

1.a.

Population: the households in 2008 in America

Sample: the 1500 people surveyed in 2008

Population parameter of interest: the average money spent on Halloween in 2008 within American families

Sample statistics: the average \$58 found in the sample

1.b.

Population: the students in this university in 2011

Sample: the 203 students being surveyed in this university in 2011

Population parameter of interest: the average GPA that students got in this university in 2011

Sample statistics: the average 3.59 GPA in the sample

2.a.

Sample space $S = \{(1,1), (1,2), (1,3), (1,4), (1,5), (1,6), (2,1), \dots, (6,6)\}$

Event E means the combination of the number of two dices which have an odd sum, such as (1,1) or (3,5). It has exactly $6*6/2 = 18$ combinations.

Event F means the combination that the first number in the bracket is 1, which are from (1,1) to (1,6), which have 6 possibilities.

2.b.

$$E \cap F: 3$$

$$E \cup F: 18+6-3 = 21$$

$$E \cap F^c: 18-3 = 15$$

3.a.

$$\text{Possibility} = 5/15 = 1/3$$

3.b.

Same as question a. It's 1/3

3.c.

$$1/15$$

4.a.

$$\text{Probability: } (212+36)/ (212+36+198+54) = 0.496$$

4.b.

$$54/ (54+198) = 3/14$$

5.a.

$$0.9*0.15 + 0.1*0.8 = 0.215$$

$$1 - 0.215 = 0.785$$

5.b.

Probability if it's dead: 0.215

Forget to wash it that cause its death: $0.1*0.8 = 0.08$

Probability = $0.08/0.215$ which is approximately 0.372

6 and 7

6-a. we can get that

$$P(L|C) = 0.135$$

$$P(L|C^c) = 0.268$$

$$P(C) = 0.7$$

$$P(C^c) = 0.3$$

when C is got cancer C^c is not got cancer
 $\Rightarrow L$ is PSA level high

$$\text{so, ask } P(C|L) = \frac{P(L \cap C)}{P(L)}$$

$$= \frac{P(L|C)P(C)}{P(L|C)P(C) + P(L|C^c)P(C^c)}$$

$$= \frac{0.268 \times 0.7}{0.268 \times 0.7 + 0.135 \times 0.3}$$

$$= \frac{0.1876}{0.2281}$$

$$\approx 0.822$$

6.b.

ask for $P(C|L^c)$

$$\text{we know that } P(L^c|C) = 1 - 0.135 = 0.865$$

$$P(L^c|C^c) = 1 - 0.268 = 0.732$$

$$\text{so } P(C|L^c) = \frac{P(L^c \cap C)}{P(L^c)}$$

$$= \frac{P(L^c|C)P(C)}{P(L^c|C)P(C) + P(L^c|C^c)P(C^c)}$$

$$= \frac{0.5124}{0.7719}$$

$$\approx 0.664$$

$$7-a. \quad \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{32}$$

$$7-b. \quad \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{32}$$

$$7-c. \quad \frac{1}{8} + \frac{1}{8} = \frac{1}{4}$$

$$7-d. \quad 1 - \frac{1}{4} = \frac{3}{4}$$