U-Prove Recommended Parameters Profile V1.1

Revision 3

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Summary

This document defines recommended group descriptions and generator values for use in the U-Prove cryptographic protocols defined in [UPCS].

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1 Introduction

The Issuer parameters defined in U-Prove Cryptographic Specification V1.1 [UPCS] contain a group description $desc(G_q)$ and Issuer generators $(g_1, ..., g_n, g_t)$. When a Device is used, a device generator g_d is also needed. These values can be shared by many Issuers; however, it is desirable to have proof that these values have been generated at random.

This document defines recommended values for different key sizes and up to 50 Issuer generators for the elliptic curve group construction.

Each recommended set of parameters is identified by a OID name that can be referenced by implementations.

2 Elliptic curve construction parameters

The following sections define recommended group descriptions (p, a, b, g, q, 1), Issuer generators $(g_1, \ldots, g_{50}, g_t)$, and Device generator g_d for the elliptic curve construction variant of the protocols and for different key sizes. Supported elliptic curves are prime curves "P-256", "P-384", and "P-521" defined in [FIPS186-3].

The Issuer generators $(g_1, \dots, g_{50}, g_t)$, and Device generator g_d were generated using the procedure defined in Figure 7 of [UPCS], using the corresponding curve and SHA-256 as the hash algorithm. The input parameter context is the UTF8 representation of the concatenation of the string "U-Prove Recommended Parameters Profile" with the associate curve name ("P-256", "P-384", or "P-521"), and the input parameter index depends on the generator, as illustrated by the following table.

Generator	Index
g_i for $1 \le i \le 20$	i
g_t	255
g_d	254

2.1 P-256

2.1.1 Naming

The set of P-256 parameters are referred to as OID: "1.3.6.1.4.1.311.75.1.2.1".

2.1.2 Group description

These parameters come from the P-256 curve defined in [FIPS186-3].

2.1.3 Issuer generators

g_1	x	f1b986d5d11f43483ae736e886af750e870d7f0c2312aad8db5c8a3e34f5391e
	у	64347b7f493187a53b370894b8f8e38fd22cb99302393d79dce225918eba61ee
g_2	x	1554cf983e0b060c78705ed7d14a4941b02e608cdb78f6a75a52345978141fd3
	y	62540e690c8fa9fe107e2141dfc6907f74f5feebdf5b12d7153b4635a2df6a76
g_3	x	32791a779e9aa475ba2666a0e47a928b21ab1905faaf48bb8062bae9009eb27d
	y	1874ba86ea194fb14dcce9fa22366f4735caea2119beb63f2baec19a9e93a545
g_4	x	c0efadb5c3015e42c1d71ac390c4d22a6f5d552f63bbcc59190aea6aee16354a
	ν	53f0133ea44da20c509a4e5be9b027dbe13e3a60439dbe72084b0c75a049723f

	1. 1F 600 16CC40402 660C - C-1 40 - 1: 0 - F 6C14C0700 11: 7F 600 - 6401: 60C - 0C0 1 - 0FF
х	bd5f29df6640493ff96c6cbc49cb8e5f61462792db75f20ef49bf86e260dc955
У	204c440ef8c6eb2bec0c343ace9c6d64e188c8b4f0613d64846adbdc3d8fdfad
x	d91abda26ec5c3001cf1ca2c09ad88662558426dc3b4d1b501e7abc2db080cdc
у	54ebb17fed855a36c1f74ab8256208e86307a9f2b756d7c84b4fb9485e0ff5f5
x	86eb2c94e2b6d620a391b4080dfe2b377cc20d981b5bc0cca94e865697959ebe
y	26ac1589c52880c3b8f81d2bf32976636019f16d8efa1f4d20950b9908ceb7e1
x	5553148e44252692d9e7ea9c189469dd2c0e8bd449405b6f3b1f279245b37f0d
y	790ca4ce90e048a7425b662a631612d0224f208e4be6e907c3e7d9607a997f6d
x	77668d97bff7d5da695d6d72e4f840205de289ce8ff1e9952435b0b4dd4e222e
y	1476060b33fe636bb9b75f10785d4b431905cd006f832bf73103b9f880378556
x	729a72be8375888f67df96d2a52e1b384af1c68ff8b73cadf6296c72c2c1fab2
y	13120e6942d0740a25f8b871e1f2fe9a8604977d1daa18af0e4fed570c6ea2e
x	cfba014ef2734bb0d51863a1e6ae8eb4ae189f8c19432af46d9f16fdd43fbc18
y	1256c784f827c31ad23d8d233678ce2eebce344629e7a5f7a6d94adc0ff47a7e
x	6c1407c49a51f67625eb8b2995ac11944288995b3a81789a5eb3e6bf4f2ded78
y	16d872494fc18d77404f906e58902150e1fcdda0cf211516f6f19415e8892f26
x	d9231c315baf722469f74fba55ba661777e91ca6320a8825bda1cbf0ea206092
y	36e4cd1288088deceea8e7b6d22cfd97b99f87facc95f1891fc6a28bd81e5f50
x	35358711384106b862a2cf0b403e8055920c7598bfb49987a89c3569e5a05b61
y	18edfa1dfc653a0574ca88fdaaecdfe9eb75309aacbe926c2110e92678c84e3d
x	25d05c261772166c08483d00003f443520e91324cbe918fc34008a932716d7eb
y	668a13c5d163f6646bf2e8f42d1f48e79a9ead020922b383006b676d29d35a42
x	fc035c85aa0e9c527ea7dca26a2db74dc250e8a5abe853bbded15959d7230f43
y	65f052a382b2c78caa9fcfc952096f4ccc4772546e5798649123fef94ec95acc
x	85b3873fd911bf06a978fa40e261e1c856f638ca9ec8cbe8826a6082c8452d0f
y	3cf00d69586f56bed849d5e9e2825a003ce562aab5f81bd718a4e941989e1101
x	4549f8c621eaba57ed2336d51920f6fc4dc34e047db134c61980e4e358c5e324
y	39e8be23f04033a0f8bc43d5a11b1e798d25b5c75d740efd309985edc5dedb98
x	b8ad386b54f9766e5cb1a2f050cbca2a22619ba008fdf9496df38a6cea784eb2
y	5b333a0cde9ddc8d6571b1cac456a47144c9c16ece866a538494ea0feaeef0ac
x	56628c7d6366e1c4a9361e5f7e49415c80fda14c04f106f0638ec8cf59aa0485
у	74fdc260802b6df55a640233889535cd04e0df84b66d9da4645da31193995046
x	8f1f5a0e342e6557b955355438608db09e4d237ec7230e2c836bd5f3e91c6c12
y	2c1a2102a69ef74a006353c2d2d1dd9dbdfab007fd08e7c88eb869a0a669b1
	x y x y x y x y x y x y x y x y x y x y

g_{22}	x	beaf7757a3ce43dc8d4a0732e1e318f49755e61e5f57a85beccf21b7dcc818e2
	y	40d26c2adc3f41d09156025a9dc34fd3ca6b96809d3d7cf5f28d00a1edbd6995
g_{23}	x	e513c3e50efa4436199c5a51fd691ea4dcabbc202a8029ba3df0336f12d82663
	y	75f42f58480d2cad569b0f13cbf376c3913271d9f7844242b870519d2be8398e
g_{24}	x	b42b3b05bcafbb72800ee242ab4cb7abd77f1fceac7ce1d327eec25b3de6c43d
	y	725f5b3d0cdd1b86bd7a8bd635c1acedbac91d6c35163eae66810751f4d46288
g_{25}	x	c8a4a7df6bef6c61ef50bffd9cfa7efde22530f0b2d0371e819b80e885d592dd
	y	196e7e0a81d03b38a8f99104812f64784b62d41991f566de27847b6bb9baa251
g_{26}	x	a22af45e5a7a9a9f94910e8cdb5e649e83c38fc1369f1ca9fa1d51887c38ddf1
	y	759bd38c6e09fe2cd75b4f355f4420e2e7b2dfd9f7147aa03d5373b3612b8389
g_{27}	x	22f47a6aaec142359481eea49098882b3ecac4625b1d2562b0271848762c5dde
	y	3e0b7e0c51a063303580ca25e326ae7e61086ea6e4c495d25162867039d9fe4c
g_{28}	x	eae24e9cbf4a8eb92c1cc80d75dcf44c39dfe4edcf13c3e5e4b7ba08c329378d
	y	2f7ffffa43a2d0268c25e4f08663fef26c57962fd5f623292f061ea19c5710a1
g_{29}	x	ad92b098528ae208572474e3ca2b1f6fbe133cb4fab5eeba0e46100c684d5bbc
	y	47978685fa8f41ca5246bd6347ba65f670ec65a136166c75e7936346e16ad790
g_{30}	x	dc5abc9d9e2a04a7ba38346e827119f50fa311b8cb4b12cf53602f3482a609c0
	y	e94f73d5d9641942188fd0ff64a7751021faf6cc9c4d2aa0318e94f05978be
g_{31}	x	5d008b9bdebb3824935bdc68a7ac426c554058a9dc4ed8bea2ea74a92df47fc3
	y	1805d5f8f097ea8b3b8608dc5f016fd909781b75900d53ce8b65846518ca0bda
g_{32}	x	4bff16067e37798ff3e3242b11be39f83dd7451ebe1101eac4887a6f93d50206
	y	65e5e31e150136036e1922549b9fd9a855997129f4566d3f5acf8a1e4d0ac83
g_{33}	x	aecba7f0745123d9c6a60e9bd461a8636131b095f59617849d335d2a7d8b187b
	y	5f62d5eaf4a9a892488c0de95d8d85eda9035b6597ea2674d7a7ee7d4a535ebd
g_{34}	x	a74ecb80732496e8f6ce72f4556937c237e19efac7567c151f386b650656a226
	y	4f661415313284d904485e6f6db8fe94782b2ba24c0cba6ca77557efcd8f05e
g_{35}	x	ed0e965669017aa71f342ec8a099bbf01a0b9eab94f62623ecf96bcc0e14e4ab
	y	244bf125523ef2978db06006cda7cf3e4d58397711d92897603dbae29b82864b
g_{36}	x	69b843bdbf017d416a767d134e1c2d497fad2cdaae36b275370ff512a34bfa7
	y	3d3be3d2e86eb07a87849b2ef16ee30310b86e63b3478163fd06b6592bbde545
g_{37}	x	592d48158a6358a2900d453d79e88d6bc20b7fa8cb2bfcfcdfd082960525ad83
	y	7231c3d1f86fcc1b6c9e8c16ae45a93508c9c49e8a745e64b07636fc6b03103f
g_{38}	x	18ffac7507b8f022eba9722aea93c6ca7470825a787c1f982b083dda0490ed32
	y	304b83604a94ff8a2787b047e823e50a64edca0b1dccb9381196597a1c63b362

dde5dfc2867a61ba2e046dd52576d3d33a24173e32d716caf0d6bc4bd1194374 \boldsymbol{x} g_{39} 79b6e30b1822d61eade59b0ab3edbe8f4291c8e081ddcedeff00bc32ebfc1a93 ν e0f72a8c71395e19063b0e09f947f86c06f4b300c81d3bbbc48dcb219ab960aa g_{40} 6f231e0a538c8f54c066c93e1af857bc3b1c418802274cbdf5e387d88736f576 γ 385388078ea2b4792dac8fbe0b4748b99800ca086662fa8eabd62596dd7e5c53 g_{41} 4d2112111d5bf47baed1c4a2688cfa616e7bbb64d412f16b371288bfe957ea61 y b108aa3e8bf1f707f6ba9556aa0f1871519734a698203f7532925443b2020cbd χ g_{42} 5a75fae7ad0be23520734779ef11f325dde7a6edc63336ef9fb58661fccc46a5 y 605b3505f77e74b22ea7e67c3333ff3b7b771738389d305aa594d8f550237db g_{43} x7487adb2e07c3ab92e1386546790a011497eb9fb9846716b04793dcea430c7ab d81883a9cf1dc3043c44f9f0f9ff502cd045e4294c375a30a8a65abc0dd28264 g_{44} 1d75c99eb44e2d8b43a53f69b6881f96929435e2b3850a3701aed026e80a3291 93ec90879cd2d86a2276f44b42df736283d297470759de0af2c6c92f168482af g_{45} \boldsymbol{x} 1f45f480a0ec7607516679c2bb9f677a89d450ec469ac930a10d213c1eb2a9cf y 4e9e9eb8e267c0d61760ecabc9ac19ddac5db95c28334ec99d49d74d40b66daf g_{46} \boldsymbol{x} 5dd71c92d311ec15d5e2e6d3b8d51336415a608e14048c86ceec764e6de6df49 ν ceb4ca98f62019596b9bc6234ea5c2029990f08d068f27eef4fa7d9897bfaf62 g_{47} 4160fbddaf2986f3a11e29b589b9d91d8b15c5f8bbf02f7f175f6ef8e7c2b1a4 ν 80e8706709bd25a84937417e2d6a6dafa83d3738dfb42f8eefa0fb5247d69985 \boldsymbol{x} g_{48} 6a8f2ea6b2301e3aefbd8246f6eb97ea0ce1155ce0b72c471d01b0d0b88da2ca 13bd26060667f8eb7e56e782854af3b3e010cf1825a684bc72b287ea7b2c234c g_{49} 1871c15aa6f8cc3ada2d4bf6bb2bc6296ca6587c122df3b47a9faa3025863a8c 7d5e69bace920e8ed2d0b43ad14849d71e26729cb37f009ae14e6d8a065e9079 g_{50} 13d6c8d6ae0273a1890129779fce34f0caf6f353bfde9ee337278678c9b6e758 e2ab81def593e999c975a8a48668b9a07e5594cfd68fac29f17a811cb26b3e10 g_t X. 756311f896c503ecdb2f608a1ccbfa378a95eb4578e65f190f1a8b544d20b082

2.1.4 Device generators

 g_d x 4ca625118d0a05d04d275dae1ff096361ebeba345c31270982f796639b1ca574 v 142d150c855ba9aa7dcc71821a538edb544836df8050912679ccd7233fbba636

2.2 P-384

2.2.1 Naming

The set of P-384 parameters are referred to as OID: "1.3.6.1.4.1.311.75.1.2.2".

2.2.2 Group description

These parameters come from the P-384 curve defined in [FIPS186-3].

- b b3312fa7e23ee7e4988e056be3f82d19181d9c6efe8141120314088f5013875ac6 56398d8a2ed19d2a85c8edd3ec2aef
- g.x aa87ca22be8b05378eb1c71ef320ad746e1d3b628ba79b9859f741e082542a3855
 02f25dbf55296c3a545e3872760ab7
- g.y 3617de4a96262c6f5d9e98bf9292dc29f8f41dbd289a147ce9da3113b5f0b8c00a 60b1ce1d7e819d7a431d7c90ea0e5f
- h 1

2.2.3 Issuer generators

- g_1 x 4aae579dd56d78090b9921f31bf729f074121a3adffa2d31d01215beee1dc4df9df463fd 5e2b8f6c6b0a4216258ac844
 - y 3c3b8a23c5d66aa2f0964521190a9281451e9ae3ace4b7376e02d7b3949e2274e8448cad ef7e51991720b49a45b05805
- g₂ x 32f086eac7beb55a0c95e5ad996e39dde74b3b66dfbc2b8f12529d9df4a2cb84aa54ce69 ab1fb22cd7fd79967d261c2
 - y 16bbf078654e391680bdb57495018cc8fe05130abfdaa84ab4af90d0d2d6c01ffda8bc96 cfcb0016f3db13d80ae8a2d0
- g_3 χ d6583afe48311bec5c9016682531c935cf3fa98e33d503354820c99fb2e902eacdb41944 1203e287b0d33adbbe912e33
 - y 7f9e35c0c0daf2e68ed135ebc07971d58e0e6ac8da69f54f0c093e24dd3f62751e816b6f 6e1fcb66226c4f0b35f9acdc
- $g_4 \qquad x \qquad \text{3ef851b6e0a84e24fc999b053cf6acf32adc941784aef0de14823ef7abbe7e7e49e7d80cd35295eadf332265d4da165f}$
 - y 182899d34652626c7474989366b1f17ad4d9c812863a67bcdf7d85c0ed59cb7320663ebb 8fff3d5f5632e0a75e009966
- $g_5 \qquad x \qquad \texttt{b8344031a958a374de8ee0711c15554404bfedca80e4889922bdb0cebad3a30c922f5492} \\ \qquad \qquad \texttt{d2ce4884ba1c77b572fa0bd}$
 - y d7d707cec2ecbced76f32d43ce7b55cbd53273f55605b7b9bac8b3f521bb1539686967be 18b5aa41a7165f726ab5dbb
- $g_6 \qquad x \qquad {\tt d8651982f1cfab267270219aee250736d535c289a38c885df28eebf60f763a12a16620ac} \\ \qquad {\tt c595697308eed1db05acd4f0}$
 - y 2fc43a11b828c8546ab8c1c6aeb41a6857c481590417b659ac8bd3ee53c70fd3f7aa13f0
 6570168823affce84a5e861d

- g_7 x e42bc176e13bdecf2b316018a22cf95102b71a1fa8ac1cfe14eec54cad256a9ab9b4a7a8 ef3cfde3384fe4a1bc11c2f4
 - y 4e26002735c92697877057256038e7934c1d428126f41e771b190840dbac0f59bd5e0702 2522b638a2933e146339dcc6
- - y 5dc9800ad0eda033abe134ddd894f296b5aebd4458ee4254ce70f84dfb0de18fca99bf79 5ca7e208182ef6c46d7bd494
- g₉ x 68872b164a6e9b8f99668b5bfd4ac0770dea64e37732a384bc39c32484b86091cd47ddea e526b18065e8663e1ecb8b80
 - y 66608aa7cf0ab53c375034dde39736dc81d6831bc6ee78c714e010afa5c85425a7ed28ef 6f462aeb4d7952eaf488d0c1
- g_{10} x a04decc7e9f0cf88930ab26c96d6952376b4c3a3db75256efdd466f51f7c01841a5f4e6a 9f11877ff286cbc74306bbf1
 - y 18c80928ac2082c04f300d31b2e6d00ee687725eb86f0dc7c7a8fb95993ceaca8afce480 edc727842efed148882dbaa6
- $g_{11} \quad x \quad \texttt{e9802ce5361dd79eb14f004d1e2a7dab4ca55862b937593c86035fce0d3a49c1a1347e9d} \\ \quad 89\texttt{e9348bf8460fe64668aae7}$
 - y 29992900811b12c42efde123cf65b80bb249e48e3f53e44775cb1b36536e286b23e08d4c
 59f50ddd89b9db4e012a4f14
- - y 75c3be295e38813b2722bcfcbad491c62bd81a1438864d8f54a48a438a6a556c5cc6bd95 49c25ce7e39d9861a30b6e08
- $g_{13} \quad \textit{x} \quad \texttt{e46be8ffb1a61277574b4d4e7520bb28df1aa92b75390bf6aa819884a47db67e0a5a3f75} \\ \quad \texttt{4cef6dc57d0725c796806d85}$
 - y 1e0cfbc5092582f702002fac85dd2f32ef568e009801c3d79611aa3aa0eebf2d55910114
 4512fb2c1a597f3f0b05f543
- - y 6d9b50e848246f310b92f01835d53dbee8e27f883aa6d2549e527fe7808a9cb61923175a 8eecd3328574a3ed7bb59ba
- g₁₅ x 388a6cb55c5d08bcead8211cfd20e32c78eb6f06d792101a00c0d757480046f9c4aa5df8 82176bbc8d831f72814a790c
 - y 427b8985182f9036019d28325619b9ca944275082bd2fd198500c17c9bb8ae7d591efd64 e18070c4cf3164e0926dfdcd
- g₁₆ x f30fbeec912971dbaad5ed633b5b2a376ae60e2786af169695af00f6da9bbcfd9a435640 97c90225c54e2a63b9c0004f
 - y 31feb5903cb5679fe9686f17303e8bcf8335fa07f6fde06b7062e2d337f72c7aa1adee5f bf5cb3742844f07e02fd476d
- $g_{17} \quad x \quad \texttt{bc}56187\texttt{e}62\texttt{b}3\texttt{a}3\texttt{c}246\texttt{d}601\texttt{d}86885\texttt{c}34\texttt{d}54\texttt{f}61424\texttt{a}\texttt{b}\texttt{d}1\texttt{d}227\texttt{b}033\texttt{f}06\texttt{e}\texttt{c}\texttt{c}\texttt{e}\texttt{c}6278\texttt{d}\texttt{c}0759\texttt{a}} \\ \quad 16\texttt{d}90\texttt{f}0\texttt{c}\texttt{c}51616\texttt{c}50\texttt{e}9\texttt{a}8845$

- y 3a532cd74d1f73dc02befd8b002db362eb133b3d9ccec54529f15d7302da1d8b4c7b3665
 4e4f8d2a3e4da5eb9b29a7e2
- g_{18} x 899772126f9838ec178961507caed8258b6f102f5a7708babf80dd1dccdc70021e4f41c2 f7438beb67c9a2a9b4d57f84
 - y 71b9a6fdb91ebd0a292bdb718377308ededa063d07cb034e1bc86ea2f65fa20f0935c6c8 c378caeefe64ddbb3adc79ed
- g_{19} x cb2ebf807f1e6fe411df6898cdf652cbb9bddf3947355011429d111bb2618dc46defca46 9a09c19748cf1d09aa8219be
 - y 50238a8b2707cdb88c381d57369b4d7838d7895876f9a3d80a9556a5c797a4d0db8399fc d657add1938b65c7afad8a72
- - y 623d37c13dcb6ea9573372888af08beacf94c8dffc2cb615030ae612b0cf1478751dc3b5 6a66a51db4b98e264eb016dd
- $g_{21} \quad x \quad 22 \\ \text{f433020dc129c7be74558ef9c291f3938e7817b47d4b41a59221d85b10ffd1b815919fb3717e3e7e15e93fb97f6f7c}$
 - y 14454cae0eeccbcc8e521555fd2ec822c290c464671ea7aa99d558909fdcccf68e4d7095 c4647a16e47f16c0b68851c1
- - y 52b8498256516a4fefde13b5a7bbd72d3f19aa00b3626decdd9cd1ff7d175cf744e22416 f351f62e5d01be651ca82747
- $g_{23} \quad x \quad 451f77 {\rm cbcf22bee6a407287ef9a36f293fa822f395f64c2edccb9ab5f8ee3fde86efddcf} \\ 3302 {\rm e8e9293732a058332816}$
 - y 773401a10fe5069dbcc6870ceb8b15d1cb35227bd8af7d70b63d36e95613deba2d600383 5027493c04630edb2700b965
- $g_{24} \quad x \quad \text{a4ad50b7dbcfcdc427e72f850a1bb040281c5f99b914151c47ac48f9fb7b85a05858f303} \\ 588c57d2ff66b5867145fbdb$
 - y a564336b5e37aac39baa0878c6c50d3d36f5409f102f9b8687328094562ca6288b2b69fe e43891ad561d32ed4bb20f8
- $g_{25} \quad x \quad \text{f1b4f132b3c29a9e3467a0220817f2587843e77543e812ec524d7d413c6c20c03ec39b55} \\ 836220717ddd9af42affe667$
 - y 3447a1342d40a8c094060345102e64b1b3871b80ef28d32770f849b57e7696118f596b8b 119babdd2d7ccf27b55acd17
- $g_{26} \quad x \quad 970279c58147dd40d2aafebce3e0bc13ee4ddbb746909cce2849bed98d8b7b36ed971a17\\ a8e75cdb5f3ebdc3e71b47b$
 - y 2cc17acda096b56393de63c66b2342a03e2e504f12398001b8d90fe1581d2696bf864346 5854e0d9ade9ee2145f3c02f
- - y 242023567c670bcf21c9c2ef69bb8b87d7a8dcd034b66606900812393ee9989bc37e25ab 672a3ea4ef3b028f83495623

bdb8d7aa75f95c53a37cf960

- g₂₉ x 46e4d4bc6281d4943e0b5cead86eb8f5821bffd42888b579db7171c82416bcf863187d86 8155b4a0ae1f3e44cf7107af
 - y 1464246c54ca3a8b70da3da93ffd8866336e7abada509d39276d085a9c9dd55c04ffdef0 c5ec06983aab0e63fc1186fd
- - y 47ec98d318f871cb6fe491bfdaf261d862ac92ea5d269b941875e636dc5ce2cc7466908a 60af479aa2c70f94ba0ad303
- $g_{31} \quad \textit{x} \quad \texttt{bd425497219e2bca3b47629b19f79d4dcb276284b45c3f5ac9b47b76b90ece9235655cf9} \\ \quad 57f77ada902dd175e494da91$
 - y 2980e0c8d44a32345211554bf1b7ac1edef0c5cc1a60d42ad4e19e9b9aaae4cf1fbca9eb 01e132df66f89857b9303008
- g₃₂ x 2a6c576df2af7b1405daade9fb24bbfeb3fa9c5586036088e07d9dbd3155e9a96922aee1 85f731579c7d8cd1a7a344e4
 - y 44916fe5da07e5adfef1837d5d3fc2aeddd5b05b9cd9d40715fea44211486d82ce95a272
 96b5ab3a901f63d501f2b1f7
- $g_{33} \quad x \quad \text{e7e5b42c722fb47bd92ca581c05aa00f1c18c0ff654939f19cccb6ed3c4df9f7b0a03bb4} \\ \quad 95c44cbbbce93f4895882637$
 - y 3092e32af39c40c24b5a11100be810329f05016f792faf50876f77f4f561f18766b01da4
 4fb2e54e84946f2a3c9670b0
- $g_{34} \hspace{0.5cm} \textit{x} \hspace{0.5cm} \texttt{a6959a68a6da7a468d0eef827492d3888af2811d0627c18aa909dd0ae4b020d133e48b91} \\ \texttt{1b377e05ccb77feeea326673}$
 - y 70edeb467c18d159474824dfbe59429b4fadc97cfe3f84986307b4ba50faf2c4b60d73f2 b395b595bb6ecdd96a4fe3e9
- $g_{35} \quad x \quad 9938127 \text{c}58 \text{e}f9 \text{e}fe69 \text{c}c43 \text{a}d758 \text{b}3 \text{a}f23 \text{b}ff \text{d}e84 \text{f}7182 \text{f}090095 \text{e}118834 \text{b}67087 \text{e}e706 \text{b}4}{6440323889253 \text{a}223 \text{e}\text{c}fc865}$
 - y 37f1c9424f0860e3ece2f8107800f6d86c909a9f44679c3557eceb4b5814b4b396bc8e9a 9a78bbeab7c1313f0a4be318
- g_{36} x 60eae169e138df4979ded509baceed03e6344910d36135ea6653eff55c076cfb54c1ee9b c0b5e8129c929fda643e82d9
 - y 65210212ca8521a0f9022063c3d81634a1b4649b02651987fce2a85e3faea6035bbfa25e
 4de47695d7ef0be7c65529f4
- g₃₇ x ab09b0485bd7eae24bf82acaf48cb3848a841fe3826ca2bfd91d2afedfbeef07a91d1d35 b7c422445315d74666a2dc5b
 - y 6be91029fed90132982e34f581b85cba8d699062b76578808693f134f203fa866a1fb2fa fc8777292bb5c62c130a9410
- $g_{38} \quad x \quad \text{ebca} \\ 9a02482d7455d0e6af492e611efc908c1fb851b58f331b2ab087a2d9b648f30f3f65} \\ 533f4c550975beb9168b0849$

- y 685df7b2c2757a5b5ba93d91286388f657b89bd12e36c8de9c95818aa4fd357b4c14df72 a2bc4136fd9476160aaf651c
- $g_{39} \quad x \quad \text{dab79fea35a2883a43c02852d28dc8b7a02d5f331cf1a5b961aa2b39a036756bfc80f51f} \\ \quad 945714209b0be881bb82c1b6$
 - y 4c2d063d405b4569aa6dc92926e3fb363b3fec762d0c6f0db267073cfe3f78baa2b8cb5d 7000bc8fdb281ff148e62676
- - y 768db9ae8de6a9d51b7325f17471ed6422b8977fbdfefefdeb0d5eb2879cf5b99de7a06b eef35d4d4b471e3dae96ae94
- g₄₁ x 5fc27113e10eb415118806869490569e9a42d4e3ceb227d8936dcea27cadb16a86fe6c11 6e60751afc5354f29f9824dd
 - y 1c7e890ea76ecafe28b6545a2005b5df5fc23918aa6d4c81f968108ff565fbee01882dee 44b23fb42427d8945f49f6f4
- $g_{42} \quad x \quad 19f736915014c121612ff0fbaa4479edba30840736d00f18d9c08cfe1770aee912b516f8 \\ 2a71f17625bc10d56ea75586$
 - y 1a5a311894e90d019fa154c68907068d1a2907e33fd683614fa02ce9e22d4cf40f9cb70f fa74388341e90635a2e260f4
- $g_{43} \quad \chi \quad \text{29763735c7f56bf6bd7a1b6a1f2f87bc7cd48592270af465970531d6d9fa9a299c4073c2} \\ \quad \text{ef5ed3f9605c7dd433b208bc}$
 - y 7484ff6532c7fb294ed4774a629aa2ebafd02b916ecd9184c134c739cd2a592a40984cd2 1a61c880067eef2c960b23a2
- g_{44} x 82ded039577f4e1db38722200adc9deee477c892948432ea0382f3d314dccbb8944718fb bf92c31a89a8c10daa778ab0
 - y 25810280fcf2809fb8e46ea5f75f9c8cd4ae3e560aafb5a0fe8bce7d8ac2811e713fdfca 7c2814841e64adc32bfb662d
- $g_{45} \quad x \quad \text{1b41502ecd20817d3c85e7004e669638c725d1158aa803d105abbf85955185598bd316fb} \\ \quad \text{bc1e9da4b0ab467e34172d41}$
 - y e3708f721dc69f92af811776fb1e2480251b204f5b1cdf4adaaed66b0698bd9fa66623c5 bf056bee34f8cba26944a7c
- $g_{46} \quad x \quad \text{4ae576a41641ac9cee68d76168ca2dd3a5a8a1c2d1b0382df8c4bf77008be3b22d16bfa9} \\ \quad \text{da4a5a1cd277a31369ad04fe}$
 - y 53c8ce7a42d2b8d5b94095931a005bd320593955e641b9d41102f81f34465ed967d69992 b7810e0b5368e11fa9bf4bc2
- g_{47} x e2ab8753b11ec352fbdc31819af1937c1d722d100b6d8a0a9dfeaf5bfe261f78801a0b80 a2028c767e5790cea94eca1d
 - y 4d7c71008a50d8b5f169d23d5821624f6879d3d6924218a94bbf8d69725770773aa87ee4
 cef01ce6e29435249117f6f
- - y c19cecb06a2dc7d0ae76ce2c450180525e3dd02b76d8097ed440bc8d94105e6b6ae57ccf 33c902a40c45fbcffd6069f

- - y 8af913bce60e84ea81c3d7aa637d4077e9a5cc4fa6a801dad9dea69a56cace6fa38b891e 3dfa07f2c6bfa45c480f42
- g_{50} x e51a94f1bb056052f468e2f21bbc5ad2f672ed3f837de089bd59a9c75a7bfb97fb87103f ff415fb194ee8b57f2dcdb25
 - y 1b5f770ebc9f6741f97d4e827bfd6acc592ace08107db26f3eb428ee18cd197e72b949e6 172545dfdee04645571a3dc7
- g_t x ae141e91578a2667f7b79061e0a0f5b9e459de3038c697753d2f7ee1c08a662316da0d04 c5d2115cfcbed003e51b8e38
 - y 4d4d60f7665183483c8bfb466c36bf1e14837a7753a0dd1dcc036d91af53c10cfe765ac6 190847d2f6683b78e1e09f0c

2.2.4 Device generators

- g_t χ ed14ac907cadcededdbb772a2c209604fad1b43bd85acf2df50e848bd9aa5b99b65b6a87 dbeac90f3301e8c9d45b037f
 - y 60448878dc34ae65673d982ef300a565ac0b46510bb962f1a00c459dc969e049add21121 0607db5a06f102505067f598

2.3 P-521

2.3.1 Naming

The set of P-521 parameters are referred to as OID: "1.3.6.1.4.1.311.75.1.2.3".

2.3.2 Group description

These parameters come from the P-521 curve defined in [FIPS186-3].

- b 51953eb9618e1c9a1f929a21a0b68540eea2da725b99b315f3b8b489918ef109e1
 56193951ec7e937b1652c0bd3bb1bf073573df883d2c34f1ef451fd46b503f00
- g.y 11839296a789a3bc0045c8a5fb42c7d1bd998f54449579b446817afbd17273e662 c97ee72995ef42640c550b9013fad0761353c7086a272c24088be94769fd16650
- h 1

2.3.3 Issuer generators

- - y c631e60abcbd970136201e5a8e4359f8cd3169cc396456b9a12d04317b3bee9aa27ac8fd 84e67a61934c63d1d95cd3f89003fdb57bfcbb71f811feb596daed7e3a
- g₂ x 1e565ee2801f3d822664777b08b43f2e50b60aa669eaf9870b37fe8f73773b8f92ebe0c0
 519f494bf938d55072dbea59395036e5c0ba68b885ad2abb47c6402b463
 - y 7233dbf746dd2c2bf62a860f36450caf295d88d395521d7356c960f65578fcc82c29d6c0 66f2c4a0f548f86cc1bc7ea12ea7d34ce241d198f954d98c4f667878bd
- g₃ x 163e41f82b9d756c774aa84a2089e7dab68a64454912d90e3cf37f9623fbd7c7402417f6
 6ae17519db4c6c698bd853dbfea2fd3ec78efe887d1bd887cddbba0bb06
 - y b0811bd82aca459f969cb5e4642e5b67b52dfc9674e2ba3d24ece862fe79ac513ef65e8c 9d3f73bb28c84f20d6b457c1941436e0f280bcd76123f7397af3a0fb8c
- $g_4 \qquad x \qquad \text{1bc68e0cccd3e2f0627589106246317fb73346feb916e2ca613c388254dd6f0f621a9a5f} \\ \qquad 56\text{cac25c353490f432e9dca76ef5a2ffb1851df892082c6d583f4eaa31}$
 - y 425abc21db658cb7d3325d7490d5372558f762001369250b8086e4d4970706eb4b51bf76
 c643aa57bfa3ce5f6b7831e8c167ff29e2c6958b5286bde4f5f320ebeb
- $g_5 \hspace{0.5cm} \textit{x} \hspace{0.5cm} 65110b80b2f3ba19ab7f5a6fbff5633bb6b3148563bd1a29ac1bb9d748800d4f28f04dee \\ \hspace{0.5cm} 10e88f86afbeab7e10fccff69903d33f7cbef6fddf651596782cd76c57$
 - y efa9bb04c1da53c5d9a7e9a26d33b641613cd37428475fdcf821948c4572db444f997f90
 7681f0c4662d8b08b52d04a109215436b0a3e48f00963b99c490e8fa39
- - y e87ebc535951ba18b9deffd808e97b337cc4ec0b2944aeaaecd34934510fee9606ec6ff2 8b4c49cc0bb6e8c50c2abdc952ae95f684027b15a10d64e76cc614f5e5
- - y 255ad2cf1440e31210f38fa70ffcdcf632e53fb8072fb0ea5ef11b6c590e0aa816163ba2 88148654bfb54b71a4e387d3c63e8e4c12f5479d4529f9fc0b2c9359f6
- g_8 x 1ffa438ff048ba539ceb37e2334eca04c82af7e9be210ce51572db53cb41e9b326b9a414 8a24991e6608fd753b2f34adfe13ab87e62dc8f077e5baef437f58f60d
 - y 9f70ff23a46618a34ba000e790544ba1bebb18f9f9974f7e1e0844a55b9a270183a1b6bb 905ba87681f9aa63cb39b57faac9bb933e9526b891b2109991c259fbc2
- $g_9 \qquad x \qquad 301 \text{cb} 6075 \text{d} 056 \text{bc} 65 \text{e} 6a \text{e} 301 \text{c} 076752 \text{e} 07 \text{e} f2 \text{d} 21 \text{f} 182 \text{ce} \text{d} \text{e} 42 \text{a} \text{b} 6f56 \text{f} 089 \text{d} \text{b} 5 \text{d} 50660 \text{f} 91 \\ 1a7f85797337a1a95056 \text{d} 4613 \text{ba} 75 \text{c} 7 \text{d} 69a5 \text{b} \text{c} \text{ba} \text{e} \text{c} 2362 \text{e} 94 \text{c} 65964565$
 - y 2dee2dcd02ae5e3d50340b3886db25c0536eadeb287d22ab8524fdf32d40d2019a9202f9 da8fa0792752dafa23a042c084f4d08ce0792f46003bf477f0a86cac85
- g_{10} x 407fc8e984c84601f3e41952fec161423017e073d33783ff05a50e0a11b94c4ebed0c8d7 671e5180f993b1e9d1e357d29177271eb29efb96cdef4edf9d8c6b7440
 - y 431df69b022004caf4c71ece51693202b510f40207e4856e94098215c01f55c19a0728c7 481cdfc24b2f80d1d229ecdac1f4d83e8c466cd3586f4e0d13ff25e988
- g₁₁ x 1dbac6be0860787def03ffc5472dc23fa06b15af01cbf8bee8f5a0e71ae28b5ecac96fda 82e8574741c219fa62d31afd658bb9578d59b279df0949063122665cfb3

- y 36da1a1fbfa65c4ee91d836c2f424ab2845cd6eb7962500665f745c7a83c4da99e07cf2f
 57d99e5769bfa70bdbde84ede562504b8e84b2c1e159f0dbb9eb58549b
- g_{12} x eda625de058340213a859df97481c06223337ab42e45599bb5431960d3b9c433d87e6df0 1bdc895a3c100cf5bd357e42d4cdbb9eeb47e1929802c20efc65e9e044
 - y c90a0efa16c0bb698e2b67b5bd498a02d8695c73f2626a96dd85371dc8d236af6f234293 d09622aa1058859b36961fd59f5e28cb480c202624bef43186fccd396e
- $g_{13} \hspace{0.5cm} \textit{x} \hspace{0.5cm} \texttt{5f8a499b93c10c49e1e29ac7ba42671fb46ae8d0320bacb5f018f450a5877c0c63656eed} \\ \hspace{0.5cm} \texttt{3c8043bfe12c9346a6ae1f81ddb90f96a0faef9def3a986becca856fd}$
 - y 63495d5eca21f270e3d599fef3492230eca64c712bb3100b14f4ae2b6218ab68355578ca
 73a26af4c802021f3a299c84d343aaef237c1ad20503532a468dbef9a5
- g_{14} x aa86fcd11cb4e5156021f511c2145df198d8fc07e437f7495604efd387100d6ac338934e 4307376feb1b9cd231f7e74e1ff768165189442d6a851858db44c3942f
 - y 46e345906c1fa961a70cec671fe984ad62926e26af0e49dbaf78081bd4c80af1426cb397 e9d414b7c2e83005be4ab1571f2843acd4834d160b38f4704c1c2d1a37
- - y d0fad9201e634b41f0b9fc7597b77b2fe487e12b83369fe7ff0b65abddac92a02deb1ac5 4c8d6e0f5e55258430ff618fd1cbf039490a03e26e61104d809de41e45
- $g_{16} \hspace{0.5cm} \chi \hspace{0.5cm} \text{1ecae8827a7b0947daa185e92900e5c5ef25dec1f0821b8a6974bda8192c07b3a3c6769a} \\ \hspace{0.5cm} \text{dfdb857c73c9674ead26a3b57a56fa6c15a4732c4bd63061e1cb8d72ea2}$
 - y 75d01f5d3b388a16546bc83efa7f97432fd0071ec7e59293232be9c6aa48d1ae5fa74ba0 dd8b99eb8409b54d6d811d164af43085ef860a3a27777c033624a8f669
- - y 44bb4ea0659a27e612ac00887949400fb8f41c9eb5daff89b5ee4ce979fa1d73b5eada1f 6037c8e016e44c1c8a4f9dc2af487cd92a19f450bd71bb4d723e9d04a9
- g_{18} x d7ea7e804529f3a0889feca632cc6907a24389bc0ba1ee0f648d52e0c0d91744359ca945 e0294204a9d8a9056cfc16a01384f43c7b0fe207f37a81ad158455831b
 - y 85fa66eede6d452d4c80fb9243bbbcd5500d7c37a87ac687a49ca020bbf00015acd5d427 b2e20e733a05849cc13d2c2045c5333d7ec10cc8f2a63f63fe781cbd42
- $g_{19} \quad \chi \quad \text{6ce87f9f5b5b6fa0fbc51c2e3a2011530bf216cc03cdea0c352733a0dab6efa7ff77efb2} \\ \quad 1698d6a2a30697e35b128c6ee2a02ebc946b7d01d6aef9c4381c12925f}$
 - y d6031016603250135e19f6bb8086b7519d223b083eb833f4eedb018c5a826ce2092925b6 8f8b3c825768b587e7400c57be2cbd5af2da4d9adbfdae09641f3eb6c2
- $g_{20} \quad x \quad 1074f1716 \text{ca} 10f00f49490c85f9c4be238ae3529ec6b2c49badcf} 702f90b4bccf915146fbcfa07cf20498677e82f47572bed9e2bb585468a9647df1aa65b10b4bee$
 - y e3735d881a471398c8554ecf7d25f5c87190c6de1a04b5c13ed168e2378691266fb98f5b d5f3360cb669cd9a4db32f42f602515a742dfec7ada842d595da6c6e3d
- - y 8437e93bf86dbd0eaba383ef307ddb98d27ae63e790338e85b2781680ab0bbfe17124785 68e12acedb976a8f38a255c870ac5f97f45141c097746377047927165

 g_{32}

126b1e605e3bae456c986addb6eba0f750229b3f971235ea827a2e16f45f3a938765af0a \boldsymbol{x} g_{22} 0812fa2af0199e2e1801679e43a1ef9421732595dba7e71d9f6d68c30cf fb8640e49a5fa09c4fcdf2c37611fc397f5f7b5991709cc6783b92885ee97984744451b5 y 33d5710c8b801d5e29ce2e373fc325f329a7502d503f423eb2a3a9d428 8094e94e1983a7611a0cd624d94cfa1b3c1e18ebd2767f4f4146c573df368281693ddfa5 g_{23} 26217a0d935d2256a526c80fe54180d63b44c5a3c44a528bb211d0d40b 2c57eeffc512d830eff90f8aa41f867157926ae53727b3651d296a6703878f96738fb308 f85cb1530b39ed24ccb60eaaef80aa22f1ca5e9ac794110ac6cd048da9 1ddc9a991f6180abefaae9351edce524db8b0d7e427c3eba58817a508396f2dbf6e1a754 g_{24} $\boldsymbol{\chi}$ 3627e05c3bbe65dfe40d0b33189401ef19ab1b16ff33bbc443a5fe547f9 fa05ccbe21e0bba18881dc662ab29f3d9c96110b2ab60fa5503221377acfb04851479a96 12dab994da5672571dc5c4393f75b2c84aab3fa6a0c4497f0e55b12cb2 1eb9035840630ac6fd0a30173a94793f7e81f34455e2e1a600fdec09bb6636163c6c4b24 g_{25} 175b56053e67c3e374d35739be31819cde7befc42ebc3aea0abdd03efc7 da5565b4f616dce18be9657f386f0c2792fcf0f602c6acf84fcbc976bb276d6d84977875 ν dc12f887654ac7c2873c3aeff1c0d45cddce4cd63328598a67b0b222bf 12a8c695c849614e9a6a1d4b3988b6a56bbceb780d1cd2b2be337b1720a27936fb05ecfa g_{26} 21aac9e99b7031bda9421b5b3b9555baadac96babce8a7ee4e1e2657527 c2c28763fd1e392d07ae2ed969912db6c78b8bbfa216e5652c6fb47731ec455938da25c1 7fb582ea502281030849726f478cad1a8b56be921a90b53610b62a09c 130b27465ad69c6732cda118050cddda2881a0870f1ee9cebd81a5656755cb6b080a4289 g_{27} 38baed1f7d6772a8f559234fba20fd300f91d88cff99b794f1fad6479d4 8c6573a89d9b48d9ee8474d747526bcd74b20d545c42ab7550d6f49061fccb09579c39e6 70bc04be0820bd2fc39a5411486041ba94e4b4056a196b076a222be01b 12caeae62f42d13141fc28bf5232f95dbe9dcd721b2599041507da3a5c1467a19fa469ba g_{28} 09140106622e67771f332e19b3c173afd1e23d845db9600be0755f85ef6 ec2f9195d2bf0f749f1a73dc13b7618924b3d379db2129137188b9e8e55335c096d63a27 f5bb02f5b4f5acd7c5c4ba9a7bfbf8beaf1c3747d94ab2fc5f1310fed8 c2182ba6e820e8ad89ac8f62552160abcabdd147e63f769adc69a623ebec89102aa83dfa g_{29} 2d6d6af6263b497a7150610eba6ad98297a278eb81d662c2def38de040 9ae7e0671572619b730b33abdc8c9a4608d641e163456310be94cf55ae4c925c6fe63a08 1fb1419b66c3a8fc199e7ecb114a9bdeb13ee7acf3ac7edd43f7223518 517c312655635d41df5efe8f8af30677e0e3cf5add48aab157f45dff6215cdcf5f5c1ad4 х g_{30} dc3474bcdd401bfa8b77103b20c9c28925a18ebfeacd8d2b0a1d52d48d 5d6830d33c7edf554d9f14c9e6ee502966f833a1c5ef506b6ef44b9171664e99e5cc1c8b 09d704ff9e72d0c60e1f7ce6e6f8989a88a03b1c300734f094c2c5624c 6f2017da1d5c88274584752c8ab8c7ef8ae7f6a9eceb3a8b3b9af16b5e0347b01fa662b0 g_{31} db27fbab75749ae68357135f3dd2544d2e1a7d9594bfd7d7ddf9d69c25

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55ae33d559df36a17d1fa4dae0b5a352f459168f94d0a5b4561470272c

196d67a036c922f087436e98187a425b9226ae75a0a91b848ada67a9be0

d62195e14e6b29654147db19d02cd73381020d7a5559880e3e2f41343ef39bd29b613d8b

1f666425fa8bde98bff138161796c12e0e1e485eadacd0ed5adab17ba92b3a29328fe057

- y b78d8152baae1fe290183564ec0cdeddef6249220b986df8bbf3cb9a047f066279d3cd07
 3b5d8f18508a17f7afccf40758324fe251c54e2bbfdd2be16ddcd35acc
- g_{33} x 1c78aa5476f6cc9b6d22c3a258bebc1df2ce2e391dc775b814cece94f64fed29c0c9a40a e7b78f2181af163dec8318678493d1b9852606e58f963754652141cd1b
 - y 3e4c468142cc1b6fb64117c6697f29c336fdb272a483642339d838220603e11d4c6dc80b 7b1e5d1321ab11a02d7d81a25a14eed5808c7a095481c7b9216d076580
- $g_{34} \hspace{0.5cm} \textit{x} \hspace{0.5cm} 14 \text{be} 306 \text{c} 2 \text{a} 30 \text{c} 0 \text{b} 90 \text{a} 741 \text{a} 37 \text{de} 382 \text{b} 565 \text{a} 0787471 \text{d} \text{b} \text{d} 3726 \text{f} 3 \text{a} \text{d} \text{e} \text{d} \text{e} 7 \text{a} \text{b} 1 \text{f} \text{d} \text{a} \text{e} 81 \text{b} \text{e} 595 \text{a} \text{d} \\ \hspace{0.5cm} 95 \text{e} 66 \text{d} 7 \text{e} 2 \text{d} \text{c} \text{f} 5387518 \text{b} \text{a} \text{d} \text{d} \text{e} 3128 \text{e} 18 \text{f} 32 \text{b} \text{c} 198 \text{c} \text{b} 700 \text{f} \text{a} 3 \text{b} 8 \text{b} 0 \text{f} \text{c} \text{f} 3879 \text{b} \\ \hspace{0.5cm} 66 \text{d} 7 \text{e} 2 \text{d} \text{c} \text{f} 5387518 \text{b} \text{a} \text{d} \text{d} \text{e} 3128 \text{e} 18 \text{f} 32 \text{b} \text{c} 198 \text{c} \text{b} 700 \text{f} \text{a} 3 \text{b} 8 \text{b} 0 \text{f} \text{c} \text{f} 3879 \text{b} \\ \hspace{0.5cm} 66 \text{d} 7 \text{e} 2 \text{d} \text{c} \text{f} 5387518 \text{b} \text{a} \text{d} \text{d} \text{e} 3128 \text{e} 18 \text{f} 32 \text{b} \text{c} 198 \text{c} \text{b} 700 \text{f} \text{a} 3 \text{b} 8 \text{b} 0 \text{f} \text{c} \text{f} 3879 \text{b} \\ \hspace{0.5cm} 66 \text{d} 7 \text{e} 2 \text{d} \text{c} \text{f} 18 \text{e} 18 \text{e$
 - y c867c121cbb34253c6d4ed65c70be22d1617b6900cabcee928e76b93bd16ba13d493d1c7 le627094dd14d6a1b2cbaea64505cc55249c9786971703502723dbeb23
- - y 1aa422ac52f5084393f4640768edf0c2858f79086f924ce3c180b7f11d91c8d4235f9f74
 57593ec821dda06a10792bd69ec341ba84b12608342cc715d1cd342ffc
- g_{36} x af4b0e427400a864af899a2a56cf650ef4d4a8665886027bbcce7c1004dd725eb4bb62d1 b73c5e285cf2aed3cd490c06ff2a1613eb661f8c0a86738caea2f5d4d9
 - y 3494aa6e02e8143a857afc9a6c79e86c31bb5de7a01bfcca4a57572fef373a3436e32299
 44cca15e526528a22b0fb1a3515695a8e4df14188f81c555e7807a3f78
- $g_{37} \quad x \quad 3593984917824 \\ \text{df5c94702cfd7b05b3eb1abf73cbab62a43df9671df6126a165a2727d27} \\ 997a2b911dc1528fe42263477ce2e8ee8bf1ec22c932459adaa3758e0d$
 - y 3e000955d568b335ff04c7f011f8b0aeae2ebd066f85bde68882fb840d05b291c94f266e 82664f239b968acb220411b546d46cb6ce72d98cd7a6dec54e2469b632
- $g_{38} \quad x \quad 19320 \texttt{c} 9939 \texttt{d} f 24711 \texttt{f} 9844 \texttt{f} 0312 \texttt{a} \texttt{a} \texttt{b} 80 \texttt{e} 447699 \texttt{e} 4 \texttt{d} 072 \texttt{a} 2 \texttt{d} 9 \texttt{e} 80 \texttt{a} 29 \texttt{d} \texttt{a} \texttt{f} \texttt{e} 86 \texttt{c} \texttt{a} \texttt{f} 058 \texttt{f} \texttt{a} \texttt{b} 3 \texttt{a} \\ 8 \texttt{a} 8 \texttt{d} 4975515864 \texttt{c} 2 \texttt{b} 931 \texttt{c} 7 \texttt{f} 7 \texttt{d} \texttt{b} 3 \texttt{b} 25 \texttt{f} 2 \texttt{f} 5 \texttt{f} 9 \texttt{e} 5 \texttt{f} 8 \texttt{b} 5315 \texttt{a} 681 \texttt{b} 393 \texttt{b} 08 \texttt{a} 7 \texttt{f} \\ \end{cases}$
 - y ab49050ea49925fc1cb86acedf4219659b2490e91b09f425bff051600a9e31464e2ea969
 74545b7c745838a75a49c88bcacd837ac8957fc14f711dea93070f3d99
- g_{39} x 12ba5b532acb5ceee9c91a325695786bf7e1842b831f8da30d360d428ae533ef2d1071e8 131f7a7a729bc2ed19ae0c129b8ab0377fb55e019e64932eb28f80b9334
 - y 803c8ebeaa493d6fcb356fb2562b79d3a376b5bcbf9b22bbee75611075f7b7ab16666abd 97be5b7ecb338841fe77ece135f4e2e4b83acafd71e704527a84789468
- - y d74a594a661d40ea629702dd1247808fb288dd5040e5410d7d6b04591e39696bf29995a3
 523928413d746acf2cdb55c40aa084cb65a289bdfc8501fdccb40209f9
- $g_{41} \quad x \quad \texttt{ef451e110daf9d5e391a5359934a9f6969517f438c7bea183d5e96290ddce120873e4548} \\ \quad 6\texttt{d0c41c887c483b4661dfb48d8d72c0fb89e87e39c8a3716e9cdc76ddd}$
 - y efa5c68d14de0eff1d729005e26e74f49f8bc083124a432ae18dd5131c04776f59a3f932
 74c5177f3c91a20160657a114f5bc0dbcc5c8069984e341320412adf1a
- g₄₂ x 118713fa11a53a24b33f9e156cecf8b415874794508fe5438f8c4dae138666a5b888e8e9 9438dabc15556465747116ac472ad95d2920fe9b36f30be0963d7e0db12
 - y 954bea5f61e4a9d8d093d1b9d6ab52b2fac8b78655802010cf5ed97459864271ef4c34d8 044c26c7763de328e509ef0a68c1173130ad6301b20c3bc8f8f26ad296

- - y 8e6efc12aad547b3e08d39f7a79e9b034616f098175f716561b7927ab115a54be4fdecd3 845f7f5358828f175b83ed25ef2492c87296d6d89ecb9881104be9be7d
- g_{44} x 1fbd78c94ec52e5d769392cf084c5e629b29cf6e3bba7f3cd0c612c2f610ce388bb72a9c 7d4ddc3f5612086cb42bf340f1e4ac7324c7359ef3351095cb00a7a304e
 - y 99dd83d1b4c0b271f51c4851b236ff7b7e866266806847961937ef20aecc988122c07603
 2674be513aa03946163477ddd205945b3917d1a3fccca2ba9d4205aff7
- - y f9735628a382e2ad84fd1badebcf6c9ee5e39789391de6bfb409b0adacc173105054118b
 443cb4eda232428f4413183a56486d073b84a56d89cb721ec985ebc751
- - y 97b3f435c00416a59586e7593128c12b734723aa887f98a0b482d18d38707bb933e4b4bc ccdc71075f5174e8f2133b74b544b29a796b4fd8b783664af1d3659e99
- g₄₇ x dbcc8bb88c00c531890bcc22a2f221b8ca916b9c324c081c7123e5ca66069e0bcac91e09
 bf95fae7d15f8aacaa1726d70ac03057f7d86f0e27376ccc1fcd7b8c7e
 - y 2d4001615d625d51263a6f7bf263c0e21c656864bd9b395c1734366ce375518c058a34e7
 4811c14ca07227baa0bd0b59c95356f47f44f390c6a4d16c4a6e0c6fec
- - y 56ec9f00a5bd39a7857836235a83f24b21ff89b85484c8a795fe3e3baeed8532ee2b9419 8c9882035c77b1e75085c5cb936df3063e7173592e2749099a62247d6d
- $g_{49} \hspace{0.5cm} \textit{x} \hspace{0.5cm} 8 \text{b7af7378ceae85d550bda52ec6744133bc0ed593d612a4718a43b0f85b057f79f434629} \\ \hspace{0.5cm} \text{b170d203a57ac4c006dc4c87b5c92fa7d4af37d5e3651a141531fc151a}$
 - y 9440c6216b46107b253c40bd70fc5fc96fe9b886cf32940958a8024c08595f90a6d783f4
 0a48b1ea9bbc8e0adbb8e4d87300aca7f712a8020b0c43d3b1fd794b1
- g_{50} x 63105a1ff0449d4d5d788395ee7141fd5c44fd0227b3bdc32b9e9d26be5c7b7945faf8ab 247eed6e50cb824abe7f5c4b7ed9ed725892d277ada462bb4e72dd5e6d
 - y cb0280e5e9293d2db08d25caad1e7b49aa52fc854fa49402e05e4b6fbcf0efc1764834c1
 c4ca13a36ca20e8b8f57bd77aca8f52be06bd9a6929f93ca172d3d86d0
- g_t x d0bfc69d957f2fc38e5170ac3aae81110dcc7a077c0094ddd29ff12057fcaf56e8d014d0 16998e44710db3fdf72da65e31cd665abcb35308a6b0ac5f18b3ffb6f7
 - y bfaba1b7ea54552b938ce89d0907797f5f55dd081ca3fb5cf01f2606d464e36e3a37e050
 cfa0fb9ceee03536707c6d117665b3b1e8344d66939b29792004475053

2.3.4 Device generators

- $g_t \quad x \quad 15 f3 a e2 e e5 7671 e1 b d c8 70 47 f3 4 c b e0 a a b c6 93 f4 63 b1 3 d4 2 df 6 fd 10 f8 6 cc 7 b4 b4 b9 99 c9 c 38 b de fa 8 e1 3 c7 01 74 f1 b e7 9 f8 e9 3 4 a 3 a 01 8 03 07 3 b 3 4 04 6 b 8 d8 ff c7 99 3 4 2$
 - y f0984ac43d1a34d52143f09abd1746bcd11e5495a096e307d1ab21648b1118c29c201f29
 d085d6a8a4da6cf760c818dcdc4ede01b411065cac92eea1cc51bdafb2

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