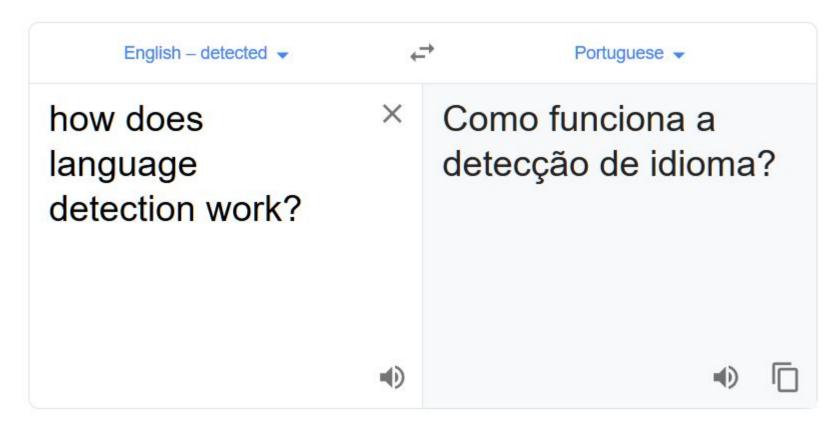
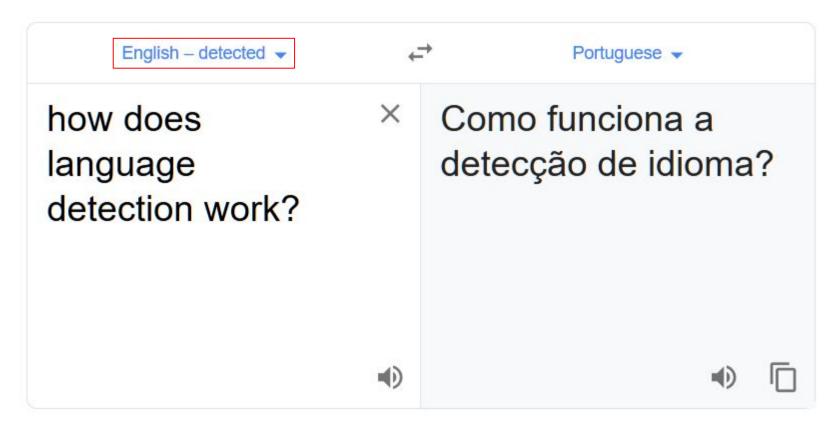
Language detection

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Goal: Software which goes from **text** (user input) to **language** (output)

System will learn from examples of what we want to do. We need to have:

- Examples of text in English
- Examples of text in Portuguese
- ... and so on for all languages we want to support

Where do we get these examples?

Getting the data

- By hand:
 - Time consuming
 - Need speakers of all languages we want to support
- We can use text from Wikipedia
 - Text from en.wikipedia.org is ~60 GB and we know it is English
 - Text from **de**.wikipedia.org is ~8 GB and we know it is **German**
 - o ... and so on

Now we have data.

What do we do with it?

How do we use the data?

- Let's look at sequences of 3 characters called trigrams
- From ~1 MB each of English and Portuguese text:

Trigram	Count in EN text	Count in PT text	EN : PT ratio
"de "	618	10964	1 : 18
"the"	14002	320	44 : 1
"ão "	6	4458	1 : 743
" th"	14538	338	43 : 1
"s d"	526	4074	1:7.7
"e f"	1508	1120	1.35 : 1

Example: "the cat"

Trigram	Count in EN text	Count in PT text
"the"	14002	320
"he "	13030	332
"e c"	1688	1910
" ca"	1581	2107
"cat"	429	163
PRODUCT	2.09e+17	6.97e+14

Example: "o gato"

Trigram	Count in EN text	Count in PT text
"o g"	148	594
" ga"	581	272
"gat"	90	65
"ato"	193	433
PRODUCT	1.49e+9	4.55e+9

Language Detector v1

- At system start:
 - O Grab 1 MB of text from Wikipedia for EN, PT, FR, ES, ...
 - Count frequencies of all trigrams in those files
- When user inputs text:
 - Multiply counts for all trigrams of input text
 - Language with highest product wins

Issues with v1

Issues with v1

- I have to have similar amount of text (1 MB) for all languages
- For longer sentences, product gets really big and can overflow
- Some sentences result in products of zero for all languages

What if I have different amounts of text per language?

Example: "o gato" with 10 MB of EN, 1 MB of PT

Trigram	1 MB EN	10 MB EN	1 MB PT
"o g"	148	148 x10	594
" ga"	581	581 x10	272
"gat"	90	90 x10	65
"ato"	193	193 x10	433
PRODUCT	1.49e+9	1.49e+13	4.55e+9

Use same amount of text?

• Difficult to get decent amounts of text for minor languages

Solution: divide by total number of trigrams in file

Trigram counts:

1 MB English: 1001976

• 10 MB English: 10019760

1 MB Portuguese: 997801

Trigram	1 MB EN	10 MB EN	1 MB PT
"o g"	148/1001976	1480/100197 60	594/997801
" ga"	581/1001976	5810/100197 60	272/997801
"gat"	90/1001976	900/1001976 0	65/997801
"ato"	193/1001976	1930/100197 60	433/997801
PRODUCT	1.48e-15	1.48e-15	4.59e-15

Language Detector v2

- At system start:
 - O Grab any size of text from Wikipedia for EN, PT, FR, ES, ...
 - O Count frequencies of all trigrams and total number of trigrams in those files
- When user inputs text:
 - Multiply (count / total trigrams) for all trigrams of input text
 - Language with highest product wins

Issues with v2

Issues with v2

- I have to have similar amount of text (1 MB) for all languages
- For longer sentences, product gets really small and can underflow
- Some sentences result in products of zero for all languages

How do I deal with underflow?

Solution: use logarithm of product instead

If X > Y, then
 log(X) > log(Y)

log(A*B*C*D) = log(A) +
 log(B) + log(C) + log(D)

Trigram	1 MB EN	1 MB PT
"o g"	log(148/1001976) = -3.83	log(594/997801) = -3.22
" ga"	log(581/1001976) = -3.23	log(272/997801) = -3.56
"gat"	log(90/1001976) = -4.05	log(65/997801) = -4.19
"ato"	log(193/1001976) = -3.72	log(433/997801) = -3.36
sum of logs	-14.83	-14.33

Language Detector v3

- At system start:
 - O Grab any size of text from Wikipedia for EN, PT, FR, ES, ...
 - Count frequencies of all trigrams and total number of trigrams in those files
- When user inputs text:
 - Add log (count / total trigrams) for all trigrams of input text
 - Language with highest (i.e. least negative) sum wins

Issues with v3

Issues with v3

- I have to have similar amount of text (1 MB) for all languages
- For longer sentences, product gets really small and can underflow
- Some sentences result in products of zero for all languages
- Some sentences result in log(0), it can't be computed

Some sentences get all products equal to zero

Example: "I stayed at Messeniuksenkatu in Finland"

Trigram	1 MB EN	1 MB PT
"i s"	log(40 / totalEN) = -4.40	log(55 / totalPT) = -4.26
"iuk"	log(0 / totalEN) = NaN	log(0 / totalPT) = NaN
"uks"	log(2 / totalEN) = -5.70	log(0 / totalPT) = NaN
"and"	log(5983 / totalEN) = -2.22	log(1686 / totalPT) = -2.77
Sum of logs	NaN	NaN

Solution (hack): add 1 to every count

Trigram	1 MB EN	1 MB PT
"i s"	log((40 + 1) / (totalEN + uEN)) = -4.39	log(55 + 1 / (totalPT + uPT)) = -4.25
"iuk"	log((0 + 1) / (totalEN + uEN)) = -6.00	log((0 + 1) / (totalPT + uPT)) = -6.00
"uks"	log((2 + 1) / (totalEN + uEN)) = -5.52	log((0 + 1) / (totalPT + uPT)) = -6.00
"and"	log((5983 + 1) / (totalEN + uEN)) = -2.22	log((1686 + 1) / (totalPT + uPT)) = -2.77
Sum of logs	-139.1	-154.6

... where uEN = unique trigrams in EN text, uPT = unique trigrams in PT text

Language Detector v4

- At system start:
 - O Grab any size of text from Wikipedia for EN, PT, FR, ES, ...
 - O Count frequencies of all trigrams, total number of trigrams, and unique trigrams in those files
- When user inputs text:
 - Add log ((count + 1) / (total trigrams + unique trigrams)) for all trigrams of input text
 - Language with highest (i.e. least negative) sum wins

Language Detector v4

- At system start:
 - O Grab any size of text from Wikipedia for EN, PT, FR, ES, ...
 - O Count frequencies of all trigrams, total number of trigrams, and unique trigrams in those files
- When user inputs text:
 - Add log ((count + 1) / (total trigrams + unique trigrams)) for all trigrams of input text
 - Language with highest (i.e. least negative) sum wins

Pseudo-code

Part 1: trigram counts and (corrected) probabilities

```
1: trigramCounts + dict()
2: trigramProbs ← dict()
3: For each language L:
      trigramCounts[L] ← dict()
4:
5:
      totalCounts ← 0.0
6:
      For each line in language's file:
            line ← line.lower()
8:
             For each trigram T in that line:
9:
                   trigramCounts[L][T] ← trigramCounts[L][T] + 1.0 /* should match the values in "counts_*.txt" */
10:
                   totalCounts ← totalCounts + 1.0
11:
      uniqueCounts + trigramCounts[L].size() // number of distinct trigrams for language L
12:
      trigramLogProbs[L] + dict()
13:
      denominator ← totalCounts + uniqueCounts
14:
      For each trigram T in trigramCounts:
15:
             numerator + trigramCounts[L][T] + 1.0
16:
            trigramLogProbs[L][T] + log10(numerator / denominator) /* should match the values in "logprobs_*.txt" */
17:
             trigramLogProbs[L]['__UNKNOWN___'] ← log10(1.0 / denominator)
```

Part 2: detecting the language

```
18: S ← input sentence
19: S ← S.lower()
20: For each language L:
      score[L] \leftarrow 0.0
22:
      For each trigram T in S:
23:
             If T is in trigramProbs[L]:
24:
                   score[L] + trigramProbs[L][T]
25:
             Else:
26:
                   score[L] ← score[L] + trigramProbs[L]['__UNKNOWN__']
/* Sentence's language is the one with highest score */
/* Scores will all be negative. That's normal. :) */
```

Thank you!

(feel free to ask for demo)

This is a case of the Naïve Bayes algorithm

$$\begin{aligned} \operatorname{argmax}_l p(l|t) &= \operatorname{argmax}_l \log p(l|t) = \operatorname{argmax}_l \frac{p(t|l)p(l))}{p(t)} = \operatorname{argmax}_l \log p(t|l)p(l) = \\ \operatorname{argmax}_l \log p(t|t) &= \operatorname{argmax}_l \log \left[p(t_1|l)p(t_2|l)...p(t_N|l) \right] = \operatorname{argmax}_l \left[\log(p(t_1|l)) + \log(p(t_2|l)) + ... + \log(p(t_N|l)) \right] \end{aligned}$$

Maximize probability of language I given the input text t

```
\begin{aligned} \operatorname{argmax}_l p(l|t) &= \operatorname{argmax}_l \log p(l|t) = \operatorname{argmax}_l \frac{p(t|l)p(l))}{p(t)} = \operatorname{argmax}_l \log p(t|l)p(l) = \\ \operatorname{argmax}_l \log p(t|l) &= \operatorname{argmax}_l \log \left[ p(t_1|l)p(t_2|l)...p(t_N|l) \right] = \operatorname{argmax}_l \left[ \log(p(t_1|l)) + \log(p(t_2|l)) + ... + \log(p(t_N|l)) \right] \end{aligned}
```

$$X > Y \Rightarrow log(X) > log(Y)$$

```
 \begin{aligned} \operatorname{argmax}_l p(l|t) &= \operatorname{argmax}_l \log p(l|t) = \operatorname{argmax}_l \frac{p(t|l)p(l))}{p(t)} = \operatorname{argmax}_l \log p(t|l)p(l) = \\ \operatorname{argmax}_l \log p(t|l) &= \operatorname{argmax}_l \log [p(t_1|l)p(t_2|l)...p(t_N|l)] = \operatorname{argmax}_l [\log(p(t_1|l)) + \log(p(t_2|l)) + ... + \log(p(t_N|l))] \end{aligned} 
                                                                                                                           p(A|B) = p(B|A) p(A) / p(B)
```

(Bayes' Theorem)

```
\begin{aligned} \operatorname{argmax}_l p(l|t) &= \operatorname{argmax}_l \log p(l|t) = \operatorname{argmax}_l \frac{p(t|l)p(l))}{p(t)} = \operatorname{argmax}_l \log p(t|l)p(l) = \\ \operatorname{argmax}_l \log p(t|l) &= \operatorname{argmax}_l \log \left[ p(t_1|l)p(t_2|l)...p(t_N|l) \right] = \operatorname{argmax}_l \left[ \log(p(t_1|l)) + \ldots + \log(p(t_N|l)) \right] \end{aligned}
```

p(t) does not depend on l

$$\begin{aligned} \operatorname{argmax}_l p(l|t) &= \operatorname{argmax}_l \log p(l|t) = \operatorname{argmax}_l \frac{p(t|l)p(l))}{p(t)} = \operatorname{argmax}_l \log p(t|l)p(l) = \\ \operatorname{argmax}_l \log p(t|l) &= \operatorname{argmax}_l \log \left[p(t_1|l)p(t_2|l)...p(t_N|l) \right] = \operatorname{argmax}_l \left[\log(p(t_1|l)) + \ldots + \log(p(t_N|l)) \right] \end{aligned}$$

First assumption

Probability of the language of the user input is the same for all languages

(called Uniform Prior)

$$\begin{aligned} \operatorname{argmax}_l p(l|t) &= \operatorname{argmax}_l \log p(l|t) = \operatorname{argmax}_l \frac{p(t|l)p(l))}{p(t)} = \operatorname{argmax}_l \log p(t|l)p(l) = \\ \operatorname{argmax}_l \log p(t|l) &= \operatorname{argmax}_l \log \left[p(t_1|l)p(t_2|l)...p(t_N|l) \right] = \operatorname{argmax}_l \left[\log(p(t_1|l)) + \log(p(t_2|l)) + ... + \log(p(t_N|l)) \right] \end{aligned}$$

Second assumption

Probability of the text is equal to the product of the probabilities of its trigrams

(that's why it's called Naïve Bayes)

$$\operatorname{argmax}_{l} p(l|t) = \operatorname{argmax}_{l} \log p(l|t) = \operatorname{argmax}_{l} \frac{p(t|l)p(l)}{p(t)} = \operatorname{argmax}_{l} \log p(t|l)p(l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) = \operatorname{argmax}_{l} \log p(t|l) + \ldots + \log p(t|l) = \operatorname{argmax}_{l} \log p(t|$$

Example for French

Example: "the cat"

Trigram	Count in EN text	Count in FR text	Count in PT text
"the"	14002	380	320
"he "	13030	547	332
"e c"	1688	2725	1910
" ca"	1581	1372	2107
"cat"	429	322	163
PRODUCT	2.09e+17	2.50e+15	6.97e+14

Example: "le chat"

Trigram	Count in EN text	Count in FR text	Count in PT text
"le "	1329	6995	531
"e c"	1688	2725	1910
" ch"	1331	1270	635
"cha"	1058	1007	393
"hat"	988	22	18
PRODUCT	3.12e+15	5.36e+14	4.56e+12