

▼ Temario

```
def rectabla(E, c):
    R = {}
    def C(i):
        if i == 1:
            R[1] = 0
        elif i == 2:
            R[2] = c(1,2)
        else:
            R[i] = min(R[i-1]+ c(i-1, i), R[i-2] + c(i-2, i))
        return R[i]
    return C(E)
```

```
def itertabla(E, c):
    R = {}
    R[1] = 0
    R[2] = c(1,2)
    for i in range(3, E+1):
        R[i] = min(R[i-1] + c(i-1, i), R[i-2]+ c(i-2, i))
    return R[E]
```

▼ Problema de la moneda

```
def moneda(Q, v):
    def M(q):
        if q == 0:
            return 0
        else:
            return min(M(q-a) + 1 for a in v if q-a >= 0)
    return M(Q)
```

```
Q = 24
v = [1,2,5,10,20,50]
```

```
moneda(Q,v)
```

```
3
```

```
def moneda_recursivo(Q, v):
    def M(q):
        if q == 0:
            return 0, []
        else:
            va = 2**31
            miniari = []
```

```

    for a in v:
        if q - a >= 0:
            valor, l = M(q-a)
            valor += 1
            if valor < va:
                va = valor
                miniari = l
            miniari.append(a)
    return va, miniari
return M(Q)

```

Q = 29

v = [1,2,5,10,20,50]

moneda_recurativo(Q,v)

(4, [20, 5, 2, 2])

Q = 29

v = [1,2,5,10,20,50]

```

def moneda_iterativo(Q, v):
    M = [None] * (Q+1)
    M[0] = 0
    for q in range(1, Q+1):
        M[q] = min(M[q-a] + 1 for a in v if q - a >= 0)
    return M[Q]

```

moneda_iterativo(Q, v)

4

Distancia de Levenshtein

```

def levenstein(x, y):
    D = {}
    D[0,0] = 0

    for i in range(1, len(x)+1):
        D[i, 0] = D[i-1, 0] + 1
    for j in range(1, len(y)+1):
        D[0, j] = D[0, j-1] + 1
        for i in range(1, len(x)+1):
            D[i, j] = min(D[i-1, 0] + 1,
                          D[i, j-1] + 1,
                          D[i-1, j-1] + (x[i-1] != y[j-1]))
    return D[len(x), len(y)]

```

levenstein("ejemplo", "campos")

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▼ Longest Common Sequence

```
# Aplicacion: Longest Comon Subsequence
def LCS(x, y):
    lcs = {}
    for i in range(len(x)+1):
        lcs[i, 0] = 0
    for j in range(1, len(y)+1):
        lcs[0, j] = 0
    for i in range(1, len(x)+1):
        if x[i-1] != y[j-1]:
            lcs[i,j] = max(lcs[i-1, j], lcs[i, j-1])
        else:
            lcs[i,j] = lcs[i-1, j-1] + 1 #Añado al contador de secuencias
    return lcs[len(x), len(y)]

LCS("comparsa", "causarte")
```

4

▼ Mochila de Dora la exportadronjas

```
def iterative_knapsack_delante(W, v, w):
    Vcurr = {0:0}
    for vi,wi in zip(v,w):
        Vnext = {}
        for peso,benef in Vcurr.items():
            Vnext[peso] = max(benef, Vnext.get(peso,0))
            if peso+wi <= W:
                Vnext[peso+wi] = max(benef+vi, Vnext.get(peso+wi,0))
        Vcurr = Vnext
    return max(Vcurr.values())
```

```
v=[4,5,3,6]
W=8
v=[2,1,1,2]
#iterative_knapsack_delante(W, v, w)
```

```
def mochidora(W, v, w):
    R = {}
    def V(i, c):
        if i== 0 or c == 0:
            R[i, c] = 0
        elif c-w[i] >= 0:
            if (i-1, c) not in R:
                V(i-1, c)
            elif (i-1, c - w[i]) not in R:
                V(i-1, c-w[i])
        else:
            return 0
    return V(len(v)-1, W)
```

```

else:
    R[i,c] = max(R[i-1, c], R[i-1, c-w[i]] +v[i]) # metemos a la mochila o no

else:
    if (i-1, c) not in R:
        R[i-1, c] = V(i-1, c)
    R[i, c] = R[i-1, c]
    return R[i,c]
return V(len(v), W)

```

▼ Practicas

```

import numpy as np
import math

def levenshtein(x, y, threshold):
    M = np.ones((len(x) + 1, len(y) + 1))*np.inf
    for i in range(0, len(x) + 1):
        M[i, 0] = i
    for j in range(0, len(y) + 1):
        M[0, j] = j
    m = len(x)/len(y)
    for i in range(1, len(x) + 1):
        colMin = np.inf;
        for j in range(max(math.floor(m*i-threshold), 1), min(math.ceil(m*i+threshold), len(y))):
            if x[i - 1] == y[j - 1]:
                M[i, j] = min(M[i - 1, j] + 1, M[i, j - 1] + 1, M[i-1][j-1])
            else:
                M[i, j] = min(M[i - 1, j] + 1, M[i, j - 1] + 1, M[i-1][j-1] + 1)
            if colMin > M[i,j]:
                colMin = M[i,j]
        if colMin > threshold:
            return None
    return M[len(x), len(y)]

def damerau_levenshtein_restringida(x, y, threshold):
    M = np.ones((len(x) + 1, len(y) + 1))*np.inf
    for i in range(0, len(x) + 1):
        M[i, 0] = i
    for j in range(0, len(y) + 1):
        M[0, j] = j
    m = len(x)/len(y)
    for i in range(1, len(x) + 1):
        colMin = np.inf;
        for j in range(max(math.floor(m*i-threshold), 1), min(math.ceil(m*i+threshold), len(y))):
            if i > 1 and j > 1 and x[i - 2] == y[j - 1] and x[i - 1] == y[j - 2]:
                if x[i - 1] == y[j - 1]:
                    M[i, j] = min(M[i - 1, j] + 1, M[i, j - 1] + 1, M[i-1][j-1], M[i-2][j-2])
                else:
                    M[i, j] = min(M[i - 1, j] + 1, M[i, j - 1] + 1, M[i-1][j-1] + 1, M[i-2][j-2] + 1)
            else:
                M[i, j] = min(M[i - 1, j] + 1, M[i, j - 1] + 1, M[i-1][j-1] + 1, M[i-2][j-2] + 1)
            if colMin > M[i,j]:
                colMin = M[i,j]
        if colMin > threshold:
            return None
    return M[len(x), len(y)]

```

```

else:
    if x[i - 1] == y[j - 1]:
        M[i, j] = min(M[i - 1, j] + 1, M[i, j - 1] + 1, M[i-1][j-1])
    else:
        M[i, j] = min(M[i - 1, j] + 1, M[i, j - 1] + 1, M[i-1][j-1] + 1)
    if colMin > M[i,j]:
        colMin = M[i,j]
if colMin > threshold:
    return None
return M[len(x), len(y)]

```

```

def damerau_levenshtein_intermedia(x, y, threshold):
    M = np.ones((len(x) + 1, len(y) + 1))*np.inf
    for i in range(0, len(x) + 1):
        M[i, 0] = i
    for j in range(0, len(y) + 1):
        M[0, j] = j
    m = len(x)/len(y)
    for i in range(1, len(x) + 1):
        colMin = np.inf;
        for j in range(max(math.floor(m*i-threshold), 1), min(math.ceil(m*i+threshold), len(y))):
            minInit = 0
            if x[i - 1] == y[j - 1]:
                minInit = min(M[i-1, j] + 1, M[i, j-1] + 1, M[i-1][j-1])
            else:
                minInit = min(M[i-1, j] + 1, M[i, j-1] + 1, M[i-1][j-1] + 1)

            if j > 1 and i > 1 and x[i - 2] == y[j - 1] and x[i - 1] == y[j - 2]:
                M[i,j] = min(minInit, M[i-2][j-2] + 1)
            elif j > 2 and i > 1 and x[i-2] == y[j-1] and x[i-1] == y[j-3]:
                M[i,j] = min(minInit, M[i-2][j-3] + 2)
            elif i > 2 and j > 1 and x[i - 3] == y[j-1] and x[i-1] == y[j-2]:
                M[i,j] = min(minInit, M[i-3][j-2] + 2)
            else:
                M[i,j] = minInit
            if colMin > M[i,j]:
                colMin = M[i,j]
        if colMin > threshold:
            return None
    return M[len(x), len(y)]

```

```

x = "google"
y = {"google", "kooble", "bubble", "gogole", "ggole"}

```

```

for w in y:
    print(levenshtein(x, w, 2))

```

```

None
2.0
2.0
0.0
2.0

```

```

def nqueens(n):
    sol = [None]*n
    def show_solution(solution):
        output = ["    "+"".join(str((i+1) % 10) for i in range(n))+"\n"]
        for i in range(n):
            output.append("%3d %s\n" % (i+1,"".join("X" if solution[j]==i else "." for j in range(n))))
        return "".join(output)

    def is_promising(longSol, queen):
        return all(queen != sol[i] and longSol-i != abs(queen-sol[i]) for i in range(longSol))

    def backtracking(longSol):
        if longSol == n:
            print(sol)
            return show_solution(sol)
        else:
            for queen in range(n):
                if is_promising(longSol, queen):
                    sol[longSol] = queen
                    r = backtracking(longSol+1)
                    if r is not None:
                        return r
            return None # explicit
    return backtracking(0)

```

```
print(nqueens(8))
```

```

[0, 4, 7, 5, 2, 6, 1, 3]
12345678
1 X.....
2 .....X.
3 ....X...
4 .....X
5 .X.....
6 ...X....
7 .....X..
8 ..X.....

```

```

def nqueens(n, allSolutions):
    sol = [None]*n
    def show_solution(solution):
        output = ["    "+"".join(str((i+1) % 10) for i in range(n))+"\n"]
        for i in range(n):
            output.append("%3d %s\n" % (i+1,"".join("X" if solution[j]==i else "-" for j in range(n))))
        return "".join(output)

    def is_promising(longSol, queen):
        return all(queen != sol[i] and longSol-i != abs(queen-sol[i]) for i in range(longSol))

    def backtracking(longSol):
        if longSol == n:
            results.append(show_solution(sol))
        if allSolutions or len(results) == 0:
            for queen in range(n):
                if is_promising(longSol, queen):
                    sol[longSol] = queen
                    backtracking(longSol+1)

```

```

        return None # explicit
    results = []
    backtracking(0)
    return results
for a in nqueens(4, 'TODAS'):
    print(a)

```

```

    1234
1  --X-
2  X---
3  ---X
4  -X--

```

```

    1234
1  -X--
2  ---X
3  X---
4  --X-

```

Ciclo Hamiltoniano

```

from random import sample

def hamiltoniano(G):
    def backtracking(path):
        if len(path) == len(G.V):
            if (path[-1] == path[0]) in G.E:
                return path + [path[0]]
            else:
                for v in G.succs(path[-1]):
                    if v not in path:
                        found = backtracking(path + [v])
                        if found:
                            return found
                return None
    [random_vertex] = sample(G.V, 1)
    return backtracking([random_vertex])

```

Reinas

```

class NQueensSolver1:
    def __init__(self, n):
        self.n = n

    def is_complete(self, s):
        return len(s) == self.n

    def is_promising(self, s, row):
        return all(row != s[i] and len(s)-i != abs(row-s[i]) for i in range(len(s)))

    def backtracking(self, s):
        if self.is_complete(s):

```

```
return s
```

```
for row in range(self.n):
    if self.is_promising(s, row):
        found = self.backtracking(s+[row])
        if found != None:
            return found
return None
```

```
def solve(self):
    return self.backtracking([])
```

```
NQueensSolver1(8).solve()
```

```
[0, 4, 7, 5, 2, 6, 1, 3]
```

```
[0, 4, 7, 5, 2, 6, 1, 3]
```

backtracking + mochila de Dora la exportadronjas

```
def subset(w, W):
    x = [0] * len(w)
    def backtracking(i):
        if i == len(w)+1: #is_complete
            if sum(w[j] * x[j] for j in range(1, len(w)+1)) == W:
                return x
        else:
            for x[i] in [0, 1]: # Exploring new branch
                if sum([w[j] * x[j] for j in range(1, i + 1)]) <= W: #is_promising
                    found = backtracking(i+1)
                    if found != None:
                        return found
            return None
    return backtracking(1)
```

```
subset(w=[4,5,3,6] ,W=8)
```



```
IndexError                                Traceback (most recent call last)
<ipython-input-31-a86c21f14083> in <module>()
    14     return backtracking(1)
```

```
12345
1 X....
2 ...X.
3 .X...
4 ....X
5 ..X..
```

SEARCH STACK OVERFLOW