

## 983 Minimum Cost For Tickets

$dp[x]$  is min cost to travel for  $1 \dots x$

$$dp[0] = 0$$

$$n = (\max(\text{days}) + 1)$$

if particular day has to be travelled we will purchase pass to minimize cost but if we don't have to travel on that day then

$$\underline{dp[x] = dp[x-1]}$$

if we have to travel on that day

$$dp[x] = \min \left[ \begin{array}{l} dp[x-1] + \text{costs}[0], \\ dp[x-2] + \text{costs}[1], \\ dp[x-3] + \text{costs}[2] \end{array} \right]$$

Basic formula

for  $x$  in range  $(1, \text{len}(dp))$ :

- if  $x$  in days:

if  $x \geq 30$

$dp[x] = \min$

$$\left[ \begin{array}{l} dp[x-1] + \text{costs}[0], \\ dp[x-7] + \text{costs}[1], \\ dp[x-30] + \text{costs}[2] \end{array} \right]$$

elif  $x \geq 1$  and  $x < 30$

$dp[x] = \min$

$$\left[ \begin{array}{l} dp[x-1] + \text{costs}[0], \\ dp[x-7] + \text{costs}[1], \\ \text{costs}[2] \end{array} \right]$$

we can just  
purchase a full  
month pass if  
its cheap and  
room on all  
days

elif  $x \geq 1$  and  $x < 7$

$dp[x] = \min$

$$\left[ \begin{array}{l} dp[x-1] + \text{costs}[0], \\ \text{costs}[1], \\ \text{costs}[2] \end{array} \right]$$

else:

$$dp[x] = dp[x-1]$$

Basically

subproblem is find min cost for

1..1

1..2

1..3

1..n

all are subproblems

$dp(2)$  represents

$dp(3)$  represents

1..2 } days

1 2 3 } days

$dp(2)$  + cost of 1 day ticket,

cost of 7 day ticket,

cost of monthly ticket

$\therefore dp(3) = \min$