

# VERIFICATION OF C3 LINEARIZATION ALGORITHM

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ADC midterm presentation

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# CONTEXT

**Great necessity of:**

- OOP
- Multiple Inheritance
- Understand behaviour

# CONTEXT

Multiple Inheritance uses C3

## Why C3

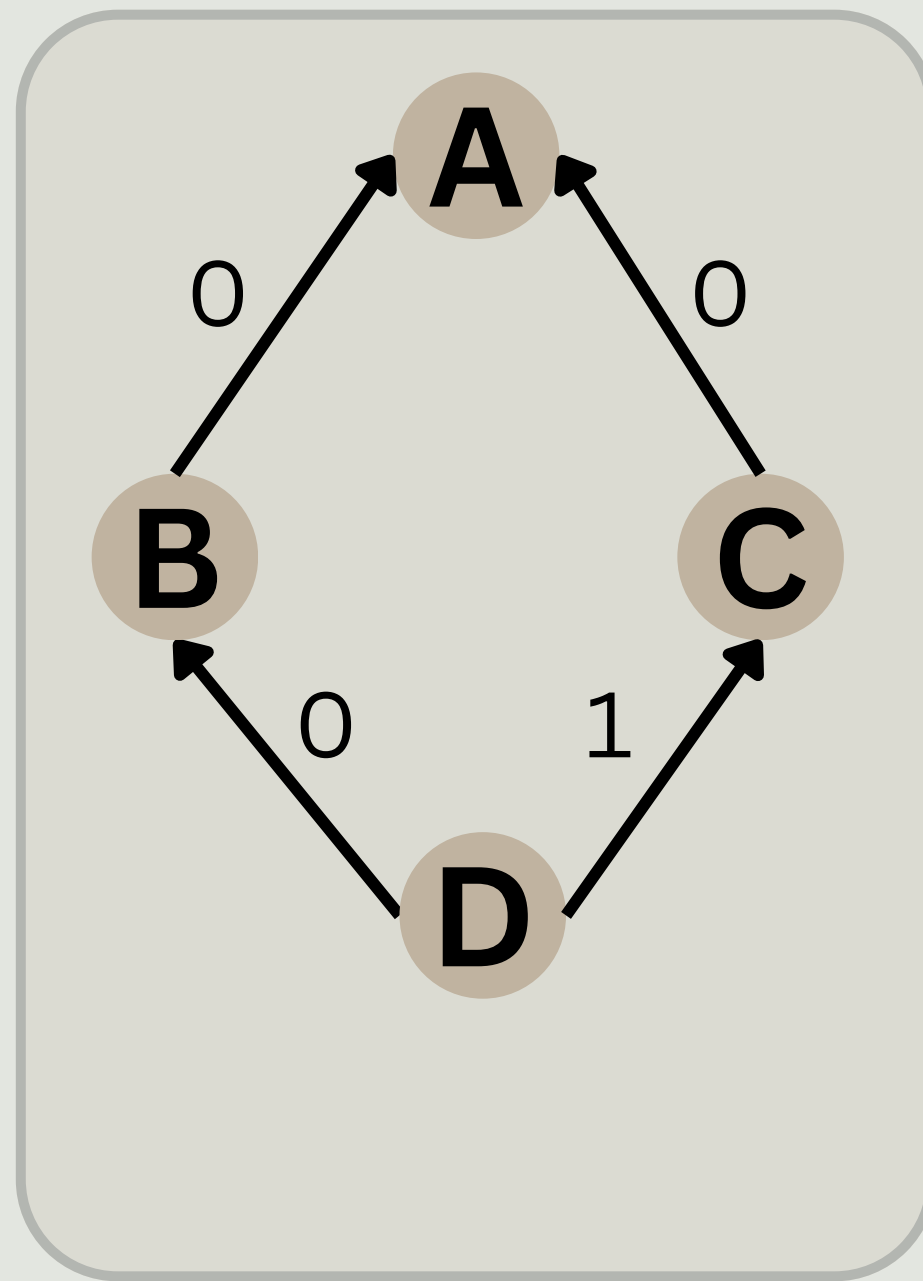
- ✓ A consistent extended precedence graph
- ✓ Preservation of Local Precedence Order
- ✓ Monotonicity Criterion

```
class B
  def m()

class C
  def m()

class D is B and C
  def m()
```

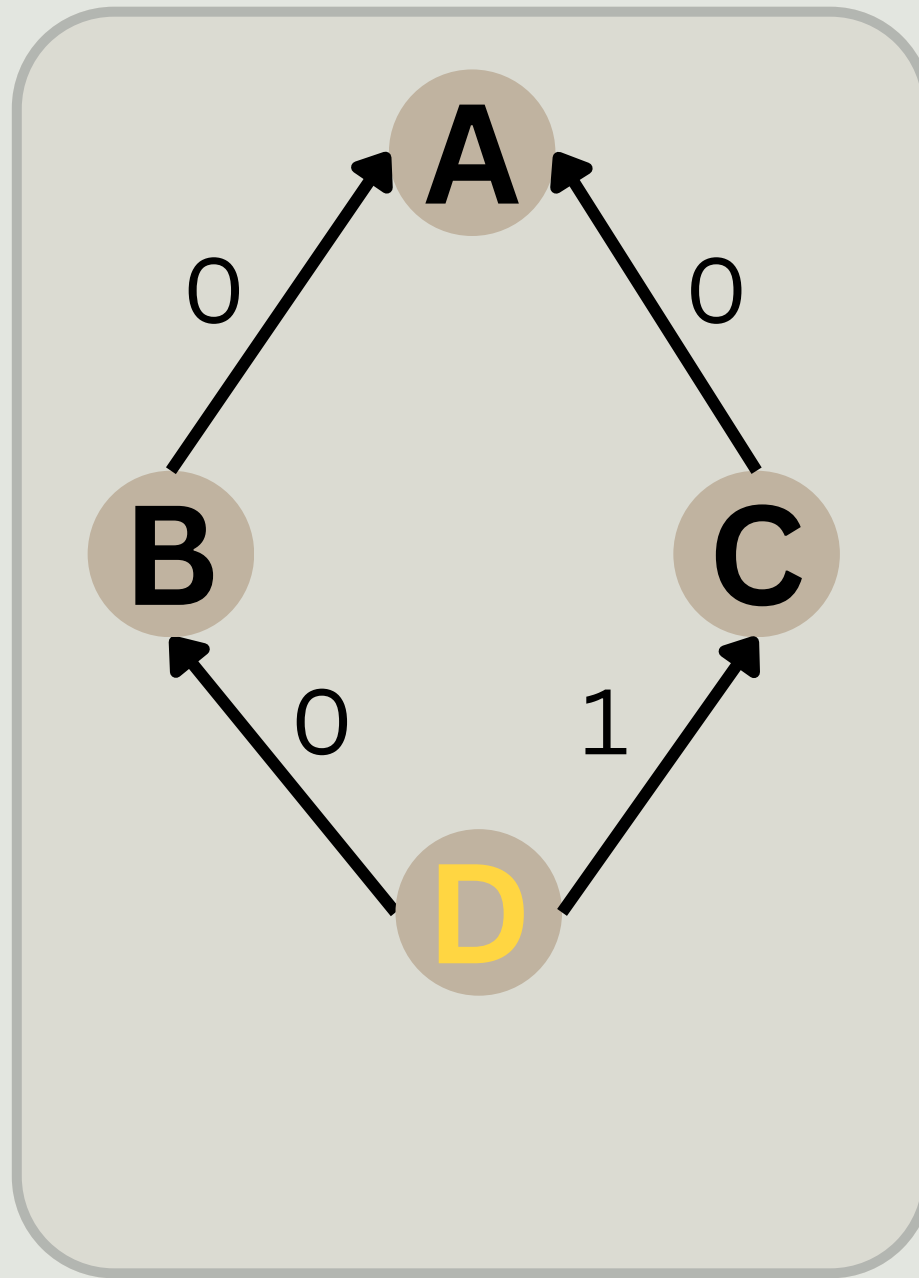
# C3 LINEARIZATION



**Result**

**$D \rightarrow B \rightarrow C \rightarrow A$**

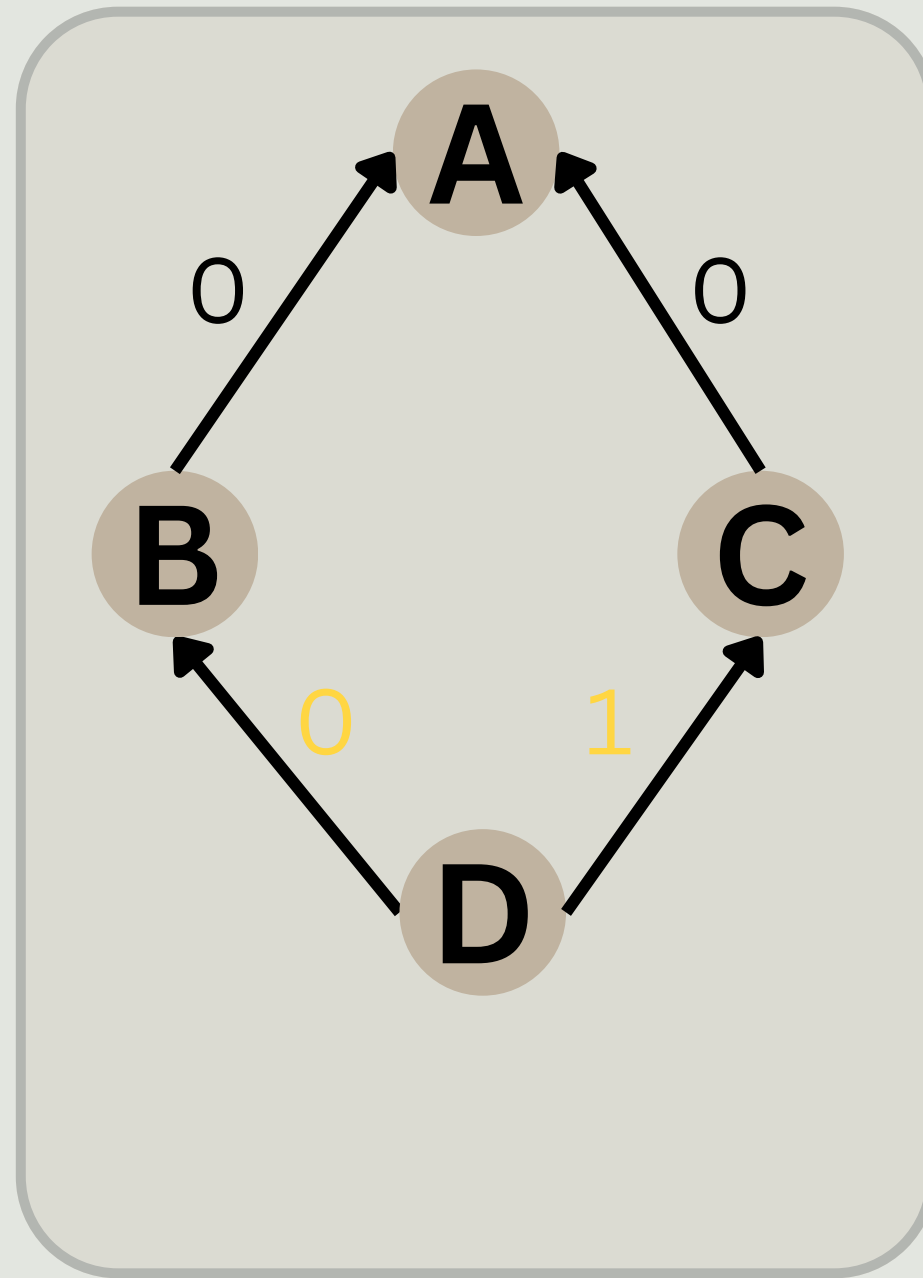
# C3 LINEARIZATION



**Result**

**D → B → C → A**

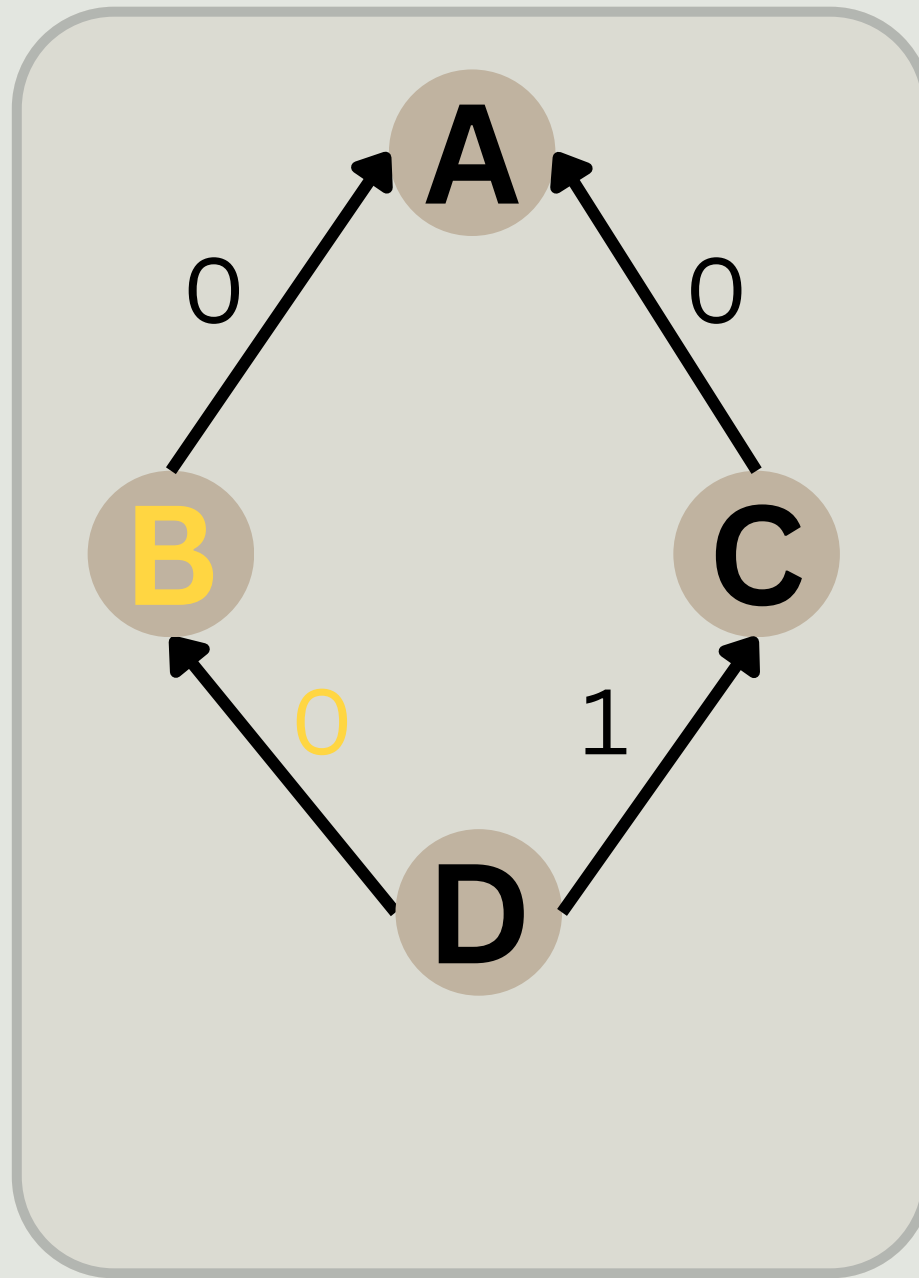
# C3 LINEARIZATION



**Result**

**$D \rightarrow B \rightarrow C \rightarrow A$**

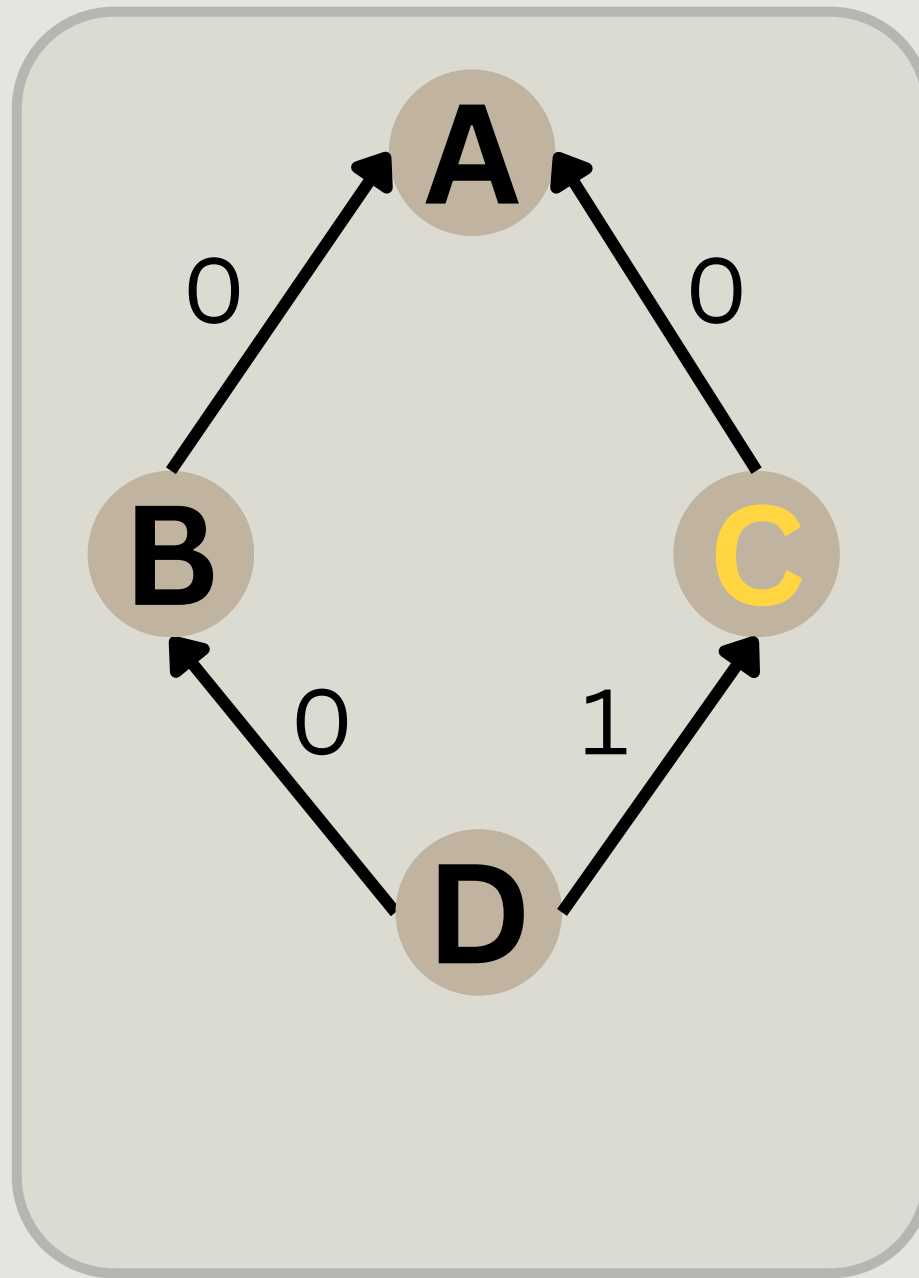
# C3 LINEARIZATION



**Result**

**D → B → C → A**

# C3 LINEARIZATION

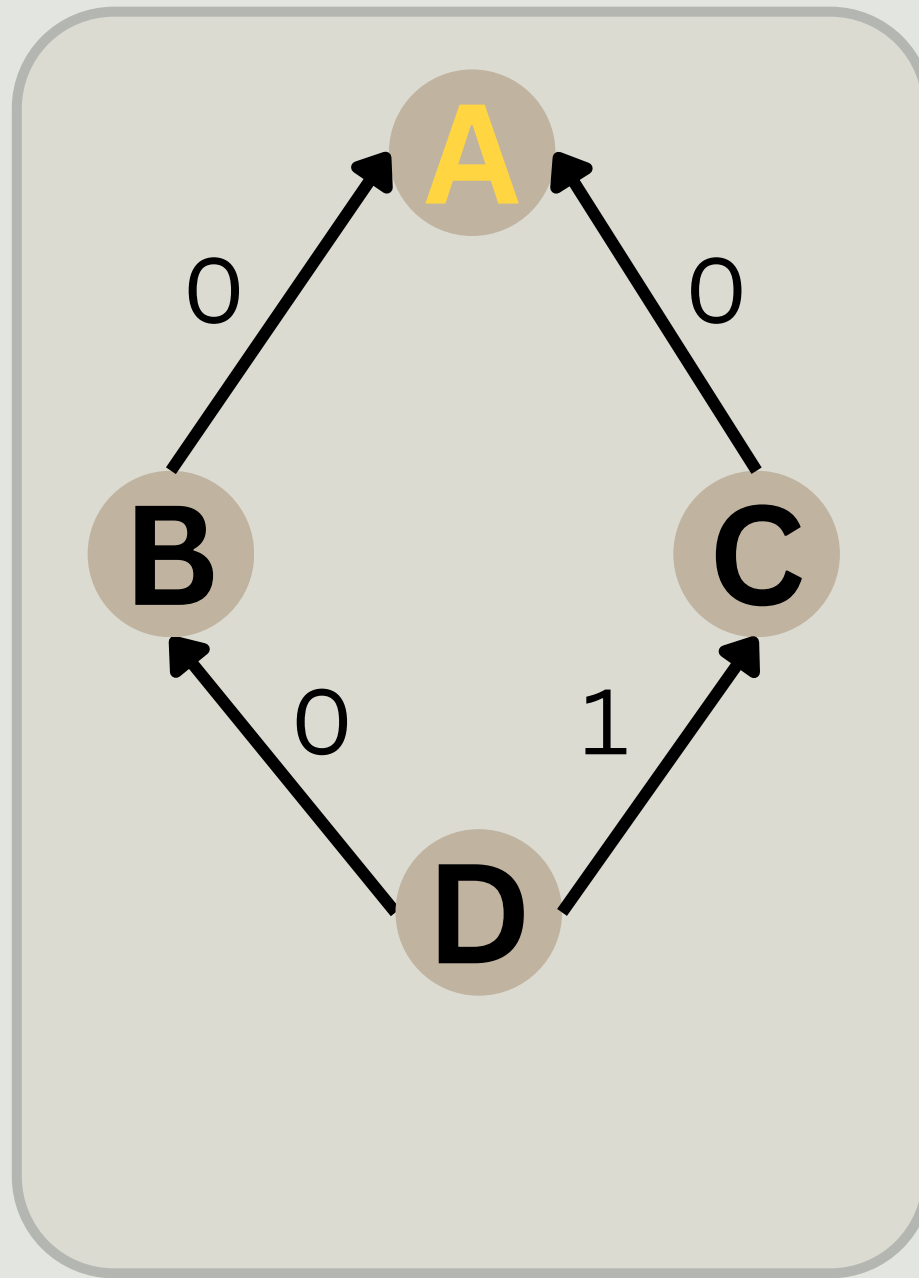


**Result**

**D → B → C → A**



# C3 LINEARIZATION

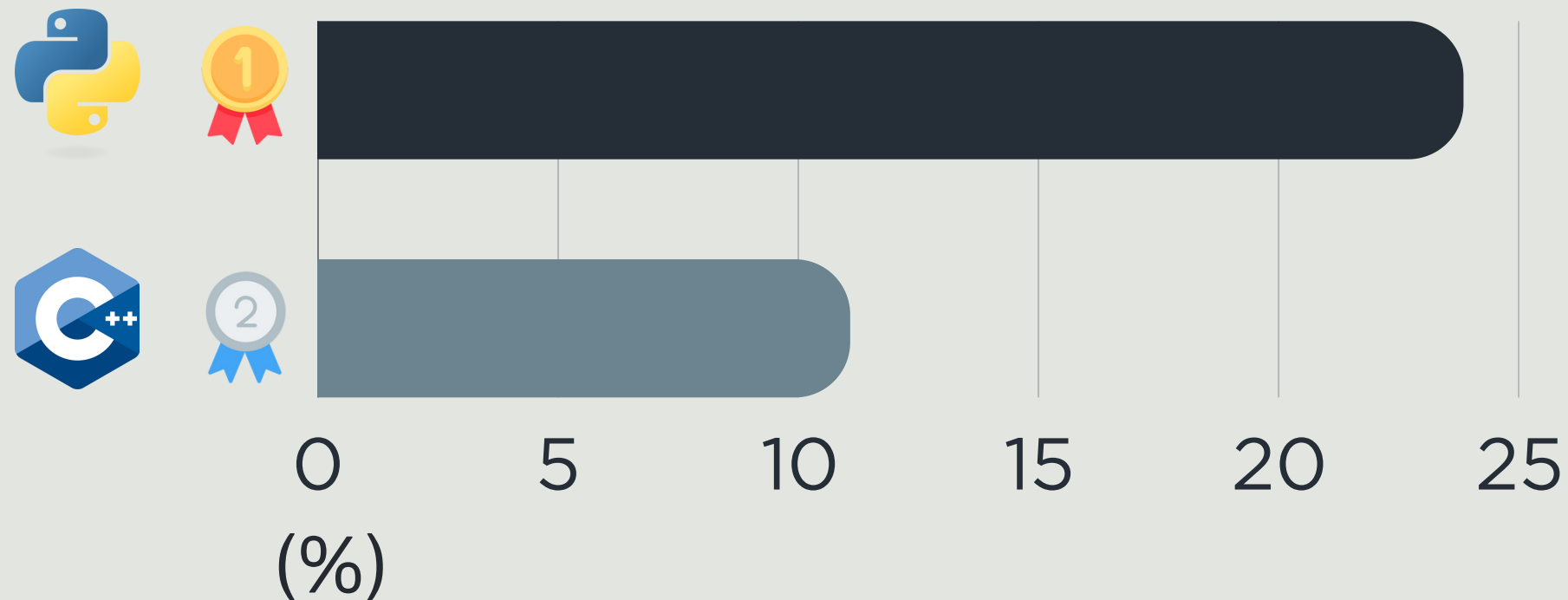


**Result**

**D → B → C → A**

# THE PROBLEM

March 2025



**48 272 (ETH/H)**



**88M (EURO/H)**



**Multiple  
Inheritance**



**Challenge**



**Soundness**

# THE PROBLEM

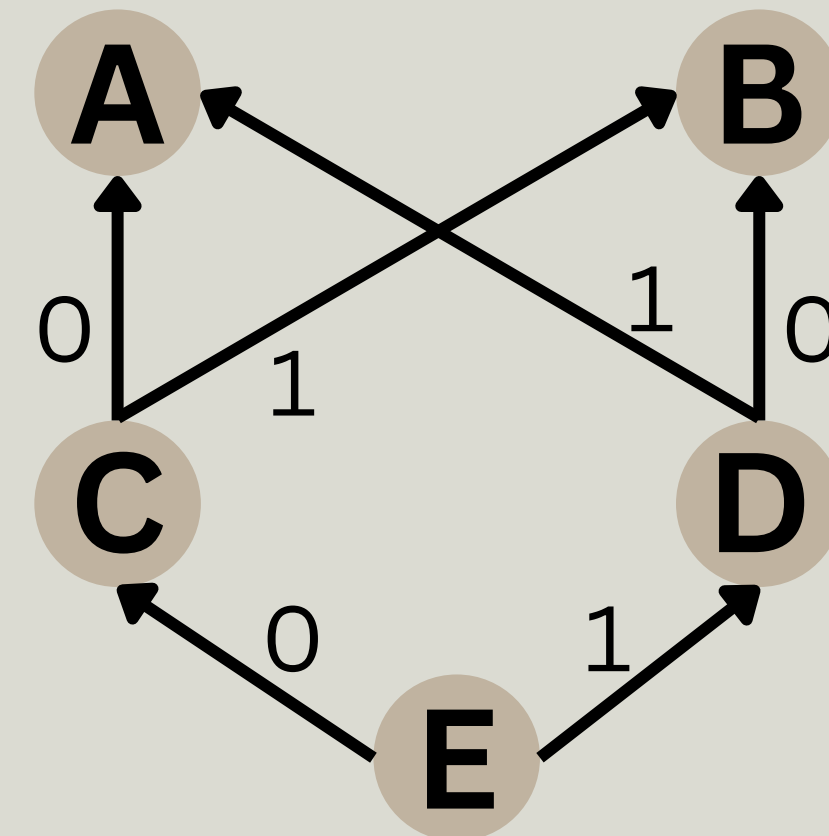
✗ Rigorous Presentation

✗ Clear Specification



Unclear behaviour

Potential bugs



**Fail**

# OBJECTIVES AND CONTRIBUTIONS

C3: consistent with 3 properties

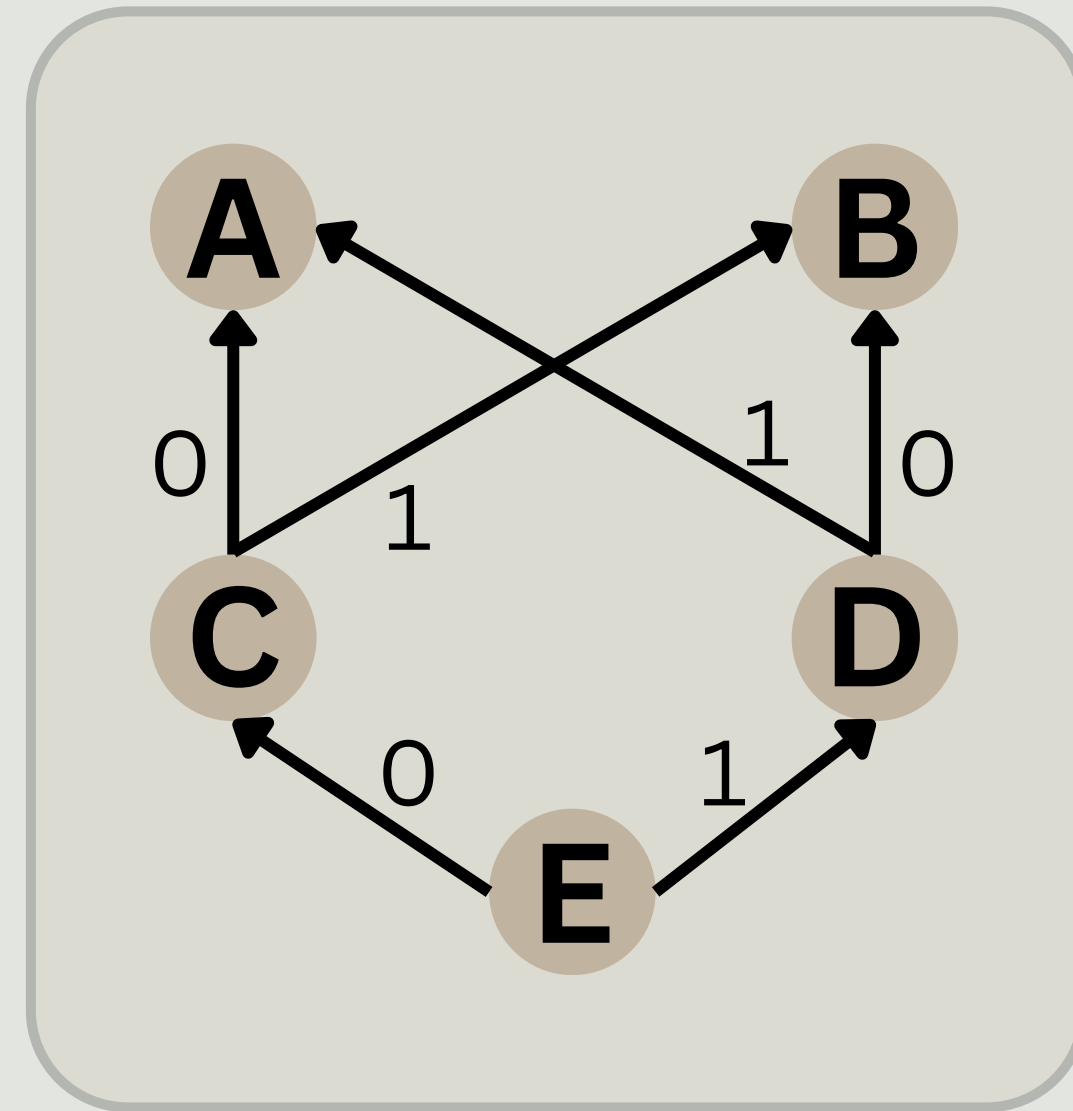
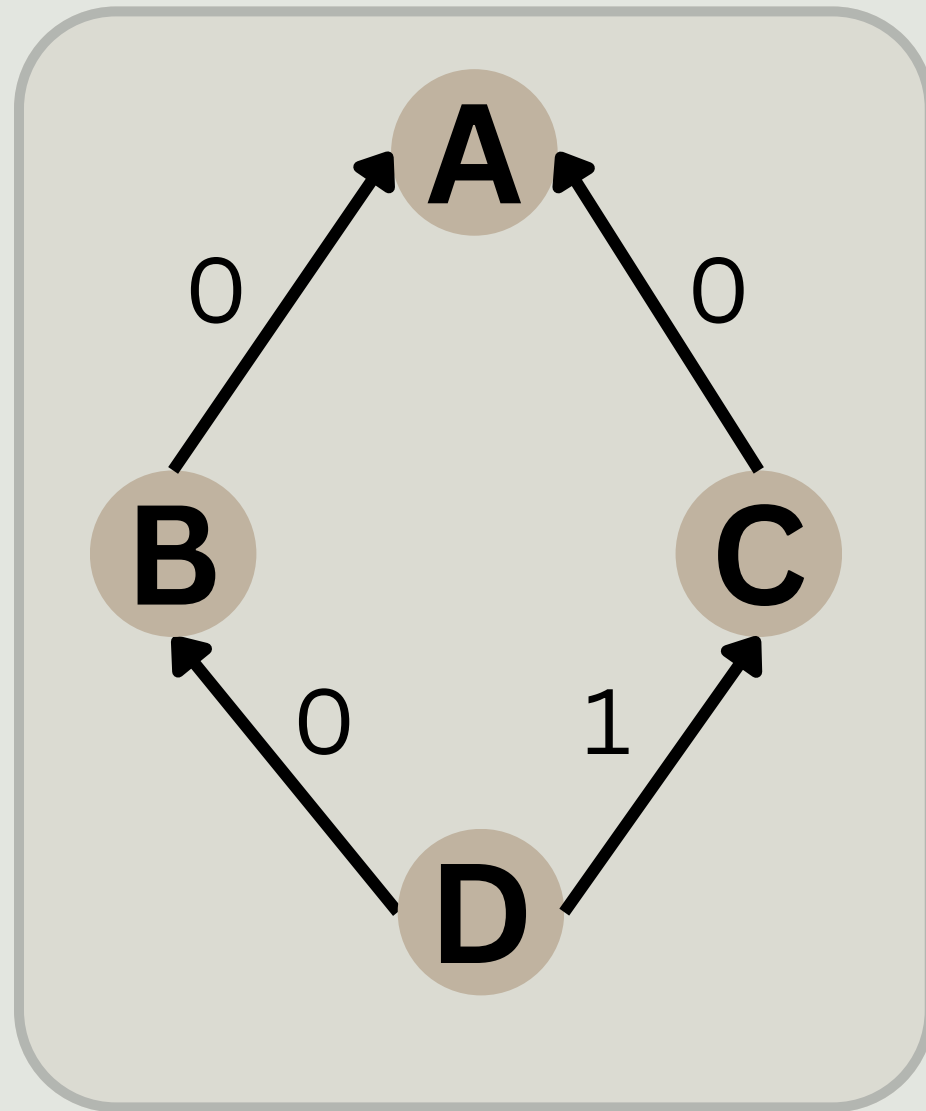
Define

- ✓ Rigorous Presentation
- ✓ Rigorous Specification
- ✓ Language Independent

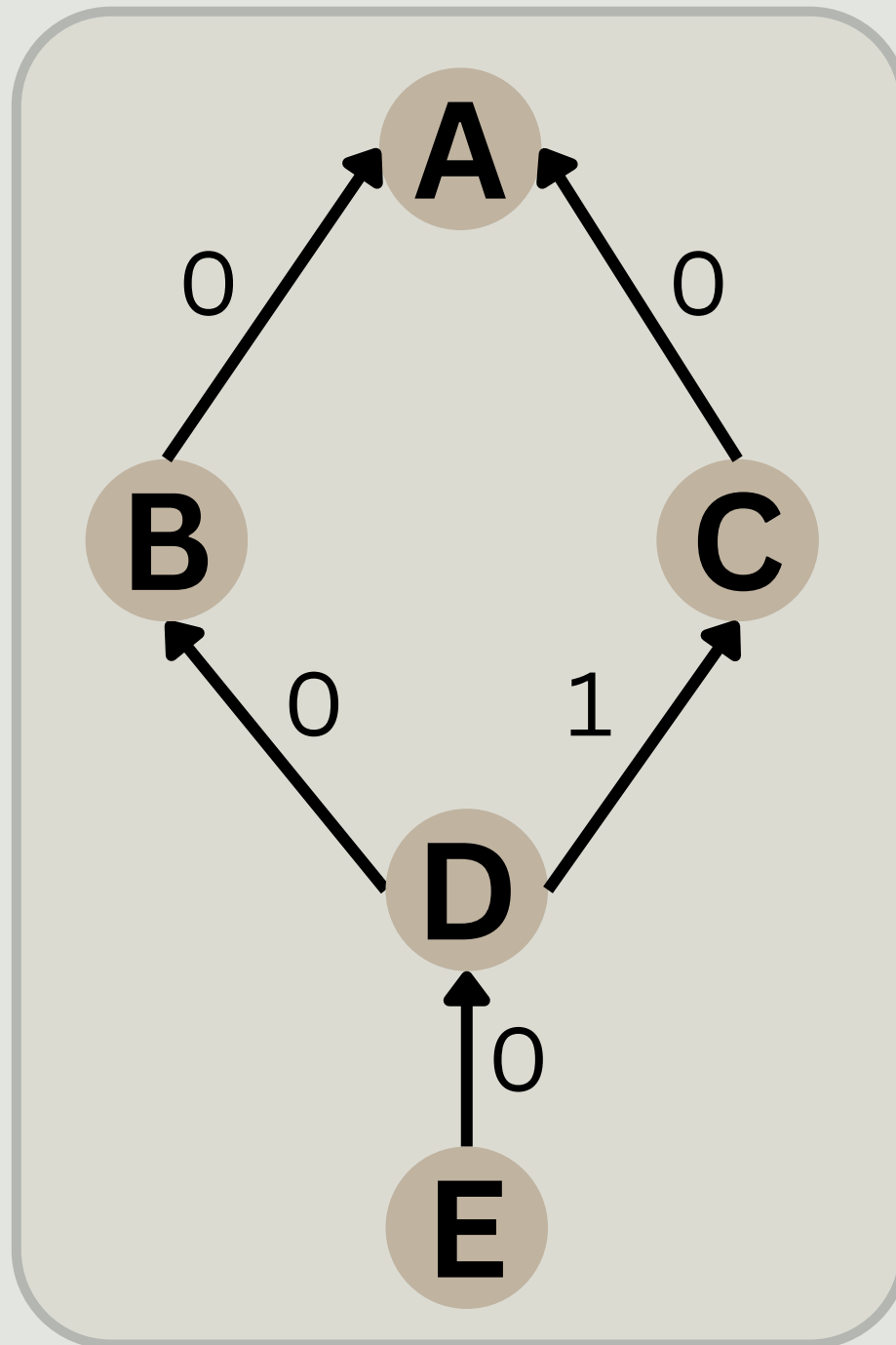
Allows to  
→  
derive

- ✓ A consistent extended precedence graph
- ✓ Preservation of Local Precedence Order
- ✓ Monotonicity Criterion

# A CONSISTENT EXTENDED PRECEDENCE GRAPH



# MONOTONICITY CRITERION



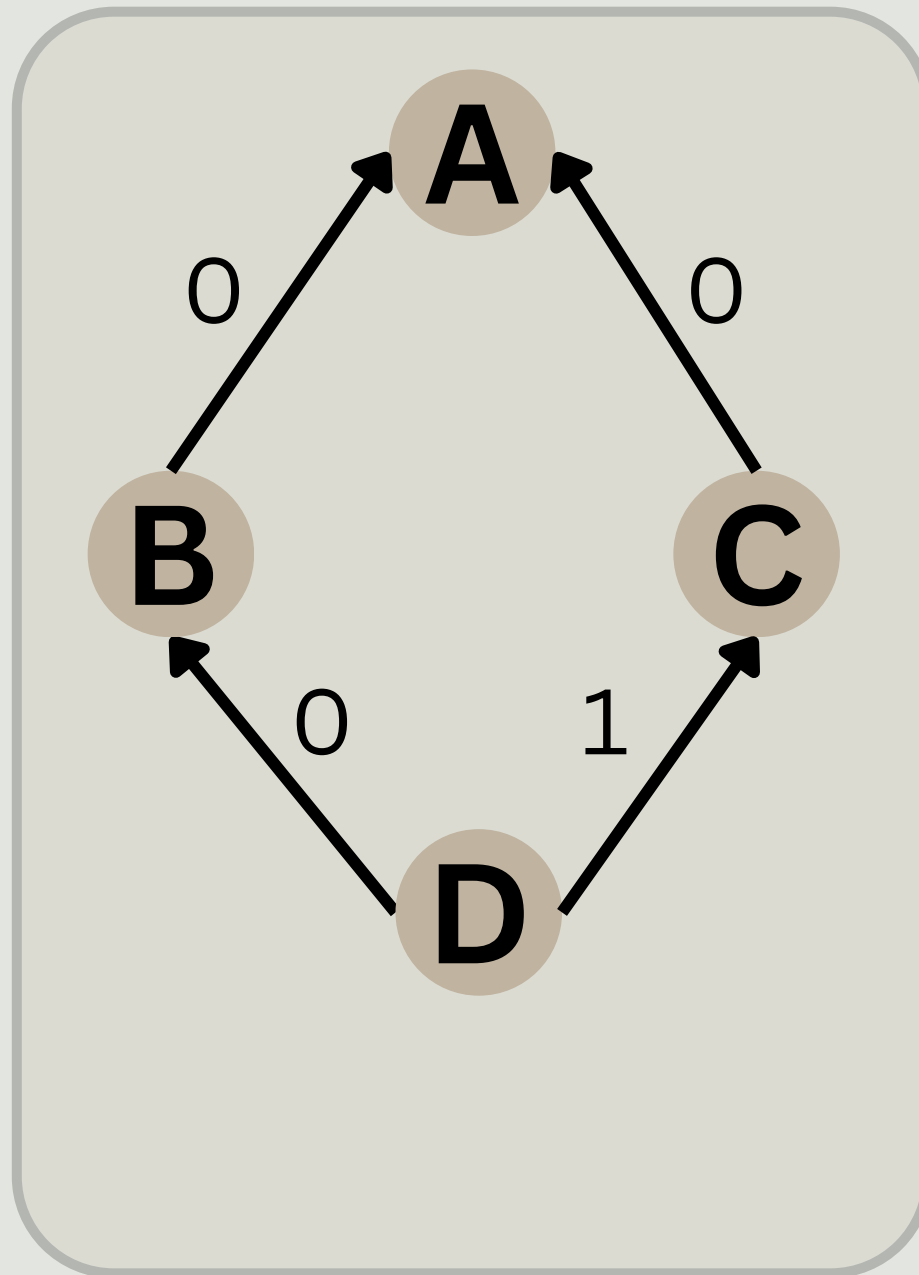
✓ Result

$E \rightarrow D \rightarrow B \rightarrow C \rightarrow A$

✗ Result

$E \rightarrow D \rightarrow C \rightarrow B \rightarrow A$

# PRESERVATION OF LOCAL PRECEDENCE ORDER



✓ Result

$D \rightarrow B \rightarrow C \rightarrow A$

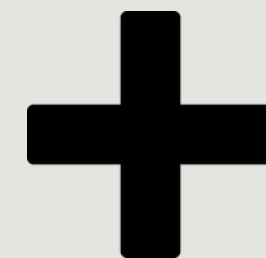
✗ Result

$D \rightarrow C \rightarrow B \rightarrow A$

# RESULTS



Correction  
Proof



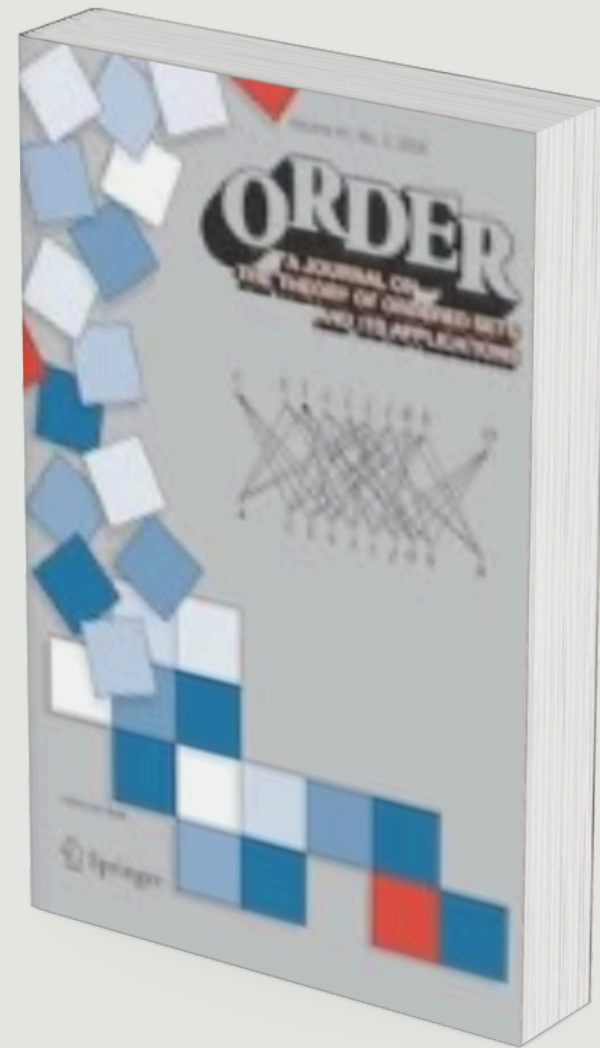
Article

Repository  
with certified C3 Ocaml



# METHODOLOGY

## Approach to develop certified code



Study

“Controlling the C3 Super Class  
Linearization Algorithm for Large  
Hierarchies of Classes”

Florent Hivert & Nicolas M. Thiéry

**Outcome**

model & properties

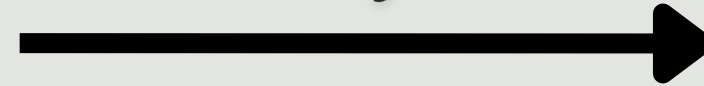
# METHODOLOGY

“Towards a solider Solidity”



João Reis

Analyse



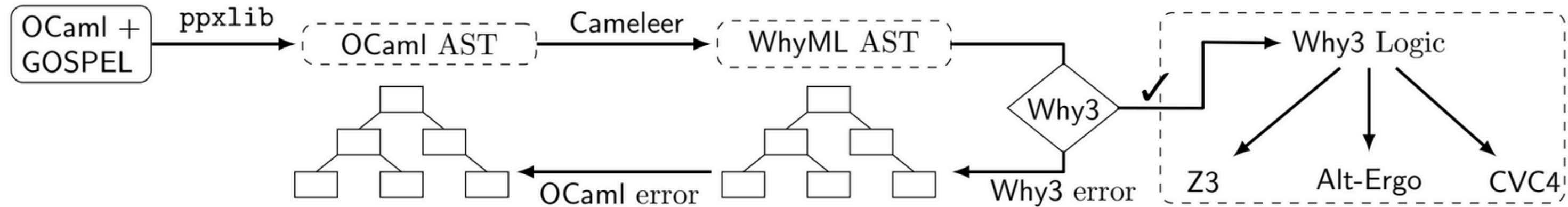
Rectify

## Outcome

Specification

C3 implementation

### Cameleer



### Combines

- Gospel comments
- Ocaml verification

# CAMELEER - Work done

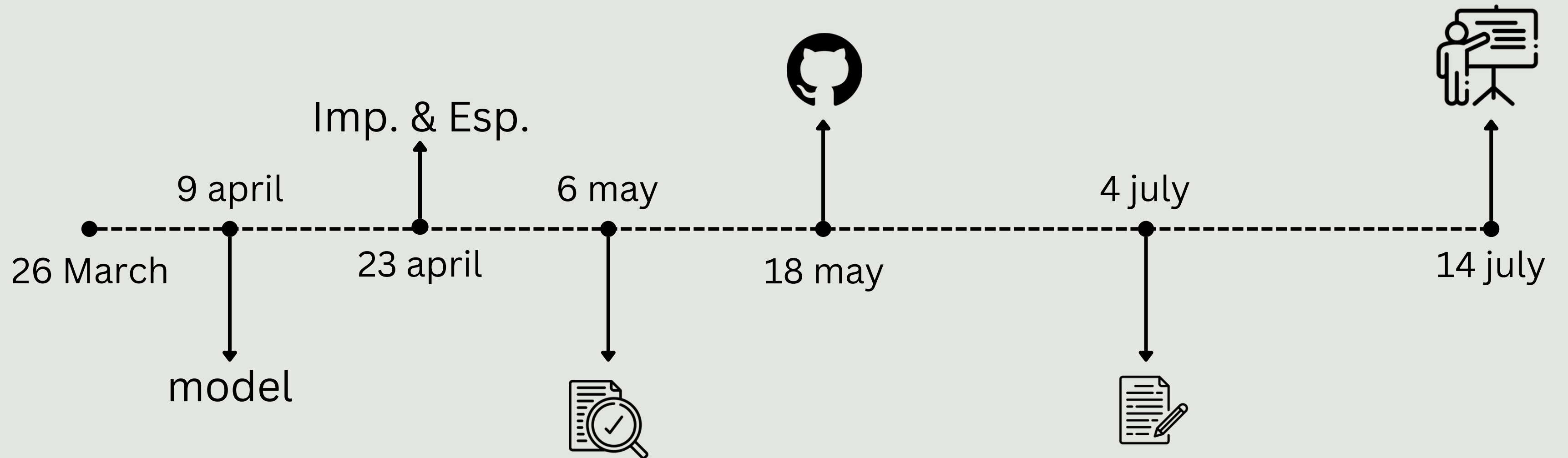
Not repeated

```
(*@ open Set *)

let rec not_in_list (x : int) (l : int list) =
  match l with
  | [] -> true
  | y :: r -> x <> y && not_in_list x r

let rec not_repeated (l: int list) =
  match l with
  | [] -> true
  | x :: r -> not_in_list x r && not_repeated r
(*@
  r = not_repeated l
  ensures (Set.cardinal (Set.of_list l) = (List.length l)) = r
*)
```

# PLAN





# Thank You

For your attention