# \* Percent Uncertainty vs. Significant Figures

The significant figures rule is only approximate, and in some cases may underestimate the accuracy (or uncertainty) of the answer. Suppose for example we divide 97 by 92:

$$\frac{97}{92} = 1.05 \approx 1.1.$$

Both 97 and 92 have two significant figures, so the rule says to give the answer as 1.1. Yet the numbers 97 and 92 both imply an uncertainty of  $\pm$  1 if no other uncertainty is stated. Both 92  $\pm$  1 and 97  $\pm$  1 imply an uncertainty of about 1% (1/92  $\approx$  0.01 = 1%). But the final result to two significant figures is 1.1, with an implied uncertainty of  $\pm$  0.1, which is an uncertainty of about 10% (0.1/1.1  $\approx$  0.1  $\approx$  10%). It is better in this case to give the answer as 1.05 (which is three significant figures). Why? Because 1.05 implies an uncertainty of  $\pm$  0.01 which is 0.01/1.05  $\approx$  0.01  $\approx$  1%, just like the uncertainty in the original numbers 92 and 97.

SUGGESTION: Use the significant figures rule, but consider the % uncertainty too, and add an extra digit if it gives a more realistic estimate of uncertainty.

## **Approximations**

Much of physics involves approximations, often because we do not have the means to solve a problem precisely. For example, we may choose to ignore air resistance or friction in doing a Problem even though they are present in the real world, and then our calculation is only an approximation. In doing Problems, we should be aware of what approximations we are making, and be aware that the precision of our answer may not be nearly as good as the number of significant figures given in the result.

# Accuracy vs. Precision

There is a technical difference between "precision" and "accuracy." **Precision** in a strict sense refers to the repeatability of the measurement using a given instrument. For example, if you measure the width of a board many times, getting results like 8.81 cm, 8.85 cm, 8.78 cm, 8.82 cm (interpolating between the 0.1 cm marks as best as possible each time), you could say the measurements give a *precision* a bit better than 0.1 cm. **Accuracy** refers to how close a measurement is to the true value. For example, if the ruler shown in Fig. 1–5 was manufactured with a 2% error, the accuracy of its measurement of the board's width (about  $8.8 \, \text{cm}$ ) would be about 2% of  $8.8 \, \text{cm}$  or about  $\pm 0.2 \, \text{cm}$ . Estimated uncertainty is meant to take both accuracy and precision into account.

# 1–5 Units, Standards, and the SI System

The measurement of any quantity is made relative to a particular standard or **unit**, and this unit must be specified along with the numerical value of the quantity. For example, we can measure length in British units such as inches, feet, or miles, or in the metric system in centimeters, meters, or kilometers. To specify that the length of a particular object is 18.6 is insufficient. The unit *must* be given, because 18.6 meters is very different from 18.6 inches or 18.6 millimeters.

For any unit we use, such as the meter for distance or the second for time, we need to define a **standard** which defines exactly how long one meter or one second is. It is important that standards be chosen that are readily reproducible so that anyone needing to make a very accurate measurement can refer to the standard in the laboratory and communicate with other people.

## Length

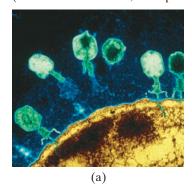
The first truly international standard was the **meter** (abbreviated m) established as the standard of length by the French Academy of Sciences in the 1790s. The standard meter was originally chosen to be one ten-millionth of the distance from the Earth's equator to either pole, and a platinum rod to represent this length was made. (One meter is, very roughly, the distance from the tip of your nose to the tip of your finger, with arm and hand stretched out horizontally.) In 1889, the meter was defined more precisely as the distance between two finely engraved marks on a particular bar of platinum-iridium alloy. In 1960, to provide even greater precision and reproducibility, the meter was redefined as 1,650,763.73 wavelengths of a particular orange light emitted by the gas krypton-86. In 1983 the meter was again redefined, this time in terms of the speed of light (whose best measured value in terms of the older definition of the meter was 299,792,458 m/s, with an uncertainty of 1 m/s). The new definition reads: "The meter is the length of path traveled by light in vacuum during a time interval of 1/299,792,458 of a second."<sup>‡</sup>

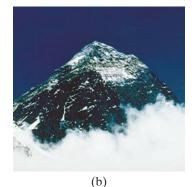
British units of length (inch, foot, mile) are now defined in terms of the meter. The inch (in.) is defined as exactly 2.54 centimeters (cm; 1 cm = 0.01 m). Other conversion factors are given in the Table on the inside of the front cover of this book. Table 1-1 presents some typical lengths, from very small to very large, rounded off to the nearest power of 10. See also Fig. 1–8. [Note that the abbreviation for inches (in.) is the only one with a period, to distinguish it from the word "in".]

## Time

The standard unit of **time** is the **second** (s). For many years, the second was defined as 1/86,400 of a mean solar day  $(24 \text{ h/day} \times 60 \text{ min/h} \times 60 \text{ s/min} =$ 86,400 s/day). The standard second is now defined more precisely in terms of the frequency of radiation emitted by cesium atoms when they pass between two particular states. [Specifically, one second is defined as the time required for 9,192,631,770 oscillations of this radiation.] There are, by definition, 60 s in one minute (min) and 60 minutes in one hour (h). Table 1–2 presents a range of measured time intervals, rounded off to the nearest power of 10.

**FIGURE 1–8** Some lengths: (a) viruses (about  $10^{-7}$  m long) attacking a cell; (b) Mt. Everest's height is on the order of 10<sup>4</sup> m (8850 m above sea level, to be precise).





(order of magnitude)	
Length (or Distance)	Meters (approxima
Neutron or proton (diameter)	10 <sup>−15</sup> m

Length (or Distance)	Meters (approximate)
Neutron or proton (diameter)	$10^{-15} \text{ m}$
Atom (diameter)	$10^{-10} \text{ m}$
Virus [see Fig. 1–8a]	$10^{-7}  \mathrm{m}$
Sheet of paper (thickness)	$10^{-4}  \text{m}$
Finger width	$10^{-2}  \text{m}$
Football field length	$10^2$ m
Height of Mt. Everest [see Fig. 1-8b]	$10^4$ m
Earth diameter	$10^7$ m
Earth to Sun	$10^{11}  \text{m}$
Earth to nearest star	$10^{16}  \text{m}$
Earth to nearest galaxy	$10^{22} \text{ m}$
Earth to farthest galaxy visible	$10^{26}$ m

TABLE 1–2	Some Typical Time Intervals
	(order of magnitude)

Time Interval	Seconds (approximate)
Lifetime of very unstable subatomic particle	$10^{-23}  \mathrm{s}$
Lifetime of radioactive elements	s $10^{-22}$ s to $10^{28}$ s
Lifetime of muon	$10^{-6}$ s
Time between human heartbeat	$10^0 s (= 1 s)$
One day	$10^5$ s
One year	$3 \times 10^{7}$ s
Human life span	$2 \times 10^9$ s
Length of recorded history	$10^{11}$ s
Humans on Earth	$10^{13}$ s
Age of Earth	$10^{17}$ s
Age of Universe	$4 \times 10^{17} \text{ s}$

<sup>&</sup>lt;sup>†</sup>Modern measurements of the Earth's circumference reveal that the intended length is off by about one-fiftieth of 1%. Not bad!

<sup>&</sup>lt;sup>‡</sup>The new definition of the meter has the effect of giving the speed of light the exact value of 299,792,458 m/s.

#### TABLE 1-3 Some Masses

Object	Kilograms (approximate)
Electron	$10^{-30} \text{ kg}$
Proton, neutron	$10^{-27} \text{ kg}$
DNA molecule	$10^{-17} { m kg}$
Bacterium	$10^{-15} \text{ kg}$
Mosquito	$10^{-5} \text{ kg}$
Plum	$10^{-1}  \mathrm{kg}$
Human	$10^2$ kg
Ship	$10^{8}$ kg
Earth	$6 \times 10^{24}$ kg
Sun	$2 \times 10^{30}$ kg
Galaxy	$10^{41}$ kg



TABLE 1-4 Metric (SI) Prefixes

**Abbreviation Prefix** Value  $10^{24}$ Y yotta Z  $10^{21}$ zetta  $10^{18}$ exa E  $10^{15}$ P peta  $10^{12}$ Τ tera  $10^{9}$ G giga  $10^{6}$ M mega  $10^{3}$ k kilo  $10^{2}$ hecto h  $10^{1}$ deka da  $10^{-1}$ deci d  $10^{-2}$ centi c  $10^{-3}$ milli m  $10^{-6}$ micro μ  $10^{-9}$ nano n  $10^{-12}$ pico p  $10^{-15}$ f femto  $10^{-18}$ atto a  $10^{-21}$ 

Z

y

 $^{\dagger}\mu$  is the Greek letter "mu."

#### Mass

The standard unit of **mass** is the **kilogram** (kg). The standard mass is a particular platinum-iridium cylinder, kept at the International Bureau of Weights and Measures near Paris, France, whose mass is defined as exactly 1 kg. A range of masses is presented in Table 1–3. [For practical purposes, 1 kg weighs about 2.2 pounds on Earth.]

When dealing with atoms and molecules, we usually use the **unified atomic** mass unit (u or amu). In terms of the kilogram,

$$1 \text{ u} = 1.6605 \times 10^{-27} \text{ kg}.$$

Precise values of this and other useful numbers are given on page A-72.

The definitions of other standard units for other quantities will be given as we encounter them in later Chapters.

## **Unit Prefixes**

In the metric system, the larger and smaller units are defined in multiples of 10 from the standard unit, and this makes calculation particularly easy. Thus 1 kilometer (km) is 1000 m, 1 centimeter is  $\frac{1}{100}$  m, 1 millimeter (mm) is  $\frac{1}{1000}$  m or  $\frac{1}{10}$  cm, and so on. The prefixes "centi-," "kilo-," and others are listed in Table 1-4 and can be applied not only to units of length but to units of volume, mass, or any other unit. For example, a centiliter (cL) is  $\frac{1}{100}$  liter (L), and a kilogram (kg) is 1000 grams (g). An 8.2-megapixel camera has a detector with 8,200,000 pixels (individual "picture elements").

In common usage,  $1 \mu m (= 10^{-6} m)$  is called 1 micron.

## Systems of Units

When dealing with the laws and equations of physics it is very important to use a consistent set of units. Several systems of units have been in use over the years. Today the most important is the Système International (French for International System), which is abbreviated SI. In SI units, the standard of length is the meter, the standard for time is the second, and the standard for mass is the kilogram. This system used to be called the MKS (meter-kilogram-second) system.

A second metric system is the cgs system, in which the centimeter, gram, and second are the standard units of length, mass, and time, as abbreviated in the title. The **British engineering system** (although more used in the U.S. than Britain) has as its standards the foot for length, the pound for force, and the second for time.

We use SI units almost exclusively in this book.

## \*Base vs. Derived Quantities

Physical quantities can be divided into two categories: base quantities and derived quantities. The corresponding units for these quantities are called base units and derived units. A base quantity must be defined in terms of a standard. Scientists, in the interest of simplicity, want the smallest number of base quantities possible consistent with a full description of the physical world. This number turns out to be seven, and those used in the SI are given in Table 1-5.

TABLE 1–5 SI Base Quantities and Units			
Quantity	Unit	Unit Abbreviation	
Length	meter	m	
Time	second	S	
Mass	kilogram	kg	
Electric current	ampere	A	
Temperature	kelvin	K	
Amount of substance	mole	mol	
Luminous intensity	candela	cd	

zepto

yocto

 $10^{-24}$