

## HW1 (Score: 17.0 / 20.0)

1. [Written response](#) (Score: 1.0 / 1.0)
2. [Comment](#)
3. [Test cell](#) (Score: 2.0 / 2.0)
4. [Comment](#)
5. [Test cell](#) (Score: 1.0 / 2.0)
6. [Comment](#)
7. [Test cell](#) (Score: 1.5 / 2.0)
8. [Coding free-response](#) (Score: 6.0 / 6.0)
9. [Comment](#)
10. [Task](#) (Score: 5.5 / 7.0)
11. [Comment](#)
12. [Coding free-response](#) (Score: 0.0 / 0.0)

# DATA 601: Fall 2019

## HW1

**Due: Wed. Sep. 18 at 23:55**

### Learning Objectives

- Gain familiarity with Markdown.
- Explore collection classes in Python.
- Use intermediate level data structures and programming concepts in the context of data related problems.

*This is an individual homework assignment.*

Please complete this homework assignment within the Jupyter notebook environment.

### Submission

Your submission will be graded using a combination of auto-grading and manual grading. In order to ensure that everything goes smoothly, please follow these instructions:

- Please provide your solutions where asked; please do not alter any other parts of this notebook.
- Submit via the HW1 dropbox on D2L. Please ensure that your submitted file is named 'HW1.ipynb'.
- Do not submit any other files.

## Question 1: Markdown

(1 point)

Please go through the following Markdown tutorial:

<https://www.markdowntutorial.com/> (<https://www.markdowntutorial.com/>).

In the cell below, use Markdown to typeset your name at heading level 3 and your student ID at heading level 4.

(Top)

**Michael Ellsworth**

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## Question 2: List Processing

(6 points)

The questions below ask you to process data stored in lists. To focus on problem solving and to make your code more readable, *you may use built-in functions*. Please try and use comprehensions whenever possible.

1. Given two lists, write a Python function called `myprod(l1, l2)` that produces a list containing all possible pairings — as tuples — of the elements in the two lists, i.e. the Cartesian product of the two lists. The first element of each tuple should come from `l1` and the second element should come from `l2`. You can assume that the lists will not have any duplicates.

For example, the Cartesian product of the two lists `['A', 'K', 'Q', 'J', '10', '9', '8', '7', '6', '5', '4', '3', '2']` and `['♠', '♥', '♦', '♣']` should yield a standard deck of playing cards.

In [1]:

(Top)

```
def myprod(l1, l2):
    new_list = [(l1[i], l2[j]) for i in range(len(l1)) for j in
range(len(l2))]
    return new_list
    raise NotImplementedError()
```

**Comments:**

raise NotImplementedError() is redundant, and this could have easily been condensed to a single line. No marks lost for that, though.

In [2]:

myprod\_test

(Top)

```
'''Check that myprod produces the correct output.'''

l1 = ['A', 'K', 'Q', 'J', '10', '9', '8', '7', '6', '5', '4',
'3', '2']
l2 = ['♠', '♥', '♦', '♣']
assert set(myprod(l1,l2)) == {
    ('A', '♠'), ('A', '♥'), ('A', '♦'), ('A', '♣'), \
    ('K', '♠'), ('K', '♥'), ('K', '♦'), ('K', '♣'), \
    ('Q', '♠'), ('Q', '♥'), ('Q', '♦'), ('Q', '♣'), \
    ('J', '♠'), ('J', '♥'), ('J', '♦'), ('J', '♣'), \
    ('10', '♠'), ('10', '♥'), ('10', '♦'), ('10', '♣'), \
    ('9', '♠'), ('9', '♥'), ('9', '♦'), ('9', '♣'), \
    ('8', '♠'), ('8', '♥'), ('8', '♦'), ('8', '♣'), \
    ('7', '♠'), ('7', '♥'), ('7', '♦'), ('7', '♣'), \
    ('6', '♠'), ('6', '♥'), ('6', '♦'), ('6', '♣'), \
    ('5', '♠'), ('5', '♥'), ('5', '♦'), ('5', '♣'), \
    ('4', '♠'), ('4', '♥'), ('4', '♦'), ('4', '♣'), \
    ('3', '♠'), ('3', '♥'), ('3', '♦'), ('3', '♣'), \
    ('2', '♠'), ('2', '♥'), ('2', '♦'), ('2', '♣')}
```

1. Write a Python function called `mytally( li )` that takes a list `li` and returns a dictionary whose keys are the unique entries in `li` and whose values are the counts of each of the unique entries. For example:

```
mytally( [1, 2, 3, 3, 4, 5, 6, 6, 6, 7, 8, 9, 9] )
```

should return

```
{1:1, 2:1, 3:2, 4:1, 5:1, 6:3, 7:1, 8:1, 9:2}
```

In [3]:

(Top)

```
def mytally( li ):
    import numpy as np
    l1 = np.unique(li)
    l2 = [0] * len(l1)
    for i in range(len(l1)):
        for j in range(len(li)):
            if l1[i] == li[j]:
                l2[i] += 1
    return dict(zip(l1, l2))
    raise NotImplementedError()
```

**Comments:**

This algorithm works, but its performance is  $O(n^2)$  when for loops are capable of  $O(n)$ . It also relies on `numpy`, which is not a built-in function.

In [4]:

mytally\_test

(Top)

```
'''Check that mytally returns the correct output'''
assert mytally([1, 2, 3, 3, 4, 5, 6, 6, 6, 7, 8, 9, 9]) == \
    {1: 1, 2: 1, 3: 2, 4: 1, 5: 1, 6: 3, 7: 1, 8: 1, 9: 2}
assert mytally(list('mississippi')) == \
    {'i': 4, 'm': 1, 'p': 2, 's': 4}
import random
random.seed(a=601, version=2)
assert mytally( [random.randint(0,10) for i in range(10000)] ) =
= \
    {0:855, 1:895, 2:946, 3:961, 4:840, 5:941, 6:875, 7:916, 8:9
32, 9:910, 10:929}
```

1. Write a function called `mysplit( li )` that takes a list `li` and splits it into sublists consisting of runs of identical elements. The returned list should be sorted in ascending order. You may assume that `li` consists of immutable and comparable objects. For example:

```
mysplit( [1, 2, 3, 3, 4, 5, 6, 6, 6, 7, 8, 9, 9] )
```

should return

```
[[1], [2], [3,3], [4], [5], [6,6,6], [7], [8], [9,9]]
```

In [5]:

(Top)

```
def mysplit( li ):
    import numpy as np
    li.sort()
    l1 = [[] for x in range(len(np.unique(li)))]
    l2 = list(np.unique(li))
    for i in range(len(l1)):
        for j in li:
            if j == l2[i]:
                l1[i].append(j)
    return l1
raise NotImplementedError()
```

**Comments:**

This algorithm has a side-effect: it alters the list it was given. You should either flag that via documentation, or alter the code to sort a copy of the original.

In [6]:

mysplit\_test

(Top)

```
'''Check that mysplit produces the correct result'''
tlist = [1, 2, 3, 3, 4, 5, 6, 6, 6, 7, 8, 9, 9]
assert mysplit(tlist) == [[1], [2], [3,3], [4], [5], [6,6,6], [7], [8], [9,9]]
assert mysplit(tlist[::-1]) == [[1], [2], [3,3], [4], [5], [6,6,6], [7], [8], [9,9]]
assert mysplit(list('mississippi')) == \
    [list("iiii"), list("m"), list("pp"), list("ssss")]
```

## Question 3: Plotting Functions

(6 points)

Please go through the following tutorial, focusing on the first two sections.

[https://matplotlib.org/users/pyplot\\_tutorial.html](https://matplotlib.org/users/pyplot_tutorial.html) ([https://matplotlib.org/users/pyplot\\_tutorial.html](https://matplotlib.org/users/pyplot_tutorial.html))

Use `matplotlib.pyplot.plot` ([https://matplotlib.org/users/pyplot\\_tutorial.html](https://matplotlib.org/users/pyplot_tutorial.html)) to plot the following sequences for  $2 \leq n \leq 100$ .

a)  $f_n = n^2$

b)  $f_n = \log_2 n$

(Use `math.log2(x)` to compute base 2 logarithms. You will need to `import math` )

c)  $f_n = \begin{cases} \frac{4}{n^2\pi^2} & \text{if } n \text{ is odd,} \\ 0 & \text{otherwise.} \end{cases}$  (Use `math.pi` for  $\pi$ . You will need to `import math` )

In order to compare the relative growth rates, **please plot within the same figure**. Use different line styles so that the sequences can be distinguished, and label your axes appropriately. Please also use logarithmic scaling on the vertical axis ( `plt.yscale( 'log' )` ) so that the relative magnitudes of the sequences is more apparent.

In [7]:

(Top)

```
#####  
import matplotlib.pyplot as plt  
import math  
  
# Define plot range  $2 \leq n \leq 100$   
plot_range = list(range(2, 101))  
  
# a  
def square(n):  
    return n**2  
squares = []  
for n in plot_range:  
    squares.append(square(n))  
  
# b  
def log_base_2(n):  
    return math.log2(n)  
logs = []  
for n in plot_range:  
    logs.append(log_base_2(n))  
  
# c  
def step(n):  
    if n % 2 == 1:  
        return 4 / ((n**2) * (math.pi**2))  
    else:  
        return 0  
steps = []  
for n in plot_range:  
    steps.append(step(n))  
  
plt.plot(plot_range, squares, 'r')  
plt.plot(plot_range, logs, 'b--')  
plt.plot(plot_range, steps, 'g')  
  
plt.yscale('log')  
  
plt.title('Plotting Functions')  
plt.xlabel('n')  
plt.ylabel('fn')  
  
plt.show()  
raise NotImplementedError()
```

**Comments:**

I'd prefer a legend, but the three functions are distinct enough that it's not necessary.

<Figure size 640x480 with 1 Axes>

```
-----  
-----  
NotImplementedError                                Traceback (most recent  
    call last)  
<ipython-input-7-be5cb0728953> in <module>  
    41  
    42 plt.show()  
----> 43 raise NotImplementedError()  
  
NotImplementedError:
```

(Top)

## Question 4: Estimating a Binomial Distribution

(7 points)

This question asks you to empirically estimate a binomial distribution by simulating binomial trials. A high-level description of the tasks that you need to perform is provided below. You will need to think about suitable data structures and programming constructs that will accomplish the tasks. You may use [built-in \(https://docs.python.org/3/library/functions.html\)](https://docs.python.org/3/library/functions.html) functions.

1. Write a function to simulate a binomial experiment. Your function should return the number of successes in  $n$  repeated trials where the probability of success for each trial is  $p$ . Take  $n = 40$  and  $p = 0.5$ . Use a random number generator to determine if the outcome is a success or a failure. Let  $\xi$  be a uniformly distributed random number in the range  $[0, 1)$ . If  $\xi < p$ , then the outcome is a success, otherwise it is a failure. You can use `math.random.random()` to generate a uniformly distributed random float in the range  $[0, 1)$ .
2. Repeat the above experiment  $N$  times to determine an empirical distribution corresponding to the probability of  $k$  success in  $n$  trials. Determine two empirical distributions by taking  $N = 10^3$  and  $N = 10^6$ .
3. On the same figure, plot the empirical distributions corresponding to  $N = 10^3$  and  $N = 10^6$ . For comparison, also plot the true binomial distribution for this scenario. How do the empirical distributions compare to the true distribution?

Please answer this question by inserting one or more code cells below. Please use a Markdown cell to explain your findings.

### Comments:

No Markdown cell was supplied. By relying on dictionary keys, the frequency of values of  $k$  that were never seen were never plotted, even though we know their frequency. As the charts overlap each other significantly, a legend would have been helpful. Kudos on code reuse, though.



In [8]:

(Top)

```

# Import random to generate random number
import random

# Create binomial experiment function
def binom_func(n):
    counter = 0
    stop = 0
    while stop < n:
        stop += 1
        if random.random() < 0.5:
            counter += 1
    return counter
print(binom_func(40))

# Create simulated binomial experiment
def simulate_binom(N, n):
    result = []
    for i in range(N):
        result.append(binom_func(n))
    dict = mytally(result) # ensure func "mytally" is loaded before running
    dict2 = {key: val / N for key, val in dict.items()}
    return dict2

# Repeat experiment  $N = 10^3$  and  $N = 10^6$ 
N10_3 = simulate_binom(10**3, 40)
N10_6 = simulate_binom(10**6, 40)
print(N10_3)
print(N10_6)

# Create binomial curve function using  $n = 40$ ,  $p = 0.5$ 
import math

def binom(k):
    prob = (math.factorial(40) / (math.factorial(40 - k) * math.factorial(k))) * 0.5**k * (1 - 0.5)**(40 - k)
    return prob

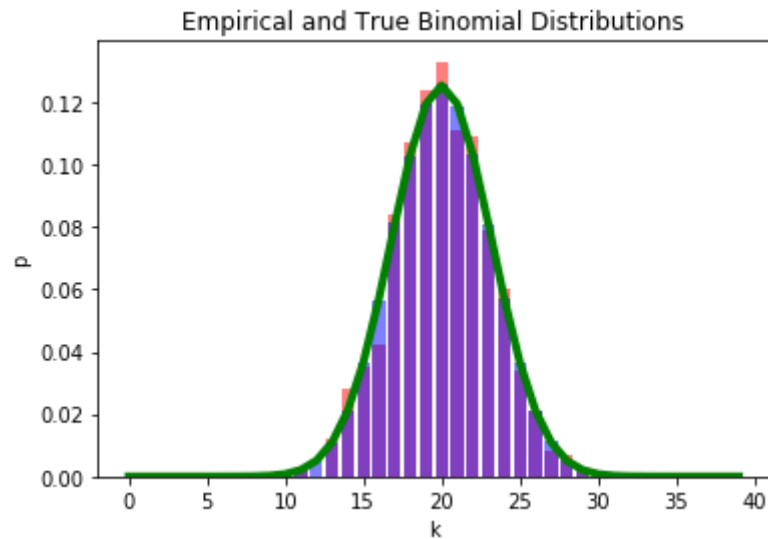
# For binom curve function
seq_k = list(range(40))
seq = []
for k in seq_k:
    seq.append(binom(k))

# Plot the two empirical distributions with the true binomial distribution
import matplotlib.pyplot as plt
plt.bar(N10_3.keys(), N10_3.values(), color='r', alpha = 0.5)
plt.bar(N10_6.keys(), N10_6.values(), color='b', alpha = 0.5)
plt.plot(seq_k, seq, 'g', linewidth = 4)
plt.title('Empirical and True Binomial Distributions')
plt.ylabel('p')
plt.xlabel('k')

plt.show()

```

```
{10: 0.002, 11: 0.002, 13: 0.012, 14: 0.028, 15: 0.035, 16: 0.042, 17: 0.084, 18: 0.107, 19: 0.124, 20: 0.133, 21: 0.111, 22: 0.109, 23: 0.079, 24: 0.06, 25: 0.034, 26: 0.021, 27: 0.008, 28: 0.007, 29: 0.002}
{5: 2e-06, 6: 5e-06, 7: 1.4e-05, 8: 7.9e-05, 9: 0.000244, 10: 0.00074, 11: 0.002068, 12: 0.005138, 13: 0.01087, 14: 0.021078, 15: 0.036399, 16: 0.056615, 17: 0.081179, 18: 0.102746, 19: 0.119471, 20: 0.126065, 21: 0.119001, 22: 0.103154, 23: 0.081054, 24: 0.057297, 25: 0.036494, 26: 0.020817, 27: 0.011197, 28: 0.005063, 29: 0.002052, 30: 0.00079, 31: 0.000259, 32: 8e-05, 33: 2.5e-05, 34: 4e-06}
```



In [ ]: