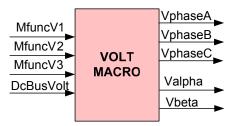
# Description

This software module calculates three phase voltages impressing to the 3-ph electric motor (i.e., induction or synchronous motor) by using the conventional voltage-source inverter. Three phase voltages can be reconstructed from the DC-bus voltage and three switching functions of the upper power switching devices in the inverter. In addition, this software module also includes the clarke transformation changing from three phase voltages into two stationary dq-axis phase voltages.



**Availability** 

This IQ module is available in one interface format:

1) The C interface version

**Module Properties** 

Type: Target Independent, Application Dependent

Target Devices: 28x Fixed and Floating Point devices

C Version File Names: volt\_calc.h

IQmath library files for C: IQmathLib.h, IQmath.lib

### C Interface

### **Object Definition**

The structure of PHASEVOLTAGE object is defined by following structure definition

```
typedef struct { _iq DcBusVolt;
                                     // Input: DC-bus voltage
               _iq MfuncV1;
                                     // Input: Modulation voltage phase A
                _iq MfuncV2;
                                     // Input: Modulation voltage phase B
                                     // Input: Modulation voltage phase C
                iq MfuncV3;
                Uint32 OutOfPhase; // Parameter: Out of Phase adjustment (0 or 1)
                _iq VphaseA;
                                     // Output: Phase voltage phase A
                                     // Output: Phase voltage phase B
                _iq VphaseB;
                                     // Output: Phase voltage phase C
                _iq VphaseC;
                                     // Output: Stationary d-axis phase voltage
                iq Valpha;
                iq Vbeta;
                                     // Output: Stationary q-axis phase voltage
              } PHASEVOLTAGE;
```

typedef PHASEVOLTAGE \* PHASEVOLTAGE\_handle;

Item	Name	Description	Format <sup>*</sup>	Range(Hex)
Inputs	DcBusVolt	DC-bus voltage	GLOBAL_Q	80000000-7FFFFFF
	MfuncV1	Switching function of upper switching device 1	GLOBAL_Q	80000000-7FFFFFF
	MfuncV2	Switching function of upper switching device 2	GLOBAL_Q	80000000-7FFFFFF
	MfuncV3	Switching function of upper switching device 3	GLOBAL_Q	80000000-7FFFFFF
Outputs	VphaseA	Line-neutral phase voltage A	GLOBAL_Q	80000000-7FFFFFF
	VphaseA	Line-neutral phase voltage A	GLOBAL_Q	80000000-7FFFFFF
	VphaseA	Line-neutral phase voltage A	GLOBAL_Q	80000000-7FFFFFF
	Valpha	Stationary d-axis phase voltage	GLOBAL_Q	80000000-7FFFFFF
	Vbeta	Stationary q-axis phase voltage	GLOBAL_Q	80000000-7FFFFFF

GLOBAL Q valued between 1 and 30 is defined in the IQmathLib.h header file.

# **Special Constants and Data types**

#### **PHASEVOLTAGE**

The module definition is created as a data type. This makes it convenient to instance an interface to phase voltage reconstruction. To create multiple instances of the module simply declare variables of type PHASEVOLTAGE.

# PHASEVOLTAGE\_handle

User defined Data type of pointer to PHASEVOLTAGE module

# PHASEVOLTAGE\_DEFAULTS

Structure symbolic constant to initialize PHASEVOLTAGE module. This provides the initial values to the terminal variables as well as method pointers.

# Methods

### VOLT\_MACRO (PHASEVOLTAGE\_handle);

This definition implements one method viz., the phase voltage reconstruction computation macro. The input argument to this macro is the module handle.

### Module Usage

#### Instantiation

The following example instances two PHASEVOLTAGE objects PHASEVOLTAGE volt1, volt2;

### Initialization

To Instance pre-initialized objects
PHASEVOLTAGE volt1 = PHASEVOLTAGE\_DEFAULTS;
PHASEVOLTAGE volt2 = PHASEVOLTAGE\_DEFAULTS;

## Invoking the computation macro

```
VOLT_MACRO(volt1);
VOLT_MACRO(volt2);
```

### Example

The following pseudo code provides the information about the module usage.

```
main()
{
}
void interrupt periodic interrupt isr()
        volt1.DcBusVolt = dc volt1;
                                               // Pass inputs to volt1
        volt1.MfuncV1 = M1_1;
                                               // Pass inputs to volt1
        volt1.MfuncV2 = M2 1;
                                               // Pass inputs to volt1
        volt1.MfuncV3 = M3 1;
                                               // Pass inputs to volt1
        volt2.DcBusVolt = dc volt2;
                                               // Pass inputs to volt2
        volt2.MfuncV1 = M1_2;
                                               // Pass inputs to volt2
        volt2.MfuncV2 = M2 2;
                                               // Pass inputs to volt2
        volt2.MfuncV3 = M3_2;
                                               // Pass inputs to volt2
        VOLT_MACRO(volt1);
                                                // Call compute macro for volt1
        VOLT_MACRO(volt2);
                                                // Call compute macro for volt2
                                                // Access the outputs of volt1
        Vd1 = volt1.Valpha;
        Vq1 = volt1.Vbeta;
                                                // Access the outputs of volt1
        Vd2 = volt2.Valpha;
                                                // Access the outputs of volt2
        Vq2 = volt2.Vbeta;
                                                // Access the outputs of volt2
}
```

# **Technical Background**

The phase voltage of a general 3-ph motor ( $V_{an}$ ,  $V_{bn}$ , and  $V_{cn}$ ) can be calculated from the DC-bus voltage ( $V_{dc}$ ) and three upper switching functions of inverter ( $S_1$ ,  $S_2$ , and  $S_3$ ). The 3-ph windings of motor are connected as the Y connection without a neutral return path (or 3-ph, 3-wire system). The overall system can be shown in Figure 1.

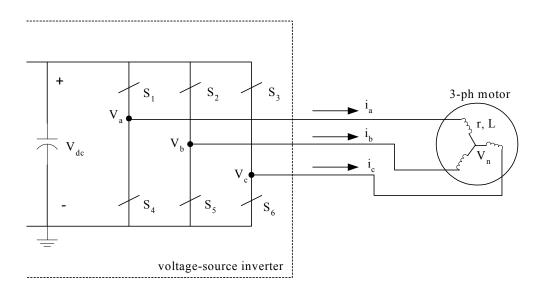


Figure 1: Voltage-source inverter with a 3-ph electric motor

Each phase of the motor is simply modeled as a series impedance of resistance and inductance (r, L) and back emf ( $e_a$ ,  $e_b$ ,  $e_c$ ). Thus, three phase voltages can be computed as

$$V_{an} = V_a - V_n = i_a r + L \frac{di_a}{dt} + e_a$$
 (1)

$$V_{bn} = V_b - V_n = i_b r + L \frac{di_b}{dt} + e_b$$
 (2)

$$V_{cn} = V_{c} - V_{n} = i_{c}r + L\frac{di_{c}}{dt} + e_{c}$$
 (3)

Summing these three phase voltages, yields

$$V_{a} + V_{b} + V_{c} - 3V_{n} = (i_{a} + i_{b} + i_{c})r + L\frac{d(i_{a} + i_{b} + i_{c})}{dt} + e_{a} + e_{b} + e_{c}$$
 (4)

Without a neutral return path, according to KCL, i.e.,  $i_a+i_b+i_c=0$ , and the back emfs are balanced and symmetrical due to the 3-ph winding structures, i.e.,  $e_a+e_b+e_c=0$ , so (4) becomes

$$V_{an} + V_{bn} + V_{cn} = 0 ag{5}$$

Furthermore, the neutral voltage can be simply derived from (4)-(5) as

$$V_{n} = \frac{1}{3} (V_{a} + V_{b} + V_{c})$$
 (6)

Now three phase voltages can be calculated as

$$V_{an} = V_{a} - \frac{1}{3} (V_{a} + V_{b} + V_{c}) = \frac{2}{3} V_{a} - \frac{1}{3} V_{b} - \frac{1}{3} V_{c}$$
 (7)

$$V_{bn} = V_b - \frac{1}{3} (V_a + V_b + V_c) = \frac{2}{3} V_b - \frac{1}{3} V_a - \frac{1}{3} V_c$$
 (8)

$$V_{cn} = V_{c} - \frac{1}{3} (V_{a} + V_{b} + V_{c}) = \frac{2}{3} V_{c} - \frac{1}{3} V_{a} - \frac{1}{3} V_{b}$$
 (9)

Three voltages  $V_a$ ,  $V_b$ ,  $V_c$  are related to the DC-bus voltage ( $V_{dc}$ ) and three upper switching functions ( $S_1$ ,  $S_2$ ,  $S_3$ ) as the following relation.

$$V_{a} = S_{1}V_{dc} \tag{10}$$

$$V_{b} = S_{2}V_{dc} \tag{11}$$

$$V_c = S_3 V_{dc} \tag{12}$$

where 
$$S_1$$
,  $S_2$ ,  $S_3$  = either 0 or 1, and  $S_4$  = 1- $S_1$ ,  $S_5$  = 1- $S_2$ , and  $S_6$  = 1- $S_3$ . (13)

As a result, three phase voltages in (7)-(9) can also be expressed in terms of DC-bus voltage and three upper switching functions as follows:

$$V_{an} = V_{dc} \left( \frac{2}{3} S_1 - \frac{1}{3} S_2 - \frac{1}{3} S_3 \right)$$
 (14)

$$V_{bn} = V_{dc} \left( \frac{2}{3} S_2 - \frac{1}{3} S_1 - \frac{1}{3} S_3 \right)$$
 (15)

$$V_{cn} = V_{dc} \left( \frac{2}{3} S_3 - \frac{1}{3} S_1 - \frac{1}{3} S_2 \right)$$
 (16)

It is emphasized that the  $S_1$ ,  $S_2$ , and  $S_3$  are defined as the upper switching functions. If the lower switching functions are available instead, then the out-of-phase correction of switching functions is required in order to get the upper switching functions as easily computed from equation (13).

Next the clarke transformation changing from three phase voltages ( $V_{an}$ ,  $V_{bn}$ , and  $V_{cn}$ ) to the stationary dq-axis phase voltages ( $V_{ds}^{s}$ , and  $V_{qs}^{s}$ ) are applied by using the following relationship. Because of the balanced system (5),  $V_{cn}$  is not used in clarke transformation.

$$V_{ds}^{s} = V_{an} \tag{17}$$

$$V_{qs}^{s} = \frac{1}{\sqrt{3}} (V_{an} + 2V_{bn})$$
 (18)

Figure 2 depicts the abc-axis and stationary dq-axis components for the stator voltages of motor. Notice that the notation of the stationary dq-axis is sometimes used as the stationary  $\alpha\beta$ -axis, accordingly.

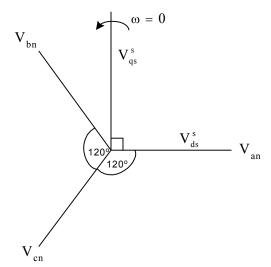


Figure 2: The abc-axis and stationary dq-axis components of the stator phase voltages

Next, Table 1 shows the correspondence of notations between variables used here and variables used in the program (i.e., volt\_calc.c, volt\_calc.h). The software module requires that both input and output variables are in per unit values.

	Equation Variables	Program Variables
Inputs	S <sub>1</sub>	MfuncV1
	$S_2$	MfuncV2
	$S_3$	MfuncV3
	$V_{dc}$	DcBusVolt
Outputs	$V_{an}$	VphaseA
	$V_{bn}$	VphaseB
	$V_{cn}$	VphaseC
	$V_{ m ds}^{ m s}$	Valpha
	$V_{qs}^s$	Vbeta

Table 1: Correspondence of notations