STAT4610 - HW5

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10/2/2022

Question 7

```
library(ISLR2)
## Warning: package 'ISLR2' was built under R version 4.1.2
library(boot)
summary(Weekly)
##
        Year
                                          Lag2
                       Lag1
                                                            Lag3
   Min.
          :1990
                  Min. :-18.1950
                                    Min. :-18.1950
                                                              :-18.1950
##
                                                       Min.
##
   1st Ou.:1995
                  1st Ou.: -1.1540
                                     1st Ou.: -1.1540
                                                       1st Ou.: -1.1580
   Median :2000
                  Median : 0.2410
                                     Median : 0.2410
                                                       Median: 0.2410
##
##
   Mean
          :2000
                  Mean : 0.1506
                                     Mean : 0.1511
                                                       Mean : 0.1472
   3rd Qu.:2005
                                                       3rd Qu.: 1.4090
##
                  3rd Qu.: 1.4050
                                     3rd Qu.: 1.4090
##
   Max.
          :2010
                  Max.
                         : 12.0260
                                     Max.
                                            : 12.0260
                                                       Max.
                                                              : 12.0260
                                            Volume
                                                              Todav
##
        Lag4
                           Lag5
   Min.
          :-18.1950
                      Min.
                             :-18.1950
                                         Min.
                                                :0.08747
                                                          Min.
                                                                 :-18.1950
##
   1st Ou.: -1.1580
                      1st Ou.: -1.1660
                                         1st Ou.:0.33202
                                                          1st Ou.: -1.1540
##
##
   Median : 0.2380
                      Median : 0.2340
                                         Median :1.00268
                                                          Median: 0.2410
         : 0.1458
                           : 0.1399
                                                :1.57462
                                                          Mean : 0.1499
##
   Mean
                      Mean
                                         Mean
   3rd Ou.: 1.4090
                                         3rd Ou.:2.05373
##
                      3rd Ou.: 1.4050
                                                          3rd Ou.:
                                                                    1.4050
##
   Max. : 12.0260
                      Max.
                           : 12.0260
                                                :9.32821
                                                                 : 12.0260
                                         Max.
                                                          Max.
   Direction
##
   Down: 484
##
##
   Up :605
##
##
##
##
```

```
part-(a)
logReg1 = glm(Direction ~ Lag1 + Lag2, data = Weekly, family = binomial)
summary(logReg1)
##
## Call:
## glm(formula = Direction ~ Lag1 + Lag2, family = binomial, data = Weekly)
##
## Deviance Residuals:
     Min
             10 Median
##
                            30
                                   Max
## -1.623 -1.261
                  1,001
                         1.083
                                 1.506
##
## Coefficients:
##
             Estimate Std. Error z value Pr(>|z|)
                        0.06147 3.599 0.000319 ***
## (Intercept) 0.22122
             ## Lag1
              ## Lag2
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 1496.2 on 1088 degrees of freedom
## Residual deviance: 1488.2 on 1086 degrees of freedom
## ATC: 1494.2
##
## Number of Fisher Scoring iterations: 4
part-(b)
set.seed(123)
logReg2 = glm(Direction ~ Lag1 + Lag2, data = Weekly[-1, ], family =
binomial)
summary(logReg2)
##
## Call:
```

```
## glm(formula = Direction ~ Lag1 + Lag2, family = binomial, data =
Weeklv[-1.
##
      1)
##
## Deviance Residuals:
##
      Min
                10
                    Median
                                 30
                                         Max
## -1.6258 -1.2617
                    0.9999
                            1.0819
                                      1.5071
##
## Coefficients:
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 0.22324 0.06150 3.630 0.000283 ***
              ## Lag1
## Lag2
              0.06085 0.02656 2.291 0.021971 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 1494.6 on 1087 degrees of freedom
##
## Residual deviance: 1486.5 on 1085 degrees of freedom
## AIC: 1492.5
## Number of Fisher Scoring iterations: 4
predict.glm(logReg2, Weekly[1, ], type = "response")
##
## 0.5713923
predict.glm(logReg2, Weekly[1, ], type = "response") > 0.5
##
     1
## TRUE
Weekly$Direction[1]
## [1] Down
## Levels: Down Up
```

- -> The prediction was $\sim\!0.57$, which is greater than 0.5, meaning the predicted direction is IIP.
- -> The actual direction was DOWN.
- -> The prediction was inaccurate.

```
part-(d)
```

```
errorCount = rep(0, dim(Weekly)[1])
for (i in 1:(dim(Weekly)[1])) {
    logReg3 = glm(Direction ~ Lag1 + Lag2, data = Weekly[-i, ], family =
    binomial)
    predUp = predict.glm(logReg3, Weekly[i, ], type = "response") > 0.5
    isUp = Weekly[i, ]$Direction == "Up"
    if (predUp != isUp)
        errorCount[i] = 1
}
sum(errorCount)
## [1] 490
```

-> The algorithm computed a sum of 490 errors.

```
part-(e)
mean(errorCount)
## [1] 0.4499541
```

-> The Leave-One-Out Cross-Validation (LOOCV) estimate for the test error is 45%.

End.