Michael DiPasquale

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RESEARCH Interests Computational commutative algebra and algebraic geometry. Emphasis on pure and applied problems which can be approached with the tools of algebraic geometry and commutative algebra.

EDUCATION

University of Illinois Urbana-Champaign (UIUC), Urbana, IL

Ph.D., Mathematics, May 2015 Advisor: Professor Hal Schenck

Thesis: Splines on polytopal complexes

Wheaton College, Wheaton, IL B.S., Mathematics, May 2009

ACADEMIC APPOINTMENTS Oklahoma State University (OSU), Stillwater, OK

Visiting Assistant Professor

August 2015 - August 2018

Colorado State University (CSU), Fort Collins, CO

Postdoctoral Fellow

August 2018 -

PUBLICATIONS

- 20. A homological characterization for freeness of multi-arrangements, accepted pending minor revision in Math. Ann. (2021). arXiv:1806.05295
- 19. Koszul multi-Rees algebras of principal L-Borel Ideals (with B. Jabbar Nezhad), accepted pending minor revision in J. Algebra. (2021) arXiv:2008.09565
- 18. A lower bound for splines on tetrahedral vertex stars (with N. Villamizar), to appear in SIAM J. Appl. Algebra Geom. (2021) arXiv:2005.13043
- 17. Counting the dimension of splines of mixed smoothness: A general recipe, and its application to meshes of arbitrary topologies. (with D. Toshniwal), Adv. Comput. Math. (2021) doi:10.1007/s10444-020-09830-x. arXiv:2001.01774
- On the apolar algebra of a product of linear forms (with Z. Flores and C. Peterson). In Proceedings of the 45th International Symposium on Symbolic and Algebraic Computation, IS-SAC '20, pages 130-137, New York, NY, USA, 2020. Association for Computing Machinery, doi:10.1145/3373207.3404014. arXiv:2002.04818
- 15. A Generalization of Wilf's Conjecture for Generalized Numerical Semigroups (with C. Cisto, G. Failla, Z. Flores, C. Peterson, and R. Utano), Semigroup Forum 101 (2020). arXiv:1909.13120
- 14. Bivariate Semialgebraic Splines (with F. Sottile), J. Approx. Theory 254 (2020), 105392, 19 pp. arXiv:1905.08438
- 13. Free and non-free multiplicities on the A₃ arrangement (with C. Francisco, J. Mermin, and J. Schweig), J. Algebra 544 (2020), 498-532. arXiv:1609.00337
- 12. Asymptotic resurgence via integral closures (with C. Francisco, J. Mermin, and J. Schweig), Trans. Amer. Math. Soc. 372 (2019), no. 9, 6655-6676. arXiv:1808.01547
- 11. The Rees algebra of a two-Borel ideal is Koszul (with C. Francisco, J. Mermin, J. Schweig, and G. Sosa), Proc. Amer. Math. Soc. 147 (2019), no. 2, 467-479. arXiv:1706.07462
- 10. Free multiplicities on the moduli of X_3 (with M. Wakefield), J. Pure Appl. Algebra 222 (2018), no. 11, 3345-3359. arXiv:1707.03961
- 9. Inequalities for free multi-braid arrangements, Proc. Japan Acad. Ser. A Math. Sci. 94 (2018), no. 4, 36-41. arXiv:1705.02409
- 8. Dimension of mixed splines on polytopal cells, Math. Comp. 87 (2018), no. 310, 905-939. arXiv:1411.2176
- Semialgebraic splines (with F. Sottile and L. Sun), Comput. Aided Geom. Design 55 (2017), 26-47. arXiv:1604.05947

- 6. Generalized splines and graphic arrangements, J. Algebraic Combin. (2016), 1-19. arXiv:1606.03091
- 5. Associated primes of spline complexes, J. Symb. Comput. (2016), 158-199. arXiv:1410.6894
- 4. Lattice-supported splines on polytopal complexes, Adv. in Appl. Math. 55 (2014), 1-21. arXiv:1312.3294
- 3. Shellability and freeness of continuous splines, J. Pure Appl. Algebra. 216 (2012), 2519-2523.
- Asymptotic connectivity of hyperbolic planar graphs (with P. Bahls), Discrete Math. 310 (2010), 3462-3472.
- 1. On the order of a group containing nontrivial Gassmann equivalent subgroups, Rose-Hulman Undergraduate Mathematics Journal 10, Issue 1 (2009).
- 0. Splines on polytopal complexes. Thesis (Ph.D.) University of Illinois at Urbana-Champaign (2015). 148 pp. ISBN: 978-1339-32551-4, ProQuest LLC.

Under review

- 2. A lower bound for the dimension of tetrahedral splines in large degree (with N. Villamizar), submitted. arXiv:2007.12274
- 1. On resurgence via asymptotic resurgence (with B. Drabkin), submitted. arXiv:2003.06980

Grants

AMS-Simons travel grant (2015-2018)

\$4,000 for three years to support collaborative research

DISSEMINATION OF RESEARCH

Lead co-author of the package AlgebraicSplines for the computer algebra system Macaulay2. This package is currently used by several researchers, including Julianna Tymoczko, who employs this package in research with undergraduates at Smith College.

MENTORING

Assistant for a minicourse on Algebraic Geometry at SMI in Perugia Summer 2019

Created problem sets and ran Macaulay2 help sessions twice per week.

Honors option for Intro to Math Reasoning and Linear Algebra Fall 2019, Fall 2020

Created additional problem sets and problem sessions for students to receive honors credit.

Mentor in the Illinois Geometry Lab

Spring 2014, Fall 2014

Co-led undergraduate research on minimal energy configurations of particles.

Teaching mentor for junior graduate students

Fall 2013

Mentored several first-year graduate students, visited classes and offered teaching feedback.

TEACHING EXPERIENCE

Instructor of record

Course	Description
Intro to Abstract Algebra (CSU)	group theory and proof writing
Intro to Math Reasoning (CSU)	proof writing
Linear Algebra (3 semesters, CSU)	matrix theory
Intro to Combinatorial Theory (CSU)	combinatorics and number theory
Calculus 2 (CSU)	sequences, series, and integration techniques
Intro to Real Analysis (OSU)	proof writing and real analysis
Calculus 1 (5 semesters, OSU)	differential and integral calculus
A Mathematical World (UIUC)	survey course emphasizing applications of mathematics
College Algebra (UIUC)	calculus preparation course

- Responsible for lecturing, grading exams and quizzes, writing worksheets and homework
- Wrote exams (except in Calculus 1 and 2)
- Often implemented group work once per week

Recitation instructor, University of Illinois Urbana-Champaign

- Led bi-weekly 50-minute problem sessions and proctored and graded quizzes and exams for seven semesters of Calculus (1,2, and 3)

- Led student groups through worksheets I had written during bi-weekly two-hour workhops for one semester of Calculus 1 in the Merit program
- Appeared on the 'List of Teachers Ranked as Excellent' by their students in three semesters

Undergraduate teaching assistant, Wheaton College

- Led problem sessions once per week at Wheaton College for Analysis I, Algebra I, and Discrete Mathematics

Conference Presentations

1. Koszul multi-Rees algebras arising from principal Borel ideals 03/2021AMS Sectional Meeting, Providence, RI (virtual due to COVID-19) Special Session on Current Trends in Combinatorial Commutative Algebra 03/2021 2. Dual sequences arising from applarity AMS Sectional Meeting, Atlanta, GA (virtual due to COVID-19) Special Session on Commutative Algebra and its Interaction with Algebraic Geometry and **Combinatorics** 3. Formal line arrangements and rigid planar frameworks 01/2021Mathematisches Forschungsinstitut Oberwolfach, Germany (virtual due to COVID-19) Workshop on Logarithmic Vector Fields and Freeness of Divisors and Arrangements 4. Regularity of uniform power ideals and the Waldschmidt constant 10/2020 AMS Sectional Meeting, University Park, PA (virtual due to COVID-19) Special Session on Commutative Algebra and Connections to Algebraic Geometry and Combinatorics5. On the apolar algebra of a product of linear forms 07/2020The 45th International Symposium on Symbolic and Algebraic Computation, ISSAC '20 (virtual due to COVID-19) 6. (Cancelled due to COVID-19) Generalizing Wilf's conjecture to higher dimensions 05/2020 AMS Sectional Meeting, Fresno, CA Special Session on Numerical Semigroups and Applications 04/20207. (Cancelled due to COVID-19) A linear bound on the regularity of power ideals AMS Sectional Meeting, West Lafayette, IN Special Session on Combinatorial Techniques in Commutative Algebra 8. A generalization of Wilf's Conjecture 01/2020AMS-MAA Joint Mathematics Meetings, Denver, CO AMS Special Session on Recent Trends in Semigroup Theory 9. Apolarity and trivariate piecewise polynomials 08/2019 Algebraic Spline Geometry Meeting, Swansea, United Kingdom 10. Algebraic Approaches to Spline Theory 07/2019SIAM Conference on Applied Algebraic Geometry, Bern, Switzerland Minisymposium on Multivariate Spline Approximation and Algebraic Geometry 11. Asymptotic Resurgence via Integral Closure and Linear Programs 02/2019Southwest Local Algebra Meeting, El Paso, TX 12. Asymptotic Resurgence and Integral Closures 11/2018 AMS Sectional Meeting, Fayetteville, AR Special Session on Interactions Between Combinatorics and Commutative Algebra 13. Freeness of Multi-arrangements via Acyclicity 06/2018Research Institute for Mathematical Sciences (RIMS), Kyoto, Japan Matroids, reflection groups, and free hyperplane arrangements 04/2018 14. A Homological Approach to Freeness of Multi-arrangements AMS Sectional Meeting, Boston, MA Special Session on Arrangements of Hypersurfaces 01/201815. The Toric Ring of a Two-Borel ideal is Koszul

AMS-MAA Joint Mathematics Meetings, San Diego, CA

AMS Special Session on Combinatorial Commutative Algebra and Polytopes

16.	Freeness of Multi-Coxeter Arrangements of type A AMS Sectional Meeting, Denton, TX	09/2017
	Special Session on Algebraic Combinatorics of Flag Varieties	
17.	Splines on planar semi-algebraic partitions	09/2017
	AMS Sectional Meeting, Denton, TX	,
	Special Session on Applicable and Computational Algebraic Geometry	
18.	Algebraic Methods in Spline Theory	08/2017
	SIAM Conference on Applied Algebraic Geometry, Atlanta, GA	,
	Minisymposium on Multivariate Splines and Algebraic Geometry	
19.	Multi-derivations on the moduli of the X_3 arrangement	04/2017
	AMS Sectional Meeting, Pullman, WA	,
	Special Session on Combinatorial and Computational Commutative Algebra and	Algebraic
	Geometry	J
20.	Splines on Tetrahedral Decompositions	05/2016
	15th International Conference on Approximation Theory, San Antonio, TX	/
	Minisymposium on Approximation Theory and Algebraic Geometry	
21.	Generalized Splines and Graphic Multi-Arrangements	10/2015
	AMS Sectional Meeting, Chicago, IL	-0/-0-0
	Special Session on Combinatorial and Computational Algebra	
22	Piecewise Polynomials and Regularity	04/2015
22.	Mathematisches Forschungsinstitut Oberwolfach, Germany	01/2010
	Workshop on Multivariate Splines and Algebraic Geometry	
23	Castelnuovo-Mumford Regularity of Mixed Spline Spaces	01/2015
20.	AMS-MAA Joint Mathematics Meetings, San Antonio, TX	01/2010
	Session on Commutative Algebra	
24	Regularity of Planar Splines	04/2014
27.	AMS Sectional Meeting, Lubbock, TX	04/2014
	Special Session on Commutative Algebra and Algebraic Geometry	
25	Regularity and Piecewise Polynomial Functions	04/2014
20.	KUMUNU jr, Lincoln, NE	04/2014
26	Local Properties of Splines	03/2014
20.	Southwest Local Algebra Meeting, College Station, TX	00/2014
	Graduate Student Poster Session	
27	Lattice-Supported Splines on Polytopal Complexes	01/2014
21.	AMS-MAA Joint Mathematics Meetings, Baltimore, MD	01/2014
20	AMS Special Session on Hyperplane Arrangements and Applications	00/2012
20.	Lattice-Supported Bases for Polyhedral Splines SIAM Conference on Applied Algebraic Geometry, Fort Collins, CO	08/2013
20	Session on Approximation Theory, Geometric Modeling, and Algebraic Geometry	04/0019
29.	Bivariate Continuous Splines on Polyhedral Complexes	04/2013
	14th International Conference on Approximation Theory, San Antonio, TX	
90	Minisymposium on Multivariate Splines	10/0010
30.	Shellability and Freeness of Continuous Splines	10/2012
	AMS Sectional Meeting, Tulane, LA	
	Special Session on Approximation Theory, Geometric Modelling, and Algebraic Ge	
31.	Exploring Gassmann Triples	01/2009
	AMS-MAA Joint Mathematics Meetings	
	Undergraduate Student Poster Session (\$100 prize)	
4	TT7:10:	11 /0000
1.	Wilf's conjecture and its extensions	11/2020
~	Graduate Seminar, Towson University, Towson, MD (virtual due to COVID-19)	00/0000
2.	Resurgence via Asymptotic Resurgence	08/2020
	Algebra and Geometry Seminar, Iowa State University, Ames, IA, (virtual due to CO	DVID-19)

SEMINAR & COLLOQUIUM TALKS

	3.	Extending Wilf's Conjecture	10/2019
	4.	Colloquium, University of North Carolina-Charlotte, Charlotte, NC Multi-derivations of hyperplane arrangements	06/2019
	5.	Mediterranea University of Reggio Calabria, Italy Combinatorics, topology, and algebra of hyperplane arrangements	06/2019
	6	University of Messina, Italy Commutative Algebra and Piecewise Polynomials	02/2018
	0.	Colloquium, Marquette University, Milwaukee, WI	02/2010
	7.	Commutative Algebra and Approximation Theory	01/2018
		Colloquium, University of Nebraska-Lincoln, Lincoln, NE	/
	8.	Homological Obstructions to Freeness of Multi-Arrangements	10/2017
		Geometry Seminar, Texas A&M University, College Station, TX	
	9.	Free Multi-Braid Arrangements and Resolutions	03/2017
		Algebra Seminar, University of Arkansas, Fayetteville, AK	
	10.	Dimensions of Spline Spaces and Commutative Algebra	11/2016
		Colloquium, Towson University, Towson, MD	11/0010
	11.	Two Tales of Freeness	11/2016
	10	Colloquium, US Naval Academy, Annapolis, MD	00/0010
	12.	Multi-Derivations of Braid Arrangements Combinatorica Seminar University of Vances Lawrence VS	09/2016
	19	Combinatorics Seminar, University of Kansas, Lawrence, KS Piecewise Polynomials and Algebraic Geometry	04/2016
	15.	Colloquium, University of Idaho, Moscow, ID	04/2010
	14	Semialgebraic Splines	03/2016
	17.	Valley Geometry Seminar, University of Massachusetts, Amherst, MA	00/2010
	15.	Commutative Algebra meets Approximation Theory	11/2015
		Numerical Analysis Seminar, Oklahoma State University, Stillwater, OK	/
	16.	Commutative Algebra and Approximation Theory	09/2015
		Colloquium, Oklahoma State University, Stillwater, OK	,
	17.	Splines, Syzygies, and Freeness	09/2015
		Algebra Seminar, Oklahoma State University, Stillwater, OK	
	18.	Regularity of Planar Splines	09/2015
		Geometry Seminar, Texas A&M University, College Station, TX	
	19.	Algebraic Geometry and Approximation Theory	02/2015
	20	Colloquium, University of South Florida, Tampa, FL	44 /004 4
	20.	Associated Primes of Complexes Arising in Approximation Theory	11/2014
	91	Commutative Algebra Seminar, UIUC	11/2014
	21.	Castelnuovo-Mumford Regularity in Approximation Theory Algebraic Geometry Seminar, UIUC	11/2014
	22	Lehmer's Picturesque Exponential Sums with a Twist (with Daniel Schultz)	02/2010
	22.	Number Theory Seminar, UIUC	02/2010
		rumber theory benimar, ere o	
TALKS FOR	1	Discouries Linear Functions Projecting Polytones and Familibrium Streeses	11/2019
Talks for Undergraduate	1.	Piecewise Linear Functions, Projecting Polytopes, and Equilibrium Stresses Symposium of Physics and Mathematics FCFM-IFM, Universidad Michoacana de Sa	11/2018
OR HIGH SCHOOL		de Hidalgo, Morelia, Michoacán, Mexico	all Micolas
AUDIENCES	2	Explorations in Rigidity	04/2018
NODILINOLD	۷.	OSU Math Club, Oklahoma State University, Stillwater OK	01/2010
	3.	The Best Way to Divide up a Cheese	10/2017
		High School Math Day, Oklahoma State University, Stillwater OK	,
	4.	The Pizza Cutting Problem	02/2017
		Stillwater High School Math Seminar, Stillwater High School, Stillwater, OK	•
	5.	Counting Piecewise Linear Functions	03/2016
		Center for Women in Mathematics, Smith College, Northampton, MA	

6. Jumping Dimensions and Projecting Polytopes	12/2014
Colloquium, Bradley University, Peoria, IL	
7. Continuous Piecewise Polynomials and Static Equilibrium	10/2014
Rose-Hulman Mathematics Seminar Terra-Haute IN	

Professional Service

Organizer

Postdoc Seminar at CSU, Fall 2020, Spring 2021

Co-organizer (with Nelly Villamizar)

Minisymposium on Algebraic Methods for Multivariate Splines and Rigidity at the SIAM conference on Applied Algebraic Geometry in College Station, Texas, August 2021.

Co-organizer (with Hendrik Speleers and Deepesh Toshniwal)

Minisymposium on Multivariate Splines: Theory and applications at the International Conference on Approximation Theory and Beyond, Nashville, TN, May 2020. (**Delayed due to COVID-19**)

Co-organizer (with Nelly Villamizar)

Minisymposium on Multivariate Spline Approximation and Algebraic Geometry at the SIAM conference on Applied Algebraic Geometry in Bern, Switzerland, July 2019.

Co-organizer (with Frank Sottile)

Minisymposium on Multivariate Splines and Algebraic Geometry at the SIAM conference on Applied Algebraic Geometry in Atlanta, GA, August 2017.

Co-organizer (with Tatyana Sorokina)

Minisymposium on Approximation Theory and Algebraic Geometry at the 15th International Conference on Approximation Theory in San Antonio, TX, May 2016.

Organizer

reading seminar on The Geometry of Syzygies in Fall 2011, Spring 2012

Referee

Mathematische Annalen, Journal of Pure and Applied Algebra, International Journal of Algebra and Computation, Pacific Journal of Mathematics, Constructive Approximation, Computer-Aided Geometric Design, Journal of Algebraic Combinatorics, Graphs and Combinatorics, Proceedings of 15th International Conference on Approximation Theory

Reviewer

Zentralblatt MATH, Mathematical Reviews

Funded Awards	Bourgain Fellowship, UIUC REGS Summer Fellowships, UIUC REU Summer Fellowships, UNC Asheville & LSU	Spring 2013 Summer 2009-2013 Summer 2008-2009
Conference- Specific	US Junior Oberwolfach Fellows grant to attend MFO workshop in Oberwolfach, Germany (not used since the cor	01/2020 aference was virtual)
Grants	SIAM Early Career Travel Award	07/2019
	to attend SIAM Conference on Applied Algebraic Geometry in Bern, Switz Supported Participant	erland 05/2017
	at CMO Workshop on Symbolic and Ordinary Powers in Oaxaca, Mexico	05/2011
	Oberwolfach Liebniz Graduate Students grant	04/2015
	to present at MFO workshop in Oberwolfach, Germany	
	AMS Student Travel Grant	04/2014
	for presentation at AMS Sectional Meeting at Texas Tech	
	AMS Student Travel Grant	01/2014
	for presentation at AMS-MAA Joint Mathematics Meetings	
	Student Travel Award	08/2013
	to attend SIAM Conference on Applied Algebraic Geometry in Fort Collins	s, CO
	Travel Award	04/2013

for presentation at 14th International Conference on Approximation Theory

	Supported Participant	utativa Algabra	12/2012
at MSRI Workshop on Combinatorial Commutative Algebra AMS Student Travel Grant		10/2012	
	for presentation at the AMS Sectional Meeting Supported Participant at IMA summer school in Applied Algebraic		06-07/2012
Selected MFO workshop on Logarithmic Vector Fields and Freeness of Divisors and Arrangements: New perspectives and applications			01/2021
ATTENDED	Oberwolfach, Germany Macaulay 2 workshop on coding in the comp Berkeley, CA	uter algebra system Macaulay2	07/2017
	CMO workshop on Ordinary and Symbolic Po Oaxaca, Mexico	owers of Ideals	05/2017
	Macaulay2 workshop on coding in the compu	iter algebra system Macaulay2	05/2015
	Boise, ID MFO workshop on Multivariate Splines and Algebraic Geometry		
	Oberwolfach, Germany MSRI workshop on Combinatorial Commutative Algebra		
	San Francisco, CA IMA summer school in Applied Algebraic Geometry at Georgia Tech Atlanta, GA		
Professional Memberships	American Mathematical Society Society for Industrial and Applied Mathematics Member of activity group on applied algebrai		
REFERENCES	Hal Schenck Auburn University hks0015@auburn.edu Chris Peterson Colorado State University peterson@math.colostate.edu Jeffrey Mermin Oklahoma State University mermin@math.okstate.edu	Frank Sottile Texas A&M University sottile@math.tamu.edu Jess Ellis Hagman Colorado State University jess.ellis@colostate.edu	