[STAT/MATH 310] PROBABILITY

FALL 2023

SECTION: STAT/MATH 310 Professor: Becky Tang (she/her)

CLASS HOURS: TRF 8:40-9:30AM OFFICE: Warner 214

ROOM: Warner 105 **E-MAIL:** btang@middlebury.edu **PREREGS:** MATH 223 **OFFICE HOURS:** M 2-4pm, R 3-4pm (ten-

tative)

COURSE DESCRIPTION

An introduction to the concepts of probability and their applications, covering both discrete and continuous random variables. Probability spaces, elementary combinatorial analysis, densities and distributions, conditional probabilities, independence, expectation, variance, weak law of large numbers, central limit theorem, and numerous applications. Students learn how to simulate and obtain samples from probability models using the programming language R.

KEY LEARNING OUTCOMES

| Apply | basic counting technique | ues (multiplicatio | n rule, combination | s, permuta- |
|--------|--------------------------|--------------------|----------------------|--------------|
| tions) | to compute probabilitie | s using the axiom | natic language of se | ts and func- |
| tions. | | | | |

- ☐ Calculate the expected value, variance and quantiles of common discrete and continuous random variables.
- ☐ Compare and describe multiple random variables using joint, marginal, and conditional distributions.
- ☐ Use moment generating functions and their properties to specify a random variable.
- ☐ Obtain new random variables by applying transformations to a class of elementary distributions.
- ☐ Use R to sample from probability models and generate simulations.
- ☐ Understand the law of large numbers and the central limit theorem.

TEXTBOOKS AND COURSE MATERIALS

TEXTBOOK: Joseph K. Blitzstein and Jessica Hwang, *Introduction to Probability*, 2nd edition.

You may either purchase a hard copy or access the free, online version provided here: http://probabilitybook.net/. We will focus on Chapters 1-10.

□ **Course website**: All of the materials for our course will be posted on the course website https://midd-stat310-fall2023.github.io/. Please bookmark this page

for quick access.

R: We will learn and frequently use the R programming language. We will program using the RStudio interface. In the second week students will be asked to ensure they have access to both R and RStudio, either by downloading the software onto their own computers, or by using a campus computer.

COURSE STRUCTURE

This course will operate in a "flipped style" with a balance between and individual and group-based learning. We will focus on developing problem-solving skills. A typical class day involves the following:

- 1. Reading assignment: Every class meeting time will have an assigned reading from the textbook. You are expected to do the reading before class. By 7:45am on the day of class where we cover the assigned material, you will answer a set of brief reflection questions on the topics covered. You are also encouraged to submit an questions or clarifications from the assigned reading.
- 2. Active class session: Our 50-minute meetings will consist of brief lecture at the beginning of class, followed by group work with your peers. The small lecture is intended to provide supplementary material, and the group session is intended for you to explore the topics more deeply.
- 3. Homework: After each class session, several homework problems will be assigned. At least one problem from each day's active class session will be assigned as homework.

A prepared student will attend the 50-minute class, and spend roughly two-four hours per day of class on work outside the classroom (reading assignment, reflection exercises, homework, studying, etc.). As this course meets three days a week, this represents a minimum 9-13 hours weekly commitment.

CLASS EXPECTATIONS AND CODE OF CONDUCT

- ★ You are expected to physically show up to class, actively participate, and make space for everyone to contribute. You are an integral part of the class community! Exceptions include previously-communicated illness or planned absence.
- ② **Please arrive on time.** I expect everyone, myself included, to arrive on time and dedicate full attention during the class. Class will begin promptly at the scheduled time. In turn, I will do my best to always end class on time.
- □ **Technology.** You are encouraged to bring a laptop and/or tablet to class each day for note-taking, referencing the textbook, and live coding.
- Cell phones should be turned to silent. I don't mind cell phones in class, but please silence them so as to not disrupt the class.
- ? Please ask questions!
- **Positively contribute to your group problem-solving**, which includes asking questions, throwing out ideas, and voicing confusions. There are many ways to solve the problems we will encounter in this class.
- I expect all members of the class to make participation a harassment-free experience for everyone, regardless of race, creed, color, place of birth, ancestry, ethnicity, national origin, religion, sex, sexual orientation, gender identity or expression, age, marital status, service in the armed forces of the United States, positive HIV-related blood test results, genetic information, or against qualified individuals with disabilities on the basis of disability and/or any other status or

characteristic as defined and to the extent protected by applicable law. We will not tolerate the use of violence against any individual.

RESOURCES

| Office hours . This time is meant | for you! Please come by to ask questions, chat |
|------------------------------------------|------------------------------------------------|
| with me, or work on homework. | You should never worry about disturbing me |
| during this time. | |

- ☐ **One-on-one meetings**. If you would like to meet with me one-on-one, please send me an e-mail or approach me after class so we can schedule a time.
- ☐ **Your peers**. Unless otherwise noted, I encourage students to work together and discuss material! However, unless the assignment explicitly states that it is to be completed as group work, the submitted material must be your own.

TIPS ON HOW TO SUCCEED

- Come to every class.
- Attend office hours.
- Attempt some problems individually before working with others.
- Complete the pre-class assignment in a timely fashion. A lot of the concepts in this class take time to sink in.
- The assigned readings are not lengthy, but they convey a lot of information.
 - Read through the material at least twice. Once without taking notes for an overall overview, then a second time to take notes.
 - Do not skim past the Examples in the readings. Make sure you understand the solutions presented in the Example problems.
- Practice problems and homework problems are intended to help you stay up-todate with the material. We will work on the practice problems in class, and it is my expectation that you will complete whatever you don't finish on your own time
- Ask questions (someone should ask me a question now!)
- Do not try to find answers on the internet or ChatGPT. Struggling through problems is how you learn!

College policies and resources

ACADEMIC INTEGRITY

As an academic community devoted to the life of the mind, Middlebury requires every student to reflect complete intellectual honesty in the preparation and submission of all academic work. Details of our Academic Honesty, Honor Code, and Related Disciplinary Policies are available in Middlebury's handbook.

Using AI tools (e.g., ChatGPT, Bard) is forbidden in this class. You may not use them to assist in any part of your homework or other assignments. Any use of generative AI tools will be treated as a violation of Middlebury's Honor Code.

HONOR CODE PLEDGE

The Honor Code pledge reads as follows: "I have neither given nor received unauthorized aid on this assignment." It is the responsibility of the student to write out in full, adhere to, and sign the Honor Code pledge on all examinations, research papers, and laboratory reports. Faculty members reserve the right to require the signed Honor Code pledge on other kinds of academic work.

DISABILITY ACCESS AND ACCOMMODATION

Students who have Letters of Accommodation in this class are encouraged to contact me as early in the semester as possible to ensure that such accommodations are implemented in a timely fashion. For those without Letters of Accommodation, assistance is available to eligible students through the Disability Resource Center (DRC). Please contact ADA Coordinators Jodi Litchfield, Peter Ploegman, and Deirdre Kelly of the DRC at ada@middlebury.edu for more information. All discussions will remain confidential.

CENTER FOR TEACHING, LEARNING, AND RESEARCH (CTLR)

The CTLR provides academic support for students in many specific content areas and in writing across the curriculum through both professional and peer tutors. The Center is also the place where students can find assistance in time management and study skills. These services are free to all students. go.middlebury.edu/connect

TYPES OF ASSIGNMENTS

- * Daily assignments. Assigned before each class session and turned in individually. These small assignments include readings from the textbook plus a few assessment questions that are designed to help you reflect on your understanding of the readings. I will review all the assignments prior to each class period. These assignments are graded on good-faith effort so you can receive feedback quickly. Daily assignments are due by 7:45am the day of each class (to give me time to review them before class). For example, the daily assignment for Tuesday 9/19 should be completed by 7:45am on Tuesday 9/19.
 - No extensions on daily assignments will be given, but up to two assignments may be missed without penalty.
 - It is not my intention or desire for you to stay up late or wake up early to complete the daily assignment. Daily assignments will be released at least one week advance so you can plan ahead.
- * **Problem sets**. Assigned weekly and turned in individually (though feel free to work with your peers). In the problem sets, you will apply what you have learned during lecture to dive deeper into the material and explore more interesting probability problems. Depending on the week, the problem sets may require R. Problems will be assigned after every class, but each week's problem set is due the following Tuesday by 11:59pm.
- * Participation. Because of the collaborative nature of this course, it is essential that you strive to attend class every day, and that you complete the assigned reading prior to the start of class. Additionally, in order to foster a positive and inclusive classroom environment, you are expected to follow our class code of conduct. Frequent absences, as well as non-constructive in-class participation, will be reflected in your final course grade. If you unable to attend class for any reason, please notify me before the start of class so that I can make appropriate group arrangements. Typically, you may miss up to two classes without penalty. However, prolonged or recurring illness, as well as other emergencies, may require individual adjustment, in which case you should contact me to make appropriate arrangements.
- * **Midterm exams**. Two midterm exams are designed as an opportunity to assess the knowledge you've learned. At least one midterms will have a take-home portion. The tentative dates for the exams are:
 - Midterm 1: Thursday, 10/12 at 7:30pm
 - Midterm 2: Thursday 11/16 at 7:30pm

Except in the cases of extreme illness or family emergency, students must take the in-person portion of the midterms on the scheduled date and time.

* **Final exam**. The final exam is designed to fully assess what you've learned in the semester. The final exam is cumulative, with a slight emphasis on material covered after Midterm 2. The final will most likely consist of both an in-person and a take-home portion.

GRADING

- * Unless otherwise noted, assignments should be turned into Gradescope.
- * Late work will always be considered within one week of the original due date. Unless otherwise stated, the late policy is as follows: for every 24-hour period the assignment is late, 10% from the maximum possible grade will be deducted.
- * I will do my best to return assignments within one week of submission.
- * Regrade requests: I do allow regrade requests, which must be submitted inperson within one week of when the assignment is returned. Keep in mind that regrade requests do not guarantee points back.
- * You must sit for each midterm and final exam in order to pass the course.

| Component | Percentage | |
|-------------------|------------|--|
| Daily assignments | 10% | |
| Homework | 25% | |
| Participation | 10% | |
| Midterm I | 15% | |
| Midterm II | 15% | |
| Final Exam | 25% | |

- **★** Letter grades will be assigned based on the following course percentages, with the upper 3% and lower 3% of each category corresponding to + and −, respectively:
 - A: 90-100%
 - B: 80-89%
 - C: 70-79%
 - D: 60-69%
 - F: <60%

In the case of decimal points, grades will not be rounded up. For example, an 92.9% will correspond to a A-, not an A.

TENTATIVE COURSE CONTENT

(Last updated: 09/07/23)

NOTE: The following dates and content may be modified due to the requirements of the class may be moved backward or forward depending on class progress and my conference travel. **Midterm dates are tentative, but will be finalized by the end of Week 2**.

| Week | Date | Topic |
|--------------------------------------|-------|------------------------------------------------------|
| 1 9/12 T - Welcome! Course logistics | | T - Welcome! Course logistics |
| | | R - Foundations of probability |
| | | F - Set theory, axioms of probability |
| 2 | 9/19 | T - Intro to R, RStudio |
| | | - Problem Set 01 due |
| | | R - Conditional probability, Bayes rule, LoTP |
| | | F - Independence |
| 3 | 9/26 | T - Monty Hall, Gambler's Ruin |
| | | - Problem Set 02 due |
| | | R - Conditional Probability in R (Zoom) |
| | | F - Random Variables, PMF, Bernoulli (Zoom) |
| 4 | 10/3 | T - More discrete RVs, CDF |
| | | - Problem Set 03 due |
| | | R - Function of RVs, independence of RVs |
| | | F - Expected values, linearity of expectation, LOTUS |
| 5 | 10/10 | T - Infinite series, Geometric, Neg. Binomial |
| | | - Problem Set 04 due |
| | | R - Indicators, bridge |
| | | - Midterm 1 at 7:30pm |
| | | F - Fall break (no class) |
| 6 | 10/17 | T - Variance |
| | | R - Poisson |
| | | F - Continuous RVs, Uniform |
| 7 | 10/24 | T - Normal |
| | | - Problem Set 05 due |
| | | R - Exponential, Continuous RVs in R |
| | | F - Moments, power series |
| 8 | 10/31 | T - Recap Power and Taylor series, MGFs |
| | | - Problem Set 06 due |

| | | R - Joint distributions (discrete) | |
|----|-------|-------------------------------------------|--|
| | | F - Joint distributions (continuous) | |
| | | - Last day to drop classes | |
| 9 | 11/7 | T - Covariance and correlation | |
| | | - Problem Set 07 due | |
| | | R - Multinomial | |
| | | F - Change of variable (calculus) | |
| 10 | 11/14 | T - Beta, Gamma | |
| | | R - Review/flex day | |
| | | - Midterm II at 7:30pm | |
| | | F - Change of variable (CDF method) | |
| | 11/21 | Thanksgiving Break | |
| 11 | 11/28 | T - Order statistics | |
| | | - Problem set 08 due | |
| | | R - Conditional Expectation (given event) | |
| | | F - Conditional Expectation (given RV) | |
| 12 | 12/5 | T - Conditional Variance | |
| | | - Problem set 09 due | |
| | | R - Inequalities, WLLN | |
| | | F - Central Limit Theorem | |
| | 12/11 | M - CLT in R | |
| | 12/14 | R - Final exam | |