Calabo I - 4. 4 - 2021/22 - exame de reaver

Perolugis

6.
$$\sum_{m=1}^{+\infty} \left(1 - \frac{h_m}{m}\right)^m$$
Note for $h_m < 1$

$$\left(\frac{h_m}{m}\right)^m = 1 - \frac{h_m}{m} \xrightarrow{m-1+\infty} 1$$

(5 pools)

O Criticis de Canchy exticado a E an apera permito concluir quand lim [Km] \$1 (rando a refixe (chrothatamenta) conveyent quand em limito de <1 a divegent quand em limito de >1

or +00). Como no carr preneta den 1, made permito concluir.

(b) lim $\left(1 - \frac{\ln n}{x}\right)^n$ de une indituminação 1°.

(15 porto) 2-1+0

Logaritanitand:

 $\ln\left(1-\frac{\ln n}{n}\right)^{n}=x.\ln\left(1-\frac{\ln n}{n}\right)=\frac{\ln\left(1-\frac{\ln n}{n}\right)}{\frac{1}{n}}$

de mus inditurningen o frank n-1+00.

Com line $\frac{1-\ln n}{1-\ln n} = -\infty$,

por fegs do Cauchy terms productions from $(1 - \frac{\ln n}{n})^n = \lim_{n \to +\infty} e^{-\frac{\ln n}{n}} = 0$

(c) Cour compainte d'aline autiris, taubé lim (1- \frac{lum}{m})=0,

(10 ports) or reje, - termer goel de sine ten l'inte terr quant most a.

E'sabile que inser mon e'enfectet para leterniser a nature.

ta de révie