Lab 2: Equilibrium on an Inclined Plane

Purpose

To measure the mass of a cart by analyzing the forces in equilibrium in an inclined plane.

Introduction

Newton's first law of motion states that **every object continues in a state of rest or of uniform speed in a straight line unless acted on by a nonzero net force**.

This means that if the sum of the forces acting on an object adds up to zero, then the object will not change its velocity (i.e. there is no acceleration). Thus if an object is not moving or moving with constant velocity, then you know that the law of equilibrium can be applied, which can be expressed mathematically in the following way

$$\sum F = F_1 + F_2 + \ldots + F_N = 0 \ . \quad \textbf{Eq. 1}$$

In this lab you will use the law of equilibrium in order to find the mass of a cart hanging on inclined plane.

Procedure

1. Setup the inclined plane so that the angle meter reads about 10°. NOTE: You will not use the angle in your calculation so it doesn't have to be exactly 10°.

2. Connect the weight hanger, the force scale, and the cart using a couple pieces of string. Let the string rest on top of the pulley.

3. While holding the cart on the ramp and letting the weight hanger hang from the pulley, add some weight to the weight hanger until you can let go the cart and it wont move (i.e the system stays in equilibrium).

4. Write down in the Data Collection table (next section) the amount of weight needed on the weight hanger in order to keep the system in equilibrium. Also measure the height (*h*) from the table to some point on the plane, and the distance (*d*) from the bottom of the plane to the point on the plane where you are measuring the height (*h*). You're basically measuring the hypotenuse (*d*) and the opposite side (*h*) of the triangle below
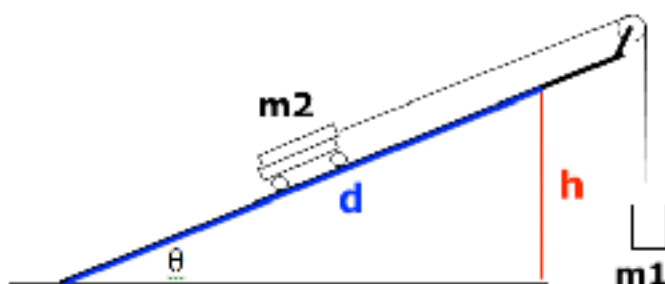

5. Repeat steps 1-4 a couple more times changing the inclination of the plane to 20° and 30°.

Data Collection

Inclination	m_1 = mass on hanger (g)	h = height (cm)	d = distance on plane (cm)
10°			
20°			
30°			

Analysis

1. In the picture below draw and label the vectors associated with every force acting on the system. Remember that the force of the gravitational pull on a mass m is given by $F_g = mg$, where $g = 9.8$ m/s$^2 \sim 10$ m/s^2 is the gravitational acceleration at the surface of the earth. NOTE: Don't do any calculations yet, just label the forces using symbols.
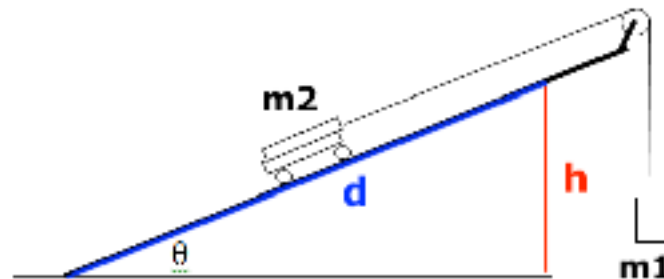
2. Now if we isolate the cart system and decompose F_g into the its components parallel ($F_{g,x}$) and perpendicular ($F_{g,y}$) to the incline, and use the law of equilibrium (**Eq. 1**), show that $F_{g,x} = -m_1 g$ and $F_{g,y} = -N$, were m_1 is the mass on the hanger and N is the normal/support force.
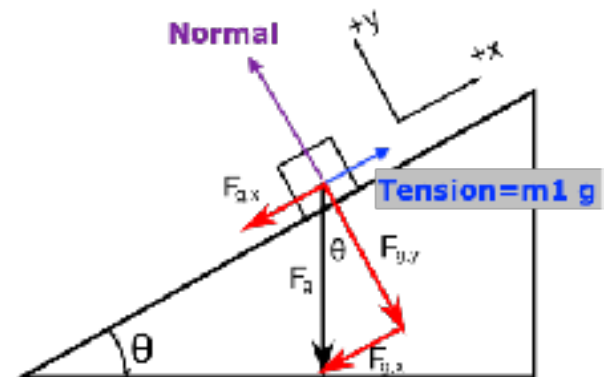
3. Finally, now that you know that $F_{g,x} = -m_1 g$ and $F_g = -m_2 g$, and using the fact that from geometry $\dfrac{F_g}{F_{g,x}} = \dfrac{m_2 g}{m_1 g} = \dfrac{d}{h}$, you can use your measurements of d an h in order to find m_2 (the mass of the cart). Find the mass of the cart from your 3 different measurements of d and h in your table (one for each inclination).

4. Now find the "actual" mass of the cart by weighting it on the lab scale, and compute the percent error between this actual mass and the average of your indirect measurements.

$$\% \text{ error} = \frac{|\text{actual} - \text{avg. of your measurements}|}{\text{actual}} \times 100$$

5. There is a source of a minor systematic error in the measurements for this lab, can you tell what it is? HINT: Did you notice if there were any differences between the mass that the force scale was reading and the actual mass on the hanger (m_2)?