

Homework 1: Conversion of Units

1. GN-z11 is the most distant galaxy we have observed, its distance from us is 9.8 Giga **parsecs** (Giga = 10^9). The **parsec** (symbol: **pc**) is a unit of length used to measure large distances to astronomical objects outside the Solar System.

If 1 **pc** = 3.26 **light years** (**ly**), and 1 **ly** = 9.45×10^{15} **m**.

a) How far is GN-z11 in **ly**?

$$9.8 \text{ Gpc} = 9.8 \times 10^9 \text{ pc} \left(\frac{3.26 \text{ ly}}{1 \text{ pc}} \right) \approx 32 \times 10^9 \text{ ly} = \boxed{3.2 \times 10^{10} \text{ ly}}$$

b) How far is GN-z11 in **km**?

$$3.2 \times 10^{10} \text{ ly} \left(\frac{9.45 \times 10^{15} \text{ m}}{1 \text{ ly}} \right) \left(\frac{1 \text{ km}}{1000 \text{ m}} \right) \approx 30 \times 10^{22} \text{ km} = \boxed{3 \times 10^{23} \text{ km}}$$

2. The size of protons have been measured to be about 1 **fm**. A **femtometer** (symbol: **fm**) is 10^{-15} **meters**. Compare the distance to GN-z11 (above) to the size of a proton. HINT: First convert the two measurements to the same units and then take the ratio between the two. I am looking for an answer telling me only the order of magnitude difference (powers of ten).

$$\frac{3 \times 10^{26} \text{ m}}{10^{-15} \text{ m}} = 3 \times 10^{26+15} = 3 \times \boxed{10^{41}}$$

3. You use about 3×10^8 **kg (m/s)²** of energy every day. How much is that in **kWh (kilowatt hour)**? HINT: look at the lecture slides for help but show the process to get to the answer.

$$1 \text{ J} = 1 \text{ kg (m/s)}^2$$

$$1 \text{ kWh} = 3.6 \times 10^6 \text{ J}$$

$$3 \times 10^8 \text{ kg (m/s)}^2 \left(\frac{1 \text{ J}}{1 \text{ kg (m/s)}^2} \right) \left(\frac{1 \text{ kWh}}{3.6 \times 10^6 \text{ J}} \right) = 0.83 \times 10^2 \text{ kWh} = \boxed{83 \text{ kWh}}$$