A CS Faraday Depth Reconstruction Framework
for the MeerKAT MIGHTEE-POL Survey

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 miguelcarcamov
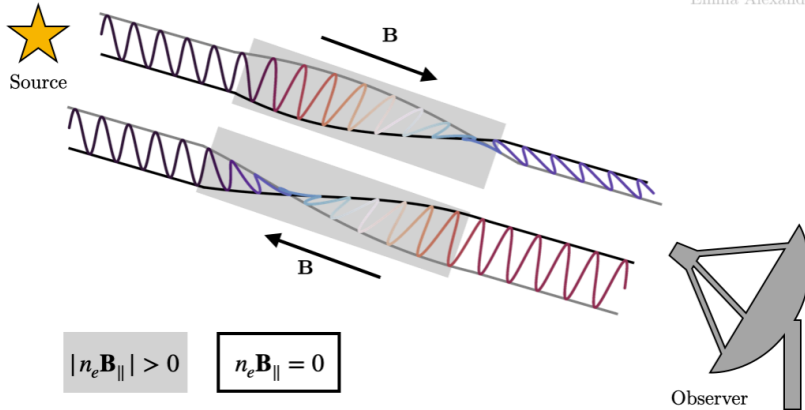 @miguel_carcamov

Anna Scaife, Russ Taylor, Matt Jarvis, Micah Bowles, Srikrishna Sekhar, Lennart Heino and Jeroen Stil
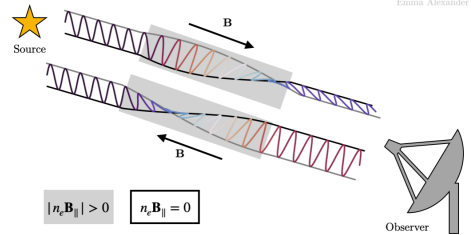
MANCHESTER
1824
The University of Manchester

Faraday rotation illustration. Credit: Emma Alexander.

Rotation Measure

$$\text{RM} = 0.81 \int_{\text{source}}^{\text{observer}} n_e(r) B_{||}(r) \cdot dr \text{ rad m}^{-2}$$

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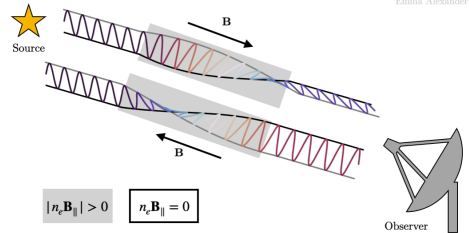What we want

Radio   X-Ray

$$F(\phi) = \frac{1}{K} \int_{-\infty}^{\infty} W(\lambda^2) P(\lambda^2) e^{-2i\phi\lambda^2} \, d\lambda^2,$$

$$P(\lambda^2) = |P(\lambda^2)| e^{2i\chi(\lambda^2)} = Q(\lambda^2) + iU(\lambda^2).$$

Faraday rotation illustration. Credit: Emma Alexander.

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- Subtraction of Galactic RM
- Spectral index correction

- Simulation of thin, thick or mixed sources
- Simulation of RFI flagging
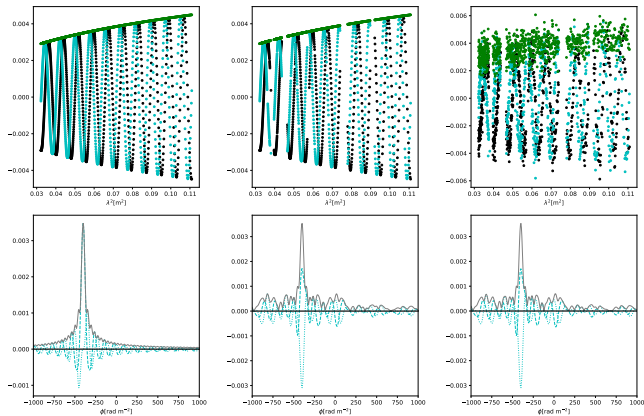- Noise application to simulated data
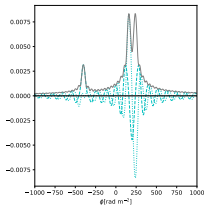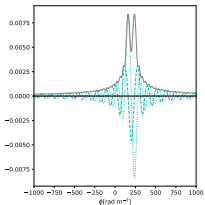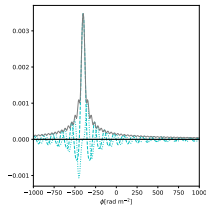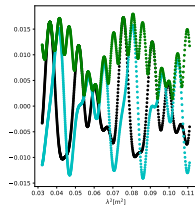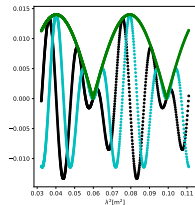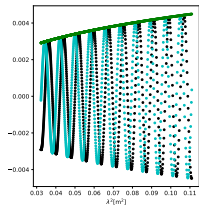
(a) Thin source (b) Thick source (c) Mixed source
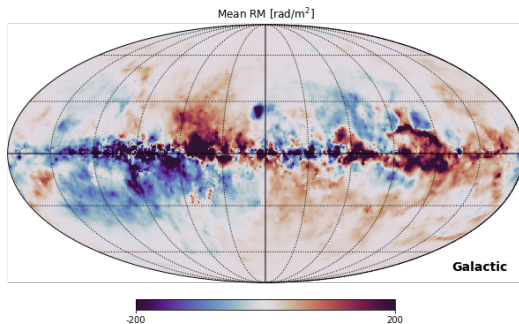
(a) Complete dataset

(b) 20% data removed

(c) 0.7 mJy/beam noise

- The framework applies the derotation directly in λ^2-space as a phase shift.

$$\hat{P}(\lambda^2) = P(\lambda^2)e^{-2i\phi_{GAL}\lambda^2}$$

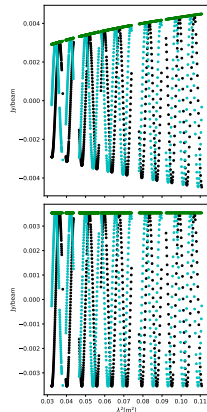Mean Galactic RM (Hutschenreuter et al., 2022)

$$F(\phi) = \frac{1}{K} \int_{-\infty}^{\infty} W(\lambda^2) \frac{P(\lambda^2)}{s(\lambda^2)} e^{-2i\phi\lambda^2} \, \mathrm{d}\lambda^2$$

$$s(\lambda^2) = \frac{I(\lambda^2)}{I(\lambda_0^2)} = \left(\frac{\lambda^2}{\lambda_0^2}\right)^{-\alpha/2}$$

- Brentjens and de Bruyn, 2005
- For real data we can use FITS/CASA spectral index images

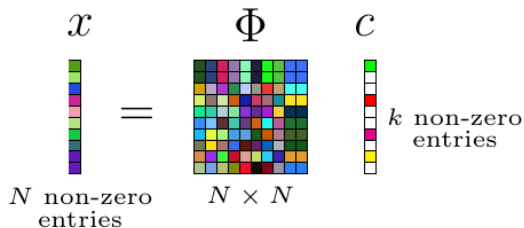λ^2-space before and after spectral index correction

- Technique that aims to solve inverse problems
- Finds the sparsest signal that is consistent with the measurements and to a specific constraint.

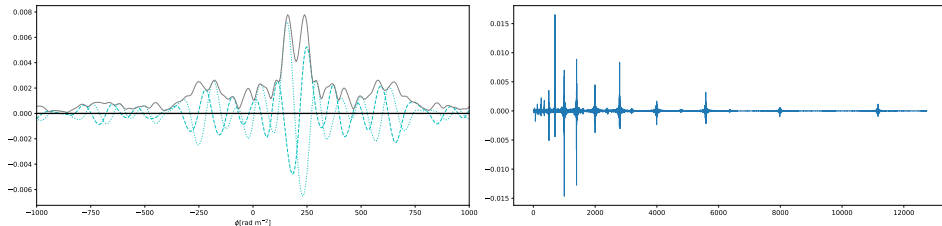$$\phi = \arg\min_{x} ||Ax - b||_2^2 + \lambda||x||_1$$

- A: Measurement matrix (Fourier transform)
- b: Observed data
- x: Signal or a sparse representation of it.

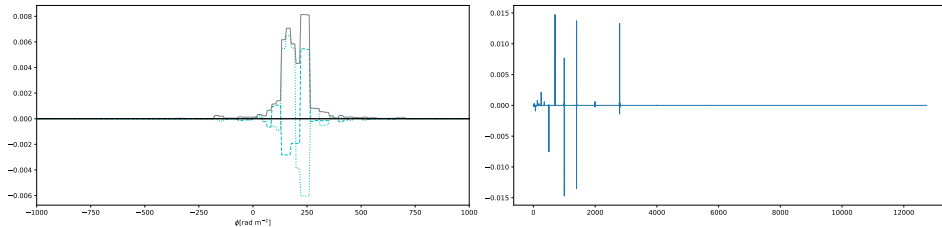$$x = \sum_{i}^{N} c_i \phi_i.$$

x Φ c

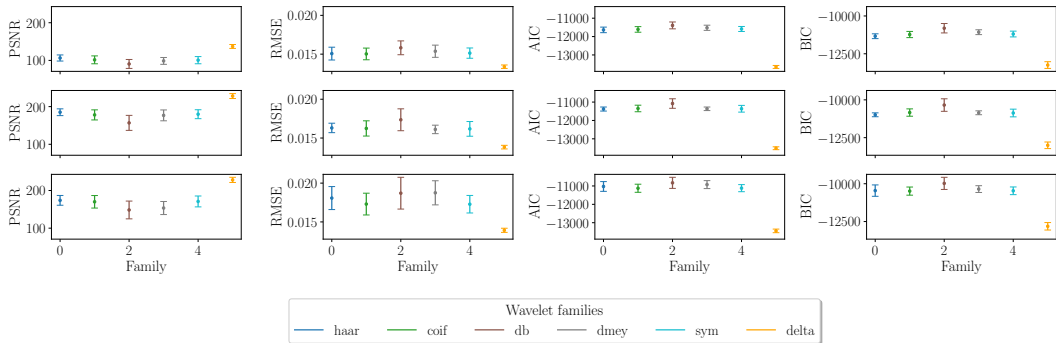k non-zero entries

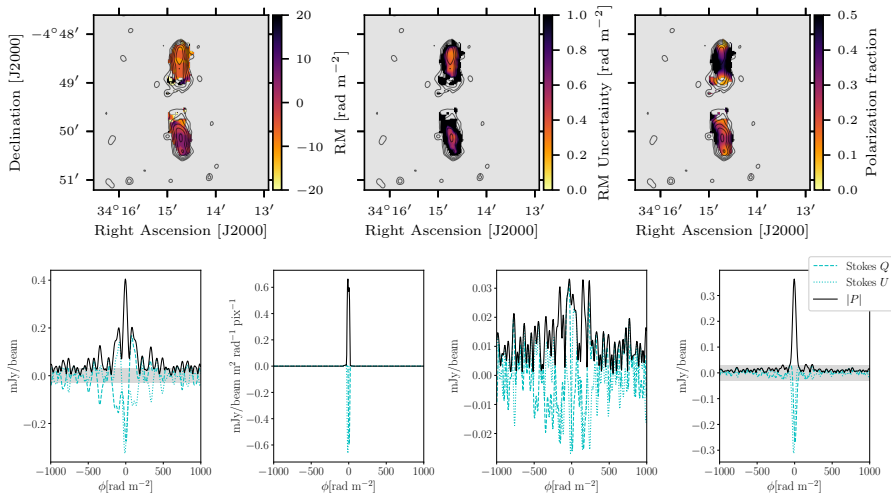N non-zero entries $N \times N$

(a) Dirty FD spectrum and coefficient representation

(b) Reconstructed FD spectrum and sparse representation (note sparsity of coefficients!)

Peak signal-to-noise ratio, root mean squared error, Akaike AIC and BIC for thin, thick and mixed sources.

(a) Dirty, model, residuals and restored Faraday depth spectra.

- We have already demonstrated this method with real data (Cárcamo et al., 2022) (`arXiv 2205.01413`).
- We need to apply this method to all the MIGHTEE-POL survey maps
- Add `cs-romer` RM and RM uncertainties to the MIGHTEE catalog
- Compare the RM values with QU-fitting and naive RM-Synthesis
- We need to incorporate big data and big computing packages such as `dask` and `cupy` to `cs-romer`