# C3 linearization properties

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### **Notation Convention**

We adopt the following convention throughout the article:

- $\bullet$  Variables with a tilde (e.g.,  $\tilde{C})$  represent sequences (finite ordered lists of elements).
- Variables with a double tilde (e.g.,  $\tilde{\tilde{C}}$ ) represent sequence of sequences.

### **Ingredients**

 $\mathcal{C}$  of classes  $C_0, C_1, C_2, \dots, C_n$ . Set  $\mathcal{D}$  of pairs (class, set of classes)  $\mathcal{C} \times \tilde{\mathcal{C}}$ .  $MRO_D : \mathcal{C} \Rightarrow \tilde{\mathcal{C}}$ .

#### Remove

$$remove : \tilde{\tilde{C}} \times C \Rightarrow \tilde{\tilde{C}}$$
  
Let  $\tilde{\tilde{L}} = [\tilde{L}_1; \dots; \tilde{L}_n], \ \tilde{\tilde{L}} \in \tilde{\tilde{C}}$   
Let  $C \in \mathcal{C}$ 

$$\frac{C \quad \tilde{\tilde{L}} = [\tilde{L}_1 \setminus \{C\}, \dots, \tilde{L}_n \setminus \{C\}]}{\text{remove}(\tilde{\tilde{L}}, C) = \tilde{\tilde{L}}}$$

## Merge

$$merge: \tilde{\tilde{\mathcal{C}}} \Rightarrow \tilde{\mathcal{C}}$$
 Let  $\tilde{\tilde{L}} = [\tilde{L}_1; \dots; \tilde{L}_n], \ \tilde{\tilde{L}} \in \tilde{\tilde{\mathcal{C}}}$ 

$$merge(\tilde{\tilde{L}}) = \begin{cases} [C] \cdot merge(remove(\tilde{\tilde{L}}, C)), & \text{if } (\exists k \in \{1, \dots, n\}, \tilde{L}_k \neq \emptyset \land C = head(\tilde{L}_k)) \land \\ & (\forall j < k, C \neq head(\tilde{L}_j)) \land \\ & (\forall i \in \{1, \dots, n\}, C \notin tail(\tilde{L}_i)) \end{cases}$$

$$fail \qquad otherwise$$

### C3 Linearization