

In [1]: ##### Aggregate Data Treatment

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## Assumption: each individual faces each and every one of the different decision problems
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```
%reset
import pandas as pd
import numpy as np
import itertools
from scipy import stats
```

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```
def ttest2s(x):
    if np.std(x) == 0:
        if np.mean(x) == 0:
            print('Elements in the vector are all zero')
            return (np.nan,1)
        if np.mean(x) != 0:
            print('Elements in the vector are all the same and different from zero')
            return (np.nan,0)
    if (np.std(x) != 0):
        n = len(x)
        tt = np.mean(x)/(np.std(x)/np.sqrt(n))
        pval = stats.t.sf(np.abs(tt), n-1)*2
        return (tt,pval)
```

```
def ttest1s(x):
    if np.std(x) == 0:
        if np.mean(x) == 0:
            print('Elements in the vector are all zero')
            return (np.nan,1)
        if np.mean(x) != 0:
            print('Elements in the vector are all the same and different from zero')
            return (np.nan,0)
    if (np.std(x) != 0):
        n = len(x)
        tt = np.mean(x)/(np.std(x)/np.sqrt(n))
        pval = stats.t.sf(tt, n-1)
        return (tt,pval)
```

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```
df = pd.read_csv('Data_for_HW_1.csv')
df['User ID'] = 1
df.loc[df['State'] == 1, 'State'] = 0
df.loc[df['State'] == 2, 'State'] = 1
df.loc[df['State'] == 5, 'State'] = 2
df.loc[df['State'] == 6, 'State'] = 3
df['Chosen Act'] = 0
df.loc[
    (df['Chosen Action'] == 11) |
    (df['Chosen Action'] == 13) |
    (df['Chosen Action'] == 15) |
    (df['Chosen Action'] == 17), 'Chosen Act'] = 1
```

```
dict_u = {8: [[1,0,10,0],[0,1,0,10]],
          9: [[10,0,1,0],[0,10,0,1]],
          10: [[1,0,1,0],[0,1,0,1]],
          11: [[10,0,10,0],[0,10,0,10]]}
```

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#####
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```
Q8 = [10,11]
Q9 = [12,13]
Q10 = [14,15]
Q11 = [16,17]
DP = sorted(list(df['Question ID'].unique()))
```

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Indiv = sorted(list(df['User ID'].unique()))
Omega = sorted(list(df['State'].unique()))
mu = [1/4, 1/4, 1/4, 1/4]
df2 = pd.DataFrame(data = {'mu(s)': mu, 'State': Omega})

# Define df for revealed information structures
temp2 = []
for A in DP:
    temp = list(itertools.product(Indiv,[A]))
    temp2 = temp2 + temp
df_rinfo = pd.DataFrame(data = temp2)
df_rinfo.columns = ['User ID', 'Question ID']

#####

data = [[i,A,a,s] for i in Indiv for A in DP for a in eval('Q'+str(A)) for s in Omega]
dftemp = pd.DataFrame(data=np.array(data), columns=['User ID','Question ID','Chosen Action','State'])

df_ind = df.groupby(['User ID','Question ID','State','Chosen Action','Chosen Act'])['Chosen Action'].count().to_frame()
df_ind.rename(columns={'Chosen Action': 'Frequency'}, inplace=True)
df_ind.reset_index(inplace=True)
df_ind = pd.merge(
    dftemp, df_ind,
    how='outer', on=['User ID','Question ID','State','Chosen Action']
)
df_ind = df_ind.fillna(0)
df_ind = pd.merge(
    df_ind, df2,
    how='outer', on=['State']
)
df_ind['PA(a|s)'] = df_ind['Frequency']/df_ind.groupby(['User ID','Question ID','State'])['Frequency'].transform('sum')

df_ind['PA(a|s)*mu(s)'] = df_ind['PA(a|s)']*df_ind['mu(s)']
df_ind['PA(s|a)'] = df_ind['PA(a|s)*mu(s)']/df_ind.groupby(['User ID','Question ID','Chosen Action'])['PA(a|s)*mu(s)'].transform('sum')
df_ind.sort_values(by=['User ID','Question ID','Chosen Action','State'], inplace=True)
df_ind['PA(s|a)'] = df_ind['PA(s|a)'].fillna(0)

df_ind.loc[
    (df_ind['Chosen Action'] == 11) |
    (df_ind['Chosen Action'] == 13) |
    (df_ind['Chosen Action'] == 15) |
    (df_ind['Chosen Action'] == 17), 'Chosen Act'] = 1

#####

# Define df for revealed posteriors
df_rpost = df_rinfo.copy(deep=True)
df_ind.sort_values(by=['User ID','Question ID','Chosen Action','State'], inplace=True)

listofpost = [
    [
        df_ind[
            (df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Action'] == a) & (
df_ind['State'] == s)
            ][ 'PA(s|a)'].tolist()[0]
        for s in Omega]
    for a in eval('Q'+str(A))] for A in DP for i in Indiv]

listofinfo = [
    [
        df_ind[
            (df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Action'] == a) & (
df_ind['State'] == s)
            ][ 'PA(a|s)'].tolist()[0]
        for s in Omega]
    for a in eval('Q'+str(A))] for A in DP for i in Indiv]

df_rpost['gammaA(s)'] = listofpost
df_rinfo['piA(gammaA|s)'] = listofinfo

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df_temp = df_rpost.set_index(['User ID','Question ID'])
dict_gammaA = df_temp['gammaA(s)'].T.to_dict()
df_temp = df_rinfo.set_index(['User ID','Question ID'])
dict_piA = df_temp['piA(gammaA|s)'].T.to_dict()

#####

def Gvalue(infopi,priormu,postgamma,u):
    G=priormu*infopi.T*((postgamma*u.T).max(0)).T
    return G

#####

NIAC_Gsum = []
NIAC_Gsumtilde = []
for i in Indiv:
    listDP = sorted(df_rinfo[df_rinfo['User ID']==i]['Question ID'].unique().tolist())
    DPTuples = list(list(itertools.permutations(listDP, x)) for x in range(2,len(listDP)+1))
    DPTuples = [item for sublist in DPTuples for item in sublist]
    NIAC_Gsumtemp = [0 for x in range(0,len(DPTuples))]
    NIAC_Gsumtildetemp = [0 for x in range(0,len(DPTuples))]
    index = 0
    for subtuple in DPTuples:
        Gsum = 0
        Gsumtilde = 0
        for node in range(0,len(subtuple)):
            Gsum = Gsum + Gvalue(np.matrix(dict_piA[(i,subtuple[node])]),mu,np.matrix(dict_gammaA[(i,subtuple[0])]),np.matrix(dict_u[subtuple[node]]))
            if node != len(subtuple)-1:
                Gsumtilde = Gsumtilde + Gvalue(np.matrix(dict_piA[(i,subtuple[node+1])]),mu,np.matrix(dict_gammaA[(i,subtuple[node+1])]),np.matrix(dict_u[subtuple[node]]))
            else:
                Gsumtilde = Gsumtilde + Gvalue(np.matrix(dict_piA[(i,subtuple[0])]),mu,np.matrix(dict_gammaA[(i,subtuple[0])]),np.matrix(dict_u[subtuple[node]]))
            NIAC_Gsumtemp[index] = np.asscalar(Gsum)
            NIAC_Gsumtildetemp[index] = np.asscalar(Gsumtilde)
            index = index + 1
        NIAC_Gsum.append(NIAC_Gsumtemp)
        NIAC_Gsumtilde.append(NIAC_Gsumtildetemp)

#####

print('NIAC: smallest difference')
print((np.array(NIAC_Gsum)-np.array(NIAC_Gsumtilde)).min(1))

temp = np.array(NIAC_Gsum)-np.array(NIAC_Gsumtilde)
np.shape(temp)
NIAC_ttest_indiv = np.apply_along_axis(ttest1s, 1, temp)
print('NIAC: t-test for each individual (t-stat,p-value)')
print(NIAC_ttest_indiv)
NIAC_ttest_poolindiv = ttest1s(np.concatenate(temp))
print('NIAC: t-test pooling all individuals (t-stat,p-value)')
print(NIAC_ttest_poolindiv)

#####

# Define df for NIAS
temp = [[i,A,a] for i in Indiv for A in DP for a in eval('Q'+str(A))]
temp2 = []
tempu = []
counter = 0
for [i,A,a] in temp:
    condprob = []
    for s in Omega:
        if len(df_ind[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Action'] == a) & (df_ind['State'] == s)]) != 0:
            condprob = condprob + [np.asscalar(df_ind[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Action'] == a) & (df_ind['State'] == s)]['PA(a|s)'])]
        else:
            condprob = condprob + [0]

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        if a in (10,12,14,16):
            tempu = tempu + [dict_u[A][0]]
        else:
            tempu = tempu + [dict_u[A][1]]
        temp2 = temp2 + [condprob]

temp3 = [temp[x]+[mu]+[temp2[x]]+[tempu[x]] for x in range(0,len(temp))]
df_nias = pd.DataFrame(data = temp3)
df_nias.columns = ['User ID', 'Question ID', 'Chosen Action', 'mu', 'PA(a|.)', 'uA']

def NIAS_comp(row):
    if row['Chosen Action'] in (10, 12, 14, 16):
        temp = 'bla'
        mu = np.matrix(row['mu'])
        temp = np.multiply(np.matrix(row['mu']),np.matrix(row['PA(a|.)'])*(np.matrix(dict_u[row['Question ID']][0])-np.matrix(dict_u[row['Question ID']][1])).T
    else:
        temp = np.multiply(np.matrix(row['mu']),np.matrix(row['PA(a|.)'])*(np.matrix(dict_u[row['Question ID']][1])-np.matrix(dict_u[row['Question ID']][0])).T
    return np.asscalar(temp)

df_nias['Sum mu(s) PA(a|s)[u(a(s))-u(b(s))'] = df_nias.apply(NIAS_comp, axis =1)
df_nias[df_nias['Sum mu(s) PA(a|s)[u(a(s))-u(b(s))']<0]

print('NIAS')
print(df_nias[['User ID', 'Question ID', 'Chosen Action', 'Sum mu(s) PA(a|s)[u(a(s))-u(b(s))']]])
print('Individuals failing NIAS deterministically')
print(df_nias[df_nias['Sum mu(s) PA(a|s)[u(a(s))-u(b(s))']<0][['User ID', 'Question ID', 'Chosen Action', 'Sum mu(s) PA(a|s)[u(a(s))-u(b(s))']]])

temp = [df_nias[df_nias['User ID'] == userid]['Sum mu(s) PA(a|s)[u(a(s))-u(b(s))'].values.tolist() for user
id in Indiv]
np.shape(temp)
NIAS_ttest_indiv = np.apply_along_axis(ttest1s, 1, temp)
print('NIAS: t-test for each individual (t-stat,p-value)')
print(NIAS_ttest_indiv)
NIAS_ttest_poolindiv = ttest1s(np.concatenate(temp))
print('NIAS: t-test pooling all individuals (t-stat,p-value)')
print(NIAS_ttest_poolindiv)

#####

# Define df for Shannon
df_ind['PA(a)'] = df_ind.groupby(['User ID','Question ID','Chosen Action'])['Frequency'].transform('sum')/df_ind.groupby(['User ID','Question ID'])['Frequency'].transform('sum')
df_ind['u(a(s))'] = 0
df_ind['u(b(s))'] = 0
df_ind['PA(s|b)'] = 0
temp = [[A,a,s] for A in DP for a in [0,1] for s in Omega]
counter = 0
for [A,a,s] in temp:
    df_ind.loc[(df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == a) & (df_ind['State'] == s), 'u(a(s))'] = dict_u[A][a][s]
    df_ind.loc[(df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == a) & (df_ind['State'] == s), 'u(b(s))'] = dict_u[A][a-1][s]
    for i in Indiv:
        if a == 0:
            df_ind.loc[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == a) & (df_ind['State'] == s), 'PA(s|b)'] = df_ind.loc[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == 1) & (df_ind['State'] == s), 'PA(s|a)'].values[0]
        if a == 1:
            df_ind.loc[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == a) & (df_ind['State'] == s), 'PA(s|b)'] = df_ind.loc[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == 0) & (df_ind['State'] == s), 'PA(s|a)'].values[0]

df_shannon = df_ind.copy(deep=True)

# Obtaining Lambda from MM conditions, avg Lambda per individual, aggregate avg Lambda
df_shannon['lambda'] = (df_shannon['u(a(s))'] - df_shannon['u(b(s))'])/(df_shannon['PA(s|a)'].apply(np.log)-

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df_shannon['PA(s|b)'].apply(np.log))
df_shannon.loc[(df_shannon['PA(s|a)'] == 0) | (df_shannon['PA(s|b)'] == 0), 'lambda'] = np.nan
df_shannon['avglambda i'] = df_shannon.groupby(['User ID'])['lambda'].transform('mean')
df_shannon['avglambda'] = df_shannon['lambda'].apply('mean')

# Obtaining difference for necessary and sufficient conditions for Shannon
df_shannon['z(a,s)'] = (df_shannon['u(a(s))']/df_shannon['lambda'])
df_shannon['z(a,s)'] = df_shannon['z(a,s)'].apply(np.exp)
df_shannon['z(b,s)'] = (df_shannon['u(b(s))']/df_shannon['lambda'])
df_shannon['z(b,s)'] = df_shannon['z(b,s)'].apply(np.exp)
df_shannon['Shannon NSCond'] = df_shannon['mu(s)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z(a,s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)'])
df_shannon['Shannon NSCond'] = df_shannon.groupby(['User ID', 'Question ID', 'Chosen Action'])['Shannon NSCond'].transform('sum')-1
df_shannon['MMCond'] = df_shannon['PA(a)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z(a,s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)']) - df_shannon['PA(a)s']
df_shannon.loc[(df_shannon['PA(a)'] == 1) | (df_shannon['PA(a)'] == 0), 'MMCond'] = 0

df_shannon['z(a,s)'] = (df_shannon['u(a(s))']/df_shannon['avglambda i'])
df_shannon['z(a,s)'] = df_shannon['z(a,s)'].apply(np.exp)
df_shannon['z(b,s)'] = (df_shannon['u(b(s))']/df_shannon['avglambda i'])
df_shannon['z(b,s)'] = df_shannon['z(b,s)'].apply(np.exp)
df_shannon['Shannon NSCond avg i'] = df_shannon['mu(s)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z(a,s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)'])
df_shannon['Shannon NSCond avg i'] = df_shannon.groupby(['User ID', 'Question ID', 'Chosen Action'])['Shannon NSCond avg i'].transform('sum')-1
df_shannon['MMCond avg i'] = df_shannon['PA(a)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z(a,s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)']) - df_shannon['PA(a)s']
df_shannon.loc[(df_shannon['PA(a)'] == 1) | (df_shannon['PA(a)'] == 0), 'MMCond avg i'] = 0

df_shannon['z(a,s)'] = (df_shannon['u(a(s))']/df_shannon['avglambda'])
df_shannon['z(a,s)'] = df_shannon['z(a,s)'].apply(np.exp)
df_shannon['z(b,s)'] = (df_shannon['u(b(s))']/df_shannon['avglambda'])
df_shannon['z(b,s)'] = df_shannon['z(b,s)'].apply(np.exp)
df_shannon['Shannon NSCond avg'] = df_shannon['mu(s)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z(a,s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)']) - df_shannon['PA(a)s']
df_shannon['Shannon NSCond avg'] = df_shannon.groupby(['User ID', 'Question ID', 'Chosen Action'])['Shannon NSCond avg'].transform('sum')-1
df_shannon['MMCond avg'] = df_shannon['PA(a)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z(a,s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)']) - df_shannon['PA(a)s']
df_shannon.loc[(df_shannon['PA(a)'] == 1) | (df_shannon['PA(a)'] == 0), 'MMCond avg'] = 0

df_shannon.drop('z(a,s)', axis=1, inplace=True)
df_shannon.drop('z(b,s)', axis=1, inplace=True)

# Testing necessary and sufficient conditions for Shannon; self-explanatory
temp = [df_shannon[(df_shannon['User ID'] == userid) & (df_shannon['PA(a)'] > 0) & (df_shannon['State'] == 0)][['Shannon NSCond avg i']].tolist() for userid in Indiv]
temp2 = [df_shannon[(df_shannon['User ID'] == userid) & (df_shannon['State'] == 0)][['Shannon NSCond avg i']].tolist() for userid in Indiv]
temp3 = [df_shannon[(df_shannon['User ID'] == userid)][['MMCond avg i']].tolist() for userid in Indiv]

Shannon_ttest_indiv1 = np.array([ttest2s(temp[indiv]) for indiv in range(0, len(temp)-1)])
Shannon_ttest_indiv2 = np.array([ttest1s(temp2[indiv]) for indiv in range(0, len(temp2)-1)])
Shannon_ttest_indiv3 = np.array([ttest2s(temp3[indiv]) for indiv in range(0, len(temp3)-1)])
print('Shannon: t-test for each individual allowing for heterog. cost functions (t-stat,p-value)')
print('For PA(a) > 0; H0: cond == 0')
print(Shannon_ttest_indiv1)
print('For all a; H0: cond <= 0')
print(Shannon_ttest_indiv2)
print('MM; H0: cond == 0')
print(Shannon_ttest_indiv3)

Shannon_ttest_poolindiv1 = ttest2s([x for x in np.concatenate(temp) if str(x) != 'nan'])
Shannon_ttest_poolindiv2 = ttest1s([x for x in np.concatenate(temp2) if str(x) != 'nan'])
Shannon_ttest_poolindiv3 = ttest2s([x for x in np.concatenate(temp3) if str(x) != 'nan'])
print('Shannon: t-test pooling all individuals allowing for heterog. cost functions (t-stat,p-value)')
print('For PA(a) > 0; H0: cond == 0')
print(Shannon_ttest_poolindiv1)
print('For all a; H0: cond <= 0')
print(Shannon_ttest_poolindiv2)
print('MM; H0: cond == 0')
print(Shannon_ttest_poolindiv3)

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temp = [df_shannon[(df_shannon['User ID'] == userid) & (df_shannon['PA(a)'] > 0) & (df_shannon['State'] == 0)]['Shannon NSCond avg'].tolist() for userid in Indiv]
temp2 = [df_shannon[(df_shannon['User ID'] == userid) & (df_shannon['State'] == 0)]['Shannon NSCond avg'].tolist() for userid in Indiv]
temp3 = [df_shannon[(df_shannon['User ID'] == userid)]['MMCond avg'].tolist() for userid in Indiv]

Shannon_avg_ttest_indiv1 = np.array([ttest2s(temp[indiv]) for indiv in range(0,len(temp)-1)])
Shannon_avg_ttest_indiv2 = np.array([ttest1s(temp2[indiv]) for indiv in range(0,len(temp2)-1)])
Shannon_avg_ttest_indiv3 = np.array([ttest2s(temp3[indiv]) for indiv in range(0,len(temp3)-1)])
print('Shannon: t-test for each individual with same cost function (t-stat,p-value)')
print('For PA(a) > 0; H0: cond == 0')
print(Shannon_avg_ttest_indiv1)
print('For all a; H0: cond <= 0')
print(Shannon_avg_ttest_indiv2)
print('MM; H0: cond == 0')
print(Shannon_avg_ttest_indiv3)

Shannon_avg_ttest_poolindiv1 = ttest2s([x for x in np.concatenate(temp) if str(x) != 'nan'])
Shannon_avg_ttest_poolindiv2 = ttest1s([x for x in np.concatenate(temp2) if str(x) != 'nan'])
Shannon_avg_ttest_poolindiv3 = ttest2s([x for x in np.concatenate(temp3) if str(x) != 'nan'])
print('Shannon: t-test pooling all individuals allwith same cost function (t-stat,p-value)')
print('For PA(a) > 0; H0: cond == 0')
print(Shannon_avg_ttest_poolindiv1)
print('For all a; H0: cond <= 0')
print(Shannon_avg_ttest_poolindiv2)
print('MM; H0: cond == 0')
print(Shannon_avg_ttest_poolindiv3)

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Once deleted, variables cannot be recovered. Proceed (y/[n])? y
NIAC: smallest difference
[ 0.12665918]
NIAC: t-test for each individual (t-stat,p-value)
[[ 2.22046525e+01 1.22797645e-30]]
NIAC: t-test pooling all individuals (t-stat,p-value)
(22.204652492136876, 1.2279764450012158e-30)
NIAS
  User ID  Question ID  Chosen Action  Sum mu(s)  PA(a|s)[u(a(s))-u(b(s))]
0         1           8           10         0.981533
1         1           8           11         0.981533
2         1           9           12         1.473491
3         1           9           13         1.473491
4         1          10           14         0.147222
5         1          10           15         0.147222
6         1          11           16         2.235541
7         1          11           17         2.235541
Individuals failing NIAS deterministically
Empty DataFrame
Columns: [User ID, Question ID, Chosen Action, Sum mu(s) PA(a|s)[u(a(s))-u(b(s))]]
Index: []
NIAS: t-test for each individual (t-stat,p-value)
[[ 4.50846280e+00 1.38505701e-03]]
NIAS: t-test pooling all individuals (t-stat,p-value)
(4.5084627959076533, 0.0013850570101961055)
Shannon: t-test for each individual allowing for heterog. cost functions (t-stat,p-value)
For PA(a) > 0; H0: cond == 0
[]
For all a; H0: cond <= 0
[]
MM; H0: cond == 0
[]
Shannon: t-test pooling all individuals allowing for heterog. cost functions (t-stat,p-value)
For PA(a) > 0; H0: cond == 0
(0.23872814552870497, 0.8181547337037739)
For all a; H0: cond <= 0
(0.23872814552870497, 0.40907736685188695)
MM; H0: cond == 0
(2.5447815089931843e-16, 0.99999999999999978)
Shannon: t-test for each individual with same cost function (t-stat,p-value)
For PA(a) > 0; H0: cond == 0
[]
For all a; H0: cond <= 0
[]
MM; H0: cond == 0
[]
Shannon: t-test pooling all individuals allwith same cost function (t-stat,p-value)
For PA(a) > 0; H0: cond == 0
(0.23872814552870497, 0.8181547337037739)
For all a; H0: cond <= 0
(0.23872814552870497, 0.40907736685188695)
MM; H0: cond == 0
(2.5447815089931843e-16, 0.99999999999999978)

```

In [2]: ##### Individual Data Treatment

```
## Assumption: each individual faces each and every one of the different decision problems

%reset
import pandas as pd
import numpy as np
import itertools
from scipy import stats

#####

def ttest2s(x):
    if np.std(x) == 0:
        if np.mean(x) == 0:
            print('Elements in the vector are all zero')
            return (np.nan,1)
        if np.mean(x) != 0:
            print('Elements in the vector are all the same and different from zero')
```



```

        return (np.nan,0)
    if (np.std(x) != 0):
        n = len(x)
        tt = np.mean(x)/(np.std(x)/np.sqrt(n))
        pval = stats.t.sf(np.abs(tt), n-1)*2
        return (tt,pval)
def ttest1s(x):
    if np.std(x) == 0:
        if np.mean(x) == 0:
            print('Elements in the vector are all zero')
            return (np.nan,1)
        if np.mean(x) != 0:
            print('Elements in the vector are all the same and different from zero')
            return (np.nan,0)
    if (np.std(x) != 0):
        n = len(x)
        tt = np.mean(x)/(np.std(x)/np.sqrt(n))
        pval = stats.t.sf(tt, n-1)
        return (tt,pval)

#####

df = pd.read_csv('Data_for_HW_1.csv')
df.loc[df['State'] == 1, 'State'] = 0
df.loc[df['State'] == 2, 'State'] = 1
df.loc[df['State'] == 5, 'State'] = 2
df.loc[df['State'] == 6, 'State'] = 3
df['Chosen Act'] = 0
df.loc[
    (df['Chosen Action'] == 11) |
    (df['Chosen Action'] == 13) |
    (df['Chosen Action'] == 15) |
    (df['Chosen Action'] == 17), 'Chosen Act'] = 1

dict_u = {8: [[1,0,10,0],[0,1,0,10]],
          9: [[10,0,1,0],[0,10,0,1]],
          10: [[1,0,1,0],[0,1,0,1]],
          11: [[10,0,10,0],[0,10,0,10]]}

#####

Q8 = [10,11]
Q9 = [12,13]
Q10 = [14,15]
Q11 = [16,17]
DP = sorted(list(df['Question ID'].unique()))
Indiv = sorted(list(df['User ID'].unique()))
Omega = sorted(list(df['State'].unique()))
mu = [1/4, 1/4, 1/4, 1/4]
df2 = pd.DataFrame(data = {'mu(s)': mu, 'State': Omega})

# Define df for revealed information structures
temp2 = []
for A in DP:
    temp = list(itertools.product(Indiv,[A]))
    temp2 = temp2 + temp
df_rinfo = pd.DataFrame(data = temp2)
df_rinfo.columns = ['User ID', 'Question ID']

#####

data = [[i,A,a,s] for i in Indiv for A in DP for a in eval('Q'+str(A)) for s in Omega]
dftemp = pd.DataFrame(data=np.array(data), columns=['User ID','Question ID','Chosen Action','State'])

df_ind = df.groupby(['User ID','Question ID','State','Chosen Action','Chosen Act'])['Chosen Action'].count()
.to_frame()
df_ind.rename(columns={'Chosen Action': 'Frequency'}, inplace=True)
df_ind.reset_index(inplace=True)

```

```

df_ind = pd.merge(
    dftemp, df_ind,
    how='outer', on=['User ID', 'Question ID', 'State', 'Chosen Action']
)
df_ind = df_ind.fillna(0)
df_ind = pd.merge(
    df_ind, df2,
    how='outer', on=['State']
)
df_ind['PA(a|s)'] = df_ind['Frequency']/df_ind.groupby(['User ID', 'Question ID', 'State'])['Frequency'].transform('sum')

df_ind['PA(a|s)*mu(s)'] = df_ind['PA(a|s)']*df_ind['mu(s)']
df_ind['PA(s|a)'] = df_ind['PA(a|s)*mu(s)']/df_ind.groupby(['User ID', 'Question ID', 'Chosen Action'])['PA(a|s)*mu(s)'].transform('sum')
df_ind.sort_values(by=['User ID', 'Question ID', 'Chosen Action', 'State'], inplace=True)
df_ind['PA(s|a)'] = df_ind['PA(s|a)'].fillna(0)

df_ind.loc[
    (df_ind['Chosen Action'] == 11) |
    (df_ind['Chosen Action'] == 13) |
    (df_ind['Chosen Action'] == 15) |
    (df_ind['Chosen Action'] == 17), 'Chosen Act'] = 1

#####

# Define df for revealed posteriors
df_rpost = df_rinfo.copy(deep=True)
df_ind.sort_values(by=['User ID', 'Question ID', 'Chosen Action', 'State'], inplace=True)

listofpost = [
    [
        df_ind[
            (df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Action'] == a) & (
df_ind['State'] == s)
            ][['PA(s|a)']].tolist()[0]
        for s in Omega]
    for a in eval('Q'+str(A))] for A in DP for i in Indiv]

listofinfo = [
    [
        df_ind[
            (df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Action'] == a) & (
df_ind['State'] == s)
            ][['PA(a|s)']].tolist()[0]
        for s in Omega]
    for a in eval('Q'+str(A))] for A in DP for i in Indiv]

df_rpost['gammaA(s)'] = listofpost
df_rinfo['piA(gammaA|s)'] = listofinfo

df_temp = df_rpost.set_index(['User ID', 'Question ID'])
dict_gammaA = df_temp['gammaA(s)'].T.to_dict()
df_temp = df_rinfo.set_index(['User ID', 'Question ID'])
dict_piA = df_temp['piA(gammaA|s)'].T.to_dict()

#####

def Gvalue(infopi, priormu, postgamma, u):
    G = priormu * infopi.T * ((postgamma * u.T).max(0)).T
    return G

#####

NIAC_Gsum = []
NIAC_Gsumtilde = []
for i in Indiv:
    listDP = sorted(df_rinfo[df_rinfo['User ID']==i]['Question ID'].unique().tolist())
    DPtuples = list(list(itertools.permutations(listDP, x)) for x in range(2, len(listDP)+1))
    DPtuples = [item for sublist in DPtuples for item in sublist]
    NIAC_Gsumtemp = [0 for x in range(0, len(DPtuples))]
    NIAC_Gsumtildetemp = [0 for x in range(0, len(DPtuples))]
    index = 0
    for subtuple in DPtuples:
        Gsum = 0

```

```

        Gsumtilde = 0
        for node in range(0,len(subtuple)):
            Gsum = Gsum + Gvalue(np.matrix(dict_piA[(i,subtuple[node])]),mu,np.matrix(dict_gammaA[(i,subtuple[
node])]),np.matrix(dict_u[subtuple[node]]))
            if node != len(subtuple)-1:
                Gsumtilde = Gsumtilde + Gvalue(np.matrix(dict_piA[(i,subtuple[node+1])]),mu,np.matrix(dict_g
ammaA[(i,subtuple[node+1])]),np.matrix(dict_u[subtuple[node]]))
            else:
                Gsumtilde = Gsumtilde + Gvalue(np.matrix(dict_piA[(i,subtuple[0])]),mu,np.matrix(dict_gammaA
[(i,subtuple[0])]),np.matrix(dict_u[subtuple[node]]))
                NIAC_Gsumtemp[index] = np.asscalar(Gsum)
                NIAC_Gsumtildetemp[index] = np.asscalar(Gsumtilde)
                index = index + 1
        NIAC_Gsum.append(NIAC_Gsumtemp)
        NIAC_Gsumtilde.append(NIAC_Gsumtildetemp)

#####

print('NIAC: smallest difference')
print((np.array(NIAC_Gsum)-np.array(NIAC_Gsumtilde)).min(1))

temp = np.array(NIAC_Gsum)-np.array(NIAC_Gsumtilde)
np.shape(temp)
NIAC_ttest_indiv = np.apply_along_axis(ttest1s, 1, temp)
print('NIAC: t-test for each individual (t-stat,p-value)')
print(NIAC_ttest_indiv)
NIAC_ttest_poolindiv = ttest1s(np.concatenate(temp))
print('NIAC: t-test pooling all individuals (t-stat,p-value)')
print(NIAC_ttest_poolindiv)

#####

# Define df for NIAS
temp = [[i,A,a] for i in Indiv for A in DP for a in eval('Q'+str(A))]
temp2 = []
tempu = []
counter = 0
for [i,A,a] in temp:
    condprob = []
    for s in Omega:
        if len(df_ind[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Action'] ==
a) & (df_ind['State'] == s)]) != 0:
            condprob = condprob + [np.asscalar(
                df_ind[
                    (df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Action'] == a)
                    & (df_ind['State'] == s)
                ]['PA(a|s)'])]
        else:
            condprob = condprob + [0]
    if a in (10,12,14,16):
        tempu = tempu + [dict_u[A][0]]
    else:
        tempu = tempu + [dict_u[A][1]]
    temp2 = temp2 + [condprob]

temp3 = [temp[x]+[mu]+[temp2[x]]+[tempu[x]] for x in range(0,len(temp))]
df_nias = pd.DataFrame(data = temp3)
df_nias.columns = ['User ID', 'Question ID', 'Chosen Action', 'mu','PA(a|.)','uA']

def NIAS_comp(row):
    if row['Chosen Action'] in (10, 12, 14, 16):
        temp = 'bla'
        mu = np.matrix(row['mu'])
        temp = np.multiply(np.matrix(row['mu']),np.matrix(row['PA(a|.)']))*(np.matrix(dict_u[row['Question I
D']][0])-np.matrix(dict_u[row['Question ID']][1])).T
    else:
        temp = np.multiply(np.matrix(row['mu']),np.matrix(row['PA(a|.)']))*(np.matrix(dict_u[row['Question I
D']][1])-np.matrix(dict_u[row['Question ID']][0])).T
    return np.asscalar(temp)

df_nias['Sum mu(s) PA(a|s)[u(a(s))-u(b(s))'] = df_nias.apply(NIAS_comp, axis =1)
df_nias[df_nias['Sum mu(s) PA(a|s)[u(a(s))-u(b(s))']<0]

```

```

print('NIAS')
print(df_nias[['User ID', 'Question ID', 'Chosen Action', 'Sum mu(s) PA(a|s)[u(a(s))-u(b(s))]]])
print('Individuals failing NIAS deterministically')
print(df_nias[df_nias['Sum mu(s) PA(a|s)[u(a(s))-u(b(s))']]<0][['User ID', 'Question ID', 'Chosen Action',
'Sum mu(s) PA(a|s)[u(a(s))-u(b(s))]]])

temp = [df_nias[df_nias['User ID'] == userid]['Sum mu(s) PA(a|s)[u(a(s))-u(b(s))']].values.tolist() for user
id in Indiv]
np.shape(temp)
NIAS_ttest_indiv = np.apply_along_axis(ttest1s, 1, temp)
print('NIAS: t-test for each individual (t-stat,p-value)')
print(NIAS_ttest_indiv)
NIAS_ttest_poolindiv = ttest1s(np.concatenate(temp))
print('NIAS: t-test pooling all individuals (t-stat,p-value)')
print(NIAS_ttest_poolindiv)

#####

# Define df for Shannon
df_ind['PA(a)'] = df_ind.groupby(['User ID', 'Question ID', 'Chosen Action'])['Frequency'].transform('sum')/df
_ind.groupby(['User ID', 'Question ID'])['Frequency'].transform('sum')
df_ind['u(a(s))'] = 0
df_ind['u(b(s))'] = 0
df_ind['PA(s|b)'] = 0
temp = [[A,a,s] for A in DP for a in [0,1] for s in Omega]
counter = 0
for [A,a,s] in temp:
    df_ind.loc[(df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == a) & (df_ind['State'] == s), 'u(a(s))'
] = dict_u[A][a][s]
    df_ind.loc[(df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == a) & (df_ind['State'] == s), 'u(b(s))'
] = dict_u[A][a-1][s]
    for i in Indiv:
        if a == 0:
            df_ind.loc[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == a)
& (df_ind['State'] == s), 'PA(s|b)'] = df_ind.loc[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) &
(df_ind['Chosen Act'] == 1) & (df_ind['State'] == s), 'PA(s|a)'].values[0]
            if a == 1:
                df_ind.loc[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) & (df_ind['Chosen Act'] == a)
& (df_ind['State'] == s), 'PA(s|b)'] = df_ind.loc[(df_ind['User ID'] == i) & (df_ind['Question ID'] == A) &
(df_ind['Chosen Act'] == 0) & (df_ind['State'] == s), 'PA(s|a)'].values[0]

df_shannon = df_ind.copy(deep=True)

# Obtaining lambda from MM conditions, avg lambda per individual, aggregate avg lambda
df_shannon['lambda'] = (df_shannon['u(a(s))'] - df_shannon['u(b(s))'])/(df_shannon['PA(s|a)'].apply(np.log)-
df_shannon['PA(s|b)'].apply(np.log))
df_shannon.loc[(df_shannon['PA(s|a)'] == 0) | (df_shannon['PA(s|b)'] == 0), 'lambda'] = np.nan
df_shannon['avglambda i'] = df_shannon.groupby(['User ID'])['lambda'].transform('mean')
df_shannon['avglambda'] = df_shannon['lambda'].apply('mean')

# Obtaining difference for necessary and sufficient conditions for Shannon
df_shannon['z(a,s)'] = (df_shannon['u(a(s))']/df_shannon['lambda'])
df_shannon['z(a,s)'] = df_shannon['z(a,s)'].apply(np.exp)
df_shannon['z(b,s)'] = (df_shannon['u(b(s))']/df_shannon['lambda'])
df_shannon['z(b,s)'] = df_shannon['z(b,s)'].apply(np.exp)
df_shannon['Shannon NSCond'] = df_shannon['mu(s)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z
(a,s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)'])
df_shannon['Shannon NSCond'] = df_shannon.groupby(['User ID', 'Question ID', 'Chosen Action'])['Shannon NSCon
d'].transform('sum')-1
df_shannon['MMCond'] = df_shannon['PA(a)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z(a,s)']+(1
-df_shannon['PA(a)'])*df_shannon['z(b,s)']) - df_shannon['PA(a|s)']
df_shannon.loc[(df_shannon['PA(a)'] == 1) | (df_shannon['PA(a)'] == 0), 'MMCond'] = 0

df_shannon['z(a,s)'] = (df_shannon['u(a(s))']/df_shannon['avglambda i'])
df_shannon['z(a,s)'] = df_shannon['z(a,s)'].apply(np.exp)
df_shannon['z(b,s)'] = (df_shannon['u(b(s))']/df_shannon['avglambda i'])
df_shannon['z(b,s)'] = df_shannon['z(b,s)'].apply(np.exp)
df_shannon['Shannon NSCond avg i'] = df_shannon['mu(s)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shanno
n['z(a,s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)'])
df_shannon['Shannon NSCond avg i'] = df_shannon.groupby(['User ID', 'Question ID', 'Chosen Action'])['Shannon
NSCond avg i'].transform('sum')-1
df_shannon['MMCond avg i'] = df_shannon['PA(a)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z(a,

```

```

s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)']) - df_shannon['PA(a|s)']
df_shannon.loc[(df_shannon['PA(a)'] == 1) | (df_shannon['PA(a)'] == 0), 'MMCond avg i'] = 0

df_shannon['z(a,s)'] = (df_shannon['u(a(s))']/df_shannon['avglambda'])
df_shannon['z(a,s)'] = df_shannon['z(a,s)'].apply(np.exp)
df_shannon['z(b,s)'] = (df_shannon['u(b(s))']/df_shannon['avglambda'])
df_shannon['z(b,s)'] = df_shannon['z(b,s)'].apply(np.exp)
df_shannon['Shannon NSCond avg'] = df_shannon['mu(s)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon[
'z(a,s)']+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)'])
df_shannon['Shannon NSCond avg'] = df_shannon.groupby(['User ID', 'Question ID', 'Chosen Action'])['Shannon NS
Cond avg'].transform('sum')-1
df_shannon['MMCond avg'] = df_shannon['PA(a)']*df_shannon['z(a,s)']/(df_shannon['PA(a)']*df_shannon['z(a,s)']
)+(1-df_shannon['PA(a)'])*df_shannon['z(b,s)']) - df_shannon['PA(a|s)']
df_shannon.loc[(df_shannon['PA(a)'] == 1) | (df_shannon['PA(a)'] == 0), 'MMCond avg'] = 0

df_shannon.drop('z(a,s)', axis=1, inplace=True)
df_shannon.drop('z(b,s)', axis=1, inplace=True)

# Testing necessary and sufficient conditions for Shannon; self-explanatory
temp = [df_shannon[(df_shannon['User ID'] == userid) & (df_shannon['PA(a)'] > 0) & (df_shannon['State'] == 0
)]['Shannon NSCond avg i'].tolist() for userid in Indiv]
temp2 = [df_shannon[(df_shannon['User ID'] == userid) & (df_shannon['State'] == 0)]['Shannon NSCond avg i'].
tolist() for userid in Indiv]
temp3 = [df_shannon[(df_shannon['User ID'] == userid)]['MMCond avg i'].tolist() for userid in Indiv]

Shannon_ttest_indiv1 = np.array([ttest2s(temp[indiv]) for indiv in range(0,len(temp)-1)])
Shannon_ttest_indiv2 = np.array([ttest1s(temp2[indiv]) for indiv in range(0,len(temp2)-1)])
Shannon_ttest_indiv3 = np.array([ttest2s(temp3[indiv]) for indiv in range(0,len(temp3)-1)])
print('Shannon: t-test for each individual allowing for heterog. cost functions (t-stat,p-value)')
print('For PA(a) > 0; H0: cond == 0')
print(Shannon_ttest_indiv1)
print('For all a; H0: cond <= 0')
print(Shannon_ttest_indiv2)
print('MM; H0: cond == 0')
print(Shannon_ttest_indiv3)

Shannon_ttest_poolindiv1 = ttest2s([x for x in np.concatenate(temp) if str(x) != 'nan'])
Shannon_ttest_poolindiv2 = ttest1s([x for x in np.concatenate(temp2) if str(x) != 'nan'])
Shannon_ttest_poolindiv3 = ttest2s([x for x in np.concatenate(temp3) if str(x) != 'nan'])
print('Shannon: t-test pooling all individuals allowing for heterog. cost functions (t-stat,p-value)')
print('For PA(a) > 0; H0: cond == 0')
print(Shannon_ttest_poolindiv1)
print('For all a; H0: cond <= 0')
print(Shannon_ttest_poolindiv2)
print('MM; H0: cond == 0')
print(Shannon_ttest_poolindiv3)

temp = [df_shannon[(df_shannon['User ID'] == userid) & (df_shannon['PA(a)'] > 0) & (df_shannon['State'] == 0
)]['Shannon NSCond avg'].tolist() for userid in Indiv]
temp2 = [df_shannon[(df_shannon['User ID'] == userid) & (df_shannon['State'] == 0)]['Shannon NSCond avg'].to
list() for userid in Indiv]
temp3 = [df_shannon[(df_shannon['User ID'] == userid)]['MMCond avg'].tolist() for userid in Indiv]

Shannon_avg_ttest_indiv1 = np.array([ttest2s(temp[indiv]) for indiv in range(0,len(temp)-1)])
Shannon_avg_ttest_indiv2 = np.array([ttest1s(temp2[indiv]) for indiv in range(0,len(temp2)-1)])
Shannon_avg_ttest_indiv3 = np.array([ttest2s(temp3[indiv]) for indiv in range(0,len(temp3)-1)])
print('Shannon: t-test for each individual with same cost function (t-stat,p-value)')
print('For PA(a) > 0; H0: cond == 0')
print(Shannon_avg_ttest_indiv1)
print('For all a; H0: cond <= 0')
print(Shannon_avg_ttest_indiv2)
print('MM; H0: cond == 0')
print(Shannon_avg_ttest_indiv3)

Shannon_avg_ttest_poolindiv1 = ttest2s([x for x in np.concatenate(temp) if str(x) != 'nan'])
Shannon_avg_ttest_poolindiv2 = ttest1s([x for x in np.concatenate(temp2) if str(x) != 'nan'])
Shannon_avg_ttest_poolindiv3 = ttest2s([x for x in np.concatenate(temp3) if str(x) != 'nan'])
print('Shannon: t-test pooling all individuals allwith same cost function (t-stat,p-value)')
print('For PA(a) > 0; H0: cond == 0')
print(Shannon_avg_ttest_poolindiv1)
print('For all a; H0: cond <= 0')
print(Shannon_avg_ttest_poolindiv2)
print('MM; H0: cond == 0')
print(Shannon_avg_ttest_poolindiv3)

```

Once deleted, variables cannot be recovered. Proceed (y/[n])? y

NIAC: smallest difference

```
[ 0.          -0.35400752 -0.17307692 -0.225         -0.08082707 -0.34377078
-2.02790552 -1.41344969 -3.82211795 -1.02857143 -0.25         -0.25817308
-1.11364694 -0.85909539 -1.37965596 -2.16769481  0.125         -0.69012605
-0.14983994  0.          0.          -0.37364166 -1.88961039 -0.32263514]
```

Elements in the vector are all zero

Elements in the vector are all zero

NIAC: t-test for each individual (t-stat,p-value)

```
[[ 1.34054549e+01  7.34751394e-20]
 [ 8.78885587e+00  1.28635212e-12]
 [ 1.30496724e+01  2.42303473e-19]
 [ 4.48519922e+00  1.71116192e-05]
 [ 1.29561181e+01  3.32506071e-19]
 [ 8.78152812e+00  1.32318659e-12]
 [-7.94315638e+00  1.00000000e+00]
 [ 1.16419009e+01  3.19040582e-17]
 [-1.53482128e+01  1.00000000e+00]
 [ 5.18291660e+00  1.39449465e-06]
 [ 1.79867646e+01  6.31602677e-26]
 [ 2.15042887e+00  1.78149181e-02]
 [-4.94040198e+00  9.99996617e-01]
 [ 4.71852142e+00  7.51016072e-06]
 [-1.55297296e+01  1.00000000e+00]
 [-1.15276522e+01  1.00000000e+00]
 [ 1.98687567e+01  4.04000335e-28]
 [-7.78435133e+00  1.00000000e+00]
 [ 1.23799008e+01  2.39369508e-18]
 [          nan  1.00000000e+00]
 [          nan  1.00000000e+00]
 [ 1.05352201e+01  1.75826592e-15]
 [-7.73302824e+00  1.00000000e+00]
 [ 5.44405810e+00  5.29310327e-07]]
```

NIAC: t-test pooling all individuals (t-stat,p-value)

(14.255407067995538, 1.5702422430857881e-43)

NIAS

	User ID	Question ID	Chosen Action	Sum mu(s)	PA(a s)[u(a(s))-u(b(s))]
0	601	8	10		-0.228365
1	601	8	11		-0.228365
2	601	9	12		0.000000
3	601	9	13		0.000000
4	601	10	14		0.000000
5	601	10	15		0.000000
6	601	11	16		0.000000
7	601	11	17		0.000000
8	602	8	10		2.598346
9	602	8	11		2.598346
10	602	9	12		2.675595
11	602	9	13		2.675595
12	602	10	14		-0.028788
13	602	10	15		-0.028788
14	602	11	16		3.875000
15	602	11	17		3.875000
16	603	8	10		2.493506
17	603	8	11		2.493506
18	603	9	12		2.334615
19	603	9	13		2.334615
20	603	10	14		0.464286
21	603	10	15		0.464286
22	603	11	16		5.000000
23	603	11	17		5.000000
24	604	8	10		2.750000
25	604	8	11		2.750000
26	604	9	12		2.750000
27	604	9	13		2.750000
28	604	10	14		0.452922
29	604	10	15		0.452922
..
162	621	9	12		0.000000
163	621	9	13		0.000000
164	621	10	14		0.000000
165	621	10	15		0.000000
166	621	11	16		0.000000
167	621	11	17		0.000000
168	622	8	10		-0.141667
169	622	8	11		-0.141667

170	622	9	12	0.625437
171	622	9	13	0.625437
172	622	10	14	0.084375
173	622	10	15	0.084375
174	622	11	16	-0.425638
175	622	11	17	-0.425638
176	623	8	10	2.750000
177	623	8	11	2.750000
178	623	9	12	0.954004
179	623	9	13	0.954004
180	623	10	14	0.500000
181	623	10	15	0.500000
182	623	11	16	4.642857
183	623	11	17	4.642857
184	624	8	10	0.013889
185	624	8	11	0.013889
186	624	9	12	2.671875
187	624	9	13	2.671875
188	624	10	14	0.500000
189	624	10	15	0.500000
190	624	11	16	4.791667
191	624	11	17	4.791667

[192 rows x 4 columns]

Individuals failing NIAS deterministically

	User ID	Question ID	Chosen Action	Sum $\mu(s)$	$PA(a s)[u(a(s))-u(b(s))]$
0	601	8	10		-0.228365
1	601	8	11		-0.228365
12	602	10	14		-0.028788
13	602	10	15		-0.028788
44	606	10	14		-0.010746
45	606	10	15		-0.010746
60	608	10	14		-0.005769
61	608	10	15		-0.005769
70	609	11	16		-0.357143
71	609	11	17		-0.357143
96	613	8	10		-0.155449
97	613	8	11		-0.155449
114	615	9	12		-0.112013
115	615	9	13		-0.112013
132	617	10	14		-0.136767
133	617	10	15		-0.136767
148	619	10	14		-0.012987
149	619	10	15		-0.012987
168	622	8	10		-0.141667
169	622	8	11		-0.141667
174	622	11	16		-0.425638
175	622	11	17		-0.425638

Elements in the vector are all zero

Elements in the vector are all zero

NIAS: t-test for each individual (t-stat,p-value)

```
[[ -1.63299316e+00  9.26755628e-01]
 [  4.52281332e+00  1.36149094e-03]
 [  4.51348647e+00  1.37675647e-03]
 [  4.97554671e+00  8.04528746e-04]
 [  2.91588324e+00  1.12356943e-02]
 [  2.07729113e+00  3.81950195e-02]
 [  1.63299316e+00  7.32443715e-02]
 [  3.46561867e+00  5.23385301e-03]
 [  1.53111946e+00  8.47985328e-02]
 [  3.30125457e+00  6.54904663e-03]
 [  3.72531683e+00  3.70207325e-03]
 [  4.61507793e+00  1.22014306e-03]
 [  2.51861392e+00  1.99456440e-02]
 [  4.10527488e+00  2.27140394e-03]
 [ -1.11285308e+00  8.48738930e-01]
 [  7.51581353e+00  6.77453933e-05]
 [  3.98583786e+00  2.64220087e-03]
 [  4.47698592e+00  1.43833880e-03]
 [  2.37864045e+00  2.44899589e-02]
 [          nan  1.00000000e+00]
 [          nan  1.00000000e+00]
 [  2.61393398e-01  4.00656576e-01]
 [  3.82268750e+00  3.25972025e-03]
 [  2.96896124e+00  1.04192109e-02]]
```

NIAS: t-test pooling all individuals (t-stat,p-value)

```

(11.09683395728077, 1.054914752141725e-22)
Elements in the vector are all zero
Elements in the vector are all zero
Shannon: t-test for each individual allowing for heterog. cost functions (t-stat,p-value)
For PA(a) > 0; H0: cond == 0
[[ 1.02832933  0.36191008]
 [ 0.28516293  0.78377208]
 [ 0.5223888  0.61751917]
 [ 0.25241293  0.80797319]
 [ 0.91670062  0.38978884]
 [ 0.39364535  0.70555804]
 [ 0.1644788  0.87400298]
 [ 0.7511978  0.47702322]
 [ 0.29913999  0.77351935]
 [ 0.19940572  0.84761405]
 [ 0.11344127  0.91286568]
 [ 0.41185653  0.69276369]
 [ 0.39112902  0.70733408]
 [ 0.54569546  0.60222308]
 [ 0.35591255  0.73239075]
 [ 0.44727929  0.66818585]
 [ 0.49453495  0.63606956]
 [ 0.1738381  0.86691315]
 [ 0.50269649  0.63060413]
 [          nan          nan]
 [          nan          nan]
 [ 0.20595851  0.84268525]
 [ 0.48058841  0.64546529]]
For all a; H0: cond <= 0
[[ 1.92731831  0.04764889]
 [ 0.28516293  0.39188604]
 [ 0.5223888  0.30875959]
 [ 0.25241293  0.40398659]
 [ 0.91670062  0.19489442]
 [ 0.39364535  0.35277902]
 [ 0.1644788  0.43700149]
 [ 0.7511978  0.23851161]
 [ 0.29913999  0.38675967]
 [ 0.19940572  0.42380703]
 [ 0.11344127  0.45643284]
 [ 0.41185653  0.34638185]
 [ 0.39112902  0.35366704]
 [ 0.54569546  0.30111154]
 [ 0.35591255  0.36619538]
 [ 0.44727929  0.33409292]
 [ 0.49453495  0.31803478]
 [ 0.1738381  0.43345658]
 [ 0.50269649  0.31530207]
 [          nan          nan]
 [          nan          nan]
 [ 0.20595851  0.42134263]
 [ 0.48058841  0.32273265]]
MM; H0: cond == 0
[[ -9.02861551e-16  1.00000000e+00]
 [  0.00000000e+00  1.00000000e+00]
 [  3.04019329e-16  1.00000000e+00]
 [  2.23964266e-16  1.00000000e+00]
 [ -3.15981790e-16  1.00000000e+00]
 [  0.00000000e+00  1.00000000e+00]
 [ -1.76102523e-16  1.00000000e+00]
 [ -1.10262080e-16  1.00000000e+00]
 [  0.00000000e+00  1.00000000e+00]
 [  5.26303143e-16  1.00000000e+00]
 [  1.43711833e-16  1.00000000e+00]
 [ -7.88492250e-17  1.00000000e+00]
 [  9.55292234e-16  1.00000000e+00]
 [ -8.31382890e-17  1.00000000e+00]
 [  0.00000000e+00  1.00000000e+00]
 [  5.13169796e-17  1.00000000e+00]
 [  1.90982899e-16  1.00000000e+00]
 [  1.13236422e-16  1.00000000e+00]
 [  0.00000000e+00  1.00000000e+00]
 [          nan  1.00000000e+00]
 [          nan  1.00000000e+00]
 [ -1.46207035e-16  1.00000000e+00]
 [  1.07427783e-16  1.00000000e+00]]

```



```

Shannon: t-test pooling all individuals allowing for heterog. cost functions (t-stat,p-value)
For PA(a) > 0; H0: cond == 0
(1.6097901198586286, 0.10927746080267502)
For all a; H0: cond <= 0
(1.6943645842810426, 0.045987438661756211)
MM; H0: cond == 0
(3.0852375045474666e-16, 0.99999999999999978)
Elements in the vector are all zero
Elements in the vector are all zero
Elements in the vector are all zero
Elements in the vector are all zero
Shannon: t-test for each individual with same cost function (t-stat,p-value)
For PA(a) > 0; H0: cond == 0
[[ 1.02832933 0.36191008]
 [ 0.28213062 0.78600258]
 [ 0.48645905 0.64150166]
 [ 0.14111055 0.89175763]
 [ 0.91740908 0.38944234]
 [ 0.37595982 0.71808168]
 [ 0.16448679 0.87399692]
 [ 0.69012585 0.51233916]
 [ 0.29839041 0.77406799]
 [ 0.18011967 0.86216206]
 [ 0.11343275 0.91287219]
 [ 0.41206726 0.69261626]
 [ 0.39114708 0.70732133]
 [ 0.54393741 0.60336956]
 [ 0.35277284 0.73464233]
 [ 0.44709489 0.6683127 ]
 [ 0.49380696 0.63655825]
 [ 0.17254231 0.86789396]
 [ 0.49352713 0.63674614]
 [      nan 1.      ]
 [      nan 1.      ]
 [ 0.20585759 0.8427611 ]
 [ 0.48094749 0.6452225 ]]
For all a; H0: cond <= 0
[[ 1.92715689 0.04766021]
 [ 0.28213062 0.39300129]
 [ 0.48645905 0.32075083]
 [ 0.14111055 0.44587882]
 [ 0.91740908 0.19472117]
 [ 0.37595982 0.35904084]
 [ 0.16448679 0.43699846]
 [ 0.69012585 0.25616958]
 [ 0.29839041 0.38703399]
 [ 0.18011967 0.43108103]
 [ 0.11343275 0.4564361 ]
 [ 0.41206726 0.34630813]
 [ 0.39114708 0.35366066]
 [ 0.54393741 0.30168478]
 [ 0.35277284 0.36732116]
 [ 0.44709489 0.33415635]
 [ 0.49380696 0.31827912]
 [ 0.17254231 0.43394698]
 [ 0.49352713 0.31837307]
 [ 2.01967807 0.04158491]
 [ 2.01967807 0.04158491]
 [ 0.20585759 0.42138055]
 [ 0.48094749 0.32261125]]
MM; H0: cond == 0
[[ -1.52080807e-15 1.00000000e+00]
 [ 4.18833280e-16 1.00000000e+00]
 [ 4.13726096e-16 1.00000000e+00]
 [ 3.51233660e-16 1.00000000e+00]
 [ 4.41600734e-16 1.00000000e+00]
 [ -2.04348899e-16 1.00000000e+00]
 [ 1.77499036e-16 1.00000000e+00]
 [ 3.25003316e-16 1.00000000e+00]
 [ 3.78080785e-16 1.00000000e+00]
 [ 3.00452674e-16 1.00000000e+00]
 [ 4.51749222e-16 1.00000000e+00]
 [ 7.20827094e-16 1.00000000e+00]
 [ 5.85682105e-16 1.00000000e+00]
 [ 6.66451978e-16 1.00000000e+00]
 [ 3.50339756e-16 1.00000000e+00]

```

```
[ 4.94943187e-16  1.00000000e+00]
[ 8.87825051e-16  1.00000000e+00]
[ 1.02792283e-16  1.00000000e+00]
[ 1.64934708e-16  1.00000000e+00]
[          nan  1.00000000e+00]
[          nan  1.00000000e+00]
[ 0.00000000e+00  1.00000000e+00]
[ 0.00000000e+00  1.00000000e+00]]
```

Shannon: t-test pooling all individuals allwith same cost function (t-stat,p-value)

For $PA(a) > 0$; H_0 : $cond == 0$

(2.1345073230372655, 0.034154367435795308)

For all a; H_0 : $cond \leq 0$

(3.3469041281183984, 0.00049204421015822401)

MM; H_0 : $cond == 0$

(1.469453749639288e-15, 0.9999999999999878)

D:\Anaconda3\lib\site-packages\scipy\stats_distn_infrastructure.py:879: RuntimeWarning: invalid value encountered in greater

```
    return (self.a < x) & (x < self.b)
```

D:\Anaconda3\lib\site-packages\scipy\stats_distn_infrastructure.py:879: RuntimeWarning: invalid value encountered in less

```
    return (self.a < x) & (x < self.b)
```

D:\Anaconda3\lib\site-packages\scipy\stats_distn_infrastructure.py:1818: RuntimeWarning: invalid value encountered in less_equal

```
    cond2 = cond0 & (x <= self.a)
```

In []: # Procedure:

```
# get list of lists with all lambdas per individual;
# get avg lambdas per individual
# compute z(a,s)
# compute mu(s)*z(a,s)
# compute PA(a)*z(a,s)
# compute mu(s)*z(a,s)/Sum PA(c)*z(c,s)
# compute Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s')
```

Test per individual

```
# 2-sided t-test: Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s') -1 == 0 for a s.t. PA(a)>0
# 1-sided t-test: Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s') -1 <= 0 for any a
# 2-sided t-test: mu(s')*z(a,s')/Sum PA(c)*z(c,s') == PA(a|s)
```

Test pooling the individuals

```
# 2-sided t-test: Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s') -1 == 0 for a s.t. PA(a)>0
# 1-sided t-test: Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s') -1 <= 0 for any a
# 2-sided t-test: mu(s')*z(a,s')/Sum PA(c)*z(c,s') == PA(a|s)
```

Get avg lambdas pooling all individuals

```
# compute z(a,s)
# compute mu(s)*z(a,s)
# compute PA(c)*z(a,s)
# compute mu(s)*z(a,s)/Sum PA(c)*z(c,s)
# compute Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s')
```

Test per individual

```
# 2-sided t-test: Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s') -1 == 0 for a s.t. PA(a)>0
# 1-sided t-test: Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s') -1 <= 0 for any a
# 2-sided t-test: PA(s)*z(a,s)/Sum PA(c)*z(c,s') == PA(a|s)
```

Test pooling the individuals

```
# 2-sided t-test: Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s') -1 == 0 for a s.t. PA(a)>0
# 1-sided t-test: Sum s': mu(s')*z(a,s')/Sum PA(c)*z(c,s') -1 <= 0 for any a
# 2-sided t-test: PA(s)*z(a,s)/Sum PA(c)*z(c,s') == PA(a|s)
```