

This problem set covers material from Week 8, dates 10/28 – 10/31.

**Instructions:** Write or type complete solutions to the following problems and submit answers to the corresponding Canvas assignment. Your solutions should be neatly-written, show all work and computations, include figures or graphs where appropriate, and include some written explanation of your method or process (enough that I can understand your reasoning without having to guess or make assumptions). A general rubric for homework problems appears on the final page of this assignment.

In some the following, you may need to use R. If you do, please write down the corresponding code to “show your work”. Drawing and labelling curves are also good examples of “showing your work”.

## Monday 10/28

1. A survey was conducted on 850 randomly sampled student loan borrowers, asking them if they owed more than \$30,000 in student debt. A 95% confidence interval for the true proportion of student loan borrowers with at \$30,000 of debt was found to be (0.135, 0.185).
  - (a) Based on this information, out of the 850 respondents, how many answered “yes” to the question? Justify your answer.
  - (b) Use hypothesis testing to examine the claim that fewer than 18.2% of all student loan borrowers owe at least \$30,000 at the 0.05 significance level.
2. Among a simple random sample of 331 American adults who do not have a four-year college degree and are not currently enrolled in school, 48% said they decided not to go to college because they could not afford school.
  - (a) A newspaper article states that only a minority of the Americans who decide not to go to college do so because they cannot afford it and uses the point estimate from this survey as evidence. Conduct a hypothesis test to determine if these data provide strong evidence supporting this statement.
  - (b) Would you expect a confidence interval for the proportion of American adults who decide not to go to college because they cannot afford it to include 0.5? Explain.

## Wednesday 10/30

3. A checkweigher is an automatic or manual machine that checks the weight of a given commercial product. For one particular checkweigher, several thousand measurements were taken, with the weight averaging out to 512 micrograms above a kilogram and a standard deviation of 50 micrograms. Then, the checkweigher is cleaned. The next 100 measurements of the same type of product average out to 508 micrograms above on kilogram with a standard deviation of 52 micrograms. Did the product weight get 4 micrograms lighter?

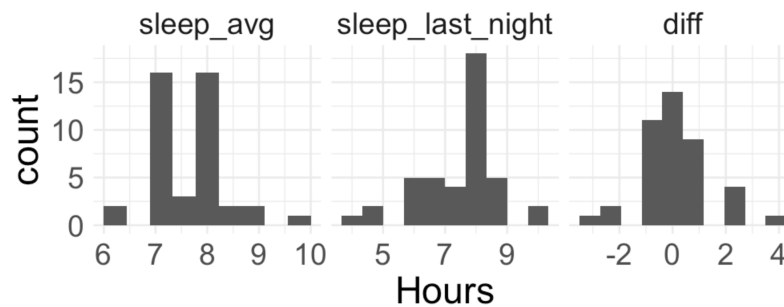
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- (a) Form a set of hypotheses that would be appropriate for testing if the weight got lighter.
- (b) Would you make a  $z$ -test or  $t$ -test? Why?
- (c) Conduct a hypothesis test for to test your hypotheses in (a) using the specific test you chose in (b). Interpret your results in context.
4. According to a report on sleep deprivation by the Centers for Disease Control and Prevention, the proportion of California residents who reported insufficient rest or sleep during each of the preceding 30 days is 8.0%, while this proportion is 8.8% for Oregon residents. These data are based on simple random samples of 11,545 California and 4,691 Oregon residents.
- (a) Conduct a hypothesis test to determine if these data provide strong evidence the rate of sleep deprivation is different for the two states. (Reminder: Check conditions)
- (b) It is possible the conclusion of the test in part (a) is incorrect. If this is the case, what type of error was made?
5. Researchers interested in lead exposure due to car exhaust sampled the blood of 52 police officers subjected to constant inhalation of automobile exhaust fumes while working traffic enforcement in a primarily urban environment. The blood samples of these officers had an average lead concentration of 124.32 microgramm/l, and a standard deviation of 37.74 microgramm/l. A previous study of individuals from a nearby suburb, with no history of exposure, found an average blood level concentration of 35 microgramm/l.
- (a) Write down the hypotheses that would be appropriate for testing if the police officers appear to have been exposed to a different concentration of lead.
- (b) Explicitly state and check all conditions necessary for inference on these data.
- (c) Regardless of your answers in part (b), test the hypothesis that the downtown police officers have a *higher* lead exposure than the group in the previous study. Interpret your results in context.

## Thursday 10/31

6. Each year the US Environmental Protection Agency (EPA) releases fuel economy data on cars manufactured in that year. Below are summary statistics on fuel efficiency (in miles/gallon) from random samples of cars with manual and automatic transmissions, as well as the summary statistics of the differences. Do these data provide strong evidence of a difference between the average fuel efficiency of cars with manual and automatic transmissions in terms of their average city mileage? Assume that conditions for inference are satisfied.

	City MPG		
	Automatic	Manual	Diff
Mean	15.26	19.64	4.41
SD	4.38	4.70	6.56
n	26	26	26

7. At the beginning of the semester, you filled out a survey where you provided the number of hours of sleep on average, and the number of hours you slept the night before. The sampled data across both classes are provided below (note this isn't a census because not everyone filled out the survey.) Did students receive less sleep on the the first or second evening of Fall 2024 semester compared to their historical average? Answer this question using a hypothesis test.



	n	mean	sd
sleep_avg	42	7.61	0.78
sleep_last_night	42	7.54	1.25
diff	42	0.07	1.25

**General rubric**

Points	Criteria
5	The solution is correct <i>and</i> well-written. The author leaves no doubt as to why the solution is valid.
4.5	The solution is well-written, and is correct except for some minor arithmetic or calculation mistake.
4	The solution is technically correct, but author has omitted some key justification for why the solution is valid. Alternatively, the solution is well-written, but is missing a small, but essential component.
3	The solution is well-written, but either overlooks a significant component of the problem or makes a significant mistake. Alternatively, in a multi-part problem, a majority of the solutions are correct and well-written, but one part is missing or is significantly incorrect.
2	The solution is either correct but not adequately written, or it is adequately written but overlooks a significant component of the problem or makes a significant mistake.
1	The solution is rudimentary, but contains some relevant ideas. Alternatively, the solution briefly indicates the correct answer, but provides no further justification.
0	Either the solution is missing entirely, or the author makes no non-trivial progress toward a solution (i.e. just writes the statement of the problem and/or restates given information).
Notes:	For problems with multiple parts, the score represents a holistic review of the entire problem. Additionally, half-points may be used if the solution falls between two point values above.
Notes:	For problems with code, well-written means only having lines of code that are necessary to solving the problem, as well as presenting the solution for the reader to easily see. It might also be worth adding comments to your code.