
Contents

1	Introduction	1
2	Related Work	1
3	Dataset description	1
4	Methods Description	1
4.1	Graph Convolutional Networks (GCN)	1
4.2	Graph Attention Networks (GAT)	2
4.3	Graph Sample and Aggregate (GraphSAGE)	2
4.4	Graph Transformer	3
5	Evaluation Strategy	3
6	Results	3
6.0.1	Conclusions	3

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1 Introduction

This project aims to test methods for predicting a paper category based on its abstract, and the graph structure of citations between papers. The main idea is to reproduce the results from the paper *Semi-Supervised Classification with Graph Convolutional Networks* by Thomas N. Kipf and Max Welling, presented at ICLR 2017, and to compare it with other methods.

2 Related Work

3 Dataset description

4 Methods Description

4.1 Graph Convolutional Networks (GCN)

Graph Convolutional Networks (GCNs) extend convolution to graph-structured data by iteratively aggregating and transforming features from a node's neighbors using the graph topology.

A common layer-wise propagation rule is:

$$H^{(l+1)} = \sigma \left(\tilde{D}^{-\frac{1}{2}} \tilde{A} \tilde{D}^{-\frac{1}{2}} H^{(l)} W^{(l)} \right)$$

where:

- $\tilde{A} = A + I$ is the adjacency matrix with self-loops.
- \tilde{D} is the degree matrix of \tilde{A} .
- $H^{(l)}$ represents the node features at layer l .
- $W^{(l)}$ denotes the learnable weights.
- $\sigma(\cdot)$ is a non-linear activation function.

We can note that when there are no edges, the $\tilde{D}^{-\frac{1}{2}} \tilde{A} \tilde{D}^{-\frac{1}{2}}$ term becomes the identity matrix, and the layer reduces to a standard feedforward layer, which will be useful for a baseline comparison.

4.2 Graph Attention Networks (GAT)

Graph Attention Networks (GATs) incorporate an attention mechanism to assign different importance to neighboring nodes when aggregating features.

For a node i , attention coefficients are computed as:

$$\alpha_{ij} = \frac{\exp(\text{LeakyReLU}(\vec{a}^\top [W\vec{h}_i \| W\vec{h}_j]))}{\sum_{k \in \mathcal{N}(i)} \exp(\text{LeakyReLU}(\vec{a}^\top [W\vec{h}_i \| W\vec{h}_k]))}$$

and the node update is:

$$\vec{h}'_i = \sigma \left(\sum_{j \in \mathcal{N}(i)} \alpha_{ij} W\vec{h}_j \right)$$

where: - \vec{h}_i represents the input node features. - W and \vec{a} are learnable parameters. - $\mathcal{N}(i)$ denotes the neighbors of node i . - $\|$ is the concatenation operation. - $\sigma(\cdot)$ is a non-linear activation function.

4.3 Graph Sample and Aggregate (GraphSAGE)

GraphSAGE is an inductive graph representation learning method that learns node embeddings by sampling and aggregating features from a fixed-size set of neighboring nodes.

For node i at layer l , the neighborhood aggregation is:

$$h_{\mathcal{N}(i)}^{(l)} = \text{AGGREGATE}^{(l)} \left(\{h_j^{(l)} : j \in \mathcal{N}(i)\} \right)$$

and the node update is:

$$h_i^{(l+1)} = \sigma \left(W^{(l)} \cdot [h_i^{(l)} \| h_{\mathcal{N}(i)}^{(l)}] \right)$$

followed by normalization.

where: - $\mathcal{N}(i)$ denotes the **sampled** neighbors of node i . - $W^{(l)}$ are the learnable weights. - $\|$ indicates concatenation. - $\text{AGGREGATE}(\cdot)$ is a differentiable function (e.g., mean, max-pooling, or LSTM).

4.4 Graph Transformer

Graph Transformers adapt the self-attention mechanism of Transformers to graph-structured data, enabling nodes to attend to other nodes based on learned attention scores while incorporating graph structure via positional or edge encodings.

For a node i , attention is computed as:

$$\text{Attn}(i, j) = \frac{(W_Q h_i)(W_K h_j)^\top}{\sqrt{d}}$$

and the node update is:

$$h'_i = \sum_{j \in \mathcal{V}} \text{softmax}_j (\text{Attn}(i, j) + b_{ij}) W_V h_j$$

where: * h_i are the node features. * W_Q, W_K, W_V are learnable projection matrices for Query, Key, and Value. * d is the attention dimension (used for scaling). * b_{ij} is a bias term encoding graph structure (e.g., shortest path distance or edge connectivity). * \mathcal{V} is the set of all nodes in the graph.

5 Evaluation Strategy

We measure the performance of each model using accuracy on a held-out test set. Additionally, we monitor training and validation loss to assess convergence and potential overfitting.

Accuracy measures the proportion of correctly classified examples and is defined as:

$$\text{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN}$$

6 Results

Model	Val Accuracy	Test Accuracy
GCN - from the original paper	-	0.703
GCN - the replication	0.718	0.691
GCN - without edges	0.572	0.571
Graph Isomorphism Network	0.666	0.648
Graph Attention Network	0.748	0.728
Graph Sample and aggregate	0.710	0.707
GraphTransformer	0.724	0.694

6.0.1 Conclusions

Across all experiments on the Citeseer dataset, models that incorporate graph structure consistently outperform those that ignore it, confirming the importance of relational information in semi-supervised node classification. Our replication of the original GCN achieved slightly lower accuracy than reported in the paper but still demonstrated strong

performance relative to baselines. Among all models evaluated, the Graph Attention Network achieved the highest accuracy, suggesting that adaptive, attention-based neighbor weighting is more effective than fixed aggregation. GraphSAGE and GraphTransformer also performed competitively, while GIN lagged somewhat, reflecting its sensitivity to hyperparameters in smaller citation networks. In contrast, models without edges—GCN without edges and an MLP—performed significantly worse, emphasizing that leveraging graph connectivity is crucial for achieving high performance in this task.