of a tree. The new tree contains the nodes
47
                         from the tree given in the parameter (deep copy)
48
            * @param
                         tree, a tree
49
50
            Tree( const Tree<INFO_T>& tree )
51
                : m_root( 0 ) {
52
                *this = tree;
53
           }
            /**
            * @function
                         ~Tree()
57
                         Destructor of a tree. Timber.
            * @abstract
58
            **/
59
            ~Tree( ) {
60
              clear( );
61
62
63
          /**
            * Ofunction begin_pre()
            st @abstract begin point for pre-order iteration
            * @return
                         interator_pre containing the beginning of the tree in
67
68
                         pre-order
            **/
69
            iterator_pre begin_pre( ) {
70
                // Pre-order traversal starts at the root
71
                return iterator_pre( m_root );
72
              }
73
74
           /**
            * Ofunction begin()
76
            st @abstract begin point for a pre-order iteration
77
78
            * @return
                         containing the beginning of the pre-Order iteration
            **/
79
           iterator_pre begin( ) {
80
                return begin_pre( );
81
82
83
           /**
84
            * @function end()
                         end point for a pre-order iteration
            * @abstract
            * @return
                         the end of the pre-order iteration
88
            **/
           iterator_pre end( ) {
89
                return iterator_pre((node_t*)0);
90
           }
91
92
93
            * @function
                        end_pre( )
            * @abstract
                         end point for pre-order iteration
95
            * @return
                         interator_pre containing the end of the tree in pre-order
            **/
97
            iterator_pre end_pre( ) {
98
                return iterator_pre( (node_t*)0 );
99
```

```
}
100
101
             /**
102
              * @function
                            begin_in()
103
              * @abstract
                             begin point for in-order iteration
104
                             interator_in containing the beginning of the tree in
105
                             in-order
106
              **/
107
              \verb|iterator_in begin_in( ) | \{
                  if( !m_root )
                       return end_in( );
                  node_t *n = m_root;
111
                   \mathbf{while} \, ( \  \, \mathtt{n-\!\!>} \mathtt{leftChild} \, ( \  \, ) \  \, )
112
                       n = n->leftChild();
113
                  return iterator_in( n );
114
                }
115
116
             /**
117
              * @function
                             end_in()
              * @abstract
                             end point for in-order iteration
120
              * @return
                             interator_in containing the end of the tree in in-order
              **/
121
              iterator_in end_in( ) {
122
                  return iterator_in( (node_t*)0 );
123
              }
124
125
             /**
126
              * @function
                            begin_post()
127
              * @abstract begin point for post-order iteration
              * @return
                             interator_post containing the beginning of the tree in
                             post-order
              **/
              iterator_post begin_post( ) {
132
                   if( !m_root )
133
                       return end_post( );
134
                  node_t *n = m_root;
135
                   \mathbf{while} \, ( \  \, \mathtt{n-\!\!>} \mathtt{leftChild} \, ( \  \, ) \  \, )
136
                       n = n - > leftChild(
137
                  return iterator_post( n );
138
              }
             /**
142
                             end_post( )
              * @function
              * @abstract
                             end point for post-order iteration
143
              * @return
                             interator_post containing the end of the tree in post-order
144
              **/
145
              iterator_post end_post( ) {
146
                  return iterator_post( (node_t*)0 );
147
              }
148
149
             /**
              * Ofunction pushBack()
              * @abstract a new TreeNode containing 'info' is added to the end
152
                             the node is added to the node that :
153
```

```
- is in the row as close to the root as possible
154
                             - has no children or only a left-child
155
                             - seen from the right hand side of the row
156
                          this is the 'natural' left-to-right filling order
157
                          compatible with array-based heaps and full b-trees
158
                          info, the contents of the new node
              @param
159
            * @post
                          A node has been added.
160
            **/
161
            virtual node_t *pushBack( const INFO_T& info ) {
                node_t *n =new node_t( info, 0 );
                if( !m_root ) { // Empty tree, simplest case
                     m_root = n;
165
166
                 else \{ // Leaf node, there are two different scenarios
167
                     int max =getRowCountRecursive( m_root, 0 );
168
                     node_t *parent;
169
                     for (int i = 1; i \le max; ++i)
170
171
                         parent =getFirstEmptySlot( i );
                         if(parent) {
                             if( !parent->leftChild( ) )
174
                                 parent->setLeftChild( n );
175
                             else if( !parent->rightChild( ) )
176
                                 parent->setRightChild( n );
177
                             n->setParent( parent );
178
                             break;
179
180
                         }
                     }
181
182
                return n;
            }
           /**
186
                          insert( )
            * @function
187
              @abstract
                          inserts node or subtree under a parent or creates an empty
188
                          root node
189
              @param
                          info, contents of the new node
190
              @param
                          parent, parent node of the new node. When zero, the root is
191
192
              @param
                          alignRight, insert() checks on which side of the parent
                          node the new node can be inserted. By default, it checks
                          the left side first.
                          To change this behavior, set preferRight =true.
196
                          replaceBehavior, action if parent already has two children.
197
              @param
                          One of:
198
                          ABORT_ON_EXISTING - abort and return zero
199
                          MOVE_EXISTING - make the parent's child a child of the new
200
                                           node, satisfies preferRight
201
                          DELETE_EXISTING - remove one of the children of parent
202
                                             completely also satisfies preferRight
203
              @return
                          pointer to the inserted TreeNode, if insertion was
                          successfull
206
              @pre
                          If the tree is empty, a root node will be created with info
                          as it contents
207
```

```
The instance pointed to by parent should be part of the
208
            * @pre
                          called instance of Tree
209
              @post
                          Return zero if no node was created. Ownership is assumed on
210
                          the new node.
211
                          When DELETE_EXISTING is specified, the entire subtree on
212
                          preferred side may be deleted first.
213
214
            virtual node_t* insert( const INFO_T& info,
215
                              node_t* parent = 0,
                              bool preferRight = false,
217
                              int replaceBehavior =ABORT_ON_EXISTING ) {
218
                 if( !parent )
219
                     parent =m_root;
220
221
                 if( !parent )
222
                     return pushBack( info );
223
224
                 node_t * node = 0;
225
                 if( !parent->leftChild( )
                       && ( !preferRight || ( preferRight &&
                            parent->rightChild( ) ) ) {
229
                     \verb"node = "new node_t( info, parent );
230
                     parent->setLeftChild( node );
231
                     node->setParent( parent );
232
233
                 } else if( !parent->rightChild( ) ) {
234
                     node =new node_t( info, parent );
235
                     parent->setRightChild( node );
236
                     node->setParent( parent );
                 else if (replaceBehavior == MOVE_EXISTING) {
240
                     node =new node_t( info, parent );
                     if( preferRight ) {
241
                         node->setRightChild( parent->rightChild( ) );
242
                         node->rightChild( )->setParent( node );
243
                         parent->setRightChild( node );
244
                     } else {
245
246
                         node->setLeftChild( parent->leftChild( ) );
                         node->leftChild( )->setParent( node );
                         parent->setLeftChild( node );
                     }
250
                 } else if( replaceBehavior == DELETE_EXISTING ) {
251
                     node =new node_t( info, parent );
252
                     if(preferRight) {
253
                         deleteRecursive( parent->rightChild( ) );
254
                         parent->setRightChild( node );
255
                     } else {
256
                         deleteRecursive( parent->leftChild( ) );
257
                         parent->setLeftChild( node );
                     }
260
                 }
261
```

```
return node;
262
            }
263
264
           /**
265
             * @function
                          replace()
266
                          replaces an existing node with a new node
            * @abstract
267
                           info, contents of the new node
             * @param
268
             * @param
                          node, node to be replaced. When zero, the root is assumed
269
             * @param
                           alignRight, only for MOVE_EXISTING. If true, node will be
                           the right child of the new node. Otherwise, it will be the
271
                           left.
              @param
                          replaceBehavior, one of:
273
                           ABORT_ON_EXISTING - undefined for replace()
274
                           MOVE_EXISTING - make node a child of the new node,
275
                                            satisfies preferRight
276
                           DELETE_EXISTING - remove node completely
277
                           pointer to the inserted TreeNode, replace() is always
               @return
278
279
                           successful
            *
              @pre
                           If the tree is empty, a root node will be created with info
                           as it contents
                          The instance pointed to by node should be part of the
               @pre
                           called instance of Tree
283
                           Ownership is assumed on the new node. When DELETE_EXISTING
284
               @post
                           is specified, the entire subtree pointed to by node is
285
                          deleted first.
286
287
            virtual node_t* replace( const INFO_T& info,
288
                               node_t* node = 0,
289
                               bool alignRight = false,
290
                               {\bf int \ replaceBehavior =} {\tt DELETE\_EXISTING \ }) \ \ \{
                 assert( replaceBehavior != ABORT_ON_EXISTING );
                 node_t *newnode =new node_t( info );
294
                 if( !node )
295
                     node =m_root;
296
                 if(!node)
297
                     return pushBack( info );
298
299
                 if( node->parent( ) ) {
300
                     newnode->setParent( node->parent( ) );
                     if(node->parent()->leftChild() == node)
                         node->parent( )->setLeftChild( newnode );
                     else
                         node->parent( )->setRightChild( newnode );
305
                 } else
306
                     m_root =newnode;
307
308
                 if(replaceBehavior = DELETE_EXISTING) {
309
310
                     deleteRecursive( node );
311
                 else if ( replaceBehavior == MOVE_EXISTING ) {
314
                     if( alignRight )
                         newnode->setRightChild( node );
315
```

```
else
316
                         newnode->setLeftChild( node );
317
                     node->setParent( newnode );
318
                }
319
                return node;
320
            }
321
322
           /**
323
            * Ofunction remove()
            st @abstract removes and deletes node or subtree
            * @param
                          n, node or subtree to be removed and deleted
            * @post
                          after remove(), n points to an invalid address
327
            **/
328
            virtual void remove( node_t *n ) {
329
                if(!n)
330
                     return;
331
                 if(n->parent())
332
                     if(n->parent()->leftChild() == n)
333
                         n->parent()->setLeftChild(0);
                     else if(n->parent()->rightChild() == n)
                         n->parent()->setRightChild(0);
336
337
                deleteRecursive( n );
338
            }
339
340
           /**
341
            * @function
                         clear( )
342
            * @abstract clears entire tree
343
            * @pre
                          tree may be empty
            * @post
                          all nodes and data are deallocated
            **/
            void clear( ) {
                deleteRecursive( m_root );
348
                m_root = 0;
349
            }
350
351
           /**
352
353
            * @function
                          empty()
            * @abstract
                          test if tree is empty
            * @return
                          true when empty
            **/
            bool isEmpty( ) const {
                return !m_root;
358
            }
359
360
          /**
361
            * @function root()
362
            * @abstract returns address of the root of the tree
363
                          the adress of the root of the tree is returned
364
365
            * @pre
                          there needs to be a tree
            **/
            node_t* root( ){
368
                return m_root;
            }
369
```

```
370
           /**
371
            * Ofunction row()
372
            * @abstract
                         returns an entire row/level in the tree
373
             * @param
                          level, the desired row. Zero gives just the root.
374
            * @return
                          a list containing all node pointers in that row
375
            * @pre
                          level must be positive or zero
376
            * @post
377
            **/
            nodelist row( int level ) {
                 nodelist rlist;
                 getRowRecursive( m_root, rlist, level );
381
                 return rlist;
382
            }
383
384
            /**
385
            * @function
                          find()
386
            * @abstract
                          find the first occurrence of info and returns its node ptr
387
            * @param
                          haystack, the root of the (sub)tree we want to look in
                          null if we want to start at the root of the tree
                          needle, the needle in our haystack
            * @param
            * @return
                          a pointer to the first occurrence of needle
391
             * @post
                          there may be multiple occurrences of needle, we only return
392
                           one. A null-pointer is returned if no needle is found
393
            **/
394
            virtual node_t* find( node_t* haystack, const INFO_T& needle ) {
395
                 if( haystack == 0 ) 
396
                          if( m_root )
397
                              haystack =m_root;
398
                          else
                              \textbf{return} \quad 0 \, ;
                 return findRecursive( haystack, needle );
402
            }
403
404
           /**
405
            * @function
                          contains()
406
407
            * @abstract
                          determines if a certain content (needle) is found
408
            * @param
                          haystack, the root of the (sub)tree we want to look in
                          null if we want to start at the root of the tree
            * @param
                          needle, the needle in our haystack
            * @return
                          true if needle is found
411
412
            **/
            bool contains( node_t* haystack, const INFO_T& needle ) {
413
                 return find( haystack, needle );
414
            }
415
416
417
            * @function
                          toDot()
418
            * @abstract
                          writes tree in Dot-format to a stream
419
            * @param
                          out, ostream to write to
            * @pre
                          out must be a valid stream
422
            * @post
                          out (file or cout) with the tree in dot-notation
            **/
423
```

```
{f void} toDot( ostream& out, {f const} string & graphName ) {
424
                     if \, ( \  \, \texttt{isEmpty} ( \  \, ) \  \, )
425
                          return;
426
                    map<node_t *, int> adresses;
427
                    typename map< node_t *, int >::iterator adrIt;
428
                    int i = 1;
429
                    int p;
430
                     iterator_pre it;
431
                     iterator_pre tempit;
                     adresses[m\_root] = 0;
                    out << "digraph "<< graphName << '\{ '<< end1 << '" '<< 0 << '" <math display="inline">';
                     \begin{tabular}{ll} for ( it = begin_pre( ); it != end_pre( ); ++it ) & ( \\ \end{tabular}
435
                          adrIt = adresses.find( \&(*it) );
436
                          if(adrIt = adresses.end())
437
                               \mathtt{adresses} \left[ \& (*\,\mathtt{it}\,) \, \right] \ = \!\!\mathtt{i}\,;
438
                               p = i;
439
                               i ++;
440
441
                          if((\&(*it))->parent()!=\&(*tempit))
                             out << ';' << end1 << '"'
                                 <\!\!< \mathtt{adresses.find} \left( \begin{array}{c} (\&(*\mathtt{it})) - \!\!> \!\! \mathtt{parent} \left( \begin{array}{c} \end{array}) \right) - \!\!> \!\! \mathtt{second} \\ <\!\!< \begin{array}{c} \text{'"'}; \end{array} \right.
                          if((\&(*it)) != m\_root)
445
                               out << " -> \"" << p << '"';
446
                          tempit =it;
447
                    }
448
                    out << '; ' << endl;
449
                     for ( adrIt =adresses.begin( ); adrIt != adresses.end( ); ++adrIt )
450
                          out << adrIt->second << " [label=\setminus""
451
                               << adrIt->first->info( ) << "\"]";
452
                    out << '} ';
               }
              /**
456
               * @function
                                copyFromNode( )
457
                                copies the the node source and its children to the node
               * @abstract
458
                                 dest
459
               * @param
                                 source, the node and its children that need to be copied
460
                 @param
                                dest, the node who is going to get the copied children
461
               * @param
462
                                left, this is true if it's a left child.
               * @pre
                                there needs to be a tree and we can't copy to a root.
               * @post
                                the subtree that starts at source is now also a child of
                                dest
466
               **/
               void copyFromNode( node_t *source, node_t *dest, bool left ) {
467
                     if (!source)
468
                          return:
469
                    node_t *acorn =new node_t( dest );
470
                     if(left) {
471
                          if ( \ \texttt{dest} -\!\! > \!\! \texttt{leftChild}( \ ))
472
                               return:
473
                          dest->setLeftChild( acorn );
                     else {
476
                          if( dest->rightChild( ))
477
```

```
478
                             return:
                        dest->setRightChild( acorn );
479
480
                    cloneRecursive( source, acorn );
481
               }
482
483
               Tree<INFO_T>& operator=( const Tree<INFO_T>& tree ) {
484
                    clear( );
                    if( tree.m_root ) {
                        \verb|m_root| = \\ new | node_t( | (node_t*)0 |);
487
                         cloneRecursive( tree.m_root, m_root );
489
                    return *this;
490
               }
491
492
          protected:
493
494
               * @function
                               cloneRecursive( )
495
               * @abstract
                               cloning a subtree to a node
               * @param
                               source, the node we want to start the cloning process from
               * @param
                               dest, the node we want to clone to
               * @post
                               the subtree starting at source is cloned to the node dest
499
               **/
500
               void cloneRecursive( node_t *source, node_t* dest ) {
501
                    dest->info() =source->info();
502
                    if( source->leftChild( ) ) {
503
                        node_t *left =new node_t( dest );
504
                         dest->setLeftChild( left );
505
                         cloneRecursive( source->leftChild( ), left );
                    if ( \  \, \texttt{source} -\!\!\!> \!\! \texttt{rightChild} ( \  \, ) \  \, ) \  \, \{
                        node_t *right =new node_t( dest );
                        dest->setRightChild( right );
510
                         {\tt cloneRecursive} \left( \begin{array}{c} {\tt source-}{\gt rightChild} \left( \begin{array}{c} \end{array} \right), \begin{array}{c} {\tt right} \end{array} \right);
511
                    }
512
              }
513
514
515
               * @function
                               deleteRecursive( )
516
               * @abstract
                               delete all nodes of a given tree
                               root, starting point, is deleted last
               * @param
               * @post
                               the subtree has been deleted
               **/
520
               \mathbf{void} \ \mathtt{deleteRecursive} ( \ \mathtt{node\_t} \ *\mathtt{root} \ ) \ \{
521
                    if(!root)
522
                        return:
523
                    deleteRecursive( root->leftChild( ) );
524
                    deleteRecursive( root->rightChild( ) );
525
                    delete root;
526
              }
527
              /**
530
               * @function
                               getRowCountRecursive( )
               * @abstract calculate the maximum depth/row count in a subtree
531
```

```
532
             * @param
                           root, starting point
                           level, starting level
             * @param
533
             * @return
                           maximum depth/rows in the subtree
534
             **/
535
             int \ \mathtt{getRowCountRecursive} \left( \ \mathtt{node\_t*} \ \mathtt{root} \ , \ int \ \mathtt{level} \ \right) \ \{
536
                 if( !root )
537
                      return level;
538
                 return max (
539
                          getRowCountRecursive( root->leftChild( ), level+1 ),
                          getRowCountRecursive( root->rightChild( ), level+1 ) );
541
             }
542
543
            /**
544
                           getRowRecursive( )
545
             * @function
              @abstract
                           compile a full list of one row in the tree
546
                           root, starting point
              @param
547
                           rlist, reference to the list so far
               @param
548
             * @param
                           level, how many level still to go
549
             * @post
                           a list of a row in the tree has been made.
             **/
             void getRowRecursive( node_t* root, nodelist &rlist, int level ) {
                 // Base-case
553
                 if (~! \, \texttt{level}~)~\{
554
                      rlist.push_back( root );
555
                 } else if( root ){
556
                      level--;
557
                      if( level && !root->leftChild( ) )
558
                          for ( int i =0; i < (level <<1); ++i )
559
                               rlist.push_back( 0 );
560
                      else
                         getRowRecursive( root->leftChild( ), rlist, level );
                      if( level && !root->rightChild( ) )
564
                          565
                              rlist.push_back(0);
566
567
                          getRowRecursive( root->rightChild( ), rlist, level );
568
                 }
569
570
             }
             /**
                          findRecursive( )
             * @function
                           first the first occurrence of needle and return its node
574
             * @abstract
575
                           ptr
                           haystack, root of the search tree
             * @param
576
             * @param
                           needle, copy of the data to find
577
             * @return
                           the node that contains the needle
578
579
             node_t *findRecursive( node_t* haystack, const INFO_T &needle ) {
580
                 if( haystack->info( ) == needle )
581
                      return haystack;
584
                 node_t *n = 0;
                 if( haystack->leftChild( ) )
585
```

```
{\tt n = findRecursive(\ haystack -> leftChild(\ )\,,\ needle\ );}
586
                 if( !n && haystack->rightChild( ) )
587
                     n =findRecursive( haystack->rightChild( ), needle );
588
                 return n;
589
             }
590
591
             friend class TreeNodeIterator_pre<INFO_T>;
592
             friend class TreeNodeIterator_in<INFO_T>;
593
             friend class SplayTree<INFO_T>;
             TreeNode<INFO_T> *m_root;
595
        private:
597
             /**
598
             * @function
                          getFirstEmptySlot( )
599
               @abstract
                          when a row has a continuous empty space on the right,
600
                           find the left-most parent in the above row that has
601
                           at least one empty slot.
602
               @param
                           level, how many level still to go
603
             * @return
                          the first empty slot where we can put a new node
             * @pre
                           level should be > 1
             **/
             node_t *getFirstEmptySlot( int level ) {
607
608
                 node_t *p = 0;
                 nodelist rlist =row( level-1 ); // we need the parents of this level
609
                 /** changed auto to int **/
610
                 for( auto it =rlist.rbegin( ); it !=rlist.rend( ); ++it ) {
611
                     if( !(*it)->hasChildren( ) )
612
                         p = (*it);
613
614
                     else if( !(*it)->rightChild( ) ) {
                         p = (*it);
                          break;
                     } else
617
                         break;
618
619
                 return p;
620
             }
621
    };
622
623
624 #endif
          TreeNode.h
    6.4
    /**
     * Treenode:
 2
     * @author Micky Faas (s1407937)
     * @author
                Lisette de Schipper (s1396250)
     * @file
                 Treenode.h
     * @date
                 26-10-2014
     **/
10 #ifndef TREENODE.H
   #define TREENODE.H
12
```

```
using namespace std;
14
   template <class INFO_T> class Tree;
15
   class ExpressionTree;
16
17
   template <class INFO_T> class TreeNode
18
19
       public:
20
21
          /**
           * Ofunction TreeNode()
22
           st @abstract Constructor, creates a node
           * @param
                         info, the contents of a node
24
           * @param
                         parent, the parent of the node
25
           * @post
                         A node has been created.
26
           **/
27
           TreeNode( const INFO_T& info, TreeNode<INFO_T>* parent =0 )
28
                : m_lchild( 0 ), m_rchild( 0 ) {
29
                m_info =info;
30
                m_parent =parent;
           }
          /**
34
           * Ofunction TreeNode()
35
           * @abstract Constructor, creates a node
36
           * @param
                         parent, the parent of the node
37
           * @post
                         A node has been created.
38
           **/
39
           TreeNode( TreeNode<INFO_T>* parent =0 )
40
                : m_lchild(0), m_rchild(0) {
41
                m_parent =parent;
           }
          /**
45
           * @function
46
           * @abstract Sets a nodes content to {\tt N}
47
           * @param
                         n, the contents you want the node to have
48
           * @post
                         The node now has those contents.
49
50
           void operator =( INFO_T n ) { m_info =n; }
51
          /**
           * @function INFO_T(), info()
           * @abstract Returns the content of a node
55
           * @return
                         m_{\text{info}}, the contents of the node
56
           **/
57
           operator INFO_T( ) const { return m_info; }
58
           const INFO_T &info( ) const { return m_info; }
59
           INFO_T &info( ) { return m_info; }
60
           /**
61
62
           * Ofunction atRow()
           st Cabstract returns the level or row-number of this node
           * @return
                         row, an int of row the node is at
           **/
65
           int atRow( ) const {
```

```
{\tt const} TreeNode<INFO_T> *n = {\tt this};
 67
                                      int row =0:
 68
                                      while( n->parent( ) ) {
 69
                                               n = n-> parent();
 70
                                               row++;
 71
 72
                                      return row;
 73
                            }
 74
                          /**
 76
                            * @function parent(), leftChild(), rightChild()
 77
                            * @abstract returns the adress of the parent, left child and right
 78
                                                            child respectively
 79
                            * @return
                                                            the adress of the requested family member of the node
 80
 81
                            TreeNode<INFO_T> *parent( ) const { return m_parent; }
 82
                            TreeNode<INFO_T> *leftChild( ) const { return m_lchild;
 83
                            TreeNode<INFO_T> *rightChild( ) const { return m_rchild; }
 84
                            /**
                            * @function
                                                          swapWith()
                            st Qabstract Swaps this node with another node in the tree
 88
                            * @param
 89
                                                            n, the node to swap this one with
                            * @pre
                                                            both this node and n must be in the same parent tree
 90
                             * @post
                                                            n will have the parent and children of this node
 91
                                                            and vice verse. Both nodes retain their data.
 92
                            **/
 93
                            void swapWith( TreeNode<INFO_T>* n ) {
                                      bool this_wasLeftChild =false;
                                       if(parent() \& parent() -> leftChild() = this)
                                                this\_wasLeftChild = true;
 97
                                       if(n->parent() \&\& n->parent()->leftChild() == n)
 99
                                                n_wasLeftChild =true;
100
                                      // Swap the family info
101
                                      {\tt TreeNode}{<}{\tt INFO\_T}{>}{*}\ {\tt newParent}\ =
102
                                                ( \  \, \mathtt{n} \!\! - \!\! > \!\! \mathtt{parent} \, ( \  \, ) \  \, = \  \, \mathbf{this} \  \, ) \  \, ? \  \, \mathtt{n} \  \, : \  \, \mathtt{n} \!\! - \!\! > \!\! \mathtt{parent} \, ( \  \, ) \, ;
103
                                      {\tt TreeNode}{<} {\tt INFO\_T}{>}{*} \ {\tt newLeft} \ =
104
105
                                                (n->leftChild() = this)? n:n->leftChild();
                                      TreeNode<INFO_T>* newRight =
                                                  ( n->rightChild( ) == this ) ? n :n->rightChild( );
                                      n->setParent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(p
109
                                      {\tt n-\!\!>\!\!setLeftChild(\ leftChild(\ ) == n\ ?\ this}\ :\ {\tt leftChild(\ )}\ );
110
                                      {\tt n-\!\!>\!\!setRightChild(\ rightChild(\ ) == n\ ?\ this\ :\ rightChild(\ )\ );}
111
112
                                      setParent( newParent );
113
                                      setLeftChild( newLeft );
114
                                      setRightChild( newRight );
115
116
                                      // Restore applicable pointers
118
                                      if( n->leftChild( ) )
                                                n{\longrightarrow} \texttt{leftChild} \left( \begin{array}{c} ){\longrightarrow} \texttt{setParent} \left( \begin{array}{c} n \end{array} \right);
119
                                      if(n->rightChild())
120
```

```
{\tt n-\!\!>} {\tt rightChild(\ )-\!\!>} {\tt setParent(\ n\ )};
121
                    if( leftChild( ) )
122
                         leftChild( )->setParent( this );
123
                    if( rightChild( ) )
124
                        rightChild( )->setParent( this );
125
                    if( n->parent( ) ) {
126
                         if( this_wasLeftChild )
127
                              n->parent( )->setLeftChild( n );
128
                             n->parent( )->setRightChild( n );
130
                    if \left( \ \mathtt{parent} \left( \ \right) \ \right) \ \{
132
                         if(n_{wasLeftChild})
133
                             parent( )->setLeftChild( this );
134
135
                             parent( )->setRightChild( this );
136
                   }
137
              }
138
              /**
              * @function
                               replace()
              * @abstract
                               Replaces the node with another node in the tree
142
              * @param
                               n, the node we replace the node with, this one gets deleted
143
              * @pre
                               both this node and n must be in the same parent tree
144
              * @post
                               The node will be replaced and n will be deleted.
145
              **/
146
              void replace( TreeNode<INFO_T>* n ) {
147
                   bool n_wasLeftChild =false;
148
149
                    if(n->parent() \&\& n->parent()->leftChild() == n)
                        n_wasLeftChild =true;
                    // Swap the family info
153
                    {\tt TreeNode}{<}{\tt INFO\_T}{>}{*} {\tt newParent} =
154
                         (\ \mathtt{n} \mathord{-\!\!>} \mathtt{parent} \, (\ ) \ \Longrightarrow \ \mathtt{this} \ ) \ ? \ \mathtt{n} \ : \ \mathtt{n} \mathord{-\!\!>} \mathtt{parent} \, (\ ) \, ;
155
                    TreeNode < INFO_T > * newLeft =
156
                         (n->leftChild() = this)? n:n->leftChild();
157
                    TreeNode<INFO_T>* newRight =
158
                          ( n->rightChild( ) == this ) ? n :n->rightChild( );
159
                    setParent( newParent );
                    setLeftChild( newLeft );
                   setRightChild( newRight );
163
                   m_info = n->m_info;
164
165
                   // Restore applicable pointers
166
                    if( leftChild( ) )
167
                         leftChild( )->setParent( this );
168
                    if( rightChild( ) )
169
170
                         rightChild( )->setParent( this );
                    if \left( \ parent \left( \ \right) \ \right) \ \{
172
                         if( n_wasLeftChild )
173
                              parent( )->setLeftChild( this );
174
```

```
else
175
                                                       parent( )->setRightChild( this );
176
177
                                     delete n;
178
                           }
179
180
181
                           * @function
                                                        sibling( )
182
                           * @abstract returns the address of the sibling
                                                         the address to the sibling or zero if there is no sibling
                           * @return
                           **/
                           TreeNode<INFO_T>* sibling( ) {
186
                                     if(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(parent(pare
187
                                              return parent( )->rightChild( );
188
                                     else if(parent()->rightChild() = this)
189
                                              return parent( )->leftChild( );
190
191
                                              return 0;
192
                           }
                         /**
                           * @function
                                                        hasChildren( ), hasParent( ), isFull( )
196
                            * @abstract
                                                        Returns whether the node has children, has parents or is
197
                                                          full (has two children) respectively
198
                               @param
199
                                @return
                                                         true or false, depending on what is requested from the node.
200
                                                          if hasChildren is called and the node has children, it will
201
                                                          return true, otherwise false.
202
                                                          If hasParent is called and the node has a parent, it will
203
                                                          return true, otherwise false.
                                                          If isFull is called and the node has two children, it will
                                                          return true, otherwise false.
                           **/
207
                           bool hasChildren( ) const { return m_lchild || m_rchild; }
208
                           bool hasParent( ) const { return m_parent; }
209
                           bool isFull( ) const { return m_lchild && m_rchild; }
210
211
                  protected:
212
213
                           friend class Tree<INFO_T>;
                           friend class ExpressionTree;
                         /**
                           * @function
                                                       setParent( ), setLeftChild( ), setRightChild( )
217
                            * @abstract
                                                         sets the parent, left child and right child of the
218
                                                          particular node respectively
219
                                                         p, the node we want to set a certain family member of
                           * @param
220
                            * @return
                                                          void
221
                                                          The node now has a parent, a left child or a right child
                            * @post
222
                                                          respectively.
223
                           **/
224
                           \mathbf{void} \ \mathtt{setParent} \left( \ \mathtt{TreeNode} {<} \mathtt{INFO\_T} {>} \ *\mathtt{p} \ \right) \ \left\{ \ \mathtt{m\_parent} \ =\! \mathtt{p} \, ; \ \right\}
                           void setLeftChild( TreeNode<INFO_T> *p ) { m_lchild =p; }
                           void setRightChild( TreeNode<INFO_T> *p ) { m_rchild =p; }
227
```

228

```
private:
229
             INFO_T m_info;
230
             {\tt TreeNode}{<}{\tt INFO\_T}{>} \ *{\tt m\_parent} \ ;
231
             TreeNode<INFO_T> *m_lchild;
232
             TreeNode<INFO_T> *m_rchild;
233
    };
234
235
   /**
236
   * @function <<
   * @abstract the contents of the node are returned
   * @param
                  out, in what format we want to get the contents
    * @param
                  rhs, the node of which we want the contents
240
    * @return
                  the contents of the node.
241
242
    template <class INFO_T> ostream &operator <<(ostream& out, const TreeNode<INFO_T> & r
243
        out << rhs.info( );</pre>
244
        return out;
245
246
248 #endif
    6.5
          TreeNodeIterator.h
```

```
* TreeNodeIterator: Provides a set of iterators that follow the STL-standard
    * @author Micky Faas (s1407937)
    * @author Lisette de Schipper (s1396250)
    * @file
               TreeNodeIterator.h
               26-10-2014
    * @date
    **/
10 #include <iterator>
  #include "TreeNode.h"
12
   template < class INFO_T > class TreeNodeIterator
13
                            : public std::iterator<std::forward_iterator_tag,
14
                                                   TreeNode<INFO_T>>> {
       public:
16
           typedef TreeNode<INFO_T> node_t;
18
          /**
19
           * @function TreeNodeIterator()
20
           * @abstract (copy)constructor
21
           * @pre
                        TreeNodeIterator is abstract and cannot be constructed
22
23
           TreeNodeIterator( node_t* ptr =0 ) : p( ptr ) { }
24
           TreeNodeIterator( const TreeNodeIterator& it ) : p( it.p ) { }
25
           * @function
                        (in)equality operator overload
29
           * @abstract Test (in)equality for two TreeNodeIterators
                        rhs, right-hand side of the comparison
           * @param
30
           * @return
                        true if both iterators point to the same node (==)
31
```

```
false if both iterators point to the same node (!=)
32
             **/
33
             bool operator == (const TreeNodeIterator& rhs) { return p=rhs.p; }
34
             bool operator != (const TreeNodeIterator& rhs) { return p!=rhs.p; }
35
36
            /**
37
             * @function
                           operator*( )
38
             * @abstract
                           Cast operator to node_t reference
             * @return
                            The value of the current node
             * @pre
                            Must point to a valid node
             **/
             node_t& operator*( ) { return *p; }
43
44
            /**
45
             * Ofunction operator++()
46
             * @abstract
                            pre- and post increment operators
47
                            TreeNodeIterator that has iterated one step
48
             **/
49
             TreeNodeIterator &operator++( ) { next( ); return *this; }
             TreeNodeIterator operator++( int )
                  \{ \  \, \texttt{TreeNodeIterator tmp(*this)}; \  \, \mathbf{operator} + + (\  \, ); \  \, \mathbf{return tmp;} \  \, \}
        protected:
53
54
            /**
55
             * Ofunction next() //(pure virtual)
56
             * @abstract Implement this function to implement your own iterator
57
58
             virtual bool next( ){ return false; }// =0;
59
60
             node_t *p;
   };
62
   template < class | INFO_T > class | TreeNodeIterator_pre
                                : public TreeNodeIterator<INFO_T> {
64
        public:
65
             typedef TreeNode<INFO_T> node_t;
66
67
             TreeNodeIterator_pre( node_t* ptr =0 )
68
                  : TreeNodeIterator<INFO_T>( ptr ) { }
69
             TreeNodeIterator_pre( const TreeNodeIterator<INFO_T>& it )
70
                  : TreeNodeIterator<INFO_T>( it ) { }
             TreeNodeIterator_pre( const TreeNodeIterator_pre& it )
                  : TreeNodeIterator<INFO_T>( it.p ) \{ \}
74
             {\tt TreeNodeIterator\_pre \ \& operator} + + (\ ) \ \{\ {\tt next(\ )}; \ {\tt return \ *this}; \ \}
75
             {\tt TreeNodeIterator\_pre~operator} + + (~{\tt int}~)
76
                   \{ \  \, \texttt{TreeNodeIterator\_pre} \  \, \texttt{tmp(} \  \, *\texttt{this} \  \, ); \  \, \texttt{operator} + + ( \  \, ); \  \, \texttt{return} \  \, \texttt{tmp;} \  \, \} 
77
78
79
             using TreeNodeIterator<INFO_T>::p;
80
81
            /**
             * @function next()
84
             * @abstract Takes one step in pre-order traversal
             * @return
                            returns true if such a step exists
```

```
*/
86
            bool next( ) {
87
                 if(!p)
88
                     return false;
89
                 if(\ p\!\! -\!\! >\! hasChildren(\ )\ ) { // a possible child that can be the next
90
                     p =p->leftChild( ) ? p->leftChild( ) : p->rightChild( );
91
                     return true;
92
93
                 else if (p->hasParent()) // we have a right brother
                         && p->parent()->rightChild()
95
96
                         && p->parent()->rightChild() != p) {
                     p =p->parent( )->rightChild( );
97
                     return true;
98
99
                 else if( p->hasParent( ) ) { // just a parent, thus we go up
100
                     TreeNode<INFO_T> *tmp =p->parent( );
101
                     while( tmp->parent( ) ) {
102
                          if ( tmp->parent( )->rightChild( )
103
                                  && tmp->parent(\ )->rightChild(\ ) != tmp ) {
                              p =tmp->parent( )->rightChild( );
                              return true;
107
                          tmp =tmp->parent( );
108
                     }
109
110
                 // Nothing left
111
112
                 p = 0;
                 return false;
113
            }
114
116
    };
117
    template < class INFO_T > class TreeNodeIterator_in
118
                              : public TreeNodeIterator<INFO_T>{
119
        public:
120
            typedef TreeNode<INFO_T> node_t;
121
122
            TreeNodeIterator_in( node_t* ptr =0 )
123
                 : TreeNodeIterator<INFO_T>( ptr ) { }
124
            {\tt TreeNodeIterator\_in(\ const\ TreeNodeIterator{<}INFO\_T{>}\&\ it\ )}
                 : TreeNodeIterator<INFO_T>( it ) { }
            TreeNodeIterator_in( const TreeNodeIterator_in& it )
                 : TreeNodeIterator<INFO_T>( it.p ) { }
128
129
            TreeNodeIterator_in &operator++( ) { next( ); return *this; }
130
            TreeNodeIterator_in operator++( int )
131
                 { TreeNodeIterator_in tmp( *this ); operator++( ); return tmp; }
132
133
        protected:
134
            using TreeNodeIterator<INFO_T>::p;
135
            /**
            * @function next()
138
            * @abstract
                          Takes one step in in-order traversal
            * @return
                           returns true if such a step exists
139
```

```
*/
140
              bool next( ) {
141
                    i\,f\,(\ p\!\!-\!\!>\!\! \text{rightChild}\,(\ )\ )\ \{
142
                        p =p->rightChild( );
143
                         while( p->leftChild( ) )
144
                             p =p->leftChild( );
145
                         return true;
146
147
                    {\tt else \ if(\ p->parent(\ )\ \&\&\ p->parent(\ )->leftChild(\ )\ ==\ p\ )\ \{}
                        p = p->parent();
149
                        return true;
                   } else if ( p->parent( ) && p->parent( )->rightChild( ) == p ) {
151
                        p = p->parent();
152
                         \mathbf{while}(\ p\text{--}\mathsf{parent}(\ )\ \&\&\ p\ =\text{p--}\mathsf{parent}(\ )\text{--}\mathsf{rightChild}(\ )\ )\ \{
153
                             p = p->parent();
154
155
                         if(p)
156
                             p = p->parent();
157
                         if( p )
                              return true;
                         else
                             return false;
161
162
                   // Er is niks meer
163
                   p = 0;
164
                   return false;
165
              }
166
167
    };
168
    template <class INFO_T> class TreeNodeIterator_post
                                   : public TreeNodeIterator<INFO_T>{
170
171
         public:
              \mathbf{typedef} \  \, \mathtt{TreeNode} {<} \mathtt{INFO\_T} {>} \  \, \mathtt{node\_t} \, ;
172
173
              TreeNodeIterator_post( node_t* ptr =0 )
174
                   : TreeNodeIterator<INFO_T>( ptr ) \{ \}
175
              {\tt TreeNodeIterator\_post(\ const\ TreeNodeIterator<INFO\_T>\&\ it\ )}
176
                   : TreeNodeIterator<INFO_T>( it ) \{ \}
177
              TreeNodeIterator_post( const TreeNodeIterator_post& it )
178
                    : TreeNodeIterator<INFO_T>( it.p ) { }
              {\tt TreeNodeIterator\_post~\& operator} + + (~)~\{~{\tt next(~)};~{\tt return~*this}\,;~\}
              TreeNodeIterator_post operator++( int )
182
                    { TreeNodeIterator_post tmp(*this); operator++(); return tmp; }
183
184
         protected:
185
              using TreeNodeIterator<INFO_T>::p;
186
             /**
187
              * @function
                              next( )
188
              * @abstract
                               Takes one step in post-order traversal
189
              * @return
                               returns true if such a step exists
              */
              bool next( ) {
192
193
```

```
if(p\rightarrow hasParent()) // We have a right brother
194
                         && p->parent( )->rightChild( )
195
                         && p->parent( )->rightChild( ) != p ) {
196
                     p = p->parent()->rightChild();
197
                     while( p->leftChild( ) )
198
                         p =p->leftChild( );
199
                     return true;
200
                 } else if( p->parent( ) ) {
201
                     p = p->parent();
                     return true;
                 // Nothing left
205
                p = 0;
206
                return false;
207
208
    };
209
    6.6
         SelfOrganizingTree.h
     * SelfOrganizingTree - Abstract base type inheriting from Tree
 2
     * @author
                Micky Faas (s1407937)
                Lisette de Schipper (s1396250)
     * @author
     * @file
                SelfOrganizingTree.h
     * @date
                3-11-2014
   #ifndef SELFORGANIZINGTREE_H
10
   #define SELFORGANIZINGTREE_H
   #include "BinarySearchTree.h"
13
14
    template <class INFO_T> class SelfOrganizingTree : public BinarySearchTree<INFO_T> {
15
        public:
16
            typedef BSTNode<INFO_T> node_t;
17
            typedef BinarySearchTree<INFO_T> S; // super class
18
          /**
            * @function
                          SelfOrganizingTree( ) : S( )
            * @abstract
                          Constructor
22
23
            SelfOrganizingTree( ) : S( ) { }
24
25
           /**
26
            * Ofunction rotateLeft() and rotateRight()
27
                         Performs a rotation with the given node as root of the
28
                          rotating subtree, either left of right.
29
                          The tree's root pointer will be updated if neccesary.
            * @param
31
                          node, the node to rotate
            * @pre
                          The node must be a node in this tree
            * @post
33
                          The node may be be the new root of the tree
                          No nodes will be invalided and no new memory is
34
```

35

allocated. Iterators may become invalid.

```
**/
36
             virtual node_t *rotateLeft( node_t * node ){
37
                  if(this->root() = node)
38
                       return static_cast<node_t *>( S::m_root = node->rotateLeft( ) );
39
40
                       return node->rotateLeft( );
41
42
43
             virtual node_t *rotateRight( node_t * node ){
                  if(this->root() = node)
                       return static_cast<node_t *>( S::m_root = node->rotateRight( ) );
                  else
47
                       return node->rotateRight( );
48
             }
49
50
        private:
51
52
   };
53
54
   #endif
   6.7
          BinarySearchTree.h
     * BinarySearchTree - BST that inherits from Tree
     * @author Micky Faas (s1407937)
     * @author Lisette de Schipper (s1396250)
     * @file
                  BinarySearchTree.h
     * @date
                  3-11-2014
     **/
  #ifndef BINARYSEARCHTREE_H
10
   #define BINARYSEARCHTREE_H
11
   #include "Tree.h"
13
   #include "BSTNode.h"
   template < class \  \, \texttt{INFO\_T} > \  \, class \  \, \texttt{BinarySearchTree} \ : \  \, public \  \, \texttt{Tree} < \texttt{INFO\_T} > \  \, \{
16
        public:
^{17}
             typedef BSTNode<INFO_T> node_t;
18
             \mathbf{typedef} \  \, \mathtt{Tree} {<} \mathtt{INFO\_T} {>} \  \, \mathtt{S} \, ; \  \, // \  \, \mathtt{super} \  \, \mathtt{class}
19
20
             BinarySearchTree( ) : S( ) { }
21
             BinarySearchTree( const BinarySearchTree& cpy ) : S( cpy ) { }
22
23
             virtual ~BinarySearchTree( ) { }
24
             * @function
                            pushBack( )
                            reimplemented virtual function from Tree<>
             * @abstract
                             this function is semantically identical to insert()
29
                             info, the contents of the new node
             * @param
30
```

```
**/
31
             virtual node_t *pushBack( const INFO_T& info ) {
32
                 return insert( info );
33
34
35
            /**
36
             * Ofunction insert()
37
             * @abstract reimplemented virtual function from Tree<>
                            the exact location of the new node is determined
                            by the rules of the binary search tree.
40
             * @param
                            info, the contents of the new node
41
             * @param
                            parent, ignored
42
                            preferRight, ignored
             * @param
43
             * @param
                            replaceBehavior, ignored
44
             * @return
                            returns a pointer to the inserted node
45
             **/
46
             virtual node_t* insert( const INFO_T& info,
47
                                    {\tt TreeNode}{<}{\tt INFO\_T}{>}{*} {\tt parent} \ = 0, \ // \ {\tt Ignored}
48
                                    {\bf bool\ preferRight\ =} {\bf false}\;, \qquad \  \  //\ {\tt Ignored}
                                    int \ \ replace \texttt{Behavior} \ = \texttt{S} :: \texttt{ABORT\_ON\_EXISTING} \ \ ) \ \ \{ \ \ \textit{//} \ \ \texttt{Ignored}
                 node_t *n =new node_t( );
                 return insertInto( info, n );
52
             }
53
54
55
             * @function
                           replace( )
56
                           reimplemented virtual function from Tree <>
57
             * @abstract
                            replaces a given node or the root
58
                            the location of the replaced node may be different
59
                            due to the consistency of the binary search tree
             * @param
                            info, the contents of the new node
             * @param
                            node, node to be replaced
63
             * @param
                            alignRight, ignored
                            {\tt replaceBehavior}\,,\,\,{\tt ignored}
64
             * @param
             * @return
                            returns a pointer to the new node
65
              @pre
                            node should be in this tree
66
             * @post
                            replace() will delete and/or remove node.
67
                            if node is 0, it will take the root instead
68
69
             **/
             virtual node_t* replace( const INFO_T& info,
                                     TreeNode < INFO_T > * node = 0,
                                     bool alignRight = false,
                                     int \ \texttt{replaceBehavior} = \!\! S:: \texttt{DELETE\_EXISTING} \ ) \ \{
73
                 node_t *newnode;
74
                 if(!node)
75
                      node =S::m_root;
76
                 if (!node)
77
                      return pushBack( info );
78
79
                 bool swap =false;
80
                 // We can either just swap the new node with the old and remove
82
                 // the old, or we can remove the old and add the new node via
83
                 // pushBack(). This depends on the value of info
                 if( !node->hasChildren( ) ) {
```

```
85
                       swap = true;
                  }
86
                   else if( !(node->leftChild( )
87
                            && node->leftChild()->info()>info)
88
                            && !(node->rightChild()
89
                            && node->rightChild( )->info( ) < info ) ) {
90
                       swap =true;
91
92
                   if(swap) {
                       newnode =new node_t( info );
                       if(node == S::m_root)
                            S::m\_root = newnode;
96
                       node->swapWith( newnode );
97
                       delete node;
98
                   } else {
99
                       remove( node );
100
                       newnode =pushBack( info );
101
102
                  return newnode;
             }
106
             /**
107
              * @function
                            remove()
108
              * @abstract
                             reimplemented virtual function from Tree <>
109
110
                             removes a given node or the root and restores the
111
                             BST properties
              * @param
                             node, node to be removed
112
              * @pre
                             node should be in this tree
113
              * @post
                             memory for node will be deallocated
              **/
              virtual void remove( TreeNode<INFO_T> *node ) {
                  node_t *n = static_cast < node_t *> (node);
117
118
                   while ( n->isFull( ) ) {
119
                       // the difficult case
120
                       // we could take either left of right here
121
                       TreeNode<INFO_T> *temp;
122
123
                       temp =n->leftChild( );
                       while( temp->rightChild( ) ) {
                            temp =temp->rightChild( );
                       if( n == S::m_root )
127
                            S::m_root =temp;
128
                       n{\longrightarrow} \texttt{swapWith} \left( \begin{array}{c} \texttt{temp} \end{array} \right);
129
                  }
130
131
132
                  // Assume the above is fixed
133
134
                   \mathbf{while} ( \  \, \mathtt{n-\!\!>\!} \mathtt{hasChildren} \, ( \  \, ) \  \, ) \  \, \{
                       if(n->leftChild())
                            if(n == S::m_root)
136
                                 S:=m\_root =n->leftChild();
137
                            n->swapWith(n->leftChild());
138
```

```
}
139
                       else
140
                             if( n == S::m_root )
141
                                 S::m_root =n->rightChild();
142
                            n->swapWith( n->rightChild( ) );
143
                       }
144
                   }
145
146
                   if(n->parent() \&\& n->parent()->leftChild() == n)
                        static\_cast < node\_t*> (n->parent())-> setLeftChild(0);
                   else \ if(\ n-\!\!>\! parent(\ ) \ \&\& \ n-\!\!>\! parent(\ )-\!\!>\! rightChild(\ ) == n\ )
                        static\_cast < node\_t*> (n->parent())-> setRightChild(0);
150
                   delete n;
151
              }
152
153
             /**
154
              * @function
                             find()
155
              * @abstract
                             reimplemented virtual function from Tree <>
156
                              performs a binary search in a given (sub)tree
              * @param
                             haystack, the subtree to search. Give 0 for the entire tree
              * @param
                             needle, key/info-value to find
              * @return
                             returns a pointer to node, if found
160
              * @pre
                             haystack should be in this tree
161
              * @post
                             may return 0
162
              **/
163
              \mathbf{virtual} \  \, \mathsf{TreeNode} {<} \mathsf{INFO}_{\mathtt{T}} {>} * \  \, \mathsf{find} \left( \  \, \mathsf{TreeNode} {<} \mathsf{INFO}_{\mathtt{T}} {>} * \  \, \mathsf{haystack} \right.,
164
                                                     const INFO_T& needle ) {
165
                   m_searchStepCounter = 0;
166
167
                   if( !haystack )
                       haystack =S::m_root;
                   while( haystack && haystack->info( ) != needle ) {
171
                       m_searchStepCounter++;
                        if( haystack->info( ) > needle )
172
                            haystack =haystack->leftChild( );
173
                       else
174
                            haystack =haystack->rightChild( );
175
176
177
                   if( !haystack )
                       m_searchStepCounter = -1;
                   return haystack;
              }
181
             /**
182
              * @function
                             lastSearchStepCount( )
183
                             gives the amount of steps needed to complete the most
               @abstract
184
                             recent call to find( )
185
                             positive amount of steps on a defined search result,
                @return
186
187
                              -1 on no search result
188
              virtual int lastSearchStepCount( ) const {
                   return m_searchStepCounter;
              }
191
```

192

```
/**
193
                               min()
             * @function
194
                               Returns the node with the least value in a binary search
               @abstract
195
                               tree. This is achieved through recursion.
196
               @param
                               node - the node from which we start looking
197
               @return
                               Eventually, at the end of the recursion, we return the
198
                               adress of the node with the smallest value.
199
             * @post
                               The node with the smallest value is returned.
200
             **/
             node_t* min( node_t* node ) const {
                  return node->leftChild() ?
                         \label{eq:cast_code_t*} \min\big(\, \mathbf{static_cast} < \! \mathsf{node_t*} > \! (\ \mathsf{node-} \! > \! \mathsf{leftChild}(\ )\ )\ )\ :\ \mathsf{node}\,;
204
             }
205
206
207
             * @function
                               min()
208
                               We call the function mentioned above and then
               @abstract
209
                               return the node with the least value in a binary search
210
                               We return the adress of the node with the smallest value.
             * @return
             * @post
                               The node with the smallest value is returned.
             **/
214
             {\tt node\_t*\ min(\ )\ const\ \{}
215
                  return min( static_cast < node_t *> ( this -> root( ) ) );
216
             }
217
218
            /**
219
             * @function
                               max()
220
             * @abstract
                               Returns the node with the highest value in a binary
                               search tree. This is achieved through recursion.
             * @param
                               node - the node from which we start looking
                               Eventually, at the end of the recursion, we return the
             * @return
225
                               adress of the node with the highest value.
             * @post
                               The node with the highest value is returned.
226
227
             node_t* max( node_t* node ) const
228
                  return node->rightChild( ) ?
229
                          max(static_cast<node_t*>( node->rightChild( ) ) ) : node;
230
231
            /**
                               max()
             * @function
             * @abstract
                               We call the function mentioned above and then
235
                               return the node with the highest value in a binary
236
                               search tree.
237
             * @return
                               We return the adress of the node with the highest value.
238
             * @post
                               The node with the highest value is returned.
239
240
             node_t* max( ) const {
241
                  return max( static_cast < node_t*>( this->root( ) ) );
242
             }
         protected:
245
             /**
246
```

```
* Ofunction insertInto()
247
             * @abstract Inserts new node into the tree following BST rules
248
                           Assumes that the memory for the node is already allocated
249
                           This function exists mainly because of derived classes
250
                           want to insert nodes of a derived type.
251
             * @param
                           info, the contents of the new node
252
             * @param
                           n, node pointer, should be already allocated
253
             * @return
                           returns a pointer to the inserted node
254
             **/
             virtual node_t* insertInto( const INFO_T& info,
                                  node_t* n ) { // Preallocated
                 n \rightarrow info() = info;
258
259
                 if( !S::m_root )
260
                     S:=m_root =n;
261
                 else {
262
                     node_t *parent = 0;
263
                     node_t *sub = static_cast < node_t *> (S::m_root);
264
                     \mathbf{do} \ \{
                          if(*n < *sub) {
                              parent =sub;
                              sub = static\_cast < node\_t*>( parent->leftChild( ) );
268
269
                          else {
270
                              parent =sub;
271
                              sub =static_cast < node_t*>( parent -> rightChild( ) );
272
273
                     } while( sub );
274
                     if(*n < *parent)
                          parent->setLeftChild( n );
                     else
                         parent->setRightChild( n );
279
                     n->setParent( parent );
280
                 return n;
281
            }
282
283
             int m_searchStepCounter;
284
285
    };
287 #endif
          BSTNode.h
    6.8
     * BSTNode - Node atom for BinarySearchTree
     * @author
                Micky Faas (s1407937)
                 Lisette de Schipper (s1396250)
     * @author
     * @file
                 BSTNode.h
     * @date
                 3-11-2014
     **/
10 #ifndef BSTNODE_H
```

```
#define BSTNODE_H
12
  #include "TreeNode.h"
13
14
   template <class INFO_T> class BinarySearchTree;
15
16
   template <class INFO_T> class BSTNode : public TreeNode <INFO_T>
17
18
       public:
19
           typedef TreeNode<INFO_T> S; // super class
20
21
           /**
22
           * Ofunction BSTNode()
23
                       Constructor, creates a node
           * @abstract
24
           * @param
                        info, the contents of a node
25
           * @param
                        parent, the parent of the node
26
                        A node has been created.
           * @post
27
           **/
28
           BSTNode( const INFO_T& info, BSTNode<INFO_T>* parent =0 )
               : S( info, parent ) { }
31
          /**
32
           * Ofunction BSTNode()
33
           * @abstract Constructor, creates a node
34
                        parent, the parent of the node
           * @param
35
           * @post
                        A node has been created.
36
           **/
37
           BSTNode( BSTNode<INFO_T>* parent =0 )
38
               : S((S)parent) \{ \}
           // Idea: rotate this node left and return the node that comes in its place
41
           BSTNode *rotateLeft( ) {
43
               if ( \ !this -\!\!\!> \!\! rightChild ( \ ) \ ) \ /\!/ \ Cannot \ rotate
44
                   return this;
45
46
               bool isLeftChild =this->parent( ) && this == this->parent( )->leftChild(
47
48
49
               // new root of tree
               // new rightchild of the node that is rotated
               BSTNode *newRight =static_cast <BSTNode *>(newTop->leftChild( ));
               // the parent under which all of the magic is happening
53
               54
55
               // We become left-child of our right-child
56
               // newTop takes our place with our parent
57
               newTop->setParent( topParent );
58
               if( isLeftChild && topParent )
59
                   topParent->setLeftChild( newTop );
60
               else if( topParent )
                   \verb|topParent-> setRightChild( newTop ); \\
62
63
               newTop->setLeftChild(this);
64
```

```
\mathbf{this} \! - \! \! \! > \! \mathtt{setParent} \left( \begin{array}{c} \mathtt{newTop} \end{array} \right);
65
66
                 // We take the left-child of newTop as our right-child
67
                 this->setRightChild( newRight );
68
                 if( newRight )
69
                      newRight->setParent( this );
70
71
                 return newTop;
72
             }
74
             // Idea: rotate this node right and return the node that comes in its place
75
             BSTNode *rotateRight( ) {
76
                 if( !this->leftChild( ) ) // Cannot rotate
77
                      return this;
78
79
                 bool isRightChild =this->parent( ) && this == this->parent( )->rightChild
80
81
                 // new root of tree
82
                 BSTNode *newTop =static_cast <BSTNode *>(this->leftChild());
                 // new leftchild of the node that is rotated
                 BSTNode *newLeft =static_cast <BSTNode *>(newTop->rightChild( ));
                 // the parent under which all of the magic is happening
86
                 BSTNode *topParent =static_cast <BSTNode *>(this->parent());
87
88
                 // We become left-child of our right-child
89
                 // newTop takes our place with our parent
90
                 newTop->setParent( topParent );
91
                 if( isRightChild && topParent )
92
                      topParent->setRightChild( newTop );
93
                  else if( topParent )
                      topParent->setLeftChild( newTop );
95
                 newTop->setRightChild(this);
97
                 this->setParent( newTop );
98
99
                 // We take the left-child of newTop as our right-child
100
                 this->setLeftChild( newLeft );
101
                  if( newLeft )
102
103
                      newLeft \rightarrow setParent(this);
                 return newTop;
             }
107
             bool operator <( const BSTNode<INFO_T> &rhs ) {
108
                 return S::info() < rhs.info();
109
             }
110
111
             bool operator <=( const BSTNode<INFO_T> &rhs ) {
112
                 return S::info() <= rhs.info();
113
             }
114
116
             bool operator >( const BSTNode<INFO_T> &rhs ) {
117
                 return S::info() > rhs.info();
             }
118
```

```
119
             bool operator >=( const BSTNode<INFO_T> &rhs ) {
120
                  return S::info() >= rhs.info();
121
             }
122
         protected:
123
             friend class BinarySearchTree<INFO_T>;
124
125
    };
126
127 #endif
    6.9 AVLTree.h
    /**
     * AVLTree - AVL-SelfOrganizingTree that inherits from SelfOrganizingTree
 2
 3
     * @author Micky Faas (s1407937)
     * @author
                  Lisette de Schipper (s1396250)
                  {\tt AVLTree.h}
     * @file
     * @date
                  9-12-2014
     **/
   #ifndef AVLTREE_H
10
    #define AVLTREE_H
11
12
   #include "SelfOrganizingTree.h"
13
   #include "AVLNode.h"
14
15
    template < class \  \, \texttt{INFO\_T} > \  \, class \  \, \texttt{AVLTree} \  \, : \  \, public \  \, \texttt{SelfOrganizingTree} < \texttt{INFO\_T} > \, \{
         public:
17
             typedef AVLNode<INFO_T> node_t;
18
             {\bf typedef~SelfOrganizingTree}{<} {\tt INFO\_T>~S;~//~super~class
19
20
            /**
21
             * @function
                                AVLTree( )
22
             * @abstract
                                constructor
23
             * @post
                                An AVLTree is created
24
25
             **/
             AVLTree( ) : S( ) { }
            /**
             * @function
                                AVLTree()
29
             * @abstract
                                {\tt constructor}
30
             * @param
31
                                сру
                                An AVLTree is created
             * @post
32
             **/
33
             AVLTree( const AVLTree& cpy ) : S( cpy ) { }
34
35
            /**
             * @function
                                insert()
             * @abstract
                                A node with label 'info' is inserted into the tree and
39
                                put in the right place. A label may not appear twice in
40
                                a tree.
                                info - the label of the node
             * @param
41
             * @return
                                the node we inserted
42
```

```
* @post
                             The tree now contains a node with 'info'
43
            **/
44
            node_t* insert( const INFO_T& info,
45
                             {\tt TreeNode}{<}{\tt INFO\_T}{>}{*} {\tt parent} \ = 0, \ // \ {\tt Ignored}
46
                             bool preferRight =false,
                                                             // Ignored
47
                             int replaceBehavior =0 ) { // Ignored
48
                if( S::find( this->root( ), info ) )
49
                    return 0;
50
                node_t *node =new node_t( );
                S::insertInto( info, node );
                rebalance( node );
                return node;
54
            }
55
56
57
            * @function
                             remove()
58
                             A node is removed in such a way that the properties of
              @abstract
59
                             an AVL tree remain intact.
60
            *
              @param
                             node - the node we're going to remove
                             The node has breen removed, but the remaining tree still
              @post
                             contains all of its other nodes and still has all the
                             AVL properties.
64
            **/
65
            void remove( node_t* node ) {
66
                // if it's a leaf
67
                if( !node->leftChild( ) && !node->rightChild( ) )
68
                    S::remove( node );
69
                // internal node with kids
70
                else {
71
                     if(node->rightChild())
                         \verb|node| = static\_cast < \verb|node\_t*| > ( S::replace(
                               S::min(static\_cast < node\_t*>(
75
                               node->rightChild( ) ) )->info( ), node ) );
                         removeMin( static_cast < node_t *> ( node -> rightChild( ) ) );
76
                         node->setRightChild( node->rightChild( ));
77
                     }
78
                     else
79
                         // just delete the node and replace it with its leftChild
80
81
                         node->replace( node->leftChild( ) );
                }
            }
       private:
85
86
           /**
87
            * @function
                             removeMin()
88
             @abstract
                             Recursively we go through the tree to find the node with
89
                             the smallest value in the subtree with root node. Then we
90
                             restore the balance factors of all its parents.
91
            *
              @param
                             node - the root of the subtree we're looking in
92
            * @return
                             At the end of the recursion we return the parent of the
                             node with the smallest value. Then we go up the tree and
95
                             rebalance every parent from this upwards.
            * @post
                             The node with the smallest value is deleted and every
96
```

```
node still has the correct balance factor.
97
              **/
98
              node_t* removeMin( node_t* node ) {
99
                  node_t* temp;
100
                   if( node->leftChild( ) )
101
                       temp =removeMin( static_cast < node_t *> ( node -> leftChild( ) ) );
102
                   else {
103
                       temp =static_cast < node_t*>( node->parent( ) );
104
                       S::remove( node );
                  rebalance( temp );
                  return temp;
108
              }
109
110
111
              * @function
                                 removeMax()
112
                @abstract
                                 Recursively we go through the tree to find the node with
113
                                 the highest value in the subtree with root node. Then we
114
                                 restore the balance factors of all its parents.
                                 node - the root of the subtree we're looking in
              *
                @param
117
                @return
                                 At the end of the recursion we return the parent of the
                                 node with the highest value. Then we go up the tree and
118
                                 {\tt rebalance}\ {\tt every}\ {\tt parent}\ {\tt from}\ {\tt this}\ {\tt upwards}\,.
119
                @post
                                 The node with the highest value is deleted and every
120
                                 node still has the correct balance factor.
121
              **/
122
              node_t* removeMax( node_t* node ) {
123
                  node_t* temp;
124
                   if( node->rightChild( ) )
125
                       \label{temp} = \\ \texttt{removeMin} ( \  \, \mathbf{static\_cast} < \\ \texttt{node\_t} * > \\ ( \  \, \texttt{node} - \\ \texttt{>} \\ \texttt{rightChild} ( \  \, ) \  \, ) \  \, );
                   else {
127
                       temp = static\_cast < node\_t*> (node->parent());
                       S::remove( node );
129
130
                  rebalance( temp );
131
                  return temp;
132
              }
133
134
             /**
135
              * @function
                                 rotateLeft()
              * @abstract
                                 We rotate a node left and make sure all the internal
                                 heights of the nodes are up to date.
               @param
139
                                 node - the node we're going to rotate left
               @return
                                 we return the node that is now at the top of this
140
                                 particular subtree.
141
              * @post
                                 The node is rotated to the left and the heights are up
142
                                 to date.
143
144
              node_t* rotateLeft( node_t* node ) {
145
                  node_t *temp =static_cast < node_t *> ( S::rotateLeft( node ) );
146
                  temp->updateHeight( );
                   if( temp->leftChild( ) )
                        {\tt static\_cast} < {\tt node\_t} \ *> ( \ {\tt temp->leftChild} ( \ ) \ )-> {\tt updateHeight} ( \ );
149
                  return temp;
150
```

```
}
151
152
           /**
153
            * @function
                             rotateRight()
154
             * @abstract
                              We rotate a node right and make sure all the internal
155
                              heights of the nodes are up to date.
156
                              node - the node we're going to rotate right
              @param
157
            *
              @return
                              we return the node that is now at the top of this
158
                              particular subtree.
            * @post
                              The node is rotated to the right and the heights are up
                              to date.
            **/
162
            node_t* rotateRight( node_t* node ) {
163
                node_t* temp =static_cast<node_t*>( S::rotateRight( node ) );
164
                 temp->updateHeight( );
165
                 if ( temp->rightChild( )
166
                     static_cast<node_t*>( temp->rightChild( ) )->updateHeight( );
167
                return temp;
168
            }
           /**
            * @function
                              rebalance()
172
              @abstract
                             The tree is rebalanced. We do the necessary rotations
173
                              from the bottom up to make sure the AVL properties are
174
                              still intact.
175
              @param
                              node - the node we're going to rebalance
176
            * @post
177
                              The tree is now perfectly balanced.
            **/
178
            void rebalance( node_t* node ) {
179
                node->updateHeight( );
                node_t* temp =node;
                 while( temp->parent( ) ) {
183
                     temp = static\_cast < node\_t*>( temp->parent( ) );
184
                     temp->updateHeight();
185
                     // right subtree too deep
186
                     if(temp->balanceFactor() == 2) {
187
                         if(temp->rightChild())
188
                              if( static_cast < node_t*>( temp->rightChild( ) )
189
                                  ->balanceFactor(\ ) < 0 )
                                  this->rotateRight(
                                  static_cast < node_t*>( temp->rightChild( ) ) );
193
                         this->rotateLeft( temp );
194
                     }
195
                     // left subtree too deep
196
                     else if ( temp->balanceFactor( ) == -2 ) {
197
                         if( temp->leftChild( ) ) {
198
                              if( static_cast<node_t*>( temp->leftChild( ) )->
199
                                  balanceFactor() > 0)
200
                                  this->rotateLeft(
                                  static_cast < node_t*>( temp->leftChild( ) );
203
                         this->rotateRight( temp );
204
```

```
}
205
                 }
206
            }
207
    };
208
209
210 #endif
    6.10 AVLNode.h
    /**
     * AVLNode - Node atom type for AVLTree
                Micky Faas (s1407937)
     * @author
                 Lisette de Schipper (s1396250)
     * @author
 5
     * @file
                 {\tt AVLNode.h}
     * @date
                 9-11-2014
   #ifndef AVLNODE.H
10
   #define AVLNODE_H
11
12
   #include "BSTNode.h"
13
14
    template <class INFO_T> class AVLTree;
15
16
    template <class INFO_T> class AVLNode : public BSTNode<INFO_T>
17
18
        public:
19
            typedef BSTNode<INFO_T> S; // super class
20
21
             /**
22
             * @function
                              AVLNode()
23
             * @abstract
                              Constructor, creates a node
24
             * @param
                              info, the contents of a node
25
             * @param
                              parent, the parent of the node
26
             * @post
                              A node has been created.
27
             **/
28
             {\tt AVLNode(\ const\ INFO\_T\&\ info\ ,\ AVLNode<INFO\_T>*\ parent\ =0\ )}
                 : S( info, parent ) {
31
32
            /**
33
             * @function
                              AVLNode()
34
             * @abstract
                              Constructor, creates a node
35
                              parent, the parent of the node
             * @param
36
             * @post
                              A node has been created.
37
             **/
38
             AVLNode( AVLNode<INFO_T>* parent =0 )
39
                 : S((S)) parent ) {
             }
41
42
            /**
43
             * @function
                              balanceFactor( )
44
                              we return the height of the rightchild subtracted with
             * @abstract
45
```

```
the height of the left child. Because of the properties
46
                             of an AVLtree, this should never be less than \mbox{-1} or more
47
                             than 1.
48
            * @return
                             we return the difference between the height of the
49
                             rightchild and the leftchild.
50
            * @post
                             The difference between the two child nodes is returned.
51
            **/
52
            int balanceFactor( ){
53
                return static_cast<AVLNode *>( this->rightChild( ) )->getHeight( ) -
                       static_cast<AVLNode *>( this->leftChild( ) )->getHeight( );
55
           }
56
57
           /**
58
                             updateHeight()
59
            * @function
            * @abstract
                             we update the height of the node.
60
            * @pre
                             The children of the node need to have the correct height.
61
                             The node now has the right height.
            * @post
62
            **/
63
            void updateHeight( ) {
                int lHeight =static_cast<AVLNode *>( this->leftChild( ) )
                              ->getHeight( );
                int r Height = static\_cast < AVLNode *>( this->rightChild( ) )
67
68
                              ->getHeight( );
69
                this->height = ( 1 + ( ( lHeight > rHeight ) ? lHeight : rHeight ) );
70
           }
71
72
           /**
73
            * @function
                             getHeight( )
74
            * @abstract
                             we want to know the height of the node.
76
            * @return
                             we return the height of the node.
            * @post
77
                             The current height of the node is returned.
78
            **/
            int getHeight( )
79
                return (this ? this->height : 0);
80
            }
81
82
            bool operator <( const AVLNode<INFO_T> &rhs ) {
83
                return S::info() < rhs.info();</pre>
84
            }
86
            bool operator <=( const AVLNode<INFO_T> &rhs ) {
                return S::info() <= rhs.info();
88
            }
89
90
            bool operator >( const AVLNode<INFO_T> &rhs ) {
91
                return S::info() > rhs.info();
92
            }
93
94
            bool operator >=( const AVLNode<INFO_T> &rhs ) {
95
                return S::info() >= rhs.info();
97
            }
98
       protected:
99
```

```
friend class AVLTree<INFO_T>;
100
101
        private:
102
            int height;
103
    };
104
105
106
   #endif
    6.11
           SplayTree.h
    /**
 1
     * SplayTree - Splay-tree implementation
 2
     * @author
                Micky Faas (s1407937)
     * @author
                 Lisette de Schipper (s1396250)
     * @file
                 SplayTree.h
                 3-11-2014
     * @date
   #ifndef SPLAYTREE_H
10
   #define SPLAYTREE_H
11
12
   #include "SelfOrganizingTree.h"
13
14
    template < class INFO_T> class SplayTree : public SelfOrganizingTree < INFO_T> \{
15
        public:
16
             typedef BSTNode<INFO_T> node_t;
17
             typedef SelfOrganizingTree<INFO_T> S; // super class
18
19
             SplayTree( ) : SelfOrganizingTree<INFO_T>( ) { }
20
21
             SplayTree( const SplayTree& copy )
22
                 : SelfOrganizingTree<INFO_T>( copy ) { }
23
24
             /**
25
             * @function
                           insert()
26
                           reimplemented virtual function from BinarySearchTree<>
             * @abstract
                           the new node will always be the root
                           info, the contents of the new node
             * @param
                           parent, ignored
             * @param
30
             * @param
31
                           preferRight, ignored
             * @param
                           replaceBehavior, ignored
32
             * @return
                           returns a pointer to the inserted node (root)
33
             **/
34
             virtual node_t* insert( const INFO_T& info,
35
                                   {\tt TreeNode}{<}{\tt INFO\_T}{>}{*} \ {\tt parent} \ =0, \ // \ {\tt Ignored}
36
                                   bool preferRight =false ,
                                                                  // Ignored
37
                                   int replaceBehavior =0 ) { // Ignored
                 {\tt return splay(S::insert(info,parent,preferRight))};\\
39
             }
40
41
             /**
42
             * Ofunction replace()
43
```

```
* @abstract reimplemented virtual function from BinarySearchTree<>
                         replaces a given node or the root
45
                         the resulting node will be propagated to location of the root
46
                         info, the contents of the new node
           * @param
47
           * @param
                         node, node to be replaced
48
           * @param
                         alignRight, ignored
49
           * @param
                         replaceBehavior, ignored
50
           * @return
                         returns a pointer to the new node (=root)
51
           * @pre
                         node should be in this tree
           * @post
                         replace() will delete and/or remove node.
                         if node is 0, it will take the root instead
           **/
55
           virtual node_t* replace( const INFO_T& info,
56
                                  TreeNode < INFO_T > * node = 0,
57
                                  bool alignRight = false,
58
                                  int replaceBehavior =0 ) {
59
                return splay( S::replace( info, node, alignRight ) );
60
           }
61
           /**
           * @function remove()
           * @abstract reimplemented virtual function from BinarySearchTree<>
65
                         removes a given node or the root and restores the
66
                         {\tt BST} properties. The node-to-be-removed will be spayed
67
                         before removal.
68
           * @param
                         node, node to be removed
69
           * @pre
                         node should be in this tree
70
           * @post
                         memory for node will be deallocated
71
           **/
72
           virtual void remove( TreeNode<INFO_T> *node ) {
                S::remove( splay( static_cast < node_t *> (node) ) );
           }
76
           /**
77
           * @function
                        find()
78
             @abstract
                         reimplemented virtual function from Tree<>
79
                         performs a binary search in a given (sub) tree
80
                         splays the node (if found) afterwards
81
82
           * @param
                         haystack, the subtree to search. Give 0 for the entire tree
           * @param
                         needle, key/info-value to find
           * @return
                         returns a pointer to node, if found
           * @pre
                         haystack should be in this tree
           * @post
                         may return 0, the structure of the tree may change
86
           **/
87
           virtual TreeNode<INFO_T>* find( TreeNode<INFO_T>* haystack,
88
                                             const INFO_T& needle ) {
89
                return splay( static_cast<node_t*>( S::find( haystack, needle ) ) );
90
           }
91
92
           /**
93
           * @function
                         splay()
           * @abstract
                         Performs the splay operation on a given node.
96
                         'Splay' means a certain amount of rotations in order
                         to make the given node be the root of the tree while
97
```

```
maintaining the binary search tree properties.
98
             * @param
                            node, the node to splay
99
             * @pre
                            The node must be a node in this tree
100
             * @post
                            The node will be the new root of the tree
101
                            No nodes will be invalided and no new memory is
102
                            allocated. Iterators may become invalid.
103
104
             node_t* splay( node_t* node ) {
105
                 enum MODE {
                      \texttt{LEFT} = 0 \texttt{x1} \;, \; \; \texttt{RIGHT} = 0 \texttt{x2} \;,
                      PLEFT =0x4, PRIGHT =0x8 };
109
110
                  // Can't splay the root (or null)
111
                  if( !node || S::m_root == node )
112
                      return node;
113
114
                  node_t *p =static_cast<node_t*>( node->parent( ) );
115
                  int mode;
                  while( p != S::m_root ) {
                      if(p->leftChild() == node)
119
                          mode =RIGHT;
120
                      else
121
                           mode = LEFT;
122
123
                      assert( p->parent( ) != nullptr );
124
125
                      // Node's grandparent
126
                      node_t* g =static_cast<node_t*>( p->parent( ) );
                      if(g->leftChild() == p)
                           mode |= PRIGHT;
130
                      else
131
                           mode |= PLEFT;
132
133
                      // True if either mode is LEFT | PLEFT or RIGHT | PRIGHT
134
                      if( (mode >> 2) == (mode & 0x3) ) {
135
136
                           // the 'zig-zig' step
                           // first rotate g-p then p-node
                           if( mode & PLEFT )
140
                               this->rotateLeft( g );
                           else
141
                               this->rotateRight( g );
142
143
                           if( mode & LEFT )
144
                               this->rotateLeft( p );
145
                           else
146
147
                               this->rotateRight( p );
                      }
                      else {
149
                           // the 'zig-zag' step
150
                           // first rotate p-node then g-p
151
```

```
152
                                 if( mode & LEFT )
153
                                       \mathbf{this} \! - \! \! > \! \! \mathsf{rotateLeft} \left( \begin{array}{c} \mathtt{p} \end{array} \right);
154
                                 else
155
                                       this->rotateRight( p );
156
157
                                 if( mode & PLEFT )
158
                                       this->rotateLeft( g );
159
                                 else
                                       this->rotateRight( g );
161
                           }
162
163
                           // perhaps we're done already...
164
                            if(] node = this->root()
165
                                 return node;
166
                           else
167
                                 p =static_cast<node_t*>( node->parent( ) );
168
                      }
169
                      // The 'zig-step': parent of node is the root
                      if(p->leftChild() == node)
173
                           this->rotateRight( p );
174
                      else
175
                           this->rotateLeft( p );
176
177
                      return node;
178
                }
179
     };
180
_{182} #endif
     6.12
              Treap.h
      * Treap - Treap that inherits from SelfOrganizingTree
      * @author Micky Faas (s1407937)
                     Lisette de Schipper (s1396250)
      * @author
      * @file
                      Treap.h
      * @date
                      9-12-2014
    #ifndef TREAP_H
10
    #define TREAP_H
11
12
    #include "SelfOrganizingTree.h"
13
    #include "TreapNode.h"
14
15
     \mathbf{template} < \mathbf{class} \hspace{0.2cm} \mathtt{INFO\_T} > \hspace{0.2cm} \mathbf{class} \hspace{0.2cm} \mathtt{Treap} \hspace{0.2cm} : \hspace{0.2cm} \mathbf{public} \hspace{0.2cm} \mathtt{SelfOrganizingTree} < \mathtt{INFO\_T} > \hspace{0.2cm} \{
16
17
           public:
                {f typedef} TreapNode<INFO_T> node_t;
18
                {\bf typedef~SelfOrganizingTree}{<} {\tt INFO\_T>~S;~//~super~class
19
20
```

```
/**
21
            * @function
                              Treap()
22
            * @abstract
                              constructor
23
            * @post
                              A Treap is created
24
            **/
25
            Treap( int randomRange =100 ) : S( ) {
26
                 random = randomRange;
27
                 srand( time( NULL ) );
28
            }
30
           /**
31
            * @function
                              Treap( )
32
            * @abstract
                              constructor
33
            * @param
34
                              сру
            * @post
                              A Treap is created
35
            **/
36
            {\tt Treap(\ const\ Treap\&\ cpy,\ int\ randomRange\ =}100\ )} : {\tt S(\ cpy)} {
37
                 random = randomRange;
38
                 srand( time( NULL ) );
            }
41
           /**
42
            * @function
                              insert( )
43
            * @abstract
                              A node with label 'info' is inserted into the tree and
44
                              put in the right place. A label may not appear twice in
45
                              a tree.
46
            * @param
                              info - the label of the node
47
            * @return
                              the node we inserted
48
            * @post
                              The tree now contains a node with 'info'
49
            **/
            node_t* insert( const INFO_T& info,
                              {\tt TreeNode}{<}{\tt INFO\_T}{>}{*} {\tt parent} \ = 0, \ // \ {\tt Ignored}
52
                              bool preferRight =false ,
53
                                                              // Ignored
                              {f int} replaceBehavior =0 ) { // Ignored
54
                 // Prevent duplicates
55
56
                 if( S::find( this->root( ), info ) )
57
                     return 0;
58
59
                 node_t *node =new node_t( );
                 S::insertInto( info, node );
                 node \rightarrow priority = rand() \% random + 1;
                 rebalance( node );
63
                 return node;
64
            }
65
66
           /**
67
            * @function
                              remove()
68
            * @abstract
                              the node provided with the parameter is deleted from the
69
70
                              tree by rotating it down until it becomes a leaf or has
71
                              only one child. In the first case it's just deleted,
72
                              in the second it's replaced by its subtree.
            * @param
73
                              node - the node to be deleted
            * @post
                              The node is deleted from the tree which still retains
74
```

```
75
                               the Treap properties.
             **/
76
             void remove( node_t* node ) {
77
                 node_t *temp = node;
78
                 // rotating it down until the condition no longer applies.
79
                  while( temp->leftChild( ) && temp->rightChild( ) )
80
                 {
81
                      if(static\_cast < node\_t* > (temp->rightChild())->priority>
82
                           static_cast < node_t*>( temp->leftChild( ) )->priority )
                           this->rotateLeft( temp );
84
                      else
85
                           this->rotateRight( temp );
86
87
                  // if it's a leaf
88
                  if( !temp->leftChild( ) && !temp->rightChild( ) )
89
                      S::remove( temp );
90
                  // if it only has a right child
91
                  else if( !temp->leftChild( ) )
92
                      temp->replace(static\_cast<node\_t*>(temp->rightChild());
                  // if it only has a left child
                  else if( !node->rightChild( ) )
                      temp->replace( static_cast<node_t*>( temp->leftChild( ) ) );
96
             }
97
98
        private:
99
             int random;
100
101
102
             * @function
                               rebalance()
103
                               The tree is rebalanced. We do the necessary rotations
             * @abstract
                               from the bottom up to make sure the Treap properties are
                               still intact.
             * @param
107
                               info - the label of the node
             * @return
                               the node we inserted
108
             * @post
                               The tree is now perfectly balanced.
109
110
             void rebalance( node_t* node ) {
111
                  if (!node)
112
113
                      return;
                 node_t* temp =node;
                 int myPriority =node->priority;
                  \mathbf{while} \, ( \  \, \mathsf{temp} \! - \! \! > \! \mathsf{parent} \, ( \  \, ) \, \, \&\& \, \,
117
                         myPriority >
                          static\_cast < node\_t*> ( temp->parent( ) )->priority ) {
118
                      temp = static\_cast < node\_t*>( temp->parent( ) );
119
                      if( temp->leftChild( ) == node )
120
                           this->rotateRight( temp );
121
                      else
122
                           this->rotateLeft( temp );
123
                 }
124
             }
127
    };
128
```

129 #endif

6.13 TreapNode.h

```
* TreapNode - Node atom type for Treap
    * @author Micky Faas (s1407937)
                Lisette de Schipper (s1396250)
    * @author
                {\tt TreapNode.h}
    * @file
    * @date
                9-11-2014
    **/
   #ifndef TREAPNODE.H
10
   #define TREAPNODE.H
11
   #include "BSTNode.h"
13
14
   \mathbf{template} \ <\! \mathbf{class} \ \ \mathtt{INFO\_T}\! > \ \mathbf{class} \ \ \mathtt{Treap} \, ;
15
16
   template <class INFO_T> class TreapNode : public BSTNode<INFO_T>
17
18
        public:
19
            typedef BSTNode<INFO_T> S; // super class
20
21
            /**
22
            * @function
                              TreapNode( )
23
            * @abstract
                              Constructor, creates a node
            * @param
                              info, the contents of a node
            * @param
                              parent, the parent of the node
            * @post
                              A node has been created.
27
28
            {\tt TreapNode(\ const\ INFO\_T\&\ info\ ,\ TreapNode<INFO\_T>*\ parent\ =0\ )}
29
                 : S(info, parent), priority(0)
30
31
32
           /**
33
            * @function
                              TreapNode( )
            * @abstract
                              Constructor, creates a node
            * @param
                              parent, the parent of the node
            * @post
                              A node has been created.
37
38
            TreapNode( TreapNode<INFO_T>* parent =0 )
39
                 : S((S)parent), priority(0)
40
41
42
            /**
43
            * @function
                         replace( )
44
            * @abstract
                          Replaces the node with another node in the tree
            * @param
                          n, the node we replace the node with, this one gets deleted
47
            * @pre
                          both this node and n must be in the same parent tree
            * @post
48
                          The node will be replaced and n will be deleted.
            **/
49
            void replace( TreapNode<INFO_T>* n ) {
50
```

```
{\tt priority} \; = \; n \!\! - \!\! > \!\! priority \; ;
51
                      \mathbf{this} \rightarrow S :: \mathtt{replace}( n );
52
                }
53
54
                {\bf bool\ operator}\ <(\ {\bf const}\ {\tt TreapNode}{<} {\tt INFO\_T}{>}\ \&{\tt rhs}\ )\ \{
55
                      return S::info() < rhs.info();</pre>
56
57
58
                bool operator <=( const TreapNode<INFO_T> &rhs ) {
                      return S::info() \le rhs.info();
61
62
                {\bf bool\ operator\ >(\ const\ TreapNode<INFO\_T>\&rhs\ )\ \{}
63
                      \mathbf{return} \ \mathtt{S}:: \mathtt{info}\,(\,) \, > \, \mathtt{rhs.info}\,(\,)\,;
64
65
66
                bool operator >=( const TreapNode<INFO_T> &rhs ) {
67
                      return S::info() >= rhs.info();
68
                int priority;
71
72
          {\bf protected}:
73
                {\bf friend \ class \ Treap}{<} {\tt INFO_T}{>};
74
    };
75
76
77
   #endif
78
```