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```
% Midterm Problem 3 (e)
% Polynomial deflation
% This script works up to 6th order

clear
clc
close all
```

Order & Coefficients of the poly

```
o = 5; % Order of the poly
itn = o;
A(:,1) = [1;-15;85;-225;274;-120]; % Coefficients of the poly (Decreasing order)
```

Setup for iteration

```
maxit = 1000000;
tol = 1e-6;
x0 = 0.5; % Initial guess for the root from the graph

if 2 < o && o < 7
```

```
for k = 1 : o-2
```

Newton's approx. method to find the 1st root

```
if itn == 6
    F = @(x) A(1,k)*x^(o+1-k) + A(2,k)*x^(o-k) + A(3,k)*x^(o-1-k) + A(4,k)*x^(o-2-k) + A(5,k)*x^(o-3-k) + A(6,k)*x^(o-4-k) + A(7,k)*x^(o-5-k);
elseif itn == 5
    F = @(x) A(1,k)*x^(o+1-k) + A(2,k)*x^(o-k) + A(3,k)*x^(o-1-k) + A(4,k)*x^(o-2-k) + A(5,k)*x^(o-3-k) + A(6,k)*x^(o-4-k);
elseif itn == 4
    F = @(x) A(1,k)*x^(o+1-k) + A(2,k)*x^(o-k) + A(3,k)*x^(o-1-k) + A(4,k)*x^(o-2-k) + A(5,k)*x^(o-3-k);
elseif itn == 3
    F = @(x) A(1,k)*x^(o+1-k) + A(2,k)*x^(o-k) + A(3,k)*x^(o-1-k) + A(4,k)*x^(o-2-k);
end % if
[roots(k,1),it(k,1),success(k,1)] = newton_approx(F,x0,maxit,tol);
table(roots,it,success)
```

ans =

1×3 table

roots	it	success
1	59	true

ans =

2×3 table

roots	it	success
1	59	true
2	216	true

ans =

3×3 table

roots	it	success
1	59	true
2	216	true
3	237	true

Division

```

N = roots(k,1) % Difine the divisor
for i = 1 : itn+1 % Reordering the coefficients
    Ap(i,k) = A(itn-i+2,k); % Increasing order
end % for
% Division
Qi(itn+1,k) = Ap(itn+1,k);
for i = itn : -1 : 1
    Qi(i,k) = Ap(i,k) + N*Qi(i+1,k); % Increasing order
end % for
R = Qi(1,k); % Remainder
% Coefficients for Q
for i = 1 : itn
    Q(i,k) = Qi(itn-i+2,k); % Decreasing order
end % for
for i = itn : -1 : 1
    A(i,k+1) = Q(i,k);
end % for
itn = itn - 1; % Update for the order of Qn-1

disp('Qn-1 = ')
disp(Q)

```

N =

1.0000

Qn-1 =

1.0000

-14.0000

71.0000

-154.0000

120.0000

N =

2.0000

Qn-1 =

1.0000 1.0000

-14.0000 -12.0000

71.0000 47.0000

-154.0000 -60.0000

120.0000 0

N =

3.0000

Qn-1 =

1.0000 1.0000 1.0000

-14.0000 -12.0000 -9.0000

71.0000 47.0000 20.0000

-154.0000 -60.0000 0

120.0000 0 0

```

end % for

```

Coefficients of the quadratic equation

```

P2 = [A(1,k+1);A(2,k+1);A(3,k+1)];
x = solveqe(P2)

```

x =

5.0000
4.0000

```
elseif o == 2
    k = 2;
    x = solveqe(A)
elseif o == 1
    k = 1;
    [roots,it,success] = newton_approx(F,x0,maxit,tol)
end % if
```