



TÉCNICO LISBOA

Pioneer 3-DX with EKF-SLAM

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Autonomous Systems

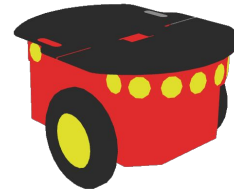
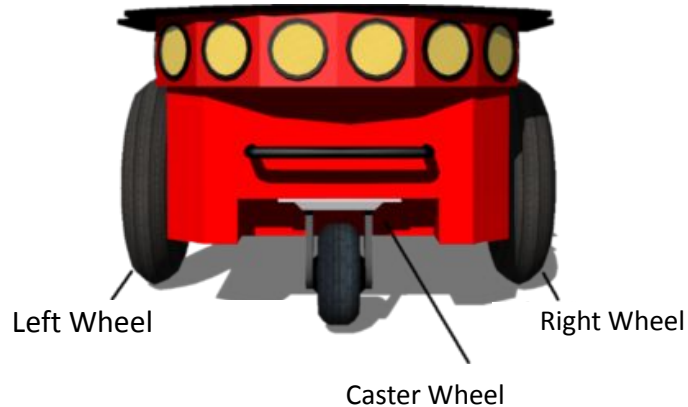
Group 17

June 2022

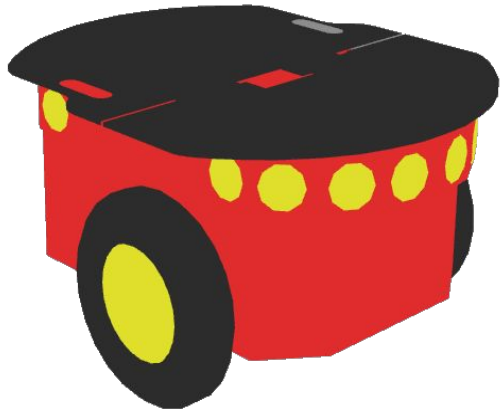
The project

Implement a **Simultaneous Localization And Mapping (SLAM)** algorithm

using an **Extended Kalman Filter (EKF)** on a **Pioneer 3-DX** robot.



Sensors

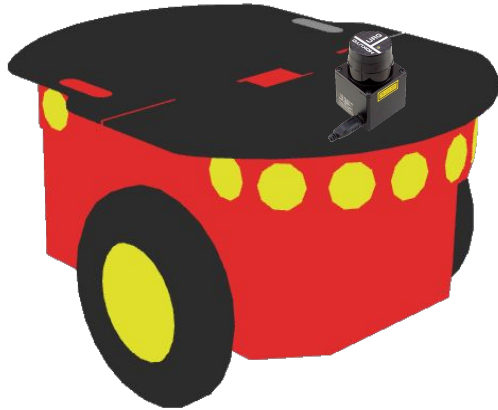


Incorporated in the robot

Odometer (left+right wheels)

8+8 sonars (front and back panels)

Sensors



Incorporated in the robot

Odometer (left+right wheels) ✓

~~8+8 sonars (front and back panels)~~

Connected through USB

Hokuyo Laser ✓

Hokuyo laser

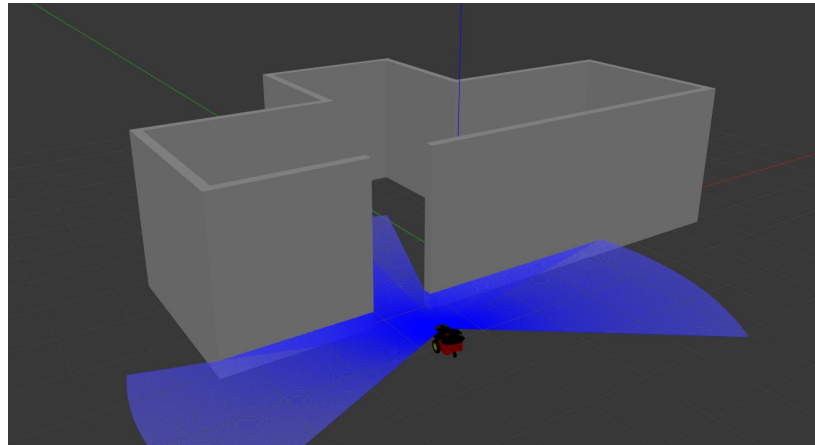
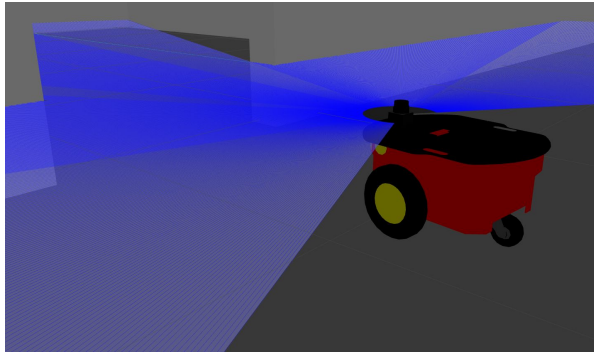


Model No.	URG-04LX-UG01
Power source	5VDC±5%(USB Bus power)
Light source	Semiconductor laser diode($\lambda=785\text{nm}$), Laser safety class 1
Measuring area	20 to 5600mm(white paper with 70mm×70mm), 240°
Accuracy	60 to 1,000mm : ±30mm, 1,000 to 4,095mm : ±3% of measurement
Angular resolution	Step angle : approx. 0.36°(360°/1,024 steps)
Scanning time	100ms/scan

Microsimulation



Gazebo creates simulated environments to test a robotic system



 [mario-sera / pioneer_p3dx_model](https://github.com/mario-sera/pioneer_p3dx_model) Public

The algorithm

$$\mu_t = \begin{bmatrix} x_t \\ y_t \\ \theta_t \\ m_{1,x,t} \\ m_{1,y,t} \\ \dots \\ m_{N,x,t} \\ m_{N,y,t} \end{bmatrix}$$

The robot moves and the new predicted state estimate is computed from the previous estimate

Prediction
step

Correction
step

Algorithm 1 Extended Kalman Filter ($\mu_{t-1}, \Sigma_{t-1}, u_t, z_t$)

1: $\bar{\mu}_t = f(u_t, \mu_{t-1})$

2: $\bar{\Sigma}_t = G_t \Sigma_{t-1} G_t^T + R_t$

3: $K_t = \bar{\Sigma}_t H_t^T (H_t \bar{\Sigma}_t H_t^T + Q_t)^{-1}$

4: $\mu_t = \bar{\mu}_t + K_t (z_t - h(\bar{\mu}_t))$

5: $\Sigma_t = (I - K_t H_t) \bar{\Sigma}_t$

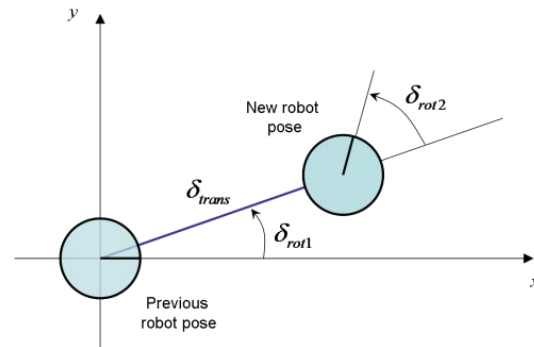
6: return μ_t, Σ_t

The laser identifies the known landmarks and the previous drawn map is corrected

Odometry and prediction step

Odometry

- The use of motion sensors to calculate the change of position of the robot in relation to a known position.
- 1st rotation + translation + 2nd rotation
- The motion model assumes that δ_{rot1} , δ_{trans} and δ_{rot2} are influenced by independent noise.

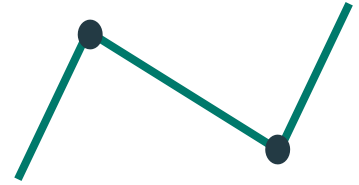


Prediction step

- The new estimate of the the predicted state is calculated from the previous estimate.

Landmarks

- We have used a mixture between lines and corners



Lines

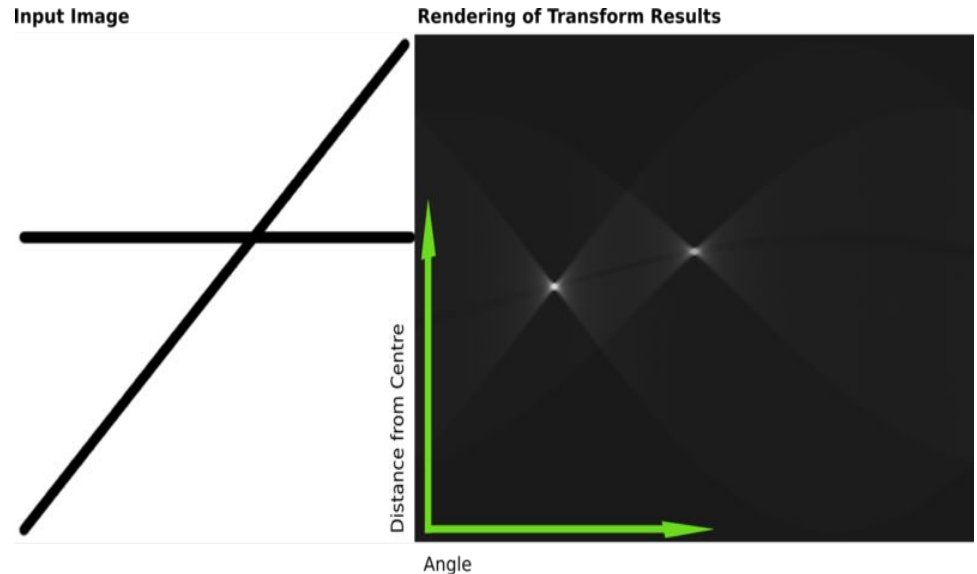
- Easy to identify
- Broad idea of the space around the robot
- Unexpected behavior in other more irregular environments

Corners

- Minimize the number of parameters exchanged between nodes
- Susceptible to noise
- The dots have to be connected to each other

Landmark detection and Hough transform

- Hough Transform is used to identify and isolate certain features presented in an image such as lines or circles.
- The points in Hough space have the form $P(\rho, \theta)$.



Hough transform

- It was implemented using the library in openCV

Probabilistic Hough Transform (used in order to detect lines/corners)

- Gives more accurate results
- Gives directly the starting and ending points of each line, which are the exact points the will be assumed as corners

Threshold: the minimum number of intersections in the parameters space to detect a line/corners

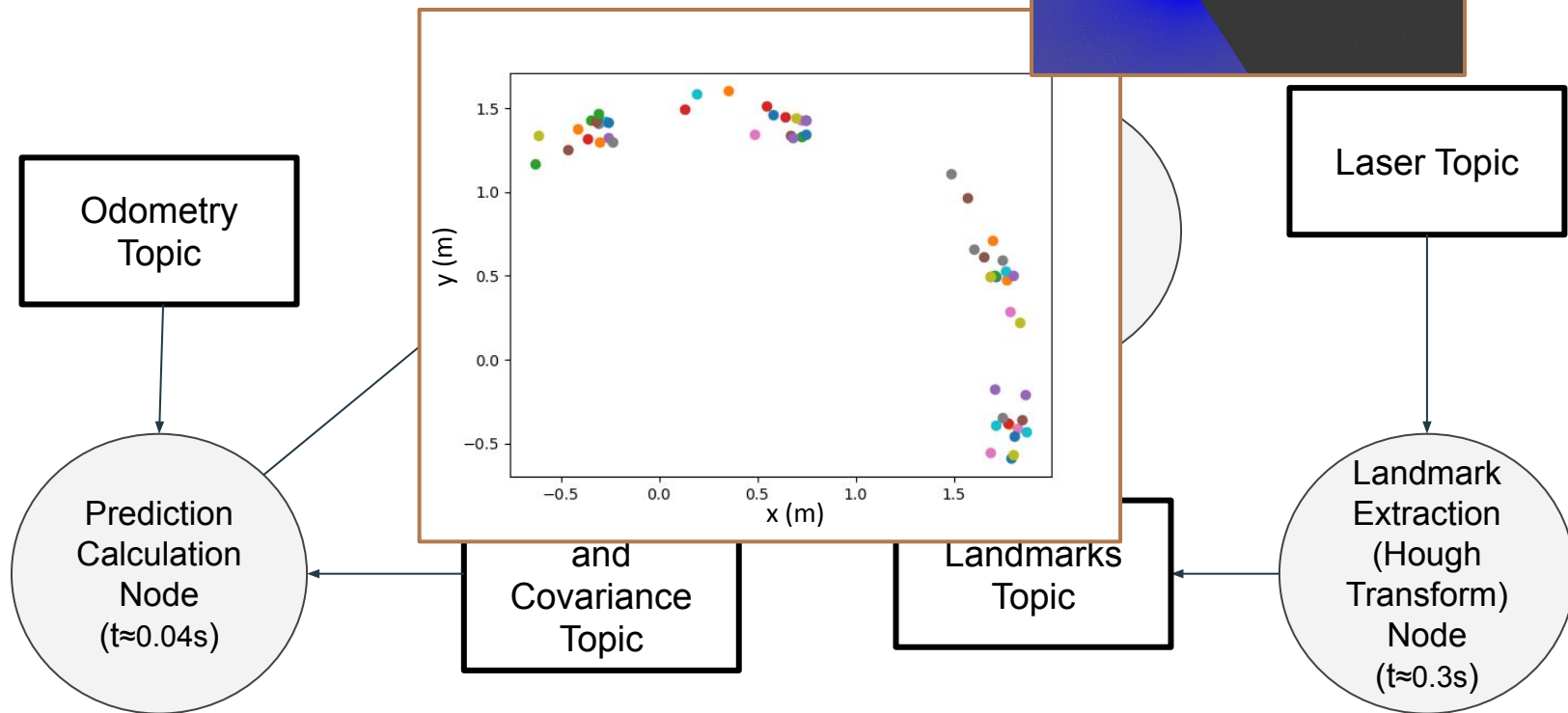


Standard method

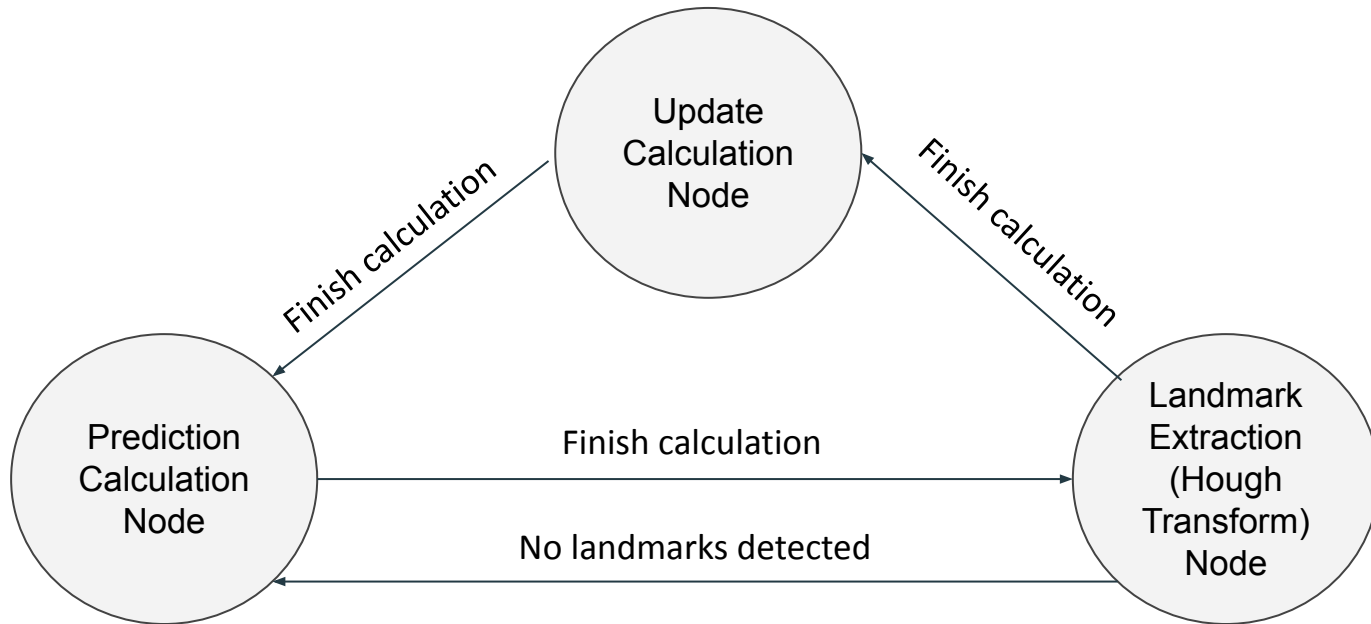


Probabilistic method

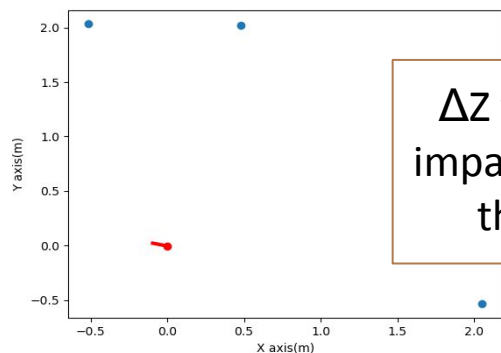
Synchronization problem



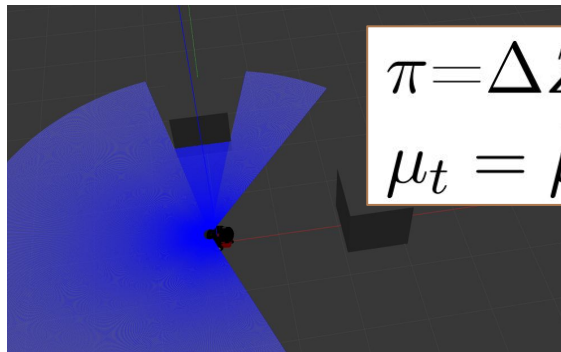
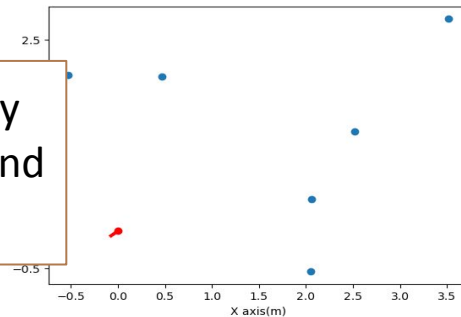
State machine implementation



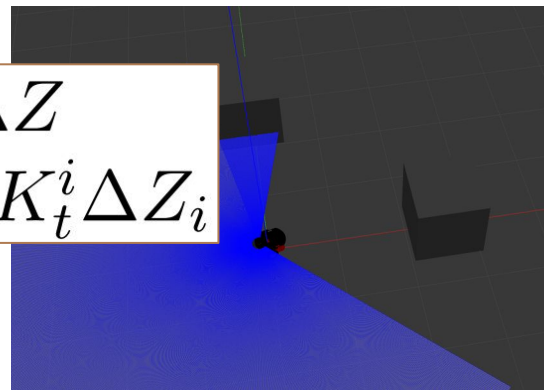
Discontinuity Problem



ΔZ vector discontinuity
impacts the matching and
the correction step

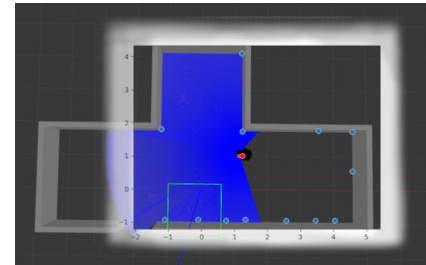
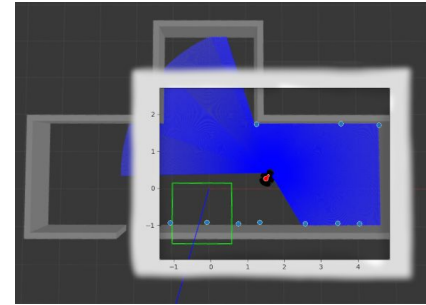
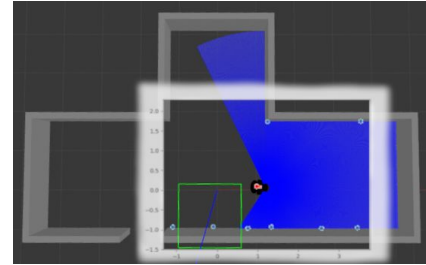
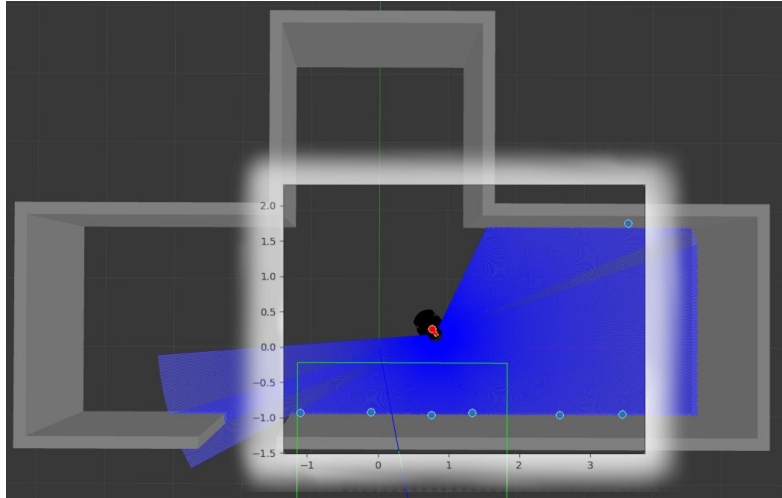


$$\pi = \Delta Z^T \Psi^{-1} \Delta Z$$
$$\mu_t = \bar{\mu}_t + \sum_i K_t^i \Delta Z_i$$



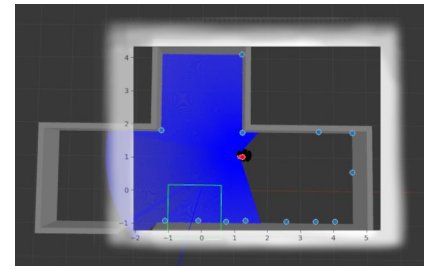
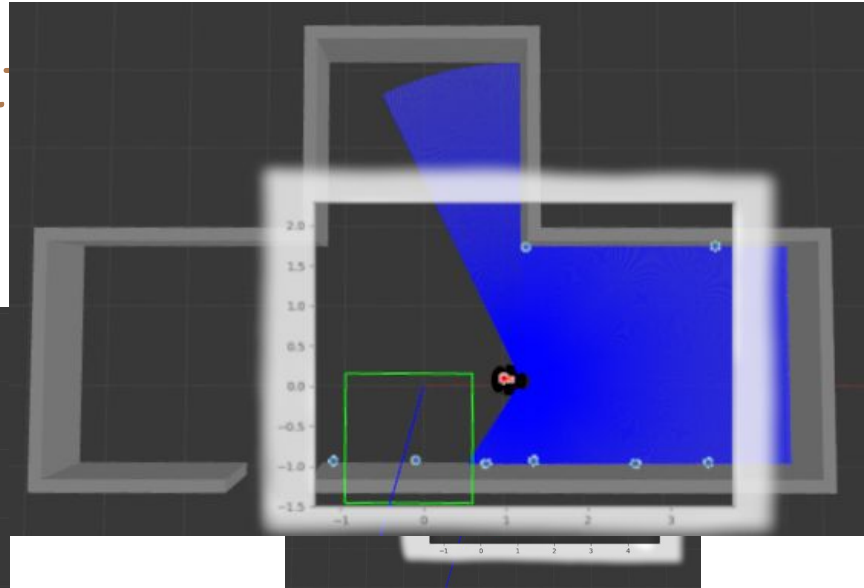
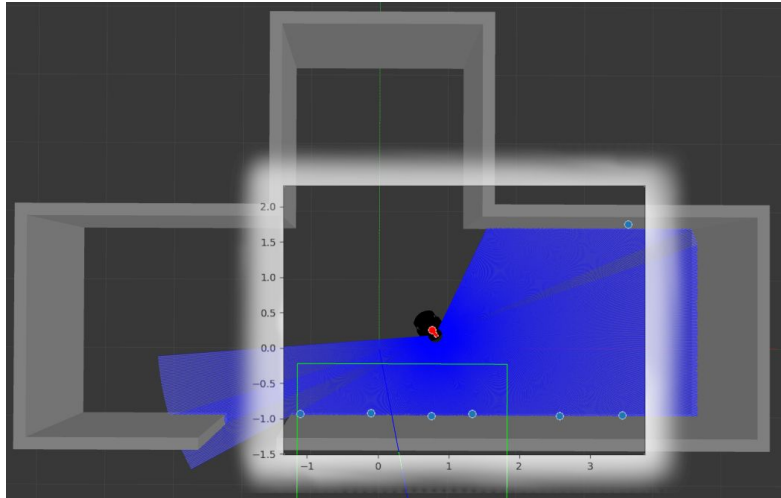
Microsimulation results

Using Gazebo to run and test our model



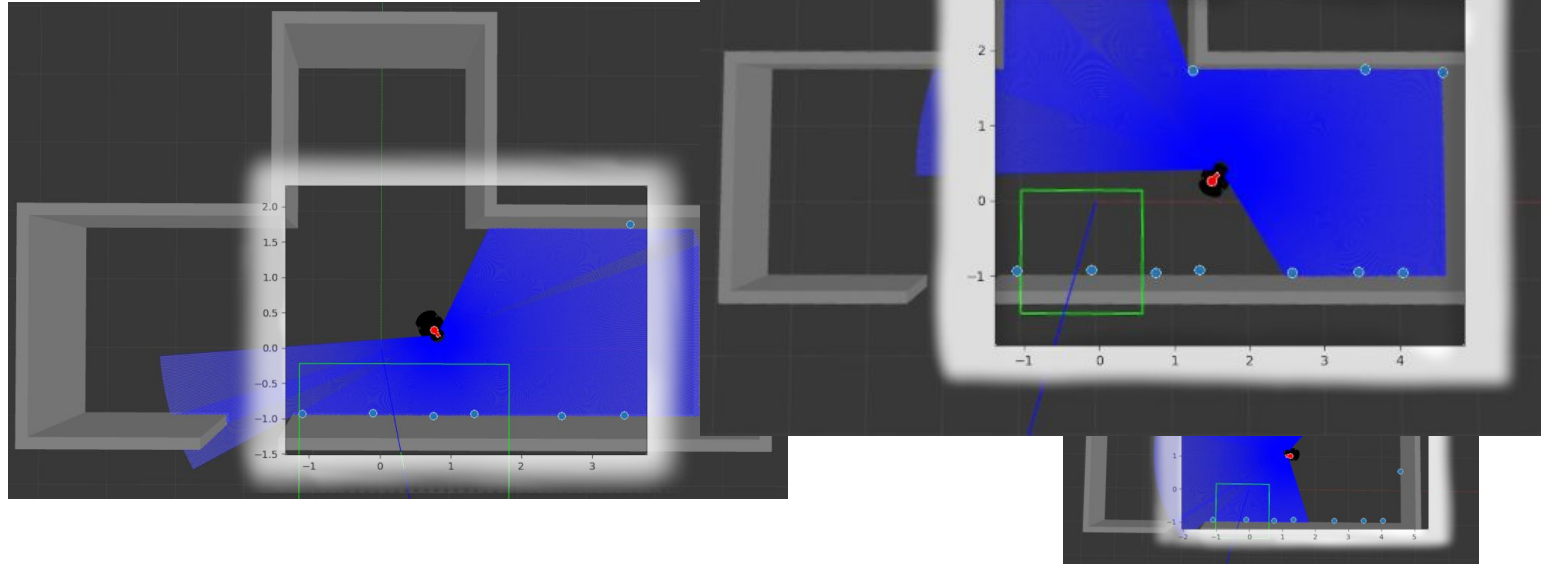
Microsimulation result

Using Gazebo to run and test our model



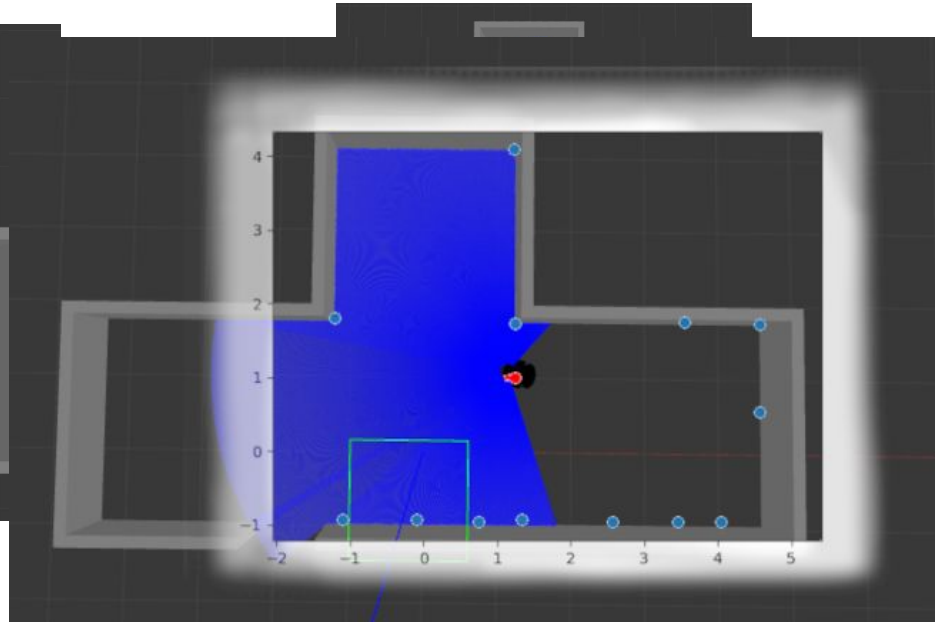
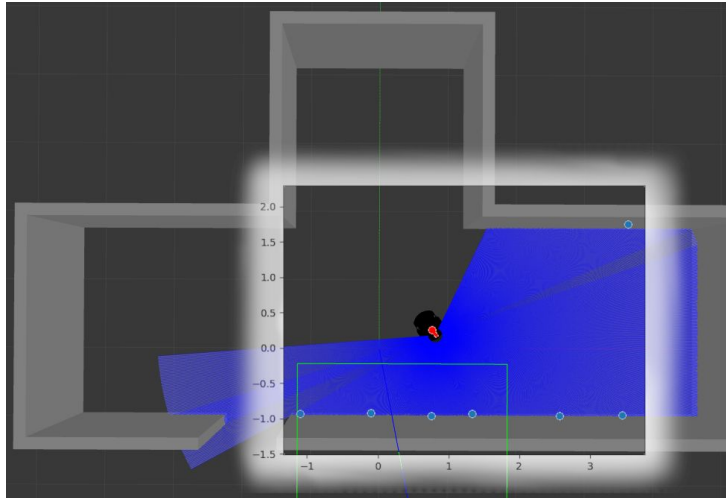
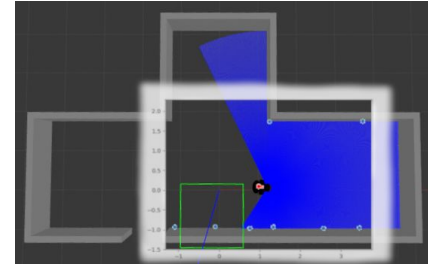
Microsimulation results

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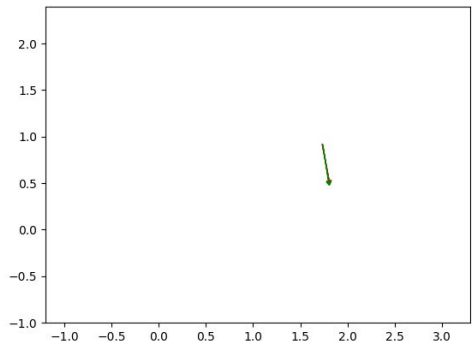


Microsimulation results

Using Gazebo to run and test our model

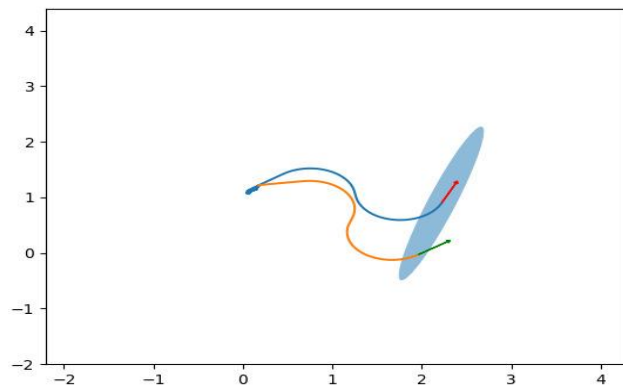


Other results

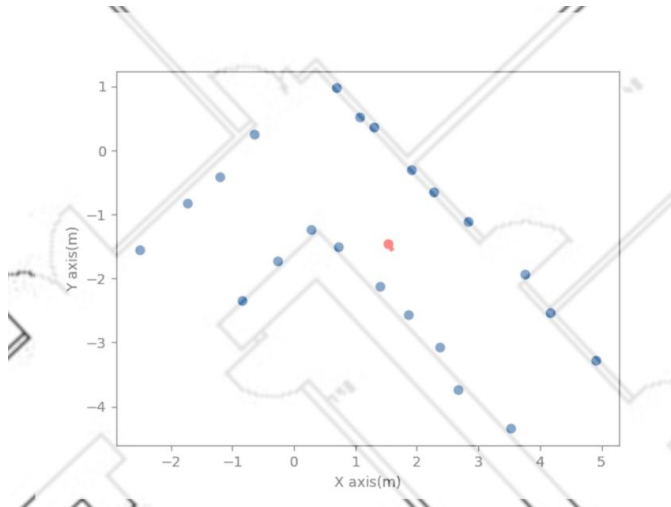


The pose prediction of the prediction method with noise influence (**blue path, red arrow**) and the truth position and orientation (**orange path, green arrow**).

The covariance matrix of the predicted pose can be represented as an ellipse



Experimental results



Results

- The algorithm is stable even after approximately 30 cycles.
- Seems to represent correctly the state vector
- Correction step is too slow (can take up to 40 seconds if there are 20 landmarks stored)

Future improvements

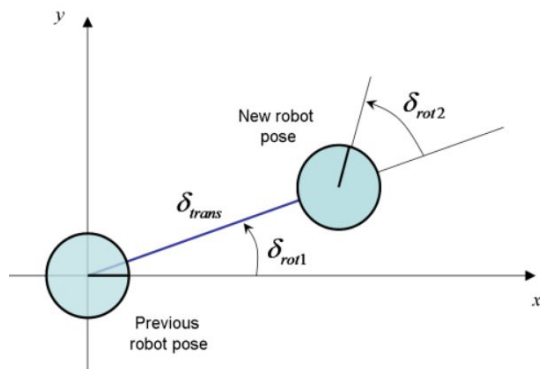
- Change our **Hough transform** algorithm:
 - Find a way of **automating** the choice of the **optimal parameters**.
- Optimize the measurement update algorithm:
 - Only apply the update with the landmarks **near the robot**.
 - Re-analyse whether **using lines** instead of corners could benefit **landmark matching**, reducing the computational load.



Thank you!

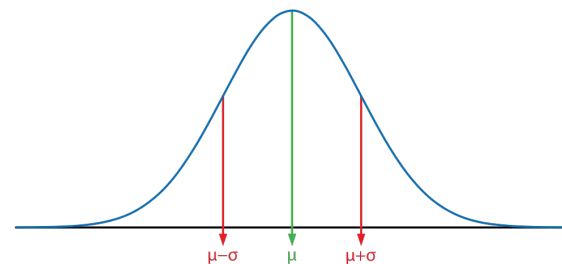


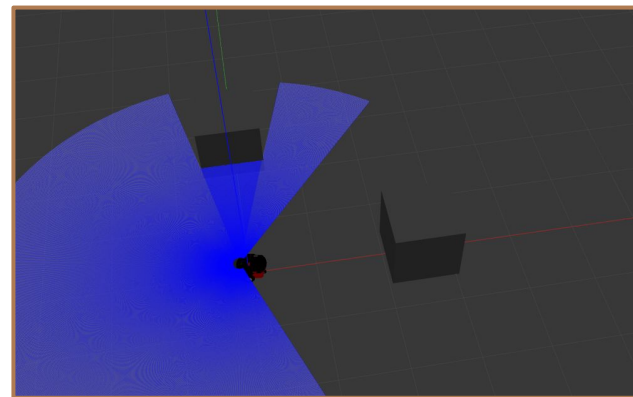
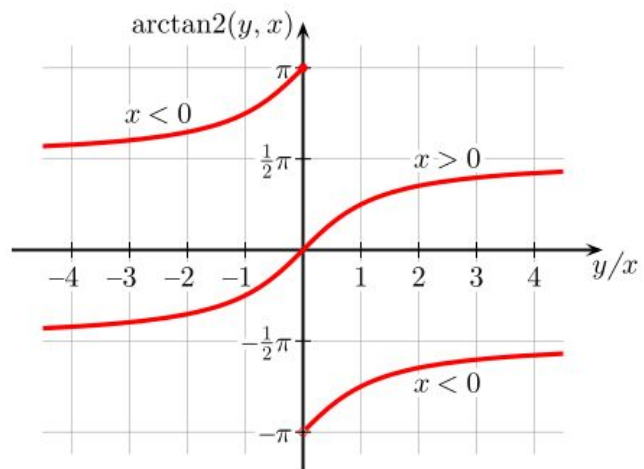
Adding noise to the simulation



$$\begin{cases} \sigma_{rot1} = \alpha_1 |\delta_{rot1}| + \alpha_2 |\delta_{trans}| \\ \sigma_{rot2} = \alpha_1 |\delta_{rot2}| + \alpha_2 |\delta_{trans}| \\ \sigma_{trans} = \alpha_3 |\delta_{trans}| + \alpha_4 (|\delta_{rot1}| + |\delta_{rot2}|) \end{cases}$$

$$\begin{cases} \varepsilon_{rot1} \sim \mathcal{N}(0, \sigma_{rot1}^2) \\ \varepsilon_{rot2} \sim \mathcal{N}(0, \sigma_{rot2}^2) \\ \varepsilon_{trans} \sim \mathcal{N}(0, \sigma_{trans}^2) \end{cases}$$





Covariance tests

