

# Co-Training

Based on

“Combining Labeled and Unlabeled Data with Co-Training”  
by A. Blum & T. Mitchell, 1998

## Problem:

Learning to classify data (ex: web pages) when the description of **each example** can be partitioned in **2 distinct views**.

**Assumption:** Either view of the example would be sufficient for learning if we had enough labeled data, but:

**Goal:** use both views to allow inexpensive unlabeled data to augment a much smaller set of labeled examples.

**Idea:** 2 learning algorithms are trained separately on each view. Then each algorithm's predictions on new unlabeled examples are used to enlarge the training set of the other.

**Empirical result** on real data: The use of unlabeled examples can lead to significant improvement of hypotheses in practice.

**Not presented here:**  
(see the paper)

**Theoretical goal:** Provide a PAC-style analysis for this setting.

**More general:** Provide a PAC-style framework for the general problem of learning from both labeled and unlabeled data.

## Example

Classify web pages at CS departments at some universities as belonging or not to faculty members.

### Views:

1. the text appearing on the document itself
2. the anchor text attached to hyperlinks pointing to this page from other pages on the web.

Use **weak predictors**, like

1. “research interests”
2. “my advisor”

Pages pointed to by links having the phrase “my advisor” can be used as ‘probably positive’ examples to further train a learning algorithm based on the words on the text page, and vice-versa.

## Co-training Algorithm

4.

Input:

$L$ , a set of labeled training examples

$U$ , a set of unlabeled examples

Create a pool  $U'$  of examples by choosing  $u$  examples at random from  $U$ .

Loop for  $k$  iterations:

use  $L$  to train a classifier  $h_1$  that considers only the  $x_1$  view of  $x$

use  $L$  to train a classifier  $h_2$  that considers only the  $x_2$  view of  $x$

select from  $U'$   $p$  most confidently labeled by  $h_1$  as positive examples

select from  $U'$   $n$  most confidently labeled by  $h_1$  as negative examples

select from  $U'$   $p$  most confidently labeled by  $h_2$  as positive examples

select from  $U'$   $n$  most confidently labeled by  $h_2$  as negative examples

add these self-labeled examples to  $L$

randomly choose  $2p+2n$  examples from  $U$  to replenish  $U'$

## Working example

### Classify course home pages

1051 web pages at CS departments at several universities:  
Cornell, Washington, Wisconsin, and Texas

22% course pages

263 (25%) were first selected as a test set;

from the remaining data it was generated  $L$ , the set of labeled examples, by selecting at random 9 negative examples and 3 positive examples;

the remaining examples form  $U$ , the set of unlabeled examples.

use a Naive Bayes classifier for each of the two views.

## Results

	<i>page-based classifier</i>	<i>hyperlink-based classifier</i>	<i>combined classifier</i>
<i>supervised training</i>	12.9	12.4	11.1
<i>co-training</i>	6.2	11.6	5.0

Explanation: The *combined* classifier uses the naive independent assumption:

$$P(Y \mid h_1 \wedge h_2) = P(Y \mid h_1)P(Y \mid h_2)$$

Conclusion: The *co-trained* classifier outperforms the classifier formed by supervised training.

## Another suggested practical application

Classifying segments of TV broadcasts, for instance:  
learning to identify televised segments containing the US president.

Views:  $X_1$  – video images,  $X_2$  – audio signals.

Weakly predictive recognizers:

1. one that spots full frontal images of the president's face
2. one that spots his voice when no background is present.

Use co-training to improve the accuracy of both classifiers.



## Another suggested practical application

Robot training, recognizing an open doorway using a collection of vision ( $X_1$ ), sonar ( $X_2$ ) and laser range ( $X_3$ ) sensors.