

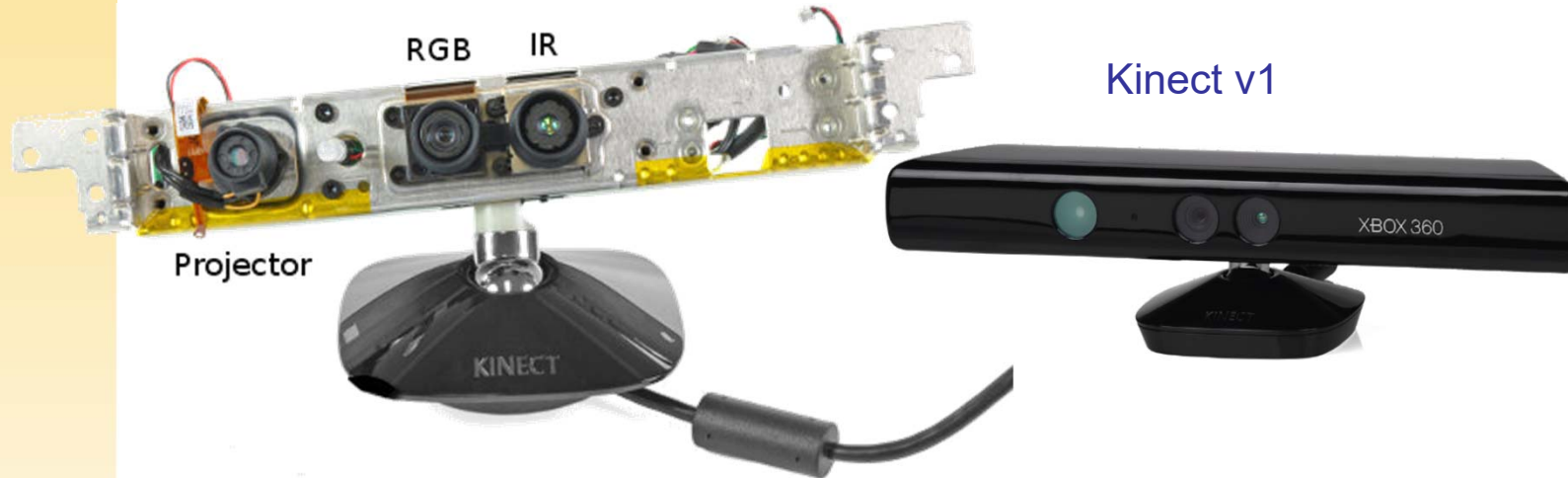
## ***U9.2. 3D Vision. ToF Systems***

**SJK002 Computer Vision**

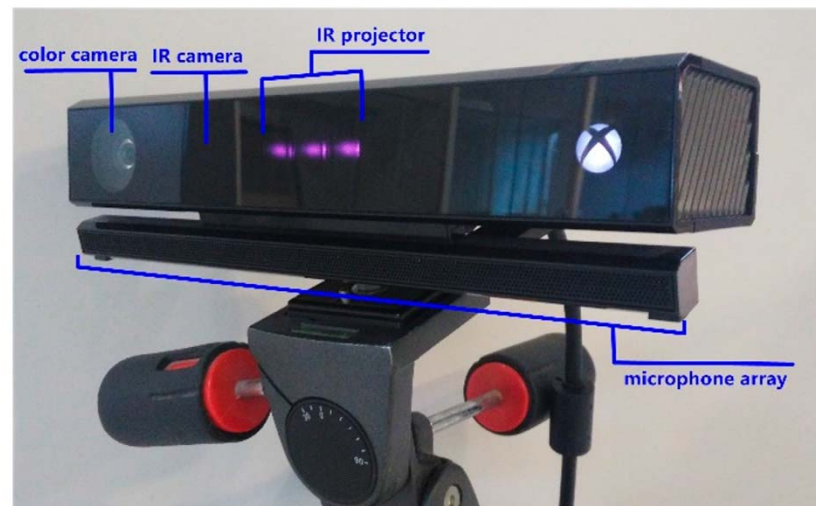
***Master in Intelligent Systems***



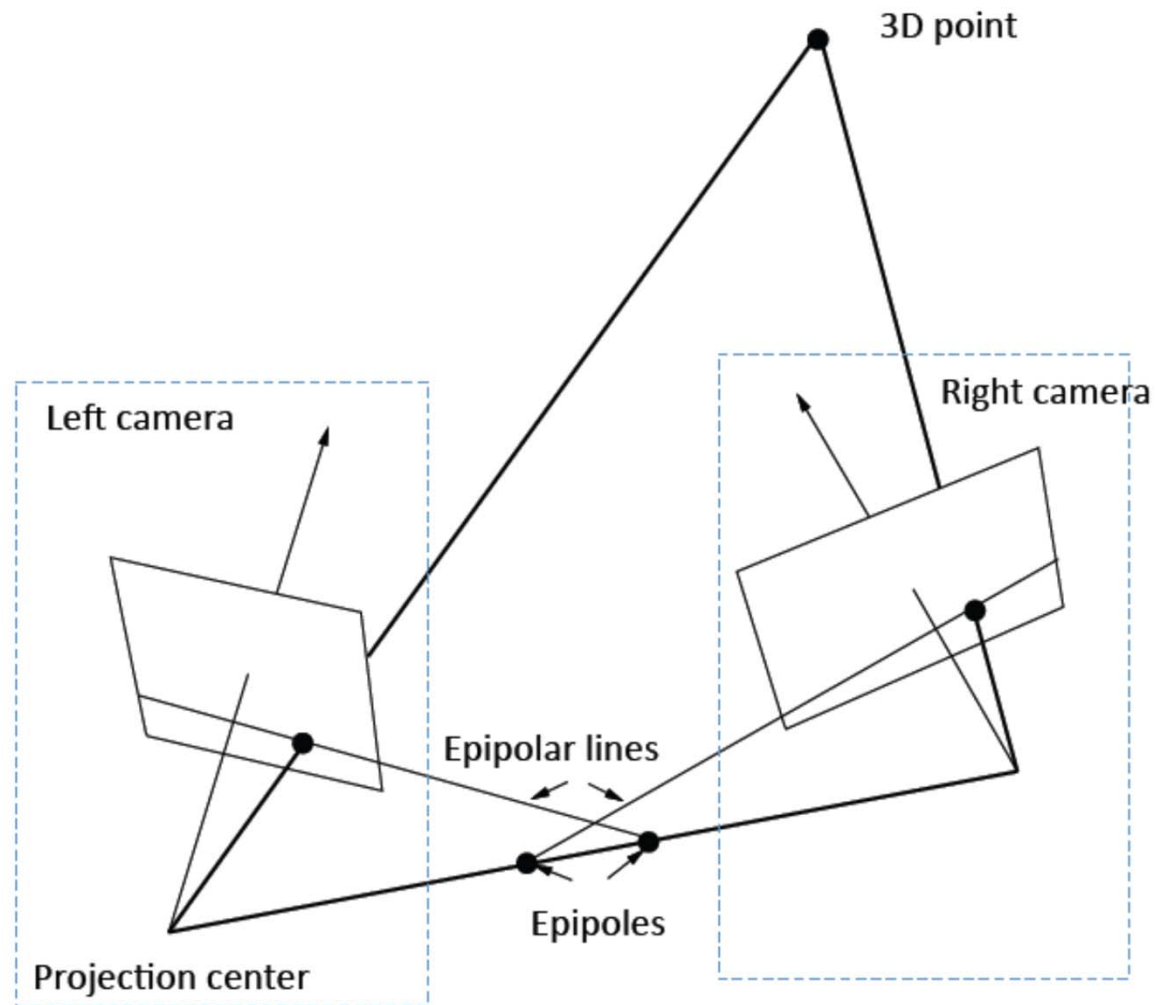
- Structured light:
  - Structured light patterns
  - Correspondence
  - Limitations
- Time of Flight, ToF:
  - Continuous Wave modulation (CW-modulation)
  - Pulsed Modulation (PM)
- LIDAR: Light Detection and Ranging



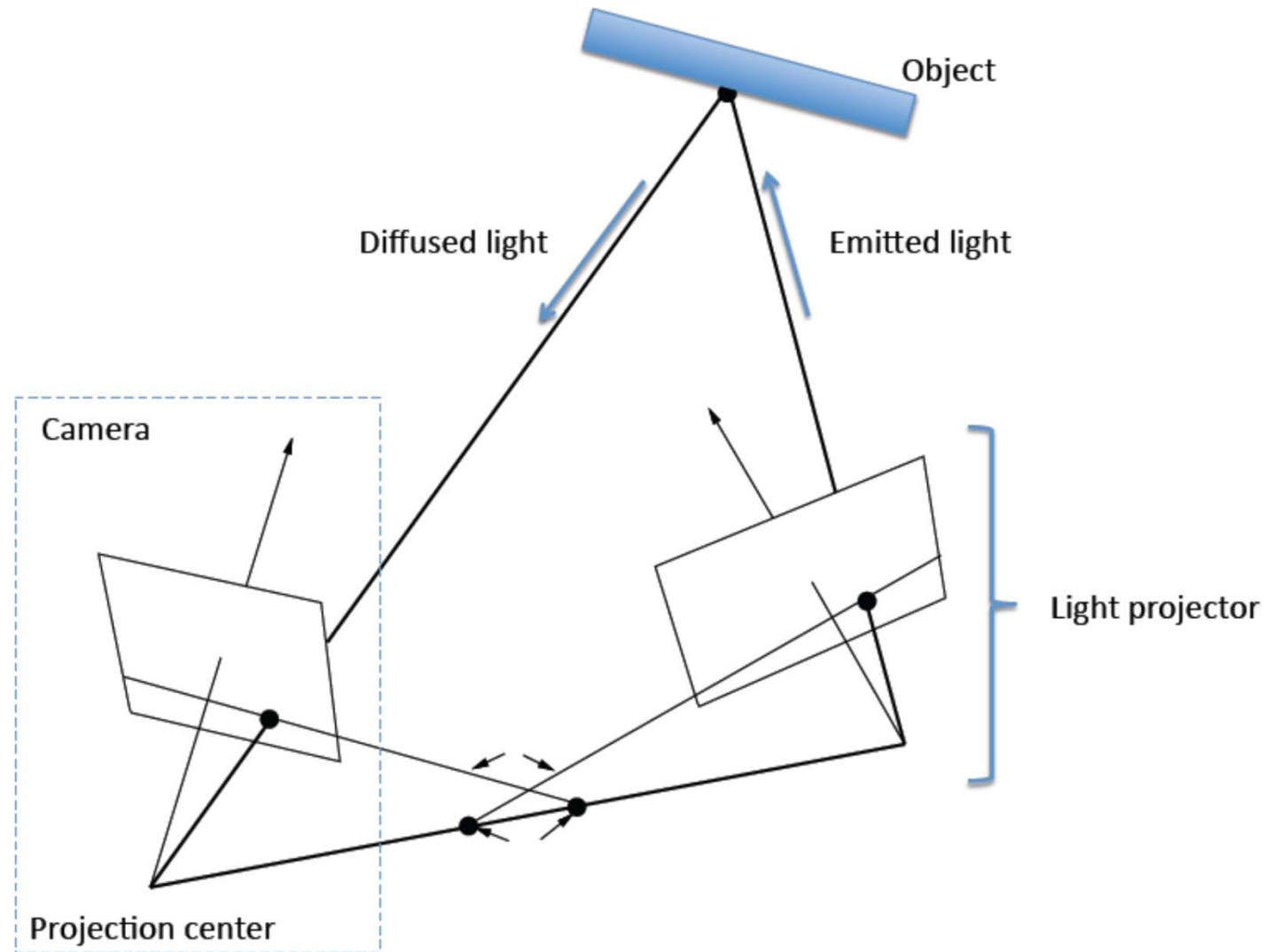
Kinect v2



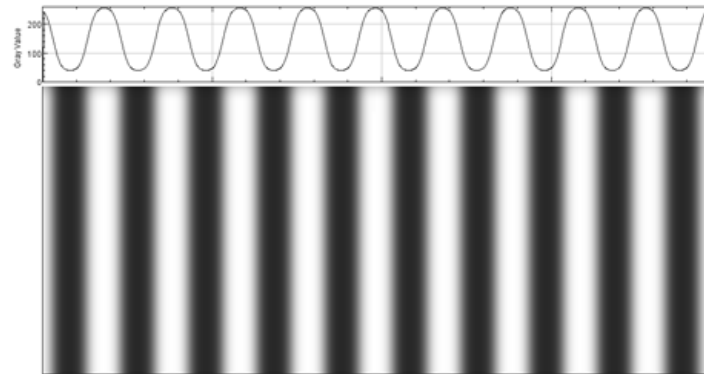
# Structured light



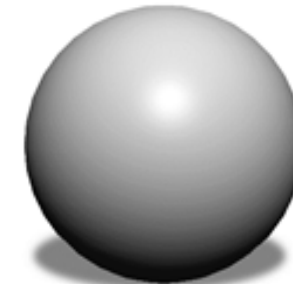
# Structured light



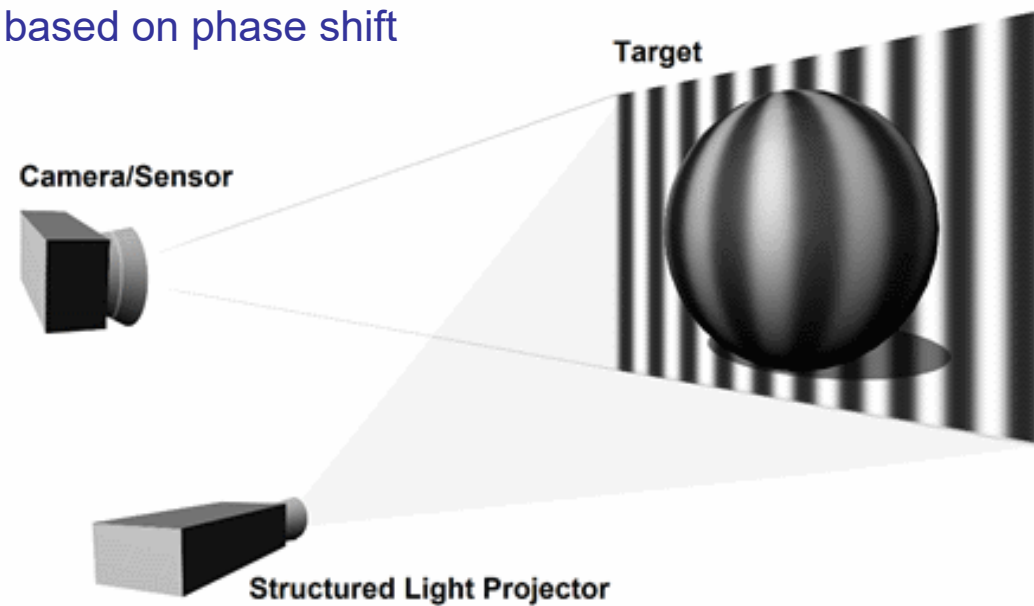
# Structured light



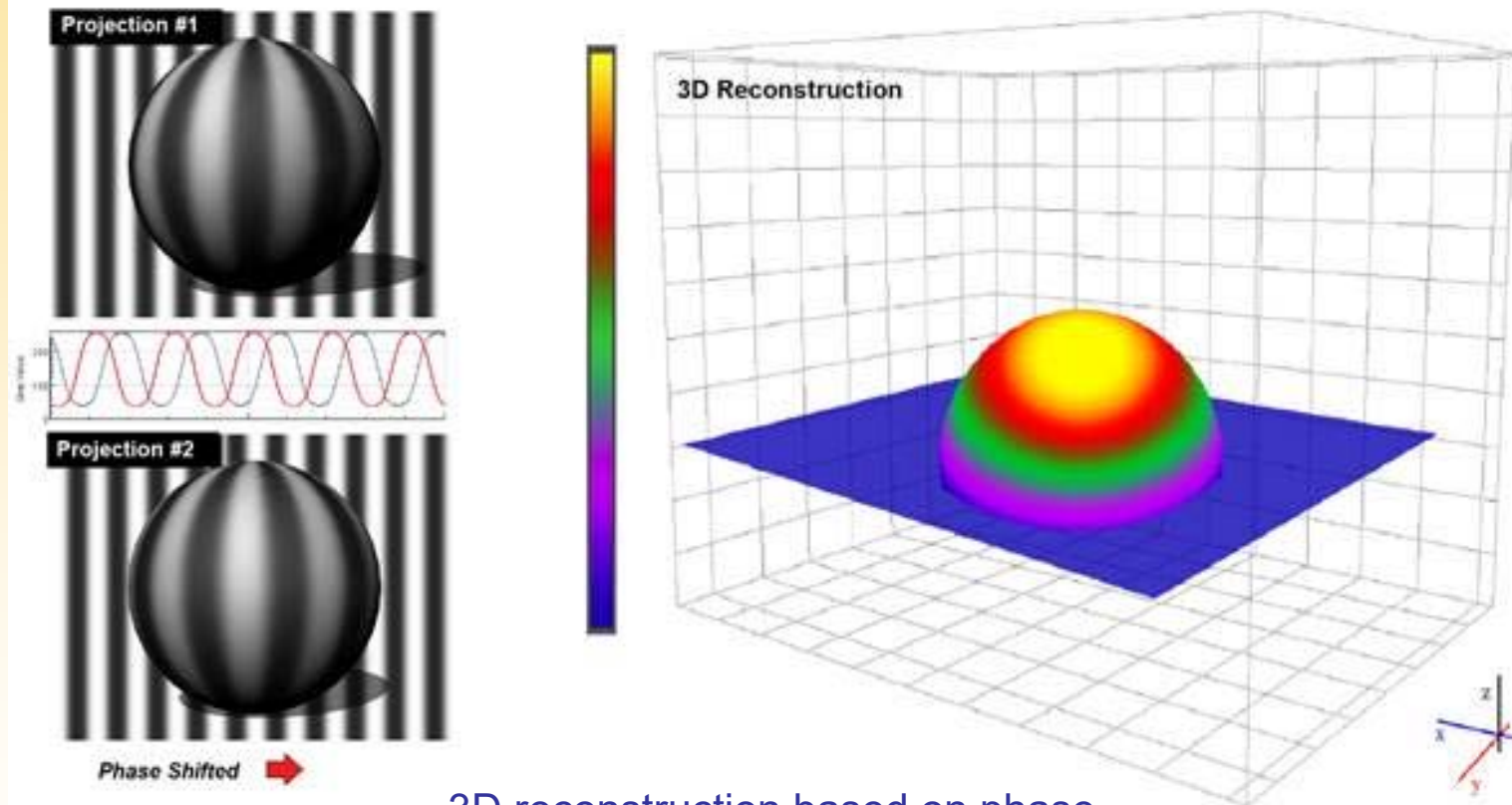
Wave pattern image for structured light based on phase shift



Target object

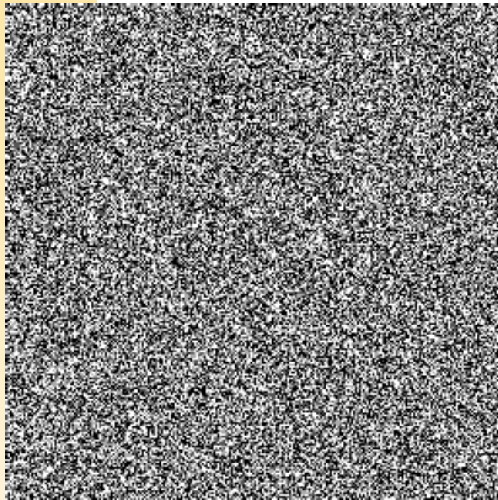


# Structured light



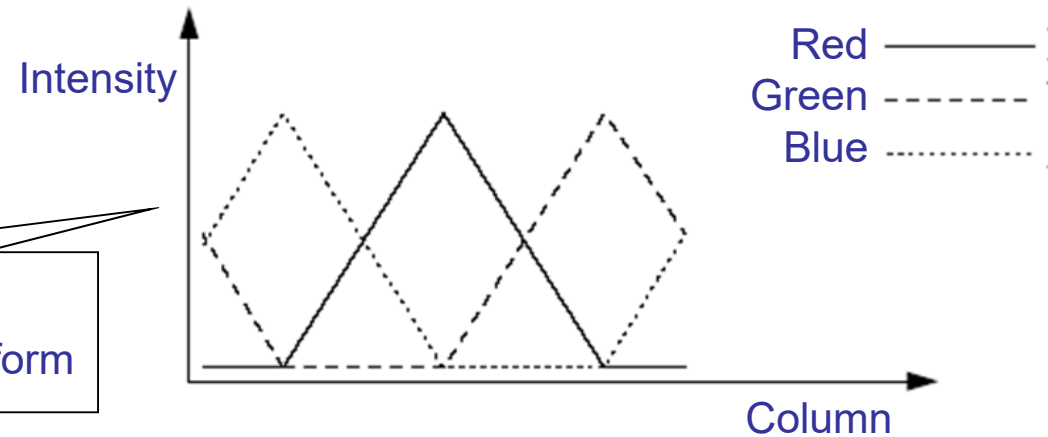
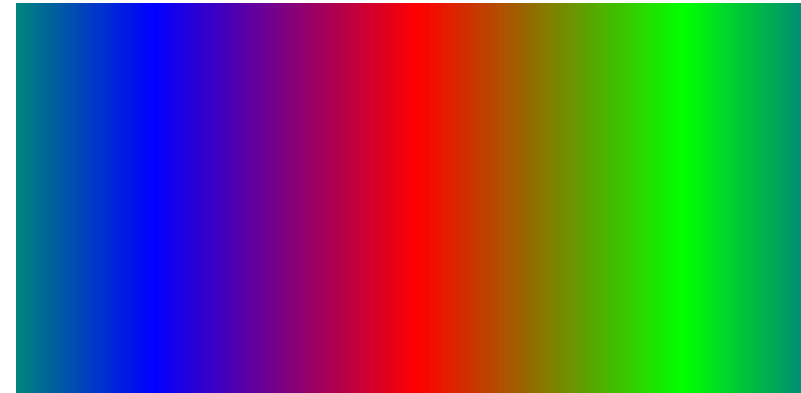
3D reconstruction based on phase  
shift wave patterns of structured light

# Structured light



Random pattern

Color pattern



One component is always null,  
and the pattern intensity is uniform

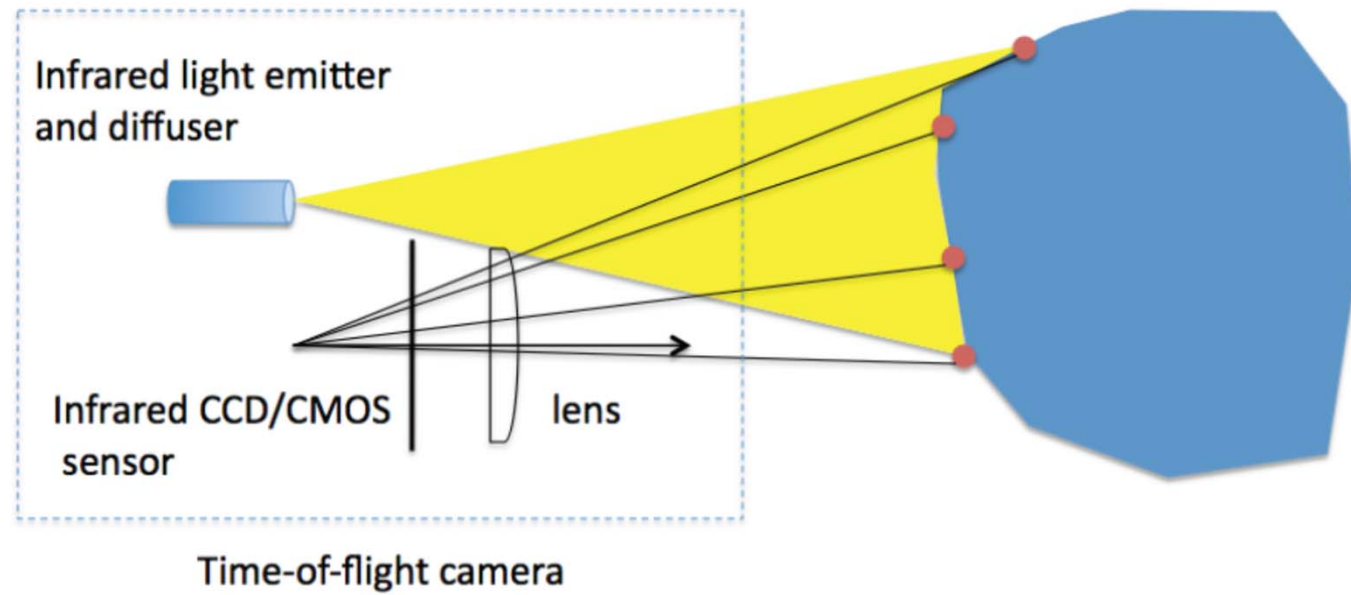


- Calibrate **intrinsic parameters** of the IR camera.
- Calibrate **extrinsic parameters** with respect to a single calibration grid.
- Transform the calibration plane in the **camera coordinates system**.
- Calibrate the **projector** in the camera reference system.
- **Move the calibration plane** to several scene positions.
- **Rectify the camera-projector system** to align the image of the camera with the projector plane.
- **Calibration software**, for example:  
<https://github.com/jakobwilm/slstudio/>

- As a stereo vision system, the problem is to find the correspondence between a point in the **image of the camera and the corresponding point in the projector pattern.**
- **Each pixel of the projector can be signaled to be** recognized by:
  - Temporal signal.
  - Spatial signal.
  - Combination of both.
- Use **cross correlation**: define a window around the target pixel and use correlation techniques between the window image values and the calibration pattern values.

- Structured light system calibration needs **projector information** (pattern, etc.):
  - Kinect does not provide this information.
- As a **stereo system**, it provides **limited range estimation**.
- Very **sensitive to light saturation**:
  - Bad behaviour in outdoor scenarios, with natural illumination.
- Problems with partial occlusion and light scattering (hair, wool fabrics, ...).
- **Advantage**:
  - **Good spatial resolution**, usually better than ToF.

- **Principle:**
  - Measure the time a light pulse lasts going from the camera light source to an object and back to the sensor.
- Light travels at a speed 300.000 Km/s
- ToF system:
  - **Pulsed modulation (PM)**
  - **Continuous Wave modulation (CW-modulation)**



- ToF distance: 
$$d = \frac{1}{2}c\tau$$
- In practice  $\tau$  is measured in an indirect way.
- Continuous Wave modulation (CW-modulation)
  - Measures the phase difference between the emitted and received signal.
  - Different signal shapes: sinusoidal, square, ...
  - Base on cross correlation between signals. Signal frequency is known.

- Amplitude modulated frequencies used between 10-100 MHz.
- Relation between signal phase and ToF:

$$\phi = 2\pi f\tau$$

- Phase  $\phi$  is defined up to  $2\pi$ : *phase warping*.
- Amplitude of the received signal  $A$  depends on object reflectivity and sensor sensitivity.
- Amplitude  $A$  decreases as  $1/d^2$ , mainly due to dispersion.
- Ambient illumination is a constant  $B$

- **Emitted** signal:

$$s(t) = a \cos(2\pi f t)$$

- **Received** signal:

$$r(t) = A \cos(2\pi f(t - \tau)) + B$$

- **Cross correlation** between emitted and received signals:

$$C(x) = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2} r(t)s(t+x)dt$$

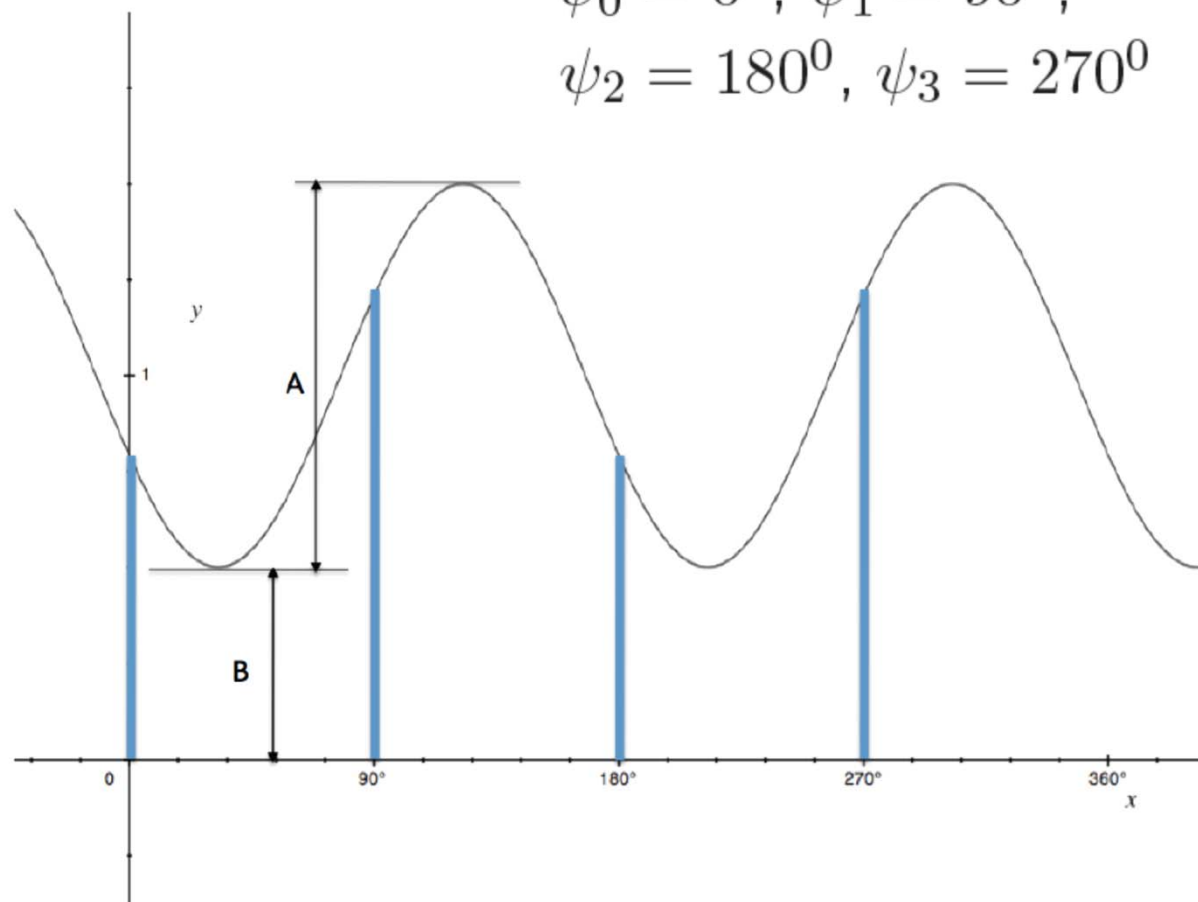
$$C(\psi) = \frac{aA}{2} \cos(\underbrace{2\pi f \tau}_{\phi} + \underbrace{2\pi f x}_{\psi}) + B$$



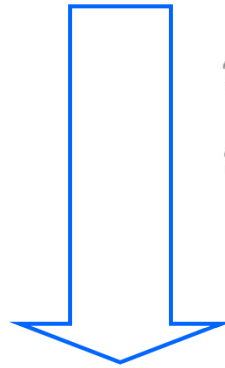
- 4 cubes method:

- Estimate values of  $C(\psi)$   
in four phases

$$\psi_0 = 0^\circ, \psi_1 = 90^\circ, \\ \psi_2 = 180^\circ, \psi_3 = 270^\circ$$



$$C(\psi) = \frac{aA}{2} \cos(\underbrace{2\pi f\tau}_{\phi} + \underbrace{2\pi fx}_{\psi}) + B$$



$$\begin{aligned} \psi_0 &= 0^0, \psi_1 = 90^0, \\ \psi_2 &= 180^0, \psi_3 = 270^0 \end{aligned}$$

$$\phi = 2\pi f\tau = \arctan \left( \frac{C(x_3) - C(x_1)}{C(x_0) - C(x_2)} \right)$$

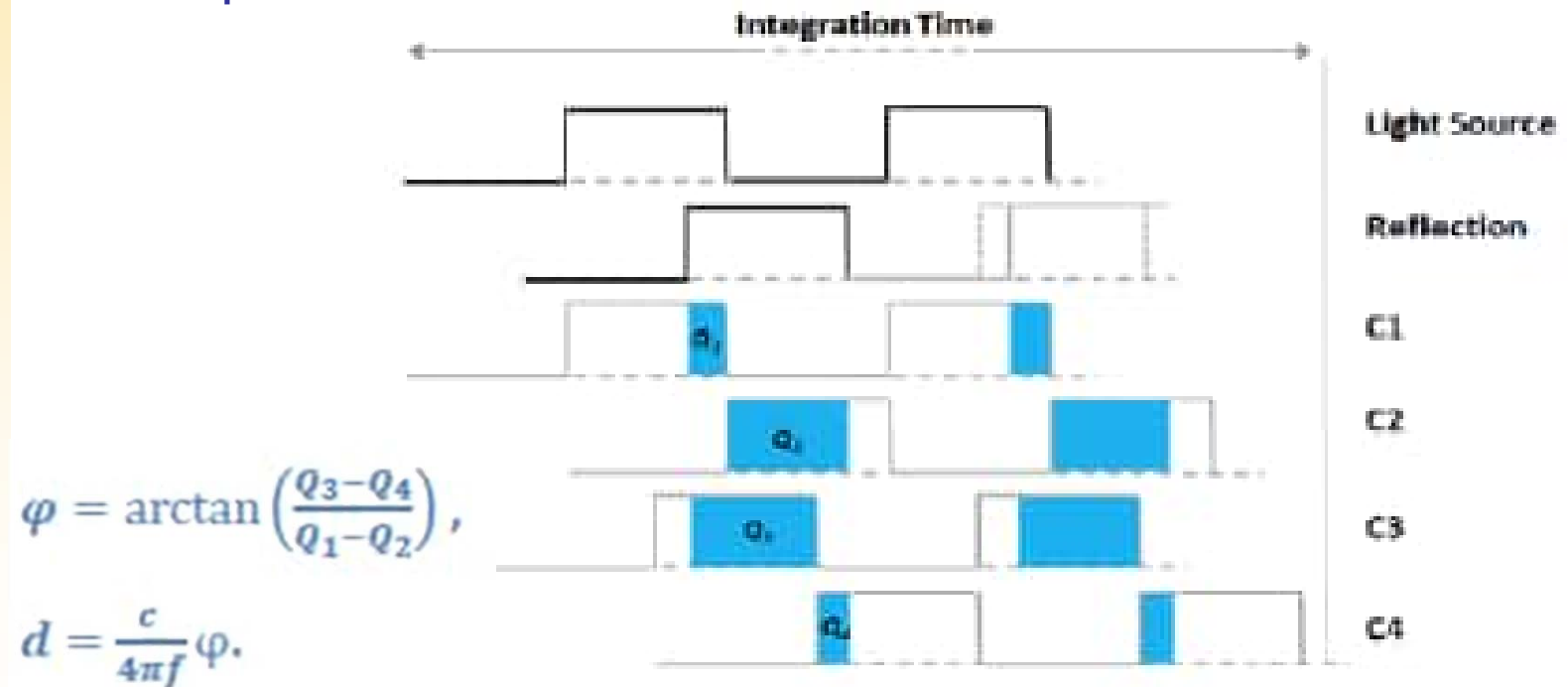
$$A = \frac{1}{2a} \sqrt{(C(x_3) - C(x_1))^2 + (C(x_0) - C(x_2))^2}$$

$$B = \frac{1}{4} (C(x_0) + C(x_1) + (C(x_2) + C(x_3)))$$

## ToF. CW-modulation

$$\phi = 2\pi f\tau \Rightarrow \tau \Rightarrow d = \frac{1}{2}c\tau \Rightarrow d = \frac{c}{2f} \frac{\phi}{2\pi}$$

- In practice:



- E.g. for a frequency  $f = 30\text{MHz}$ 
  - Unambiguous range from  $d_{\min} = 0$  to  $d_{\max} = 5\text{ m}$ .
- For larger distance we must apply “phase unwrapping” techniques.
- Accuracy increases with modulation frequency.
- Several and different ToF frequencies can be combined.
- Needs significant integration times, over several periods, in order to increase SNR:
- Blurring effects because of motion.



## ToF Camera Module

### Features:

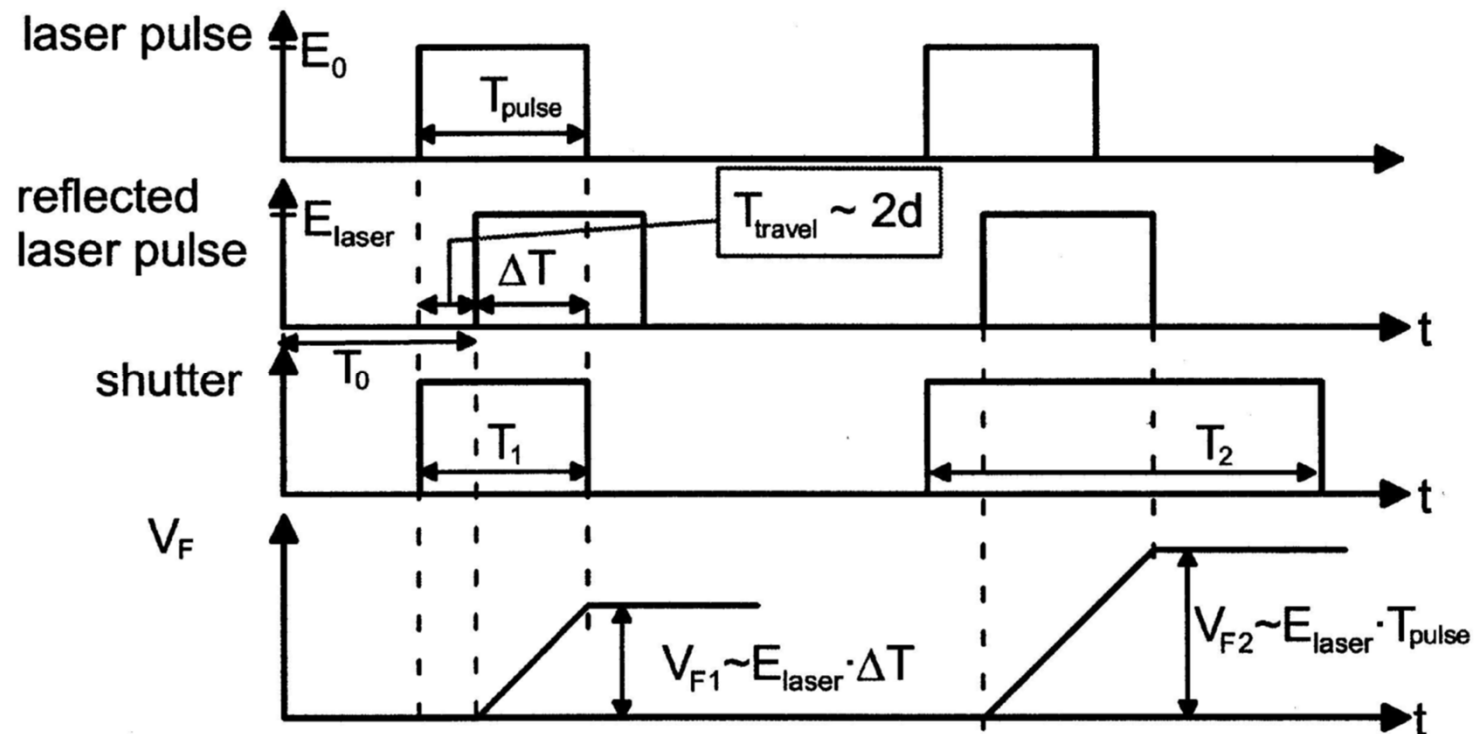
- Based on ADI's ToF Signal Chain Products and Technology
- Can output depth map and (710 version) TOF + RGB Image (can disable)
- FOV 70 X 54
- Depth camera support image size: up to 640\*480@30FPS
- RGB camera support image size: up to 1920\*1080@30FPS
- USB 2.0 interface
- Support OS: Runs on Android / Runs on Linux / Runs on Windows 7/8/10
- Pico depth sensor SDK, sample code and tools (Open NI SDK Compatible)
- Sample application algorithms available from ADI in Python

<https://www.analog.com/en/applications/technology/3d-time-of-flight.html>

## ToF. Pulsed Modulation

- Laser light pulse of **nanoseconds order**.
- Distance is estimated **by directly measuring the delay** between the emitted pulse and received signal.
- **Very short pulses of high optical power** can be used:
  - Pulse irradiance should be much higher than the background illumination.
- **Total emitted energy should be low** (class 1).
- Does not suffer from ambiguous range, as in CW.
- Can be used **outdoors**.

# ToF. Pulsed Modulation



Elkhalili et al. (2004). IEEE Transactions on Solid-State Circuits, Vol. 39. No 7, pages 1208-1212

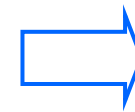
# ToF. Pulsed Modulation

$$\Delta T = T_{\text{pulse}} - T_{\text{travel}}$$

During the first  
integration

$$V_{F1} \propto E_{\text{laser}} \Delta T$$

$$V_{F2} \propto E_{\text{laser}} T_{\text{pulse}}$$



$$\Delta T = \frac{V_{F1}}{V_{F2}} T_{\text{pulse}}$$

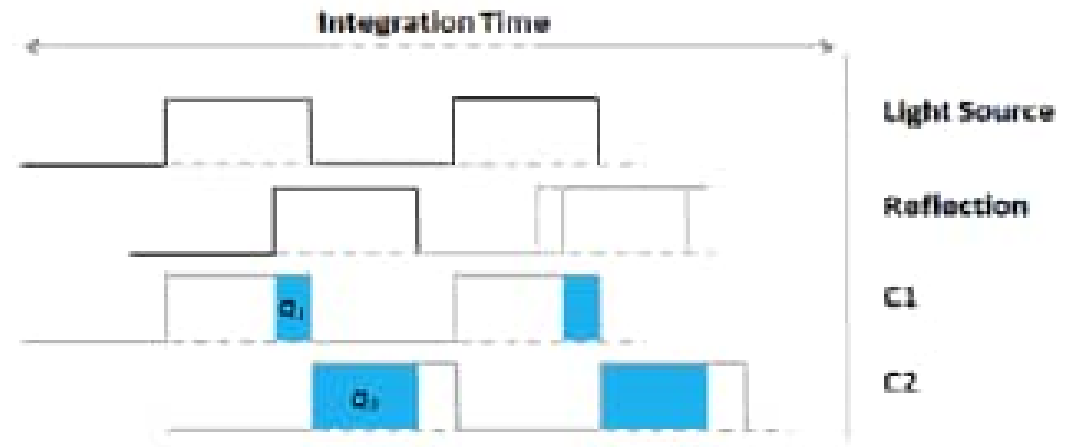
During the second integration, total  
reflected pulse energy is measured

$$d = \frac{c}{2} T_{\text{travel}} = \frac{c}{2} (T_{\text{pulse}} - \Delta T) = \frac{c}{2} T_{\text{pulse}} \left( 1 - \frac{V_{F1}}{V_{F2}} \right)$$

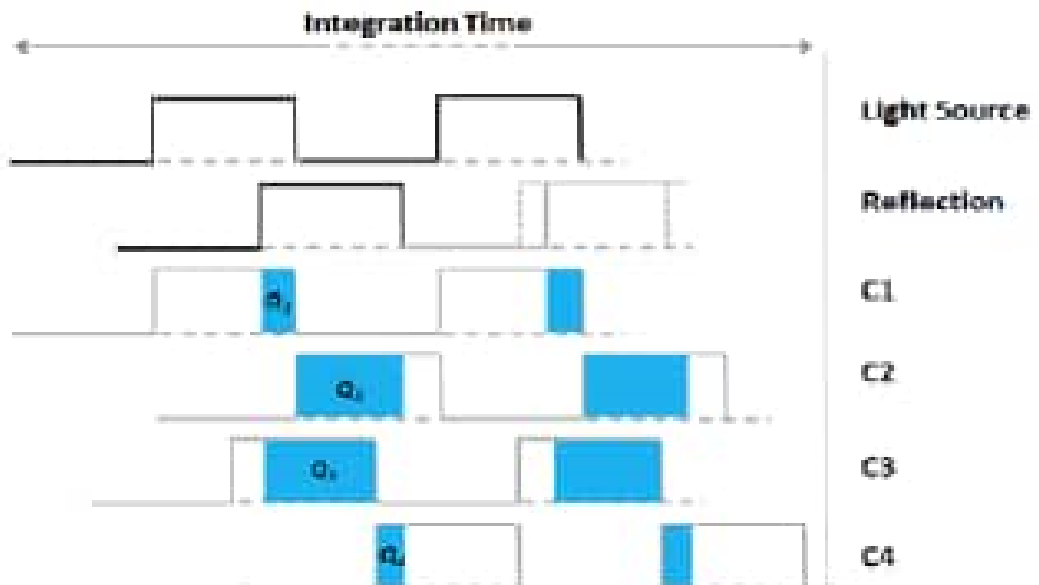


# ToF. Pulsed Modulation

Pulsed modulation



Continuous Wave  
modulation CW



# ToF. Pulsed Modulation

## ■ Precision:

- Based on estimating  $\Delta T = T_{\text{pulse}} - T_{\text{travel}}$
- Note that it is zero if  $T_{\text{travel}} = T_{\text{pulse}}$
- Maximum range  $d_{\text{max}} = \frac{c}{2} T_{\text{pulse}}$

■ **Example:**  $T_{\text{pulse}} = 30\text{ns}$  maximum distance 4,5 m.

## ■ Maximum range can be extended by:

- Increment light pulse duration.
- Introduce a delay between the emitted pulse start and the beginning of integration time (shutter):
  - ▶ Produces a minimum distance  $d_{\text{min}} > 0$

## ToF. Pulsed Modulation

- Example of sensor parameters for a ToF system:

Number of pixels:	$4 \times 64$
Pixel size:	$130 \times 300 \mu m^2$
Laser wavelength:	$850 - 910 nm$
Depth accuracy (1 pulse):	$< 5 cm$
Depth accuracy (100 pulses):	$< 1 cm$

## Tiger Eye 3D video camera



- 128 x 128 pixels APD (avalanche photo diode); 30Hz
- 1570 nm eye-safe laser
- 3° field of view (actual full FOV = 3° x 3°); Range up to 1100 meters
- 9° field of view (actual full FOV = 8.6° x 8.6°); Range up to 450 meters
- 45° x 22° field of view; Range up to 150 meters
- 45° field of view; Range up to 60 meters