[STAT 4400] HW-5

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```
library(lme4)
library(ggplot2)
df <- read.table(file = "/Users/Home/Documents/Michael Ghattas/School/</pre>
CU Boulder/2022/Spring 2022/STAT - 4400/Data/apt.txt", header = TRUE)
head(df)
         defects
                     poor race floor dist bldg
##
## 1 1 0.0000000 2.000000
                                             1
                                   2
## 2 0 1.0000000 4.000000
                                        1
                                             1
                             4
## 3 0 0.0000000 1.000000
                             3
                                   2
                                        1
                                             1
                             4
                                   2
## 4 0 1.0000000 2.000000
                                        1
                                             1
                            2
## 5 0 0.2320124 2.325472
                                   3
                                             2
                                        1
## 6 1 1.0000000 3.000000
                             2
                                   2
                                        1
                                             3
(a)
m1 \leftarrow lmer(v \sim dist + (0 + dist | race), data = df)
summary(m1)
## Linear mixed model fit by REML ['lmerMod']
## Formula: y ~ dist + (0 + dist | race)
##
      Data: df
##
## REML criterion at convergence: 14577.2
##
## Scaled residuals:
##
        Min
                  10
                       Median
                                    30
                                            Max
## -0.91090 -0.75478 -0.38006 0.07048 2.52334
##
## Random effects:
```

```
## Groups
             Name Variance Std.Dev.
## race
             dist 5.638e-06 0.002375
                  1.662e-01 0.407688
## Residual
## Number of obs: 13931, groups: race, 7
##
## Fixed effects.
##
                 Estimate Std. Error t value
## (Intercept) 0.3723157 0.0075180 49.523
## dist
               -0.0036107 0.0009787 -3.689
##
## Correlation of Fixed Effects:
        (Intr)
## dist -0.210
(b)
m2 \leftarrow lmer(y \sim dist + (1 + dist | race), data = df)
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
control$checkConv, :
## unable to evaluate scaled gradient
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl =
control$checkConv. :
## Model failed to converge: degenerate Hessian with 1 negative eigenvalues
summary(m2)
## Linear mixed model fit by REML ['lmerMod']
## Formula: y ~ dist + (1 + dist | race)
##
      Data: df
##
## REML criterion at convergence: 14238.4
##
## Scaled residuals:
       Min
                10 Median
##
                                 30
                                        Max
## -1.3293 -0.7025 -0.2874 -0.1619 2.3229
##
## Random effects:
```

```
Groups
                         Variance Std.Dev. Corr
##
             Name
##
    race
             (Intercept) 2.729e-01 0.522387
             dist
##
                         2.453e-05 0.004953 -1.00
##
   Residual
                         1.620e-01 0.402447
## Number of obs: 13931, groups: race, 7
##
## Fixed effects:
##
                Estimate Std. Error t value
## (Intercept) 0.388548
                          0.198228
                                      1.960
## dist
               -0.003893
                           0.001898 -2.052
##
## Correlation of Fixed Effects:
##
        (Intr)
## dist -0.991
## optimizer (nloptwrap) convergence code: 0 (OK)
## unable to evaluate scaled gradient
## Model failed to converge: degenerate Hessian with 1 negative eigenvalues
```

```
library(reshape)
##
## Attaching package: 'reshape'
## The following object is masked from 'package:data.table':
##
## melt
## The following object is masked from 'package:Matrix':
##
## expand
library("stringr")
library(zoo)
filename <- "/Users/Home/Documents/Michael_Ghattas/School/CU_Boulder/2022/
Spring 2022/STAT - 4400/Data/olympics1932.txt"</pre>
```

```
olympics1932 na \leftarrow read.fwf(filename, widths = c(2, 14, 9, 9, 9, 9, 9, 9),
skip = 21, header = FALSE)
colnames(olympics1932 na)<- c("pair", "criterion", "judge 1", "judge 2",</pre>
"judge 3", "judge 4", "judge 5", "judge 6", "judge 7")
olvmpics1932 <- na.locf(olvmpics1932 na)</pre>
olympics1932$criterion <- str trim(olympics1932 na$criterion)</pre>
(a)
arr olym <- melt(data = olympics1932, id.vars = c("pair", "criterion"),</pre>
measure.vars=c(colnames(olvmpics1932)[3:9]))
arr olym
             criterion variable value
##
      pair
## 1
         1
               Program
                       iudge 1
                                   5.6
## 2
         1 Performance judge 1
                                   5.6
## 3
         2
               Program judge 1
                                   5.5
## 4
         2 Performance judge 1
                                   5.5
## 5
         3
               Program judge 1
                                   6.0
## 6
         3 Performance judge 1
                                   6.0
## 7
               Program
                       judge 1
                                   5.6
## 8
         4 Performance judge 1
                                   5.6
## 9
         5
                        judge 1
                                   5.4
               Program
         5 Performance judge_1
## 10
                                   4.8
## 11
         6
               Program
                        judge 1
                                   5.2
## 12
         6 Performance
                        judge 1
                                   4.8
## 13
               Program judge 1
                                   4.8
## 14
         7 Performance
                        judge 1
                                   4.3
## 15
         1
               Program
                       judge 2
                                   5.5
         1 Performance judge_2
## 16
                                   5.5
## 17
         2
               Program
                        judge_2
                                   5.2
                                   5.7
## 18
         2 Performance
                        judge 2
## 19
         3
               Program
                        judge 2
                                   5.3
## 20
         3 Performance
                        judge_2
                                   5.5
## 21
               Program
                        judge 2
                                   5.3
## 22
         4 Performance
                        judge 2
                                   5.3
## 23
               Program
                        judge_2
                                   4.5
## 24
         5 Performance
                        judge 2
                                   4.8
```

```
## 25
                Program
                          judge 2
                                     5.1
         6
## 26
         6 Performance
                          judge 2
                                     5.6
## 27
         7
                Program
                          iudge 2
                                     4.0
## 28
         7 Performance
                          judge 2
                                     4.6
## 29
         1
                Program
                          judge 3
                                     5.8
## 30
         1 Performance
                          judge 3
                                     5.8
## 31
         2
                Program
                          judge 3
                                     5.8
## 32
         2 Performance
                          judge_3
                                     5.6
## 33
         3
                                     5.8
                Program
                          judge 3
## 34
         3 Performance
                          judge 3
                                     5.7
## 35
                Program
                          judge 3
                                     5.8
## 36
         4 Performance
                                     5.8
                          judge_3
## 37
                          judge 3
         5
                Program
                                     5.8
## 38
         5 Performance
                          judge 3
                                     5.5
## 39
         6
                Program
                          judge_3
                                     5.3
## 40
         6 Performance
                          judge 3
                                     5.0
## 41
                                     4.7
         7
                Program
                          judge_3
## 42
         7 Performance
                          judge 3
                                     4.5
## 43
         1
                          judge 4
                                     5.3
                Program
## 44
                                     4.7
         1 Performance
                          judge_4
## 45
         2
                Program
                          judge 4
                                     5.8
## 46
         2 Performance
                          judge 4
                                     5.4
## 47
                          judge_4
         3
                Program
                                     5.0
## 48
         3 Performance
                          judge 4
                                     4.9
## 49
         4
                Program
                          judge_4
                                     4.4
## 50
         4 Performance
                          judge 4
                                     4.8
## 51
         5
                Program
                          judge_4
                                     4.0
## 52
         5 Performance
                          judge 4
                                     4.4
## 53
         6
                Program
                          judge_4
                                     5.4
                                     4.7
## 54
         6 Performance
                          judge_4
## 55
         7
                Program
                          judge_4
                                     4.0
## 56
         7 Performance
                          judge_4
                                     4.0
## 57
                          judge 5
                                     5.6
                Program
## 58
         1 Performance
                          judge_5
                                     5.7
## 59
         2
                Program
                          judge_5
                                     5.6
```

```
## 60
         2 Performance
                          judge 5
                                     5.5
## 61
         3
                Program
                          judge 5
                                     5.4
## 62
         3 Performance
                          iudge 5
                                     5.5
## 63
                Program
                          judge 5
                                     4.5
## 64
         4 Performance
                          judge 5
                                     4.5
## 65
         5
                          judge 5
                                     5.5
                Program
## 66
         5 Performance
                          judge 5
                                     4.6
## 67
                          judge_5
                                     4.5
         6
                Program
## 68
         6 Performance
                                     4.0
                          judge 5
## 69
                Program
                          judge 5
                                     3.7
## 70
         7 Performance
                          judge 5
                                     3.6
## 71
         1
                                     5.2
                Program
                          judge_6
                          judge 6
## 72
         1 Performance
                                     5.3
## 73
         2
                Program
                          judge 6
                                     5.1
## 74
         2 Performance
                          judge_6
                                     5.3
## 75
         3
                Program
                          judge 6
                                     5.1
## 76
         3 Performance
                          judge_6
                                     5.2
## 77
         4
                Program
                          judge 6
                                     5.0
## 78
         4 Performance
                          judge 6
                                     5.0
## 79
         5
                Program
                          judge_6
                                     4.8
## 80
         5 Performance
                          judge 6
                                     4.8
## 81
         6
                Program
                          judge 6
                                     4.5
## 82
         6 Performance
                          judge 6
                                     4.6
## 83
                Program
                          judge_6
         7
                                     4.0
## 84
                          judge_6
         7 Performance
                                     4.0
## 85
         1
                          judge 7
                                     5.7
                Program
## 86
         1 Performance
                          judge_7
                                     5.4
## 87
         2
                Program
                          judge 7
                                     5.8
## 88
         2 Performance
                          judge_7
                                     5.7
## 89
         3
                Program
                          judge_7
                                     5.3
## 90
         3 Performance
                          judge_7
                                     5.7
## 91
                Program
                          judge_7
                                     5.1
## 92
         4 Performance
                          judge 7
                                     5.5
## 93
         5
                Program
                          judge_7
                                     5.5
## 94
         5 Performance
                          judge_7
                                     5.2
```

```
## 95
                        judge 7
                                   5.0
               Program
         6 Performance
## 96
                        iudge 7
                                   5.2
## 97
                        iudge 7
         7
                                   4.8
               Program
## 98
         7 Performance
                         judge 7
                                   4.8
(b)
olym 984 <- arr olym[order(arr olym$variable), ]</pre>
olym_984 <- olym_984[c("criterion", "value", "pair", "variable")]</pre>
olym 984
        criterion value pair variable
##
## 1
          Program
                     5.6
                            1 judge 1
## 2
      Performance
                     5.6
                            1 judge 1
## 3
                     5.5
          Program
                            2 judge 1
## 4
      Performance
                     5.5
                            2 judge 1
## 5
          Program
                     6.0
                            3 judge 1
## 6
      Performance
                     6.0
                            3 judge 1
## 7
                     5.6
                            4 judge_1
          Program
## 8
     Performance
                     5.6
                            4 judge 1
## 9
          Program
                     5.4
                            5 judge_1
## 10 Performance
                     4.8
                            5 judge 1
## 11
                     5.2
                            6 judge 1
          Program
## 12 Performance
                     4.8
                            6 judge_1
## 13
          Program
                     4.8
                            7 judge 1
## 14 Performance
                     4.3
                            7 judge_1
## 15
          Program
                     5.5
                            1 judge_2
## 16 Performance
                     5.5
                            1 judge 2
## 17
                     5.2
                            2 judge_2
          Program
## 18 Performance
                     5.7
                            2 judge 2
                            3 judge 2
## 19
          Program
                     5.3
## 20 Performance
                     5.5
                            3 judge_2
## 21
                     5.3
          Program
                            4 judge 2
## 22 Performance
                     5.3
                            4 judge_2
## 23
          Program
                     4.5
                              judge_2
## 24 Performance
                     4.8
                               judge_2
```

```
## 25
          Program
                     5.1
                                judge 2
## 26 Performance
                     5.6
                                judge 2
## 27
                     4.0
                                iudge 2
          Program
## 28 Performance
                     4.6
                                judge_2
## 29
                     5.8
                                judge 3
          Program
## 30 Performance
                     5.8
                                judge 3
                                judge 3
## 31
          Program
                     5.8
## 32 Performance
                                judge 3
                     5.6
                                judge_3
## 33
                     5.8
          Program
## 34 Performance
                     5.7
                                judge 3
                                judge 3
## 35
          Program
                     5.8
## 36 Performance
                     5.8
                                judge_3
## 37
          Program
                     5.8
                                judge 3
## 38 Performance
                     5.5
                                judge 3
## 39
          Program
                     5.3
                                judge_3
## 40 Performance
                     5.0
                                judge 3
## 41
                     4.7
                                judge_3
          Program
## 42 Performance
                     4.5
                                judge 3
## 43
                     5.3
                                judge 4
          Program
                     4.7
## 44 Performance
                                judge_4
## 45
                                judge_4
          Program
                     5.8
## 46 Performance
                     5.4
                                judge_4
## 47
                     5.0
                                judge_4
          Program
                                judge_4
## 48 Performance
                     4.9
                                judge_4
## 49
          Program
                     4.4
## 50 Performance
                     4.8
                                judge_4
## 51
          Program
                     4.0
                                judge_4
## 52 Performance
                     4.4
                                judge 4
                                judge_4
## 53
                     5.4
          Program
## 54 Performance
                     4.7
                                judge_4
## 55
          Program
                     4.0
                                judge_4
## 56 Performance
                     4.0
                                judge_4
                                judge_5
                     5.6
## 57
          Program
## 58 Performance
                     5.7
                                judge_5
## 59
          Program
                     5.6
                                judge_5
```

```
## 60 Performance
                     5.5
                                judge 5
## 61
          Program
                     5.4
                                judge 5
## 62 Performance
                     5.5
                                iudge 5
## 63
          Program
                     4.5
                                judge_5
## 64 Performance
                     4.5
                                judge 5
## 65
                     5.5
                                judge 5
          Program
                                judge_5
## 66 Performance
                     4.6
## 67
          Program
                     4.5
                                judge 5
## 68 Performance
                     4.0
                                judge_5
                                judge_5
## 69
          Program
                     3.7
                                judge 5
## 70 Performance
                     3.6
## 71
                     5.2
                                judge_6
          Program
## 72 Performance
                     5.3
                                judge 6
## 73
          Program
                     5.1
                                judge 6
## 74 Performance
                     5.3
                                judge_6
## 75
          Program
                     5.1
                                judge 6
## 76 Performance
                     5.2
                                judge 6
## 77
          Program
                     5.0
                                judge 6
## 78 Performance
                     5.0
                                judge 6
## 79
                     4.8
                                judge_6
          Program
                                judge_6
## 80 Performance
                     4.8
## 81
                     4.5
          Program
                                judge_6
## 82 Performance
                                judge_6
                     4.6
                                judge_6
## 83
          Program
                     4.0
                                judge_6
## 84 Performance
                     4.0
## 85
          Program
                     5.7
                                judge_7
## 86 Performance
                     5.4
                                judge_7
## 87
          Program
                     5.8
                                judge 7
## 88 Performance
                     5.7
                                judge_7
## 89
                     5.3
                                judge_7
          Program
## 90 Performance
                     5.7
                                judge_7
## 91
          Program
                     5.1
                                judge_7
## 92 Performance
                     5.5
                                judge_7
## 93
                     5.5
                                judge_7
          Program
## 94 Performance
                     5.2
                                judge_7
```

```
## 95
          Program
                    5.0
                            6 judge 7
                    5.2
## 96 Performance
                            6 iudge 7
## 97
                    4.8
                               iudge 7
          Program
                            7
## 98 Performance
                    4.8
                            7
                               judge 7
olvm 984$SameCountry <- ifelse(olym 984[, 3] == " 1"&olym_984[, 4] ==
"iudge 5", 1, ifelse(olvm 984[, 3] == " 2"&olym 984[, 4] == "judge 7", 1,
  ifelse(olym 984[, 3] == " 3"&olym 984[, 4] == "judge 1", 1,
ifelse(olym 984[, 3] == " 4"&olym 984[, 4] == "judge 1", 1,
  ifelse(olym 984[, 3] == " 7"&olym 984[, 4] == "judge 7", 1, 0)))))
olvm 984
        criterion value pair variable SameCountry
##
                           1 judge_1
## 1
          Program
                    5.6
                                                 0
## 2
      Performance
                    5.6
                                                 0
                               judge 1
## 3
                    5.5
          Program
                            2 judge 1
                                                 0
## 4
     Performance
                    5.5
                            2 judge 1
                                                 0
## 5
          Program
                    6.0
                            3 judge 1
                                                 a
## 6
     Performance
                    6.0
                            3 judge 1
                                                 0
## 7
                                                 0
          Program
                    5.6
                            4 judge 1
## 8
      Performance
                    5.6
                            4 judge 1
                                                 0
                    5.4
                            5 judge 1
## 9
          Program
                                                 0
## 10 Performance
                    4.8
                                                 0
                            5 judge 1
## 11
          Program
                    5.2
                            6 judge 1
                                                 0
## 12 Performance
                    4.8
                            6 judge 1
                                                 0
                    4.8
                                                 0
## 13
          Program
                            7 judge 1
## 14 Performance
                               judge 1
                    4.3
                                                 0
## 15
          Program
                    5.5
                               iudge 2
                                                 0
## 16 Performance
                    5.5
                                                 0
                            1 judge 2
## 17
          Program
                    5.2
                            2 judge 2
                                                 0
                    5.7
## 18 Performance
                            2 judge 2
                                                 0
## 19
                    5.3
                            3 judge_2
                                                 0
          Program
## 20 Performance
                    5.5
                            3 judge 2
                                                 0
## 21
          Program
                    5.3
                            4 judge 2
                                                 0
## 22 Performance
                    5.3
                               judge 2
                                                 0
```

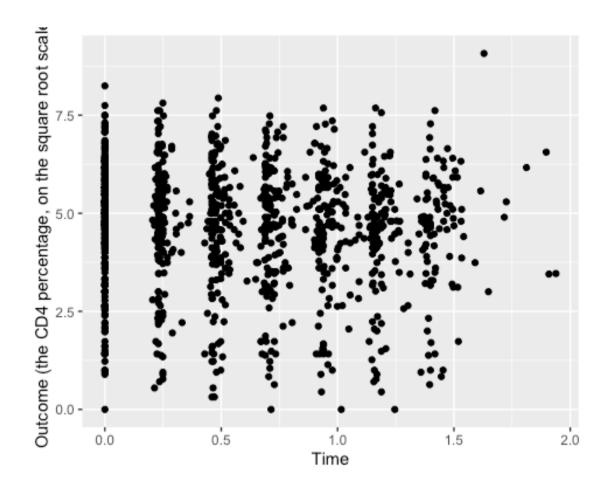
##	23	Program	4.5	5	judge_2	0
##	24	Performance	4.8	5	judge_2	0
##	25	Program	5.1	6	judge_2	0
##	26	Performance	5.6	6	judge_2	0
##	27	Program	4.0	7	judge_2	0
##	28	Performance	4.6	7	judge_2	0
##	29	Program	5.8	1	judge_3	0
##	30	Performance	5.8	1	judge_3	0
##	31	Program	5.8	2	judge_3	0
##	32	Performance	5.6	2	judge_3	0
##	33	Program	5.8	3	judge_3	0
##	34	Performance	5.7	3	judge_3	0
##	35	Program	5.8	4	judge_3	0
##	36	Performance	5.8	4	judge_3	0
##	37	Program	5.8	5	judge_3	0
##	38	Performance	5.5	5	judge_3	0
##	39	Program	5.3	6	judge_3	0
##	40	Performance	5.0	6	judge_3	0
##	41	Program	4.7	7	judge_3	0
##	42	Performance	4.5	7	judge_3	0
##	43	Program	5.3	1	judge_4	0
##	44	Performance	4.7	1	judge_4	0
##	45	Program	5.8	2	judge_4	0
##	46	Performance	5.4	2	judge_4	0
##	47	Program	5.0	3	judge_4	0
##	48	Performance	4.9	3	judge_4	0
##	49	Program	4.4	4	judge_4	0
##	50	Performance	4.8	4	judge_4	0
##	51	Program	4.0	5	judge_4	0
##	52	Performance	4.4	5	judge_4	0
##	53	Program	5.4	6	judge_4	0
##	54	Performance	4.7	6	judge_4	0
##	55	Program	4.0	7	judge_4	0
##	56	Performance	4.0	7	judge_4	0
##	57	Program	5.6	1	judge_5	0

## 58	Performance	5.7	1	judge_5	0
## 59	Program	5.6	2	judge_5	0
## 60	Performance	5.5	2	judge_5	0
## 61	Program	5.4	3	judge_5	0
## 62	Performance	5.5	3	judge_5	0
## 63	Program	4.5	4	judge_5	0
## 64	Performance	4.5	4	judge_5	0
## 65	Program	5.5	5	judge_5	0
## 66	Performance	4.6	5	judge_5	0
## 67	Program	4.5	6	judge_5	0
## 68	Performance	4.0	6	judge_5	0
## 69	Program	3.7	7	judge_5	0
## 70	Performance	3.6	7	judge_5	0
## 71	Program	5.2	1	judge_6	0
## 72	Performance	5.3	1	judge_6	0
## 73	Program	5.1	2	judge_6	0
## 74	Performance	5.3	2	judge_6	0
## 75	Program	5.1	3	judge_6	0
## 76	Performance	5.2	3	judge_6	0
## 77	Program	5.0	4	judge_6	0
## 78	Performance	5.0	4	judge_6	0
## 79	Program	4.8	5	judge_6	0
## 80	Performance	4.8	5	judge_6	0
## 81	Program	4.5	6	judge_6	0
	Performance	4.6	6	judge_6	0
## 83	· ·	4.0	7	judge_6	0
	Performance	4.0	7	judge_6	0
## 85	•	5.7	1	judge_7	0
	Performance	5.4	1	judge_7	0
## 87	· ·	5.8	2	judge_7	0
	Performance	5.7	2	judge_7	0
## 89	•	5.3	3	judge_7	0
	Performance	5.7	3	judge_7	0
## 91	•	5.1	4	judge_7	0
## 92	Performance	5.5	4	judge_7	0

```
## 93
          Program
                     5.5
                            5 judge 7
                                                  a
## 94 Performance
                     5.2
                            5 iudge 7
                                                  a
## 95
          Program
                     5.0
                            6 judge 7
                                                  a
## 96 Performance
                     5.2
                            6 judge 7
                                                  0
## 97
                    4.8
                            7 iudge 7
          Program
                                                  0
## 98 Performance
                    4.8
                               judge 7
                                                  a
```

```
library(tidyverse)
## — Attaching packages
                                                                 tidvverse
1.3.1 -
## ✓ tibble 3.1.6
                            ✓ purrr
                                      0.3.4
## ✓ tidyr
                            ✓ dplyr
             1.2.0.9000
                                      1.0.8
## ✓ readr
             2.1.2
                            ✓ forcats 0.5.1
## Warning: package 'readr' was built under R version 4.1.2
## Warning: package 'dplyr' was built under R version 4.1.2
## - Conflicts -
tidyverse conflicts() —
## x dplyr::between()
                        masks data.table::between()
## x dplyr::combine()
                        masks gridExtra::combine()
## x tidyr::expand()
                        masks reshape::expand(), Matrix::expand()
## x tidyr::extract()
                        masks rstan::extract()
## x dplyr::filter()
                        masks stats::filter()
## x dplyr::first()
                        masks data.table::first()
                        masks stats::lag()
## x dplyr::lag()
## x dplyr::last()
                        masks data.table::last()
## x tidyr::pack()
                        masks Matrix::pack()
## x dplyr::recode()
                        masks car::recode()
## x dplyr::rename()
                        masks reshape::rename()
## x dplyr::select()
                        masks MASS::select()
## x purrr::some()
                        masks car::some()
## x purrr::transpose() masks data.table::transpose()
## x tidyr::unpack()
                        masks Matrix::unpack()
```

```
library(ggvis)
##
## Attaching package: 'ggvis'
## The following object is masked from 'package:Matrix':
##
##
       band
## The following object is masked from 'package:ggplot2':
##
       resolution
##
library(data.table)
hiv.data.raw <- fread("/Users/Home/Documents/Michael Ghattas/School/</pre>
CU Boulder/2022/Spring 2022/STAT - 4400/Data/allvar.csv")
invisible(hiv.data.raw[,ok := !is.na(CD4PCT) ])
hiv.data<-hiv.data.raw[ok==TRUE]</pre>
invisible(hiv.data[,v :=sqrt (CD4PCT)])
# kid's age (yrs) at the beginning of the study
invisible(hiv.data[,age.baseline := baseage ] )
# kids age (yrs) at the time of measurement
invisible(hiv.data[,age.measurement := visage ] )
invisible(hiv.data[,time := visage - baseage ] )
setnames(hiv.data, "treatmnt", "treatment")
hiv.data<-
hiv.data[complete.cases(hiv.data[,list(y,time,age.baseline,treatment)])]
(a)
ggplot(hiv.data) + geom point(aes(x = time, y = y)) + xlab("Time") +
ylab("Outcome (the CD4 percentage, on the square root scale)")
```



```
(b)
r_np \leftarrow lm(y \sim time + factor(newpid) - 1, data = hiv.data)
summary(r_np)
##
## Call:
## lm(formula = y ~ time + factor(newpid) - 1, data = hiv.data)
##
## Residuals:
       Min
                1Q Median
                                 3Q
##
                                         Max
## -3.6595 -0.3293 0.0000 0.3347 4.0036
##
## Coefficients:
                      Estimate Std. Error t value Pr(>|t|)
##
```

```
## time
                      -0.38629
                                   0.05455
                                             -7.081 3.07e-12 ***
                                                    < 2e-16 ***
## factor(newpid)1
                       4.56368
                                   0.34896
                                             13.078
## factor(newpid)2
                       0.81507
                                   0.54578
                                              1,493 0,135716
## factor(newpid)3
                       5.95004
                                   0.29534
                                             20,146
                                                     < 2e-16 ***
## factor(newpid)4
                                             17.722
                                                     < 2e-16 ***
                       5.61374
                                   0.31677
## factor(newpid)5
                                              5.183 2.76e-07 ***
                       4.00000
                                   0.77180
## factor(newpid)6
                       5.36947
                                   0.31738
                                             16.918
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)7
                       5.61896
                                   0.29436
                                             19.088
## factor(newpid)8
                       5.14703
                                   0.38791
                                             13.268
                                                     < 2e-16 ***
## factor(newpid)9
                       6.21645
                                   0.34732
                                             17.898
                                                     < 2e-16 ***
## factor(newpid)10
                                   0.31739
                                                     < 2e-16 ***
                       5.71848
                                             18.017
## factor(newpid)11
                       2,44507
                                   0.29417
                                              8.312 3.89e-16 ***
## factor(newpid)12
                       4.36330
                                   0.31699
                                             13.765
                                                     < 2e-16 ***
## factor(newpid)13
                       5.33903
                                   0.44635
                                             11.962
                                                     < 2e-16 ***
## factor(newpid)14
                       3.00000
                                   0.77180
                                              3.887 0.000110 ***
## factor(newpid)15
                       5.24008
                                   0.31759
                                             16.499
                                                     < 2e-16 ***
## factor(newpid)16
                                   0.38705
                                              6.198 9.03e-10 ***
                       2.39908
## factor(newpid)17
                       6.10066
                                   0.31839
                                             19.161
                                                     < 2e-16 ***
## factor(newpid)18
                                                     < 2e-16 ***
                       6.02588
                                   0.34608
                                             17.412
## factor(newpid)19
                       4.10797
                                   0.38783
                                             10.592
                                                     < 2e-16 ***
## factor(newpid)20
                       5.00962
                                   0.44580
                                             11.237
                                                     < 2e-16 ***
                                             6.478 1.60e-10 ***
## factor(newpid)21
                       5.00000
                                   0.77180
                                             7.987 4.66e-15 ***
## factor(newpid)22
                       6.16441
                                   0.77180
## factor(newpid)23
                       1.59920
                                   0.34723
                                              4.606 4.76e-06 ***
## factor(newpid)24
                       4.81823
                                   0.44728
                                             10.772
                                                     < 2e-16 ***
## factor(newpid)25
                       4.76132
                                   0.31717
                                             15.012
                                                     < 2e-16 ***
## factor(newpid)26
                       4.63303
                                   0.31656
                                             14.636
                                                     < 2e-16 ***
## factor(newpid)27
                       4.38498
                                   0.31672
                                             13.845
                                                     < 2e-16 ***
## factor(newpid)28
                       5.65959
                                   0.54590
                                             10.367
                                                     < 2e-16 ***
## factor(newpid)29
                                   0.38717
                                             11.696
                                                     < 2e-16 ***
                       4.52845
## factor(newpid)30
                                   0.77180
                                             1.296 0.195454
                       1.00000
## factor(newpid)31
                       4.45824
                                   0.54608
                                             8.164 1.22e-15 ***
## factor(newpid)32
                       4.64821
                                   0.34892
                                             13.322
                                                     < 2e-16 ***
## factor(newpid)33
                                             17.108
                                                     < 2e-16 ***
                       5.03494
                                   0.29431
## factor(newpid)34
                       6.49167
                                   0.54579
                                             11.894
                                                     < 2e-16 ***
```

```
## factor(newpid)35
                       4.93661
                                   0.38757
                                            12.737 < 2e-16 ***
                                             7.302 6.72e-13 ***
## factor(newpid)37
                       3.98526
                                   0.54579
                                                     < 2e-16 ***
## factor(newpid)38
                       6.15939
                                   0.44617
                                            13.805
## factor(newpid)39
                       4.84721
                                   0.34613
                                            14,004
                                                     < 2e-16 ***
## factor(newpid)40
                       3.60555
                                             4.672 3.49e-06 ***
                                   0.77180
## factor(newpid)41
                                             6.478 1.60e-10 ***
                       5.00000
                                   0.77180
                                                     < 2e-16 ***
## factor(newpid)42
                       3.26132
                                   0.29446
                                            11.076
                                                     < 2e-16 ***
## factor(newpid)43
                       4.93493
                                   0.29446
                                            16.759
## factor(newpid)44
                       2,49104
                                   0.44579
                                             5.588 3.13e-08 ***
## factor(newpid)45
                       5.16288
                                   0.31782
                                            16.245
                                                     < 2e-16 ***
## factor(newpid)46
                       3.50085
                                   0.31798
                                            11.010
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)47
                       4.85968
                                   0.31796
                                            15.284
## factor(newpid)48
                       4.45407
                                   0.38739
                                            11.498
                                                     < 2e-16 ***
                                            18.339
## factor(newpid)49
                       5.39827
                                   0.29437
                                                     < 2e-16 ***
## factor(newpid)50
                       4.32745
                                   0.29426
                                            14.706
                                                     < 2e-16 ***
## factor(newpid)51
                       3.94551
                                   0.34618
                                            11.397
                                                     < 2e-16 ***
                                             6.109 1.54e-09 ***
## factor(newpid)52
                       1.79719
                                   0.29417
## factor(newpid)53
                       4.81554
                                   0.29411
                                            16.373
                                                     < 2e-16 ***
## factor(newpid)54
                                                     < 2e-16 ***
                       4.46903
                                   0.29419
                                            15.191
                                             8.084 2.24e-15 ***
## factor(newpid)55
                       2.37752
                                   0.29410
## factor(newpid)56
                       2.79201
                                   0.54578
                                             5.116 3.90e-07 ***
                                             6.784 2.24e-11 ***
## factor(newpid)57
                       2.14991
                                   0.31692
                                             6.361 3.32e-10 ***
## factor(newpid)58
                       2.01600
                                   0.31692
## factor(newpid)59
                       5.12724
                                   0.29440
                                            17.416
                                                    < 2e-16 ***
## factor(newpid)60
                       2.04462
                                   0.54578
                                             3.746 0.000192 ***
## factor(newpid)61
                       5.23903
                                   0.31671
                                            16.542
                                                     < 2e-16 ***
## factor(newpid)62
                       5.65826
                                   0.29448
                                            19.215
                                                     < 2e-16 ***
## factor(newpid)63
                       1.92512
                                   0.29426
                                             6.542 1.07e-10 ***
## factor(newpid)64
                       5.42219
                                   0.29418
                                            18.431
                                                     < 2e-16 ***
## factor(newpid)65
                       1.42126
                                   0.34611
                                             4.106 4.42e-05 ***
## factor(newpid)66
                       6.46556
                                   0.44592
                                            14.499
                                                    < 2e-16 ***
## factor(newpid)67
                       2.50677
                                   0.54579
                                             4.593 5.06e-06 ***
                                   0.77180
## factor(newpid)68
                       5.87367
                                             7.610 7.50e-14 ***
## factor(newpid)69
                                            13.766
                                                     < 2e-16 ***
                       5.37708
                                   0.39062
## factor(newpid)70
                       5.04789
                                   0.38676
                                            13.052
                                                     < 2e-16 ***
```

```
## factor(newpid)71
                       2,64575
                                   0.77180
                                              3.428 0.000638 ***
                                                     < 2e-16 ***
## factor(newpid)72
                       3.79504
                                   0.38672
                                              9.813
                                                     < 2e-16 ***
## factor(newpid)73
                       6.85565
                                   0.77180
                                              8.883
## factor(newpid)74
                       5.15287
                                   0.29412
                                            17.519
                                                     < 2e-16 ***
## factor(newpid)75
                                                     < 2e-16 ***
                       5.83766
                                   0.29416
                                            19.845
## factor(newpid)76
                                                     < 2e-16 ***
                       4.92242
                                   0.34748
                                            14.166
## factor(newpid)77
                       4.01660
                                   0.38672
                                             10.386
                                                     < 2e-16 ***
## factor(newpid)78
                       5.99278
                                   0.29415
                                            20.373
                                                     < 2e-16 ***
## factor(newpid)79
                       4.90326
                                   0.44575
                                            11.000
                                                     < 2e-16 ***
## factor(newpid)81
                       0.97153
                                   0.54589
                                              1.780 0.075492 .
## factor(newpid)82
                       3.25905
                                   0.34636
                                              9.409
                                                     < 2e-16 ***
## factor(newpid)83
                       0.94868
                                   0.77180
                                              1,229 0,219356
## factor(newpid)84
                       2.25870
                                   0.34701
                                             6.509 1.32e-10 ***
## factor(newpid)85
                       1.58969
                                   0.34705
                                             4.581 5.36e-06 ***
## factor(newpid)86
                                                     < 2e-16 ***
                       6.44121
                                   0.34644
                                            18.593
## factor(newpid)87
                       6.09731
                                   0.29421
                                             20.724
                                                     < 2e-16 ***
## factor(newpid)88
                                   0.54579
                                                     < 2e-16 ***
                       4.83296
                                              8.855
## factor(newpid)89
                       5.02052
                                   0.34621
                                            14.501
                                                     < 2e-16 ***
## factor(newpid)90
                                              7.577 9.53e-14 ***
                       5.84808
                                   0.77180
                                             6.586 8.09e-11 ***
## factor(newpid)91
                       2.54897
                                   0.38706
## factor(newpid)92
                       2.68623
                                   0.54579
                                             4.922 1.04e-06 ***
                                              3.945 8.64e-05 ***
## factor(newpid)93
                       1.52443
                                   0.38637
## factor(newpid)94
                       4.94328
                                   0.44775
                                            11.040
                                                     < 2e-16 ***
## factor(newpid)95
                       2.78151
                                   0.54578
                                              5.096 4.30e-07 ***
## factor(newpid)96
                       4.89898
                                   0.77180
                                              6.347 3.62e-10 ***
## factor(newpid)97
                       7.70878
                                   0.44671
                                            17.257
                                                     < 2e-16 ***
## factor(newpid)98
                       4.79583
                                   0.77180
                                              6.214 8.22e-10 ***
## factor(newpid)99
                       6.58753
                                   0.38674
                                            17.033
                                                     < 2e-16 ***
## factor(newpid)100
                       6.54584
                                   0.34609
                                            18.914
                                                     < 2e-16 ***
## factor(newpid)101
                                   0.77180
                                              7.329 5.54e-13 ***
                       5.65685
## factor(newpid)103
                                   0.29512
                                            20.708
                                                     < 2e-16 ***
                       6.11117
## factor(newpid)104
                       3.55877
                                   0.31688
                                            11.230
                                                     < 2e-16 ***
## factor(newpid)105
                       4.66845
                                   0.29461
                                            15.846
                                                     < 2e-16 ***
## factor(newpid)106
                                              9.822
                                                     < 2e-16 ***
                       3.79964
                                   0.38686
## factor(newpid)107
                       5.79041
                                   0.38686
                                            14.968
                                                     < 2e-16 ***
```

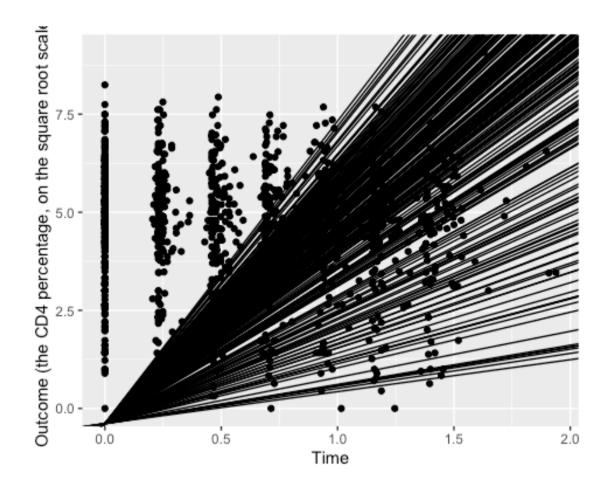
```
## factor(newpid)108
                       1.17737
                                   0.38739
                                              3.039 0.002447 **
## factor(newpid)109
                       4.04447
                                   0.54579
                                              7.410 3.13e-13 ***
## factor(newpid)110
                       5.32304
                                   0.29448
                                                     < 2e-16 ***
                                             18,076
## factor(newpid)111
                       2.13749
                                   0.54580
                                              3.916 9.74e-05 ***
## factor(newpid)112
                       4.04681
                                   0.29465
                                                     < 2e-16 ***
                                             13.734
## factor(newpid)113
                                                     < 2e-16 ***
                       6.34488
                                   0.31739
                                             19.991
                                                     < 2e-16 ***
## factor(newpid)114
                       4.95064
                                   0.29459
                                             16.805
## factor(newpid)115
                                                     < 2e-16 ***
                       5.62952
                                   0.29454
                                             19.113
                                             7.795 1.95e-14 ***
## factor(newpid)116
                       4.25683
                                   0.54612
## factor(newpid)117
                       4.41240
                                   0.34852
                                             12,660
                                                     < 2e-16 ***
## factor(newpid)118
                       5.31355
                                             15.341
                                                     < 2e-16 ***
                                   0.34636
                                              3.534 0.000432 ***
## factor(newpid)119
                       1.92914
                                   0.54582
## factor(newpid)120
                       6.83535
                                   0.31712
                                             21,555
                                                     < 2e-16 ***
## factor(newpid)121
                       6.12904
                                   0.44703
                                             13.711
                                                     < 2e-16 ***
## factor(newpid)122
                       5.43379
                                   0.44651
                                             12.169
                                                     < 2e-16 ***
## factor(newpid)123
                       2.96695
                                   0.54578
                                              5.436 7.18e-08 ***
                                              4.097 4.60e-05 ***
## factor(newpid)124
                                   0.77180
                       3.16228
## factor(newpid)126
                       4.48243
                                   0.38753
                                             11.567
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)127
                       5.25547
                                   0.34628
                                             15.177
                                                     < 2e-16 ***
## factor(newpid)128
                       4.75350
                                   0.54668
                                              8.695
                                              2.825 0.004836 **
## factor(newpid)129
                       0.97864
                                   0.34636
                                                     < 2e-16 ***
## factor(newpid)130
                       3.70472
                                   0.38672
                                              9.580
## factor(newpid)131
                       4.25708
                                   0.38711
                                             10.997
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)132
                       4.73853
                                   0.38778
                                             12.220
## factor(newpid)133
                       3.77490
                                   0.31673
                                             11.918
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)134
                       6.72519
                                   0.29422
                                             22.858
## factor(newpid)135
                       5.60776
                                   0.29440
                                             19.048
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)136
                       6.64977
                                   0.29433
                                             22.593
## factor(newpid)137
                       5.67273
                                   0.29452
                                             19.261
                                                     < 2e-16 ***
## factor(newpid)138
                       7.48331
                                   0.77180
                                                     < 2e-16 ***
                                              9.696
## factor(newpid)139
                       4.85189
                                   0.29479
                                                     < 2e-16 ***
                                             16.459
                                                     < 2e-16 ***
## factor(newpid)140
                       5.47249
                                   0.29452
                                             18.581
                                                     < 2e-16 ***
## factor(newpid)141
                       7.16773
                                   0.29440
                                             24.347
## factor(newpid)142
                                   0.31707
                                                     < 2e-16 ***
                       2.82420
                                              8.907
## factor(newpid)143
                       2.88106
                                   0.29437
                                              9.787
                                                     < 2e-16 ***
```

```
## factor(newpid)144
                       6.04833
                                   0.29423
                                             20.556
                                                      < 2e-16 ***
## factor(newpid)145
                       5.55106
                                   0.31688
                                             17.518
                                                     < 2e-16 ***
## factor(newpid)146
                                                      < 2e-16 ***
                       5,46320
                                   0.31677
                                             17.246
## factor(newpid)147
                       6.18166
                                   0.34655
                                             17.838
                                                      < 2e-16 ***
## factor(newpid)148
                       5.34407
                                             11.988
                                                     < 2e-16 ***
                                   0.44578
                                                      < 2e-16 ***
## factor(newpid)149
                       5.67007
                                   0.34615
                                             16.381
                                                      < 2e-16 ***
## factor(newpid)150
                       4.39422
                                   0.38642
                                             11.372
                                                     < 2e-16 ***
## factor(newpid)151
                       5.68779
                                   0.38640
                                             14.720
                                                    3.33e-09 ***
## factor(newpid)152
                       4.61519
                                   0.77180
                                              5.980
## factor(newpid)153
                       7.21403
                                   0.44577
                                             16.183
                                                     < 2e-16 ***
## factor(newpid)154
                       5.71394
                                   0.44580
                                             12.817
                                                      < 2e-16 ***
                                                      < 2e-16 ***
## factor(newpid)155
                       6.27073
                                   0.44579
                                             14.067
                                                      < 2e-16 ***
## factor(newpid)156
                       6.34439
                                   0.54578
                                             11,624
## factor(newpid)157
                       6.41098
                                   0.44609
                                             14.371
                                                      < 2e-16 ***
## factor(newpid)158
                       6.08632
                                   0.34692
                                             17.544
                                                     < 2e-16 ***
## factor(newpid)159
                                                      < 2e-16 ***
                       5.29916
                                   0.54594
                                              9.706
                                   0.54579
## factor(newpid)160
                       5.04712
                                                      < 2e-16 ***
                                              9.247
                                                     < 2e-16 ***
## factor(newpid)161
                       5.14072
                                   0.38657
                                             13.298
                                                     < 2e-16 ***
## factor(newpid)162
                       4.69277
                                   0.44588
                                             10.525
                                                      < 2e-16 ***
## factor(newpid)163
                       7.42011
                                   0.38647
                                             19.200
## factor(newpid)164
                       7.07418
                                   0.34873
                                             20.286
                                                      < 2e-16 ***
                                                      < 2e-16 ***
## factor(newpid)165
                       4.40042
                                   0.34744
                                             12.665
## factor(newpid)166
                       5.63845
                                   0.54812
                                             10.287
                                                      < 2e-16 ***
                                                      < 2e-16 ***
## factor(newpid)167
                       4.93276
                                   0.38713
                                             12.742
## factor(newpid)168
                       5.79989
                                   0.29425
                                             19.711
                                                     < 2e-16 ***
                                              5.188 2.69e-07 ***
## factor(newpid)169
                       2.83271
                                   0.54605
## factor(newpid)170
                       4.52041
                                   0.34670
                                             13.039
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)171
                       6.70820
                                   0.77180
                                              8.692
## factor(newpid)172
                       5.26891
                                   0.34643
                                             15.209
                                                      < 2e-16 ***
## factor(newpid)173
                       1.59625
                                   0.54592
                                              2.924 0.003551 **
## factor(newpid)174
                       3.80765
                                   0.34709
                                             10.970
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)175
                       5.86770
                                   0.34640
                                             16.939
                                                     < 2e-16 ***
## factor(newpid)176
                       5.71388
                                   0.44591
                                             12.814
## factor(newpid)177
                                             12.022
                                                     < 2e-16 ***
                       4.65448
                                   0.38715
## factor(newpid)178
                       6.64100
                                   0.34712
                                             19.132
                                                     < 2e-16 ***
```

```
## factor(newpid)179
                       5,42868
                                   0.44577
                                             12.178
                                                     < 2e-16 ***
## factor(newpid)180
                       5.38254
                                   0.29417
                                             18.297
                                                     < 2e-16 ***
## factor(newpid)181
                                                     < 2e-16 ***
                       7.58231
                                   0.31737
                                             23.891
## factor(newpid)182
                       6.87445
                                   0.44674
                                             15.388
                                                     < 2e-16 ***
## factor(newpid)183
                                   0.54591
                                                     < 2e-16 ***
                       4.73226
                                              8.669
                                              6.077 1.87e-09 ***
## factor(newpid)184
                       4.69042
                                   0.77180
                                                     < 2e-16 ***
## factor(newpid)185
                       5.32106
                                   0.31790
                                             16.738
                                              6.521 1.22e-10 ***
## factor(newpid)186
                       2.26637
                                   0.34754
                                                     < 2e-16 ***
## factor(newpid)187
                       5.96108
                                   0.31804
                                             18.743
                                                     < 2e-16 ***
## factor(newpid)188
                       5,64729
                                   0.34676
                                             16.286
## factor(newpid)189
                       0.89556
                                   0.54589
                                              1.641 0.101277
                                              7.203 1.34e-12 ***
## factor(newpid)190
                       3.93221
                                   0.54593
## factor(newpid)191
                       4.73072
                                   0.44582
                                             10.611
                                                     < 2e-16 ***
## factor(newpid)192
                       4.63493
                                   0.29415
                                             15.757
                                                     < 2e-16 ***
## factor(newpid)193
                                   0.29414
                                             11.952
                                                     < 2e-16 ***
                       3.51569
                                              5.286 1.60e-07 ***
## factor(newpid)194
                       1.67399
                                   0.31665
## factor(newpid)195
                                   0.44708
                                             14.701
                                                     < 2e-16 ***
                       6.57259
## factor(newpid)196
                       4.28686
                                   0.38778
                                             11.055
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)197
                       4.52015
                                   0.38659
                                             11.692
                                                     < 2e-16 ***
## factor(newpid)198
                       6.11686
                                   0.34677
                                             17.640
## factor(newpid)199
                       3.58154
                                   0.38734
                                              9.247
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)200
                       6.33062
                                   0.31871
                                             19.863
## factor(newpid)201
                       4.88817
                                   0.38837
                                             12.586
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)202
                       6.08433
                                   0.54598
                                             11.144
                                                     < 2e-16 ***
## factor(newpid)203
                       6.31594
                                   0.38792
                                             16.282
                                                     < 2e-16 ***
## factor(newpid)204
                       5.44066
                                   0.38672
                                             14.069
## factor(newpid)205
                       3.66210
                                   0.34771
                                             10.532
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)206
                       5.98915
                                   0.29415
                                             20.361
## factor(newpid)207
                       6.08204
                                   0.31761
                                             19.149
                                                     < 2e-16 ***
## factor(newpid)208
                                   0.34723
                                                     < 2e-16 ***
                       4.17020
                                             12.010
## factor(newpid)209
                       6.43027
                                                     < 2e-16 ***
                                   0.31684
                                             20.295
                                                     < 2e-16 ***
## factor(newpid)210
                       5.21148
                                   0.29412
                                             17.719
                                                      < 2e-16 ***
## factor(newpid)211
                       5.34459
                                   0.29419
                                             18.167
## factor(newpid)212
                                             16.468
                                                     < 2e-16 ***
                       5.21535
                                   0.31670
## factor(newpid)213
                       4.67607
                                   0.44578
                                             10.490
                                                     < 2e-16 ***
```

```
## factor(newpid)214
                       6.54179
                                   0.29428
                                             22,230
                                                     < 2e-16 ***
## factor(newpid)215
                       5.04463
                                   0.31666
                                             15.931
                                                     < 2e-16 ***
## factor(newpid)216
                                                     < 2e-16 ***
                       3.74901
                                   0.34628
                                             10.827
## factor(newpid)217
                       3.09943
                                   0.54578
                                              5.679 1.88e-08 ***
## factor(newpid)218
                       4.76821
                                   0.29420
                                             16.207
                                                     < 2e-16 ***
                                             7.097 2.76e-12 ***
## factor(newpid)219
                       5.47723
                                   0.77180
                                                     < 2e-16 ***
## factor(newpid)220
                       6.34478
                                   0.29424
                                             21.564
                                                     < 2e-16 ***
## factor(newpid)221
                       5.78464
                                   0.31662
                                             18.270
                                                     < 2e-16 ***
## factor(newpid)222
                       5.27235
                                   0.31785
                                             16.587
## factor(newpid)223
                       5.34864
                                   0.31661
                                             16.894
                                                     < 2e-16 ***
## factor(newpid)224
                       3.80821
                                   0.54578
                                              6.978
                                                    6.19e-12 ***
                                                     < 2e-16 ***
## factor(newpid)225
                       6.47400
                                   0.29413
                                             22.010
                                                     < 2e-16 ***
## factor(newpid)226
                       6.85178
                                   0.34695
                                             19.748
## factor(newpid)227
                       6.21616
                                   0.31664
                                             19.631
                                                     < 2e-16 ***
## factor(newpid)228
                                   0.31665
                                                     < 2e-16 ***
                       4.67312
                                             14.758
                                                     < 2e-16 ***
## factor(newpid)229
                       5.25787
                                   0.34628
                                             15.184
## factor(newpid)230
                                                     < 2e-16 ***
                       5.96217
                                   0.34628
                                             17.218
## factor(newpid)231
                       5.95432
                                   0.38653
                                             15.405
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)232
                       6.17519
                                   0.44620
                                             13.840
                                                     < 2e-16 ***
## factor(newpid)233
                       4.36377
                                   0.38636
                                             11.295
## factor(newpid)234
                       6.22240
                                   0.54578
                                             11.401
                                                     < 2e-16 ***
                                             7.193 1.43e-12 ***
## factor(newpid)235
                       3.21066
                                   0.44635
## factor(newpid)236
                       2.83698
                                   0.34674
                                              8.182 1.06e-15 ***
                                                     < 2e-16 ***
## factor(newpid)237
                       5.43365
                                   0.31707
                                             17.137
## factor(newpid)238
                       5.05647
                                   0.38660
                                             13.079
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)239
                       5.54035
                                   0.44593
                                             12.424
## factor(newpid)240
                       3.51138
                                   0.34603
                                             10.148
                                                     < 2e-16 ***
## factor(newpid)241
                       6.11555
                                   0.77180
                                              7.924 7.49e-15 ***
## factor(newpid)242
                       5.16910
                                   0.44592
                                             11.592
                                                     < 2e-16 ***
## factor(newpid)243
                       5.89800
                                             13.213
                                                     < 2e-16 ***
                                   0.44636
## factor(newpid)244
                       5.94175
                                   0.54578
                                             10.887
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)245
                       4.92484
                                   0.38641
                                             12.745
                                                     < 2e-16 ***
## factor(newpid)246
                       5.05558
                                   0.54579
                                              9.263
## factor(newpid)247
                                              6.200 8.92e-10 ***
                       4.78539
                                   0.77180
                                             10.336
## factor(newpid)248
                       5.64132
                                   0.54579
                                                     < 2e-16 ***
```

```
## factor(newpid)249 5.59464
                                0.77180
                                          7.249 9.71e-13 ***
                                         10.691 < 2e-16 ***
## factor(newpid)250 5.83524
                                0.54579
                                          4.848 1.49e-06 ***
## factor(newpid)251 3.74166
                                0.77180
## factor(newpid)252 4.51291
                                0.54582
                                         8.268 5.45e-16 ***
                                          4.672 3.49e-06 ***
## factor(newpid)253 3.60555
                                0.77180
                                          6.878 1.20e-11 ***
## factor(newpid)254 3.75520
                                0.54598
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7718 on 821 degrees of freedom
## Multiple R-squared: 0.9809, Adjusted R-squared: 0.9751
## F-statistic: 168.1 on 251 and 821 DF, p-value: < 2.2e-16
ggplot(aes(x = time, y = y), data = hiv.data) + geom point() +
geom_abline(intercept = coef(r_np)[1], slope = coef(r_np)
[2:length(coef(r np))]) +
  xlab("Time") + ylab("Outcome (the CD4 percentage, on the square root
scale)")
```



```
(c)
r1 <- lm(y ~ time + factor(newpid) - 1, data = hiv.data)
summary(r1)
##
## Call:
## lm(formula = y ~ time + factor(newpid) - 1, data = hiv.data)
##
## Residuals:
                1Q Median
                                3Q
##
       Min
                                       Max
## -3.6595 -0.3293 0.0000 0.3347 4.0036
##
## Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
##
```

```
## time
                      -0.38629
                                   0.05455
                                             -7.081 3.07e-12 ***
                                                    < 2e-16 ***
## factor(newpid)1
                       4.56368
                                   0.34896
                                             13.078
## factor(newpid)2
                       0.81507
                                   0.54578
                                              1,493 0,135716
## factor(newpid)3
                       5.95004
                                   0.29534
                                             20,146
                                                     < 2e-16 ***
## factor(newpid)4
                                             17.722
                                                     < 2e-16 ***
                       5.61374
                                   0.31677
## factor(newpid)5
                                              5.183 2.76e-07 ***
                       4.00000
                                   0.77180
## factor(newpid)6
                       5.36947
                                   0.31738
                                             16.918
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)7
                       5.61896
                                   0.29436
                                             19.088
## factor(newpid)8
                       5.14703
                                   0.38791
                                             13.268
                                                     < 2e-16 ***
## factor(newpid)9
                       6.21645
                                   0.34732
                                             17.898
                                                     < 2e-16 ***
## factor(newpid)10
                                   0.31739
                                                     < 2e-16 ***
                       5.71848
                                             18.017
## factor(newpid)11
                       2,44507
                                   0.29417
                                              8.312 3.89e-16 ***
## factor(newpid)12
                       4.36330
                                   0.31699
                                             13.765
                                                     < 2e-16 ***
## factor(newpid)13
                       5.33903
                                   0.44635
                                             11.962
                                                     < 2e-16 ***
## factor(newpid)14
                       3.00000
                                   0.77180
                                              3.887 0.000110 ***
## factor(newpid)15
                       5.24008
                                   0.31759
                                             16.499
                                                     < 2e-16 ***
## factor(newpid)16
                                   0.38705
                                              6.198 9.03e-10 ***
                       2.39908
## factor(newpid)17
                       6.10066
                                   0.31839
                                             19.161
                                                     < 2e-16 ***
## factor(newpid)18
                                                     < 2e-16 ***
                       6.02588
                                   0.34608
                                             17.412
## factor(newpid)19
                       4.10797
                                   0.38783
                                             10.592
                                                     < 2e-16 ***
## factor(newpid)20
                       5.00962
                                   0.44580
                                             11.237
                                                     < 2e-16 ***
                                             6.478 1.60e-10 ***
## factor(newpid)21
                       5.00000
                                   0.77180
                                             7.987 4.66e-15 ***
## factor(newpid)22
                       6.16441
                                   0.77180
## factor(newpid)23
                       1.59920
                                   0.34723
                                              4.606 4.76e-06 ***
## factor(newpid)24
                       4.81823
                                   0.44728
                                             10.772
                                                     < 2e-16 ***
## factor(newpid)25
                       4.76132
                                   0.31717
                                             15.012
                                                     < 2e-16 ***
## factor(newpid)26
                       4.63303
                                   0.31656
                                             14.636
                                                     < 2e-16 ***
## factor(newpid)27
                       4.38498
                                   0.31672
                                             13.845
                                                     < 2e-16 ***
## factor(newpid)28
                       5.65959
                                   0.54590
                                             10.367
                                                     < 2e-16 ***
## factor(newpid)29
                                   0.38717
                                             11.696
                                                     < 2e-16 ***
                       4.52845
## factor(newpid)30
                                   0.77180
                                             1.296 0.195454
                       1.00000
## factor(newpid)31
                       4.45824
                                   0.54608
                                             8.164 1.22e-15 ***
## factor(newpid)32
                       4.64821
                                   0.34892
                                             13.322
                                                     < 2e-16 ***
## factor(newpid)33
                                             17.108
                                                     < 2e-16 ***
                       5.03494
                                   0.29431
## factor(newpid)34
                       6.49167
                                   0.54579
                                             11.894
                                                     < 2e-16 ***
```

```
## factor(newpid)35
                       4.93661
                                   0.38757
                                            12.737 < 2e-16 ***
                                             7.302 6.72e-13 ***
## factor(newpid)37
                       3.98526
                                   0.54579
                                                     < 2e-16 ***
## factor(newpid)38
                       6.15939
                                   0.44617
                                            13.805
## factor(newpid)39
                       4.84721
                                   0.34613
                                            14,004
                                                     < 2e-16 ***
## factor(newpid)40
                       3.60555
                                             4.672 3.49e-06 ***
                                   0.77180
## factor(newpid)41
                                             6.478 1.60e-10 ***
                       5.00000
                                   0.77180
                                                     < 2e-16 ***
## factor(newpid)42
                       3.26132
                                   0.29446
                                            11.076
                                                     < 2e-16 ***
## factor(newpid)43
                       4.93493
                                   0.29446
                                            16.759
## factor(newpid)44
                       2,49104
                                   0.44579
                                             5.588 3.13e-08 ***
## factor(newpid)45
                       5.16288
                                   0.31782
                                            16.245
                                                     < 2e-16 ***
## factor(newpid)46
                       3.50085
                                   0.31798
                                            11.010
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)47
                       4.85968
                                   0.31796
                                            15.284
## factor(newpid)48
                       4.45407
                                   0.38739
                                            11.498
                                                     < 2e-16 ***
                                            18.339
## factor(newpid)49
                       5.39827
                                   0.29437
                                                     < 2e-16 ***
## factor(newpid)50
                       4.32745
                                   0.29426
                                            14.706
                                                     < 2e-16 ***
## factor(newpid)51
                       3.94551
                                   0.34618
                                            11.397
                                                     < 2e-16 ***
                                             6.109 1.54e-09 ***
## factor(newpid)52
                       1.79719
                                   0.29417
## factor(newpid)53
                       4.81554
                                   0.29411
                                            16.373
                                                     < 2e-16 ***
## factor(newpid)54
                                                     < 2e-16 ***
                       4.46903
                                   0.29419
                                            15.191
                                             8.084 2.24e-15 ***
## factor(newpid)55
                       2.37752
                                   0.29410
## factor(newpid)56
                       2.79201
                                   0.54578
                                             5.116 3.90e-07 ***
                                             6.784 2.24e-11 ***
## factor(newpid)57
                       2.14991
                                   0.31692
                                             6.361 3.32e-10 ***
## factor(newpid)58
                       2.01600
                                   0.31692
## factor(newpid)59
                       5.12724
                                   0.29440
                                            17.416
                                                    < 2e-16 ***
## factor(newpid)60
                       2.04462
                                   0.54578
                                             3.746 0.000192 ***
## factor(newpid)61
                       5.23903
                                   0.31671
                                            16.542
                                                     < 2e-16 ***
## factor(newpid)62
                       5.65826
                                   0.29448
                                            19.215
                                                     < 2e-16 ***
## factor(newpid)63
                       1.92512
                                   0.29426
                                             6.542 1.07e-10 ***
## factor(newpid)64
                       5.42219
                                   0.29418
                                            18.431
                                                     < 2e-16 ***
## factor(newpid)65
                       1.42126
                                   0.34611
                                             4.106 4.42e-05 ***
## factor(newpid)66
                       6.46556
                                   0.44592
                                            14.499
                                                    < 2e-16 ***
## factor(newpid)67
                       2.50677
                                   0.54579
                                             4.593 5.06e-06 ***
                                   0.77180
## factor(newpid)68
                       5.87367
                                             7.610 7.50e-14 ***
## factor(newpid)69
                                            13.766
                                                     < 2e-16 ***
                       5.37708
                                   0.39062
## factor(newpid)70
                       5.04789
                                   0.38676
                                            13.052
                                                     < 2e-16 ***
```

```
## factor(newpid)71
                       2,64575
                                   0.77180
                                              3.428 0.000638 ***
                                                     < 2e-16 ***
## factor(newpid)72
                       3.79504
                                   0.38672
                                              9.813
                                                     < 2e-16 ***
## factor(newpid)73
                       6.85565
                                   0.77180
                                              8.883
## factor(newpid)74
                       5.15287
                                   0.29412
                                            17.519
                                                     < 2e-16 ***
## factor(newpid)75
                                                     < 2e-16 ***
                       5.83766
                                   0.29416
                                            19.845
## factor(newpid)76
                                                     < 2e-16 ***
                       4.92242
                                   0.34748
                                            14.166
## factor(newpid)77
                       4.01660
                                   0.38672
                                             10.386
                                                     < 2e-16 ***
## factor(newpid)78
                       5.99278
                                   0.29415
                                            20.373
                                                     < 2e-16 ***
## factor(newpid)79
                       4.90326
                                   0.44575
                                            11.000
                                                     < 2e-16 ***
## factor(newpid)81
                       0.97153
                                   0.54589
                                              1.780 0.075492 .
## factor(newpid)82
                       3.25905
                                   0.34636
                                              9.409
                                                     < 2e-16 ***
## factor(newpid)83
                       0.94868
                                   0.77180
                                              1,229 0,219356
## factor(newpid)84
                       2.25870
                                   0.34701
                                             6.509 1.32e-10 ***
## factor(newpid)85
                       1.58969
                                   0.34705
                                             4.581 5.36e-06 ***
## factor(newpid)86
                                                     < 2e-16 ***
                       6.44121
                                   0.34644
                                            18.593
## factor(newpid)87
                       6.09731
                                   0.29421
                                             20.724
                                                     < 2e-16 ***
## factor(newpid)88
                                   0.54579
                                                     < 2e-16 ***
                       4.83296
                                              8.855
## factor(newpid)89
                       5.02052
                                   0.34621
                                            14.501
                                                     < 2e-16 ***
## factor(newpid)90
                                              7.577 9.53e-14 ***
                       5.84808
                                   0.77180
                                             6.586 8.09e-11 ***
## factor(newpid)91
                       2.54897
                                   0.38706
## factor(newpid)92
                       2.68623
                                   0.54579
                                             4.922 1.04e-06 ***
                                              3.945 8.64e-05 ***
## factor(newpid)93
                       1.52443
                                   0.38637
## factor(newpid)94
                       4.94328
                                   0.44775
                                            11.040
                                                     < 2e-16 ***
## factor(newpid)95
                       2.78151
                                   0.54578
                                              5.096 4.30e-07 ***
## factor(newpid)96
                       4.89898
                                   0.77180
                                              6.347 3.62e-10 ***
## factor(newpid)97
                       7.70878
                                   0.44671
                                            17.257
                                                     < 2e-16 ***
## factor(newpid)98
                       4.79583
                                   0.77180
                                              6.214 8.22e-10 ***
## factor(newpid)99
                       6.58753
                                   0.38674
                                            17.033
                                                     < 2e-16 ***
## factor(newpid)100
                       6.54584
                                   0.34609
                                            18.914
                                                     < 2e-16 ***
## factor(newpid)101
                                   0.77180
                                              7.329 5.54e-13 ***
                       5.65685
## factor(newpid)103
                                   0.29512
                                            20.708
                                                     < 2e-16 ***
                       6.11117
## factor(newpid)104
                       3.55877
                                   0.31688
                                            11.230
                                                     < 2e-16 ***
## factor(newpid)105
                       4.66845
                                   0.29461
                                            15.846
                                                     < 2e-16 ***
## factor(newpid)106
                                              9.822
                                                     < 2e-16 ***
                       3.79964
                                   0.38686
## factor(newpid)107
                       5.79041
                                   0.38686
                                            14.968
                                                     < 2e-16 ***
```

```
## factor(newpid)108
                       1.17737
                                   0.38739
                                              3.039 0.002447 **
## factor(newpid)109
                       4.04447
                                   0.54579
                                              7.410 3.13e-13 ***
## factor(newpid)110
                       5.32304
                                   0.29448
                                                     < 2e-16 ***
                                             18,076
## factor(newpid)111
                       2.13749
                                   0.54580
                                              3.916 9.74e-05 ***
## factor(newpid)112
                       4.04681
                                   0.29465
                                                     < 2e-16 ***
                                             13.734
## factor(newpid)113
                                                     < 2e-16 ***
                       6.34488
                                   0.31739
                                             19.991
                                                     < 2e-16 ***
## factor(newpid)114
                       4.95064
                                   0.29459
                                             16.805
## factor(newpid)115
                                                     < 2e-16 ***
                       5.62952
                                   0.29454
                                             19.113
                                             7.795 1.95e-14 ***
## factor(newpid)116
                       4.25683
                                   0.54612
## factor(newpid)117
                       4.41240
                                   0.34852
                                             12,660
                                                     < 2e-16 ***
## factor(newpid)118
                       5.31355
                                             15.341
                                                     < 2e-16 ***
                                   0.34636
                                              3.534 0.000432 ***
## factor(newpid)119
                       1.92914
                                   0.54582
## factor(newpid)120
                       6.83535
                                   0.31712
                                             21,555
                                                     < 2e-16 ***
## factor(newpid)121
                       6.12904
                                   0.44703
                                             13.711
                                                     < 2e-16 ***
## factor(newpid)122
                       5.43379
                                   0.44651
                                             12.169
                                                     < 2e-16 ***
## factor(newpid)123
                       2.96695
                                   0.54578
                                              5.436 7.18e-08 ***
                                              4.097 4.60e-05 ***
## factor(newpid)124
                                   0.77180
                       3.16228
## factor(newpid)126
                       4.48243
                                   0.38753
                                             11.567
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)127
                       5.25547
                                   0.34628
                                             15.177
                                                     < 2e-16 ***
## factor(newpid)128
                       4.75350
                                   0.54668
                                              8.695
                                              2.825 0.004836 **
## factor(newpid)129
                       0.97864
                                   0.34636
                                                     < 2e-16 ***
## factor(newpid)130
                       3.70472
                                   0.38672
                                              9.580
## factor(newpid)131
                       4.25708
                                   0.38711
                                             10.997
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)132
                       4.73853
                                   0.38778
                                             12.220
## factor(newpid)133
                       3.77490
                                   0.31673
                                             11.918
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)134
                       6.72519
                                   0.29422
                                             22.858
## factor(newpid)135
                       5.60776
                                   0.29440
                                             19.048
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)136
                       6.64977
                                   0.29433
                                             22.593
## factor(newpid)137
                       5.67273
                                   0.29452
                                             19.261
                                                     < 2e-16 ***
## factor(newpid)138
                       7.48331
                                   0.77180
                                                     < 2e-16 ***
                                              9.696
## factor(newpid)139
                       4.85189
                                   0.29479
                                                     < 2e-16 ***
                                             16.459
                                                     < 2e-16 ***
## factor(newpid)140
                       5.47249
                                   0.29452
                                             18.581
                                                     < 2e-16 ***
## factor(newpid)141
                       7.16773
                                   0.29440
                                             24.347
## factor(newpid)142
                                   0.31707
                                                     < 2e-16 ***
                       2.82420
                                              8.907
## factor(newpid)143
                       2.88106
                                   0.29437
                                              9.787
                                                     < 2e-16 ***
```

```
## factor(newpid)144
                       6.04833
                                   0.29423
                                             20.556
                                                      < 2e-16 ***
## factor(newpid)145
                       5.55106
                                   0.31688
                                             17.518
                                                     < 2e-16 ***
## factor(newpid)146
                                                      < 2e-16 ***
                       5,46320
                                   0.31677
                                             17.246
## factor(newpid)147
                       6.18166
                                   0.34655
                                             17.838
                                                      < 2e-16 ***
## factor(newpid)148
                       5.34407
                                             11.988
                                                     < 2e-16 ***
                                   0.44578
                                                      < 2e-16 ***
## factor(newpid)149
                       5.67007
                                   0.34615
                                             16.381
                                                      < 2e-16 ***
## factor(newpid)150
                       4.39422
                                   0.38642
                                             11.372
                                                     < 2e-16 ***
## factor(newpid)151
                       5.68779
                                   0.38640
                                             14.720
                                                    3.33e-09 ***
## factor(newpid)152
                       4.61519
                                   0.77180
                                              5.980
## factor(newpid)153
                       7.21403
                                   0.44577
                                             16.183
                                                     < 2e-16 ***
## factor(newpid)154
                       5.71394
                                   0.44580
                                             12.817
                                                      < 2e-16 ***
                                                      < 2e-16 ***
## factor(newpid)155
                       6.27073
                                   0.44579
                                             14.067
                                                      < 2e-16 ***
## factor(newpid)156
                       6.34439
                                   0.54578
                                             11,624
## factor(newpid)157
                       6.41098
                                   0.44609
                                             14.371
                                                      < 2e-16 ***
## factor(newpid)158
                       6.08632
                                   0.34692
                                             17.544
                                                     < 2e-16 ***
## factor(newpid)159
                                                      < 2e-16 ***
                       5.29916
                                   0.54594
                                              9.706
                                   0.54579
## factor(newpid)160
                       5.04712
                                                      < 2e-16 ***
                                              9.247
                                                     < 2e-16 ***
## factor(newpid)161
                       5.14072
                                   0.38657
                                             13.298
                                                     < 2e-16 ***
## factor(newpid)162
                       4.69277
                                   0.44588
                                             10.525
                                                      < 2e-16 ***
## factor(newpid)163
                       7.42011
                                   0.38647
                                             19.200
## factor(newpid)164
                       7.07418
                                   0.34873
                                             20.286
                                                      < 2e-16 ***
                                                      < 2e-16 ***
## factor(newpid)165
                       4.40042
                                   0.34744
                                             12.665
## factor(newpid)166
                       5.63845
                                   0.54812
                                             10.287
                                                      < 2e-16 ***
                                                      < 2e-16 ***
## factor(newpid)167
                       4.93276
                                   0.38713
                                             12.742
## factor(newpid)168
                       5.79989
                                   0.29425
                                             19.711
                                                     < 2e-16 ***
                                              5.188 2.69e-07 ***
## factor(newpid)169
                       2.83271
                                   0.54605
## factor(newpid)170
                       4.52041
                                   0.34670
                                             13.039
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)171
                       6.70820
                                   0.77180
                                              8.692
## factor(newpid)172
                       5.26891
                                   0.34643
                                             15.209
                                                      < 2e-16 ***
## factor(newpid)173
                       1.59625
                                   0.54592
                                              2.924 0.003551 **
## factor(newpid)174
                       3.80765
                                   0.34709
                                             10.970
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)175
                       5.86770
                                   0.34640
                                             16.939
                                                     < 2e-16 ***
## factor(newpid)176
                       5.71388
                                   0.44591
                                             12.814
## factor(newpid)177
                                             12.022
                                                     < 2e-16 ***
                       4.65448
                                   0.38715
## factor(newpid)178
                       6.64100
                                   0.34712
                                             19.132
                                                     < 2e-16 ***
```

```
## factor(newpid)179
                       5,42868
                                   0.44577
                                             12.178
                                                     < 2e-16 ***
## factor(newpid)180
                       5.38254
                                   0.29417
                                             18.297
                                                     < 2e-16 ***
## factor(newpid)181
                                                     < 2e-16 ***
                       7.58231
                                   0.31737
                                             23.891
## factor(newpid)182
                       6.87445
                                   0.44674
                                             15.388
                                                     < 2e-16 ***
## factor(newpid)183
                                   0.54591
                                                     < 2e-16 ***
                       4.73226
                                              8.669
                                              6.077 1.87e-09 ***
## factor(newpid)184
                       4.69042
                                   0.77180
                                                     < 2e-16 ***
## factor(newpid)185
                       5.32106
                                   0.31790
                                             16.738
                                              6.521 1.22e-10 ***
## factor(newpid)186
                       2.26637
                                   0.34754
                                                     < 2e-16 ***
## factor(newpid)187
                       5.96108
                                   0.31804
                                             18.743
                                                     < 2e-16 ***
## factor(newpid)188
                       5,64729
                                   0.34676
                                             16.286
## factor(newpid)189
                       0.89556
                                   0.54589
                                              1.641 0.101277
                                              7.203 1.34e-12 ***
## factor(newpid)190
                       3.93221
                                   0.54593
## factor(newpid)191
                       4.73072
                                   0.44582
                                             10.611
                                                     < 2e-16 ***
## factor(newpid)192
                       4.63493
                                   0.29415
                                             15.757
                                                     < 2e-16 ***
## factor(newpid)193
                                   0.29414
                                             11.952
                                                     < 2e-16 ***
                       3.51569
                                              5.286 1.60e-07 ***
## factor(newpid)194
                       1.67399
                                   0.31665
## factor(newpid)195
                                   0.44708
                                             14.701
                                                     < 2e-16 ***
                       6.57259
## factor(newpid)196
                       4.28686
                                   0.38778
                                             11.055
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)197
                       4.52015
                                   0.38659
                                             11.692
                                                     < 2e-16 ***
## factor(newpid)198
                       6.11686
                                   0.34677
                                             17.640
## factor(newpid)199
                       3.58154
                                   0.38734
                                              9.247
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)200
                       6.33062
                                   0.31871
                                             19.863
## factor(newpid)201
                       4.88817
                                   0.38837
                                             12.586
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)202
                       6.08433
                                   0.54598
                                             11.144
                                                     < 2e-16 ***
## factor(newpid)203
                       6.31594
                                   0.38792
                                             16.282
                                                     < 2e-16 ***
## factor(newpid)204
                       5.44066
                                   0.38672
                                             14.069
## factor(newpid)205
                       3.66210
                                   0.34771
                                             10.532
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)206
                       5.98915
                                   0.29415
                                             20.361
## factor(newpid)207
                       6.08204
                                   0.31761
                                             19.149
                                                     < 2e-16 ***
## factor(newpid)208
                                   0.34723
                                                     < 2e-16 ***
                       4.17020
                                             12.010
## factor(newpid)209
                       6.43027
                                                     < 2e-16 ***
                                   0.31684
                                             20.295
                                                     < 2e-16 ***
## factor(newpid)210
                       5.21148
                                   0.29412
                                             17.719
                                                      < 2e-16 ***
## factor(newpid)211
                       5.34459
                                   0.29419
                                             18.167
## factor(newpid)212
                                             16.468
                                                     < 2e-16 ***
                       5.21535
                                   0.31670
## factor(newpid)213
                       4.67607
                                   0.44578
                                             10.490
                                                     < 2e-16 ***
```

```
## factor(newpid)214
                       6.54179
                                   0.29428
                                             22,230
                                                     < 2e-16 ***
## factor(newpid)215
                       5.04463
                                   0.31666
                                             15.931
                                                     < 2e-16 ***
## factor(newpid)216
                                                     < 2e-16 ***
                       3.74901
                                   0.34628
                                             10.827
## factor(newpid)217
                       3.09943
                                   0.54578
                                              5.679 1.88e-08 ***
## factor(newpid)218
                       4.76821
                                   0.29420
                                             16.207
                                                     < 2e-16 ***
                                             7.097 2.76e-12 ***
## factor(newpid)219
                       5.47723
                                   0.77180
                                                     < 2e-16 ***
## factor(newpid)220
                       6.34478
                                   0.29424
                                             21.564
                                                     < 2e-16 ***
## factor(newpid)221
                       5.78464
                                   0.31662
                                             18.270
                                                     < 2e-16 ***
## factor(newpid)222
                       5.27235
                                   0.31785
                                             16.587
## factor(newpid)223
                       5.34864
                                   0.31661
                                             16.894
                                                     < 2e-16 ***
## factor(newpid)224
                       3.80821
                                   0.54578
                                              6.978
                                                    6.19e-12 ***
                                                     < 2e-16 ***
## factor(newpid)225
                       6,47400
                                   0.29413
                                             22.010
                                                     < 2e-16 ***
## factor(newpid)226
                       6.85178
                                   0.34695
                                             19.748
## factor(newpid)227
                       6.21616
                                   0.31664
                                             19.631
                                                     < 2e-16 ***
## factor(newpid)228
                                   0.31665
                                                     < 2e-16 ***
                       4.67312
                                             14.758
                                                     < 2e-16 ***
## factor(newpid)229
                       5.25787
                                   0.34628
                                             15.184
## factor(newpid)230
                                                     < 2e-16 ***
                       5.96217
                                   0.34628
                                             17.218
## factor(newpid)231
                       5.95432
                                   0.38653
                                             15.405
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)232
                       6.17519
                                   0.44620
                                             13.840
                                                     < 2e-16 ***
## factor(newpid)233
                       4.36377
                                   0.38636
                                             11.295
## factor(newpid)234
                       6.22240
                                   0.54578
                                             11.401
                                                     < 2e-16 ***
                                             7.193 1.43e-12 ***
## factor(newpid)235
                       3.21066
                                   0.44635
## factor(newpid)236
                       2.83698
                                   0.34674
                                              8.182 1.06e-15 ***
                                                     < 2e-16 ***
## factor(newpid)237
                       5.43365
                                   0.31707
                                             17.137
## factor(newpid)238
                       5.05647
                                   0.38660
                                             13.079
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)239
                       5.54035
                                   0.44593
                                             12.424
## factor(newpid)240
                       3.51138
                                   0.34603
                                             10.148
                                                     < 2e-16 ***
## factor(newpid)241
                       6.11555
                                   0.77180
                                              7.924 7.49e-15 ***
## factor(newpid)242
                       5.16910
                                   0.44592
                                             11.592
                                                     < 2e-16 ***
## factor(newpid)243
                       5.89800
                                             13.213
                                                     < 2e-16 ***
                                   0.44636
## factor(newpid)244
                       5.94175
                                   0.54578
                                             10.887
                                                     < 2e-16 ***
                                                     < 2e-16 ***
## factor(newpid)245
                       4.92484
                                   0.38641
                                             12.745
                                                     < 2e-16 ***
## factor(newpid)246
                       5.05558
                                   0.54579
                                              9.263
## factor(newpid)247
                                              6.200 8.92e-10 ***
                       4.78539
                                   0.77180
                                             10.336
## factor(newpid)248
                       5.64132
                                   0.54579
                                                     < 2e-16 ***
```

```
## factor(newpid)249 5.59464
                                 0.77180
                                           7.249 9.71e-13 ***
## factor(newpid)250 5.83524
                                 0.54579
                                          10.691 < 2e-16 ***
                                          4.848 1.49e-06 ***
## factor(newpid)251 3.74166
                                 0.77180
## factor(newpid)252 4.51291
                                 0.54582
                                         8.268 5.45e-16 ***
## factor(newpid)253 3.60555
                                         4.672 3.49e-06 ***
                                 0.77180
                                 0.54598 6.878 1.20e-11 ***
## factor(newpid)254 3.75520
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.7718 on 821 degrees of freedom
## Multiple R-squared: 0.9809, Adjusted R-squared: 0.9751
## F-statistic: 168.1 on 251 and 821 DF, p-value: < 2.2e-16
child <- hiv.data %>% select(newpid, age.baseline, treatment)
child <- unique(child)</pre>
r1.coef <- data.frame(child, r1$coefficients[2:length(r1$coefficients)])</pre>
colnames(r1.coef) <- c("newpid", "age.baseline", "treatment", "coef.id")</pre>
rownames(r1.coef) <- 1:250
r1 coef.id <- lm(coef.id ~ age.baseline + factor(treatment), data = r1.coef)
summary(r1 coef.id)
##
## Call:
## lm(formula = coef.id ~ age.baseline + factor(treatment), data = r1.coef)
##
## Residuals:
                10 Median
       Min
                                       Max
##
                                30
## -4.1594 -0.7039 0.2265 1.1215 2.7256
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                  0.18728 27.265 < 2e-16 ***
                       5.10627
## age.baseline
                      -0.12088
                                  0.04023 -3.005 0.00293 **
## factor(treatment)2 0.14558
                                  0.18421 0.790 0.43012
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.455 on 247 degrees of freedom
## Multiple R-squared: 0.03753, Adjusted R-squared: 0.02974
## F-statistic: 4.816 on 2 and 247 DF, p-value: 0.008875
```

```
(a)
```

```
M0 <- lmer (v \sim time + (1 \mid newpid), data = hiv.data)
display(M0)
## lmer(formula = y ~ time + (1 | newpid), data = hiv.data)
##
               coef.est coef.se
## (Intercept) 4.76
                         0.10
## time
               -0.37
                         0.05
##
## Error terms:
## Groups
                         Std.Dev.
             Name
## newpid
            (Intercept) 1.40
## Residual
                         0.77
## ---
## number of obs: 1072, groups: newpid, 250
## AIC = 3148.8, DIC = 3126.9
## deviance = 3133.9
M0.coef <- data.frame(unique(hiv.data$newpid),coef(M0)$newpid)</pre>
colnames(M0.coef) <- c("newpid", "intercept", "time")</pre>
head(coef(M0)$newpid)
##
     (Intercept)
                       time
## 1
        4.557250 -0.3660932
## 2
       1.335566 -0.3660932
## 3
     5.884129 -0.3660932
## 4
     5.561130 -0.3660932
```

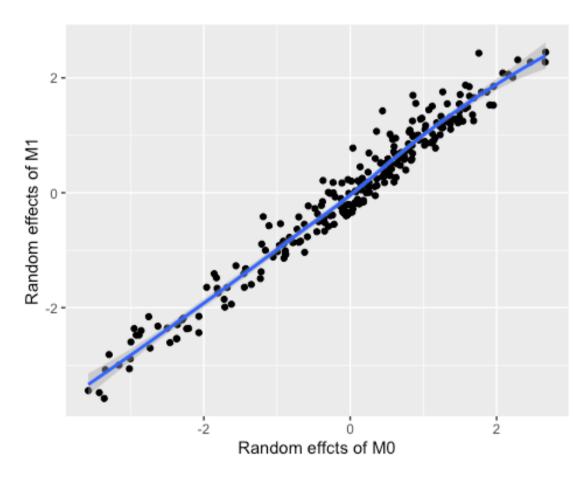
```
## 5 4.178397 -0.3660932
## 6 5.326751 -0.3660932
```

The coefficient for time is \sim (-0.3661), constant across the children. Thus if the time increases by 1 unit, then the CD4 percentage on the square root scale will decrease by \sim (0.3661) units.

```
M1 <- lmer (v ~ time + factor(treatment) + age.baseline + (1 | newpid), data
= hiv.data)
display(M1)
## lmer(formula = y ~ time + factor(treatment) + age.baseline +
       (1 | newpid), data = hiv.data)
##
                      coef.est coef.se
##
## (Intercept)
                       5.09
                                0.19
## time
                      -0.36
                                0.05
## factor(treatment)2 0.18
                                0.18
## age.baseline
                                0.04
                      -0.12
##
## Error terms:
## Groups
                         Std.Dev.
             Name
## newpid
             (Intercept) 1.37
## Residual
                         0.77
## ---
## number of obs: 1072, groups: newpid, 250
## AIC = 3149.2, DIC = 3110.9
## deviance = 3124.1
head(coef(M1)$newpid)
                       time factor(treatment)2 age.baseline
##
     (Intercept)
## 1
        5.012677 -0.3621573
                                     0.1800822
                                                 -0.1194538
        1.607624 -0.3621573
## 2
                                     0.1800822 -0.1194538
## 3
       6.593175 -0.3621573
                                     0.1800822 -0.1194538
## 4
        5.834945 -0.3621573
                                     0.1800822
                                                 -0.1194538
       4.320103 -0.3621573
                                     0.1800822
                                                 -0.1194538
## 5
## 6
        5.499405 -0.3621573
                                     0.1800822
                                                 -0.1194538
```

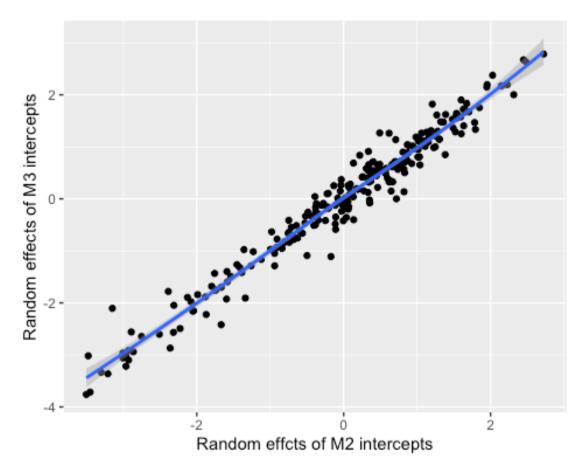
- 1. The coefficients for time, treatment and age.baseline are all constant across the children
- 2. The coefficient for time is \sim (-0.36216), thus if the time increases by 1 unit, then CD4 percentage on the square root scale will decrease by \sim (0.36216) units
- 3. The coefficient for treatment is \sim (0.18008), thus the CD4 percentage on the square root scale for children under treatment 2 is \sim (0.18008) more than treatment 1
- 4. The coefficient for time is \sim (-0.11945), thus if the age.baseline increases by 1 unit, CD4 percentage on the square root scale will decrease by \sim (0.11945) units

```
(c)
data plot <- as.data.frame(cbind(unlist(ranef(M0)), unlist(ranef(M1))))</pre>
colnames(data plot) <- c("M0", "M1")</pre>
ggplot(data = data plot, aes(x = M0, y = M1)) + geom point() + geom smooth() +
xlab("Random effcts of M0") + ylab("Random effects of M1")
## `geom smooth()` using method = 'loess' and formula 'v ~ x'
```



```
display(M0)
## lmer(formula = y ~ time + (1 | newpid), data = hiv.data)
              coef.est coef.se
##
                        0.10
## (Intercept) 4.76
               -0.37
## time
                        0.05
##
## Error terms:
## Groups
            Name
                         Std.Dev.
## newpid
            (Intercept) 1.40
## Residual
                         0.77
## ---
## number of obs: 1072, groups: newpid, 250
```

```
## AIC = 3148.8, DIC = 3126.9
## deviance = 3133.9
display(M1)
## lmer(formula = v ~ time + factor(treatment) + age.baseline +
       (1 | newpid), data = hiv.data)
##
                      coef.est coef.se
##
## (Intercept)
                       5.09
                                0.19
## time
                      -0.36
                                0.05
## factor(treatment)2 0.18
                                0.18
## age.baseline
                      -0.12
                                0.04
##
## Error terms:
## Groups
             Name
                         Std.Dev.
## newpid
             (Intercept) 1.37
## Residual
                         0.77
## ---
## number of obs: 1072, groups: newpid, 250
## AIC = 3149.2, DIC = 3110.9
## deviance = 3124.1
(d)
M2<-lmer(hiv.data$y ~ hiv.data$time + (1 + hiv.data$time | hiv.data$newpid))
M3<-lmer(hiv.data$y ~ factor(hiv.data$time) + (1 | hiv.data$newpid))
data plot2 inter <- as.data.frame(cbind(unlist(ranef(M2))[1:250],</pre>
unlist(ranef(M3))[1:250]))
colnames(data plot2 inter) <- c("M2", "M3")</pre>
ggplot(data = data_plot2_inter, aes(x = M2,y = M3)) + geom_point() +
geom smooth() +
  xlab("Random effcts of M2 intercepts") + ylab("Random effects of M3
intercepts")
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
```



```
display(M2)
## lmer(formula = hiv.data$y ~ hiv.data$time + (1 + hiv.data$time |
       hiv.data$newpid))
##
                 coef.est coef.se
##
## (Intercept)
                  4.76
                           0.09
## hiv.data$time -0.36
                           0.07
##
## Error terms:
  Groups
                    Name
                                   Std.Dev. Corr
    hiv.data$newpid (Intercept)
                                   1.39
##
                    hiv.data$time 0.58
                                           -0.05
                                   0.72
##
    Residual
##
```

```
## number of obs: 1072, groups: hiv.data$newpid, 250
## AIC = 3123.2, DIC = 3098.2
## deviance = 3104.7
display(M3)
## lmer(formula = hiv.data$v ~ factor(hiv.data$time) + (1 | hiv.data$newpid))
                                          coef.est coef.se
##
## (Intercept)
                                           4.77
                                                    0.10
## factor(hiv.data$time)0.205
                                          -1.23
                                                    0.67
## factor(hiv.data$time)0.20999999999999
                                           0.21
                                                    0.89
## factor(hiv.data$time)0.213333333333333
                                           0.16
                                                    0.94
## factor(hiv.data$time)0.2133333333333 -1.20
                                                    0.94
## factor(hiv.data$time)0.21583333333333 1.47
                                                    0.90
## factor(hiv.data$time)0.21583333333333 -0.25
                                                    0.84
## factor(hiv.data$time)0.21666666666667 -0.35
                                                    0.80
## factor(hiv.data$time)0.218333333333334
                                                    0.90
## factor(hiv.data$time)0.21916666666667 -0.48
                                                    0.85
## factor(hiv.data$time)0.22166666666667
                                                    0.94
                                           0.19
## factor(hiv.data$time)0.22416666666666
                                                    0.86
                                           1.65
## factor(hiv.data$time)0.22416666666667 -1.53
                                                    0.63
## factor(hiv.data$time)0.22666666666667
                                                    0.59
## factor(hiv.data$time)0.2274999999999 -1.56
                                                    0.89
## factor(hiv.data$time)0.2275
                                           0.07
                                                    0.46
## factor(hiv.data$time)0.2299999999999 -0.36
                                                    0.59
## factor(hiv.data$time)0.23
                                          -0.11
                                                    0.12
## factor(hiv.data$time)0.2325
                                                    0.40
                                          -0.59
## factor(hiv.data$time)0.233333333333333
                                                    0.84
                                           0.02
## factor(hiv.data$time)0.23500000000001 -1.96
                                                    0.80
## factor(hiv.data$time)0.235833333333333
                                                    0.29
                                           0.04
## factor(hiv.data$time)0.235833333333334
                                           0.18
                                                    0.62
## factor(hiv.data$time)0.2375
                                           1.44
                                                    0.89
## factor(hiv.data$time)0.2383333333333 -0.27
                                                    0.49
## factor(hiv.data$time)0.238333333333334
                                           0.85
                                                    0.82
## factor(hiv.data$time)0.2408333333333 -0.21
                                                    0.78
## factor(hiv.data$time)0.2408333333333 0.34
                                                    0.59
```

```
## factor(hiv.data$time)0.2433333333333 -0.51
                                              0.89
## factor(hiv.data$time)0.244166666666667
                                              0.48
                                      0.09
## factor(hiv.data$time)0.2458333333333333
                                      0.09
                                              0.43
## factor(hiv.data$time)0.24583333333333 -0.25
                                              0.60
0.65
## factor(hiv.data$time)0.24666666666667
                                      0.38
                                              0.85
## factor(hiv.data$time)0.24916666666666
                                      0.15
                                              0.39
## factor(hiv.data$time)0.24916666666667 -0.48
                                              0.19
## factor(hiv.data$time)0.25166666666667
                                              0.43
                                      0.25
## factor(hiv.data$time)0.25166666666668
                                      0.31
                                              0.80
## factor(hiv.data$time)0.2525
                                              0.94
                                      -0.05
## factor(hiv.data$time)0.25416666666667 -0.63
                                              0.84
## factor(hiv.data$time)0.255
                                      0.33
                                              0.80
## factor(hiv.data$time)0.25666666666667
                                      0.29
                                              0.63
## factor(hiv.data$time)0.25749999999999
                                              0.84
                                      0.09
## factor(hiv.data$time)0.2575
                                      0.45
                                              0.63
## factor(hiv.data$time)0.2625
                                              0.84
                                      -0.04
## factor(hiv.data$time)0.265
                                      -0.16
                                              0.85
## factor(hiv.data$time)0.26583333333333 -0.36
                                              0.84
## factor(hiv.data$time)0.26833333333333 -0.34
                                              0.59
## factor(hiv.data$time)0.268333333333333
                                      0.07
                                              0.49
## factor(hiv.data$time)0.2875
                                              0.53
                                      0.50
0.94
## factor(hiv.data$time)0.2933333333333 -0.28
                                              0.94
## factor(hiv.data$time)0.30416666666667
                                      0.31
                                              0.89
0.89
## factor(hiv.data$time)0.30666666666667
                                      0.22
                                              0.59
## factor(hiv.data$time)0.3258333333333 -0.16
                                              0.89
## factor(hiv.data$time)0.3283333333333 -0.87
                                              0.94
## factor(hiv.data$time)0.33166666666667
                                              0.94
                                      0.05
## factor(hiv.data$time)0.358333333333333
                                              0.86
                                      0.57
## factor(hiv.data$time)0.36416666666667 -0.07
                                              0.61
0.94
## factor(hiv.data$time)0.429166666666667 -0.44
                                              0.90
## factor(hiv.data$time)0.4383333333333 -0.85
                                              0.90
```

```
## factor(hiv.data$time)0.44083333333333 -0.10
                                              0.77
## factor(hiv.data$time)0.443333333333333
                                              0.85
## factor(hiv.data$time)0.44916666666667 -0.08
                                              0.79
## factor(hiv.data$time)0.45416666666666
                                      0.27
                                              0.90
                                              0.86
## factor(hiv.data$time)0.45416666666667
                                      0.09
## factor(hiv.data$time)0.455
                                     -1.45
                                              0.89
## factor(hiv.data$time)0.456666666666667
                                      0.24
                                              0.94
## factor(hiv.data$time)0.4575
                                     -0.14
                                              0.49
## factor(hiv.data$time)0.459166666666667
                                      0.27
                                              0.62
0.46
## factor(hiv.data$time)0.46
                                              0.17
## factor(hiv.data$time)0.46000000000000 -0.27
                                              0.31
0.48
## factor(hiv.data$time)0.4625
                                      0.43
                                              0.41
## factor(hiv.data$time)0.4633333333333 -0.70
                                              0.81
## factor(hiv.data$time)0.465
                                     -0.88
                                              0.48
## factor(hiv.data$time)0.46583333333333 0.32
                                              0.59
## factor(hiv.data$time)0.46583333333333 -0.60
                                              0.83
## factor(hiv.data$time)0.4675
                                      1.61
                                              0.61
## factor(hiv.data$time)0.4683333333333 -0.80
                                              0.85
## factor(hiv.data$time)0.4708333333333 -0.36
                                              0.46
## factor(hiv.data$time)0.4708333333333 -0.46
                                              0.61
## factor(hiv.data$time)0.4733333333333 -0.17
                                              0.62
## factor(hiv.data$time)0.4733333333333 0.45
                                              0.79
0.82
## factor(hiv.data$time)0.47416666666667 -0.81
                                              0.80
## factor(hiv.data$time)0.4758333333333 -0.46
                                              0.80
## factor(hiv.data$time)0.4758333333333 -1.41
                                              0.58
## factor(hiv.data$time)0.47666666666667
                                              0.40
0.58
## factor(hiv.data$time)0.47916666666666 -0.03
                                              0.25
## factor(hiv.data$time)0.48166666666666
                                      0.11
                                              0.59
                                      0.22
## factor(hiv.data$time)0.48166666666667
                                              0.43
## factor(hiv.data$time)0.48416666666667 -2.71
                                              0.81
## factor(hiv.data$time)0.485
                                      0.90
                                              0.62
```

```
## factor(hiv.data$time)0.48749999999999 -0.23
                                                0.77
## factor(hiv.data$time)0.4875
                                       1.80
                                                0.82
## factor(hiv.data$time)0.487500000000001
                                       1.76
                                                0.80
## factor(hiv.data$time)0.489999999999999
                                       0.09
                                                0.85
## factor(hiv.data$time)0.495
                                                0.60
                                      -0.14
## factor(hiv.data$time)0.49583333333333 -0.47
                                                0.86
## factor(hiv.data$time)0.49583333333333 -0.12
                                                0.94
## factor(hiv.data$time)0.49833333333333 -0.59
                                                0.39
## factor(hiv.data$time)0.49833333333333 -0.58
                                                0.38
## factor(hiv.data$time)0.50083333333333 -0.26
                                                0.79
## factor(hiv.data$time)0.5008333333333 0.05
                                                0.81
## factor(hiv.data$time)0.50166666666667 -1.18
                                                0.61
## factor(hiv.data$time)0.503333333333333
                                       0.59
                                                0.84
## factor(hiv.data$time)0.50416666666666 0.24
                                                0.52
## factor(hiv.data$time)0.50583333333333 -1.53
                                                0.82
0.90
## factor(hiv.data$time)0.51166666666667 -1.10
                                                0.87
## factor(hiv.data$time)0.5141666666666 0.12
                                                0.62
## factor(hiv.data$time)0.515
                                       0.16
                                                0.94
## factor(hiv.data$time)0.5175
                                      -0.42
                                                0.38
## factor(hiv.data$time)0.51750000000001 -1.13
                                                0.82
## factor(hiv.data$time)0.5333333333333 -0.27
                                                0.64
## factor(hiv.data$time)0.5333333333333 -1.07
                                                0.87
## factor(hiv.data$time)0.53416666666667 0.22
                                                0.62
## factor(hiv.data$time)0.53666666666667 -0.48
                                                0.44
## factor(hiv.data$time)0.5558333333333 -0.22
                                                0.62
0.94
## factor(hiv.data$time)0.56416666666667 -0.77
                                                0.89
## factor(hiv.data$time)0.575
                                      -0.35
                                                0.63
## factor(hiv.data$time)0.5808333333333 -0.28
                                                0.94
## factor(hiv.data$time)0.5825
                                                0.94
## factor(hiv.data$time)0.59416666666667 -0.48
                                                0.89
## factor(hiv.data$time)0.6108333333333 -1.09
                                                0.94
## factor(hiv.data$time)0.6375
                                                0.90
                                       1.80
0.89
```

```
0.87
## factor(hiv.data$time)0.6575
                                      -1.01
                                                0.94
## factor(hiv.data$time)0.67
                                      -0.43
                                                0.85
## factor(hiv.data$time)0.67083333333333 -0.99
                                                0.49
## factor(hiv.data$time)0.6733333333333333
                                                0.94
## factor(hiv.data$time)0.67583333333333 -0.15
                                                0.67
## factor(hiv.data$time)0.68416666666667
                                       0.53
                                                0.63
## factor(hiv.data$time)0.685
                                       0.61
                                                0.84
## factor(hiv.data$time)0.6875
                                                0.61
                                      -1.59
0.89
## factor(hiv.data$time)0.68916666666667
                                       0.16
                                                0.81
## factor(hiv.data$time)0.69
                                      -0.18
                                                0.16
## factor(hiv.data$time)0.6925
                                       0.52
                                                0.55
## factor(hiv.data$time)0.692500000000001
                                       0.90
                                                0.84
## factor(hiv.data$time)0.6933333333333 -0.48
                                                0.85
## factor(hiv.data$time)0.695
                                       0.37
                                                0.84
## factor(hiv.data$time)0.69583333333333 -0.32
                                                0.86
## factor(hiv.data$time)0.69583333333333 -1.68
                                                0.83
## factor(hiv.data$time)0.69583333333333 0.82
                                                0.59
## factor(hiv.data$time)0.69750000000001 -1.49
                                                0.79
## factor(hiv.data$time)0.6983333333333 0.05
                                                0.84
## factor(hiv.data$time)0.69833333333333 -0.61
                                                0.59
## factor(hiv.data$time)0.700833333333333
                                                0.49
## factor(hiv.data$time)0.7033333333333 -0.89
                                                0.58
## factor(hiv.data$time)0.7033333333333 -1.07
                                                0.82
## factor(hiv.data$time)0.70416666666667 -4.77
                                                0.80
## factor(hiv.data$time)0.7058333333333 -0.48
                                                0.49
## factor(hiv.data$time)0.7058333333333 -0.45
                                                0.77
## factor(hiv.data$time)0.70666666666667
                                                0.80
0.80
## factor(hiv.data$time)0.70916666666667
                                                0.28
                                       0.23
## factor(hiv.data$time)0.71166666666666
                                       0.10
                                                0.84
## factor(hiv.data$time)0.71166666666667 -0.47
                                                0.81
## factor(hiv.data$time)0.7116666666666 -0.88
                                                0.57
## factor(hiv.data$time)0.71416666666667 -1.43
                                                0.58
```

```
0.79
## factor(hiv.data$time)0.71500000000001 -0.62
                                              0.86
## factor(hiv.data$time)0.7175
                                     -1.01
                                              0.81
## factor(hiv.data$time)0.72
                                     -4.32
                                              0.78
## factor(hiv.data$time)0.725
                                              0.60
                                     -0.65
## factor(hiv.data$time)0.725833333333333
                                      0.35
                                              0.84
## factor(hiv.data$time)0.7258333333333333
                                      0.72
                                              0.83
## factor(hiv.data$time)0.7258333333333334
                                      0.33
                                              0.94
## factor(hiv.data$time)0.72833333333333 -0.26
                                              0.29
## factor(hiv.data$time)0.7308333333333333
                                              0.51
                                      0.08
## factor(hiv.data$time)0.7333333333333 -0.74
                                              0.84
0.81
## factor(hiv.data$time)0.7358333333333 -0.93
                                              0.67
## factor(hiv.data$time)0.73666666666666
                                      0.05
                                              0.85
## factor(hiv.data$time)0.73666666666667
                                              0.84
                                      1.51
## factor(hiv.data$time)0.7425
                                     -0.48
                                              0.94
## factor(hiv.data$time)0.74416666666667 0.15
                                              0.57
## factor(hiv.data$time)0.745
                                     -0.39
                                              0.82
## factor(hiv.data$time)0.7475
                                     -0.36
                                              0.37
## factor(hiv.data$time)0.75250000000001 -1.65
                                              0.84
## factor(hiv.data$time)0.75833333333333 0.22
                                              0.86
## factor(hiv.data$time)0.76166666666667 -0.59
                                              0.81
## factor(hiv.data$time)0.7633333333333 -0.13
                                              0.81
## factor(hiv.data$time)0.7633333333333 -0.02
                                              0.87
0.86
0.87
## factor(hiv.data$time)0.76666666666667 -0.44
                                              0.39
## factor(hiv.data$time)0.775
                                     -1.57
                                              0.81
## factor(hiv.data$time)0.78
                                      0.89
                                              1.58
## factor(hiv.data$time)0.7833333333333333
                                              0.89
                                     1.05
## factor(hiv.data$time)0.785
                                              0.83
                                     -0.23
## factor(hiv.data$time)0.7858333333333 0.44
                                              0.80
## factor(hiv.data$time)0.7883333333333 -0.74
                                              0.94
## factor(hiv.data$time)0.794166666666667 -0.66
                                              0.82
## factor(hiv.data$time)0.8025
                                     -0.56
                                              0.58
```

```
## factor(hiv.data$time)0.805
                                         -1.58
                                                   0.82
## factor(hiv.data$time)0.805000000000001
                                         0.08
                                                   0.79
## factor(hiv.data$time)0.80750000000001 -0.32
                                                   0.89
## factor(hiv.data$time)0.82416666666667 -0.01
                                                   0.63
## factor(hiv.data$time)0.8625
                                                   0.61
                                         -0.45
## factor(hiv.data$time)0.8675
                                          0.56
                                                   0.90
## factor(hiv.data$time)0.87833333333333 -0.23
                                                   0.89
## factor(hiv.data$time)0.88166666666666
                                                   0.94
## factor(hiv.data$time)0.8958333333333 -0.73
                                                   0.89
## factor(hiv.data$time)0.90083333333333 -0.49
                                                   0.85
## factor(hiv.data$time)0.900833333333333
                                                   0.58
0.76
## factor(hiv.data$time)0.903333333333334
                                          2.25
                                                   0.94
## factor(hiv.data$time)0.905833333333333
                                          1.26
                                                   0.90
## factor(hiv.data$time)0.9083333333333 -0.44
                                                   0.90
## factor(hiv.data$time)0.90916666666666
                                                   0.94
## factor(hiv.data$time)0.90916666666667 -0.30
                                                   0.81
## factor(hiv.data$time)0.91166666666667 -0.26
                                                   0.79
## factor(hiv.data$time)0.914166666666667
                                         0.58
                                                   0.59
## factor(hiv.data$time)0.9175
                                         -0.49
                                                   0.84
## factor(hiv.data$time)0.919166666666667
                                          0.05
                                                   0.48
## factor(hiv.data$time)0.9199999999999 -0.94
                                                   0.79
                                                   0.27
## factor(hiv.data$time)0.92
                                         -0.95
## factor(hiv.data$time)0.92000000000001 -0.15
                                                   0.46
## factor(hiv.data$time)0.9225
                                                   0.59
                                         -0.53
## factor(hiv.data$time)0.92583333333333 -1.74
                                                   0.59
## factor(hiv.data$time)0.9258333333333334
                                          0.34
                                                   0.84
## factor(hiv.data$time)0.928333333333333
                                                   0.79
                                          0.04
## factor(hiv.data$time)0.9283333333333 -0.94
                                                   0.83
## factor(hiv.data$time)0.9308333333333 -0.72
                                                   0.56
## factor(hiv.data$time)0.9308333333333 -1.97
                                                   0.81
## factor(hiv.data$time)0.9333333333333 0.43
                                                   0.82
## factor(hiv.data$time)0.9333333333333 0.01
                                                   0.59
## factor(hiv.data$time)0.9341666666666 -0.82
                                                   0.84
## factor(hiv.data$time)0.93416666666667 -1.03
                                                   0.80
```

```
## factor(hiv.data$time)0.93583333333333 -0.52
                                              0.59
## factor(hiv.data$time)0.93583333333333 -0.73
                                              0.83
## factor(hiv.data$time)0.93666666666667
                                              0.79
## factor(hiv.data$time)0.938333333333333
                                              0.80
                                      0.03
## factor(hiv.data$time)0.93916666666666 -0.19
                                              0.33
## factor(hiv.data$time)0.93916666666667
                                      0.04
                                              0.33
## factor(hiv.data$time)0.93916666666666 -1.72
                                              0.82
0.41
## factor(hiv.data$time)0.94166666666667 -0.49
                                              0.81
## factor(hiv.data$time)0.94416666666667
                                      0.12
                                              0.59
## factor(hiv.data$time)0.9475
                                      0.66
                                              0.59
## factor(hiv.data$time)0.952500000000001 -0.45
                                              0.79
## factor(hiv.data$time)0.955
                                      1.56
                                              0.84
## factor(hiv.data$time)0.95500000000001 -0.47
                                              0.81
## factor(hiv.data$time)0.95583333333333 -1.06
                                              0.85
## factor(hiv.data$time)0.9575
                                      0.39
                                              0.79
## factor(hiv.data$time)0.95833333333333 0.11
                                              0.36
## factor(hiv.data$time)0.95833333333333 -0.14
                                              0.46
0.82
0.84
## factor(hiv.data$time)0.96416666666667
                                              0.83
## factor(hiv.data$time)0.9658333333333333
                                              0.85
                                      0.05
## factor(hiv.data$time)0.97666666666667 -0.51
                                              0.84
## factor(hiv.data$time)0.9774999999999 -3.22
                                              0.81
## factor(hiv.data$time)0.9775
                                              0.36
                                     -0.39
## factor(hiv.data$time)0.97750000000000 0.58
                                              0.86
## factor(hiv.data$time)0.98249999999999 -0.31
                                              0.82
## factor(hiv.data$time)0.9825
                                     -0.08
                                              0.84
## factor(hiv.data$time)0.9833333333333 -0.02
                                              0.88
## factor(hiv.data$time)0.9858333333333 -0.41
                                              0.94
0.57
## factor(hiv.data$time)0.9966666666666 -0.95
                                              0.42
## factor(hiv.data$time)0.99916666666667 -0.98
                                              0.78
## factor(hiv.data$time)1
                                     -0.99
                                              0.84
## factor(hiv.data$time)1.0016666666667
                                     -0.36
                                              0.84
```

```
## factor(hiv.data$time)1.0025
                                                    0.84
                                          -1.30
## factor(hiv.data$time)1.01083333333333
                                          -0.32
                                                    0.81
## factor(hiv.data$time)1.0125
                                          -0.75
                                                    0.81
## factor(hiv.data$time)1.015833333333333
                                          -0.96
                                                    0.61
## factor(hiv.data$time)1.02083333333333
                                                    0.85
                                          -1.29
## factor(hiv.data$time)1.023333333333333
                                          -0.57
                                                    0.90
## factor(hiv.data$time)1.0325
                                          0.79
                                                    0.89
## factor(hiv.data$time)1.035
                                          -0.37
                                                    0.39
## factor(hiv.data$time)1.048333333333333
                                          -1.29
                                                    0.87
## factor(hiv.data$time)1.053333333333333
                                          -0.13
                                                    0.83
## factor(hiv.data$time)1.0541666666667
                                          -0.54
                                                    0.58
## factor(hiv.data$time)1.075833333333333
                                          -1.00
                                                    0.85
## factor(hiv.data$time)1.08666666666667
                                          0.13
                                                    1.58
## factor(hiv.data$time)1.09
                                          -1.53
                                                   0.94
## factor(hiv.data$time)1.0925
                                          -0.63
                                                    0.50
## factor(hiv.data$time)1.11416666666667
                                           0.10
                                                    0.85
## factor(hiv.data$time)1.11666666666667
                                          0.94
                                                    0.94
## factor(hiv.data$time)1.13083333333333
                                           0.28
                                                    0.85
## factor(hiv.data$time)1.135833333333333
                                          -2.80
                                                    0.94
## factor(hiv.data$time)1.13916666666667
                                          0.11
                                                    0.79
## factor(hiv.data$time)1.14166666666667
                                          -0.48
                                                    0.57
## factor(hiv.data$time)1.14416666666667
                                           1.06
                                                    0.86
## factor(hiv.data$time)1.145
                                          -0.42
                                                    0.89
## factor(hiv.data$time)1.1475
                                                    0.84
                                          -1.35
## factor(hiv.data$time)1.14916666666667
                                                    0.57
                                          -0.67
## factor(hiv.data$time)1.15
                                          -0.41
                                                    0.22
## factor(hiv.data$time)1.1525
                                          -0.92
                                                    0.46
## factor(hiv.data$time)1.155833333333333
                                          -1.17
                                                    0.49
## factor(hiv.data$time)1.1575
                                          -0.14
                                                    0.46
0.59
                                          -1.63
## factor(hiv.data$time)1.16083333333333
                                          -1.02
                                                    0.41
## factor(hiv.data$time)1.163333333333333
                                          0.86
                                                    0.59
## factor(hiv.data$time)1.1641666666667
                                          0.31
                                                    0.84
## factor(hiv.data$time)1.165833333333333
                                          -1.58
                                                    0.83
-0.32
                                                    0.80
```

```
## factor(hiv.data$time)1.1691666666667
                                           -0.52
                                                      0.31
## factor(hiv.data$time)1.1716666666667
                                           -1.39
                                                      0.57
## factor(hiv.data$time)1.17666666666667
                                           -1.31
                                                      0.83
## factor(hiv.data$time)1.1775
                                           -0.10
                                                      0.80
## factor(hiv.data$time)1.18
                                                      0.80
                                           -0.45
## factor(hiv.data$time)1.188333333333333
                                           -0.10
                                                      0.22
## factor(hiv.data$time)1.19666666666667
                                            0.32
                                                      0.63
## factor(hiv.data$time)1.2016666666667
                                            0.09
                                                      0.48
## factor(hiv.data$time)1.2041666666667
                                           -0.62
                                                      0.59
## factor(hiv.data$time)1.20666666666667
                                            0.30
                                                      0.79
## factor(hiv.data$time)1.2075
                                           -1.07
                                                      0.47
## factor(hiv.data$time)1.2125
                                            0.10
                                                      0.84
## factor(hiv.data$time)1.2241666666667
                                           -0.31
                                                      0.86
## factor(hiv.data$time)1.225833333333333
                                            0.02
                                                      0.86
## factor(hiv.data$time)1.2266666666667
                                           -0.02
                                                      0.59
## factor(hiv.data$time)1.22916666666667
                                           -0.12
                                                      0.59
## factor(hiv.data$time)1.2316666666667
                                           -1.42
                                                      0.80
## factor(hiv.data$time)1.2325
                                           -0.12
                                                      0.80
## factor(hiv.data$time)1.245833333333333
                                           -1.10
                                                      0.48
## factor(hiv.data$time)1.248333333333333
                                           -1.65
                                                      0.84
## factor(hiv.data$time)1.253333333333333
                                           -0.99
                                                      0.90
## factor(hiv.data$time)1.2616666666667
                                           -0.42
                                                      0.81
## factor(hiv.data$time)1.265
                                           -0.19
                                                      0.47
## factor(hiv.data$time)1.2675
                                           -0.26
                                                      0.84
## factor(hiv.data$time)1.2841666666667
                                           -2.30
                                                      0.86
## factor(hiv.data$time)1.3025
                                           -0.69
                                                      0.87
## factor(hiv.data$time)1.303333333333333
                                           -0.34
                                                      0.57
## factor(hiv.data$time)1.3116666666667
                                           -1.86
                                                      0.81
## factor(hiv.data$time)1.3416666666667
                                                      0.79
                                           -1.11
## factor(hiv.data$time)1.35
                                           -0.55
                                                      0.87
## factor(hiv.data$time)1.358333333333333
                                                      0.84
                                           -1.66
## factor(hiv.data$time)1.36
                                           -0.09
                                                      0.89
## factor(hiv.data$time)1.36083333333333
                                           -0.05
                                                      0.89
## factor(hiv.data$time)1.36583333333333
                                           -0.75
                                                      0.79
## factor(hiv.data$time)1.37166666666667
                                           -0.35
                                                      0.57
```

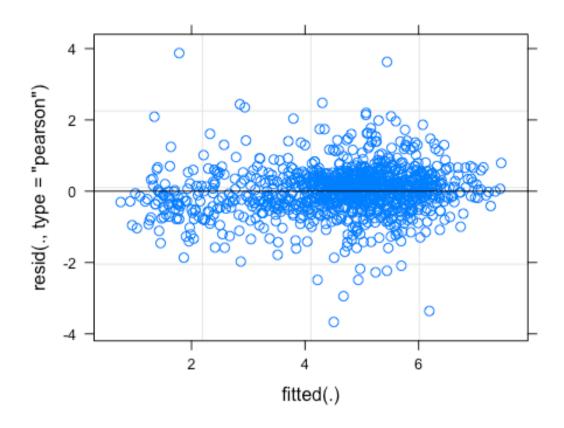
```
## factor(hiv.data$time)1.3741666666667
                                                     0.79
                                           -0.69
## factor(hiv.data$time)1.375
                                           -0.83
                                                     0.79
## factor(hiv.data$time)1.3766666666667
                                           -3.03
                                                     0.76
## factor(hiv.data$time)1.3791666666667
                                           0.03
                                                     0.78
## factor(hiv.data$time)1.38
                                                     0.32
                                           -0.42
## factor(hiv.data$time)1.3825
                                           -1.52
                                                     0.55
## factor(hiv.data$time)1.385833333333333
                                           -0.78
                                                     0.59
## factor(hiv.data$time)1.38583333333334
                                           0.17
                                                     0.83
## factor(hiv.data$time)1.3875
                                           -0.22
                                                     0.57
## factor(hiv.data$time)1.388333333333333
                                          -1.47
                                                     0.80
## factor(hiv.data$time)1.39083333333333
                                           -0.58
                                                     0.57
## factor(hiv.data$time)1.395833333333333
                                           -0.57
                                                     0.60
## factor(hiv.data$time)1.3966666666667
                                           0.32
                                                     0.77
## factor(hiv.data$time)1.398333333333333
                                          -0.33
                                                     0.82
## factor(hiv.data$time)1.3991666666667
                                                     0.31
                                           -0.47
## factor(hiv.data$time)1.4016666666667
                                           -2.16
                                                     0.60
## factor(hiv.data$time)1.41
                                           -1.28
                                                     0.55
## factor(hiv.data$time)1.4125
                                           -0.69
                                                     0.83
## factor(hiv.data$time)1.415
                                           -0.18
                                                     0.57
## factor(hiv.data$time)1.418333333333333
                                           -0.14
                                                     0.46
## factor(hiv.data$time)1.420833333333333
                                           -0.74
                                                     0.94
## factor(hiv.data$time)1.42416666666667
                                           0.39
                                                     0.79
## factor(hiv.data$time)1.425833333333333
                                           -0.19
                                                     0.81
## factor(hiv.data$time)1.42916666666667
                                           0.67
                                                     0.87
## factor(hiv.data$time)1.43166666666667
                                           -0.13
                                                     0.58
## factor(hiv.data$time)1.4366666666667
                                           0.45
                                                     0.81
## factor(hiv.data$time)1.4375
                                           -0.88
                                                     0.79
## factor(hiv.data$time)1.445833333333333
                                          -3.39
                                                     0.81
-0.85
                                                     0.90
## factor(hiv.data$time)1.4541666666667
                                           -0.44
                                                     0.86
## factor(hiv.data$time)1.455833333333333
                                           -0.56
                                                     0.79
## factor(hiv.data$time)1.4566666666667
                                           -0.19
                                                     0.41
## factor(hiv.data$time)1.4625
                                           0.31
                                                     0.80
## factor(hiv.data$time)1.47
                                           0.18
                                                     0.58
## factor(hiv.data$time)1.4725
                                           0.13
                                                     0.82
```

```
## factor(hiv.data$time)1.475
                                            0.27
                                                     0.84
## factor(hiv.data$time)1.4816666666667
                                           -1.52
                                                     0.84
## factor(hiv.data$time)1.483333333333333
                                           -0.60
                                                     0.90
## factor(hiv.data$time)1.4925
                                           -2.59
                                                     0.80
## factor(hiv.data$time)1.495
                                            0.20
                                                     0.48
## factor(hiv.data$time)1.4975
                                            0.43
                                                     0.63
## factor(hiv.data$time)1.5
                                           -0.30
                                                     0.81
## factor(hiv.data$time)1.505833333333333
                                           -0.83
                                                     0.89
## factor(hiv.data$time)1.51416666666667
                                            0.25
                                                     0.79
## factor(hiv.data$time)1.5166666666667
                                           -1.94
                                                     0.84
## factor(hiv.data$time)1.5191666666667
                                           -3.13
                                                     0.86
## factor(hiv.data$time)1.53
                                            0.51
                                                     0.85
## factor(hiv.data$time)1.53083333333333
                                            0.11
                                                     0.89
## factor(hiv.data$time)1.533333333333333
                                           -0.13
                                                     0.58
## factor(hiv.data$time)1.5416666666667
                                           -0.91
                                                     0.81
## factor(hiv.data$time)1.59083333333333
                                           -1.28
                                                     0.87
## factor(hiv.data$time)1.615
                                           -0.73
                                                     0.83
## factor(hiv.data$time)1.6291666666667
                                            3.59
                                                     0.80
## factor(hiv.data$time)1.6483333333333333
                                           -1.52
                                                     0.85
## factor(hiv.data$time)1.7166666666667
                                            0.00
                                                     0.84
## factor(hiv.data$time)1.725
                                           -0.38
                                                     0.79
## factor(hiv.data$time)1.8116666666667
                                            0.35
                                                     0.85
## factor(hiv.data$time)1.8966666666667
                                           -0.41
                                                     0.82
## factor(hiv.data$time)1.908333333333333
                                           -0.73
                                                     0.86
## factor(hiv.data$time)1.93833333333333
                                                     0.94
                                           -0.88
##
## Error terms:
  Groups
                    Name
                                 Std.Dev.
##
    hiv.data$newpid (Intercept) 1.41
    Residual
                                 0.70
##
## ---
## number of obs: 1072, groups: hiv.data$newpid, 250
## AIC = 2980.5, DIC = 2698.6
## deviance = 2434.5
```

Problem - 5

```
one <- lmer(formula = hiv.data$v ~ hiv.data$time + hiv.data$age.baseline +
hiv.data$treatment + (1 | hiv.data$newpid))
summary(one)
## Linear mixed model fit by REML ['lmerMod']
## Formula:
## hiv.data$y ~ hiv.data$time + hiv.data$age.baseline + hiv.data$treatment +
       (1 | hiv.data$newpid)
##
##
## REML criterion at convergence: 3137.2
##
## Scaled residuals:
##
      Min
                10 Median
                                30
                                       Max
## -4.7490 -0.4392 0.0097 0.4282 5.0141
##
## Random effects:
## Groups
                    Name
                                Variance Std.Dev.
## hiv.data$newpid (Intercept) 1.8897
                                         1.3747
## Residual
                                0.5969
                                         0.7726
## Number of obs: 1072, groups: hiv.data$newpid, 250
##
## Fixed effects:
##
                         Estimate Std. Error t value
## (Intercept)
                                     0.31684 15.485
                          4.90606
## hiv.data$time
                         -0.36216
                                     0.05399 -6.708
## hiv.data$age.baseline -0.11945
                                     0.04000 -2.986
## hiv.data$treatment
                          0.18008
                                     0.18262 0.986
##
## Correlation of Fixed Effects:
##
               (Intr) hv.dt$tm hv.d$.
## hiv.data$tm -0.086
## hv.dt$g.bsl -0.430 -0.017
## hv.dt$trtmn -0.850 0.010
                               -0.003
```

plot(one)



Original formula of the multilevel model:

$$\begin{split} y &= \beta_{0[j]i} + X_{i1} * \beta_{1[j]i} + X_{i2} * \beta_{2[j]i} + X_{i3} * \beta_{3[j]i} + \epsilon_i \\ y &= \alpha_{j[i]} + \beta_1 X_{i1} + \beta_2 X_{i2} + \beta_3 X_{i3} + \epsilon_i \\ \alpha_j &\sim N(\mu_i, \sigma_i^2) \end{split}$$

X1 = time, X2 = age.baseline, X3 = treatment

Method1: Allowing regression coefficients to vary accross groups

$$y = 4.91 + X_{i1}*(-0.36) + X_{i2}*(-0.12) + X_{i3}*0.18 + 0.77$$
 , for $i = 1, \dots, n_{250}$

 $\alpha_j\simeq \mathbb{N}(0,1.37^2)\$

Method2: Combining separate local regressions

$$y \sim N(4.91 + X_{i1}^*(-0.36) + X_{i2}^*(-0.12) + X_{i3}^*0.18, 0.77^2), for i = 1, ..., n_{250}$$

 $\alpha_j\simeq \mathbb{N}_{n-1}.37^2)\$

Method3: Modeling the coefficients of a large regression model

$$y_i \sim N(4.91 + X_{i1}^*(-0.36) + X_{i2}^*(-0.12) + X_{i3}^*0.18, 0.77^2)$$

$$\beta_i \sim N(0, 1.37^2)$$

Method4: Regression with multiple error terms

$$y_i \sim N(4.91 + X_{i1}^*(-0.36) + X_{i2}^*(-0.12) + X_{i3}^*0.18 + 1.37^2, 0.77^2)$$

Method5: Large regression with correlated errors

$$y_i \sim N(4.91 + X_{i1}^*(-0.36) + X_{i2}^*(-0.12) + X_{i3}^*0.18, 1.37^2 + 0.77^2)$$