

$$\bar{x} = \frac{1}{n} \sum x_i$$

$$E[\bar{x}] = ?$$

$$= E\left[\frac{1}{n} \sum_{i=1}^n x_i\right]$$

$$= \frac{1}{n} E\left[\sum_{i=1}^n x_i\right]$$

$$= \frac{1}{n} E[x_1 + x_2 + x_3 \dots + x_n]$$

if  $X$  is i.i.d., then

$$x_1 = x_2 = x_3$$

$$= \frac{1}{n} E[x + x + x]$$

$$= \frac{1}{n} E[nx]$$

$$= \frac{n}{n} E[x]$$