# COMENIUS UNIVERSITY IN BRATISLAVA FACULTY OF MATHEMATICS, PHYSICS AND INFORMATICS

# SOFTWARE FOR ISOMETRIC GENE TREE RECONCILIATION

Master's thesis

# COMENIUS UNIVERSITY IN BRATISLAVA FACULTY OF MATHEMATICS, PHYSICS AND INFORMATICS

# SOFTWARE FOR ISOMETRIC GENE TREE RECONCILIATION

Master's thesis

Study programme: Applied Computer Science

Field of study: Computer Science

Department: Department of Computer Science

Supervisor: doc. Mgr. Bronislava Brejová, PhD.





### Univerzita Komenského v Bratislave Fakulta matematiky, fyziky a informatiky

#### ZADANIE ZÁVEREČNEJ PRÁCE

Meno a priezvisko študenta: Dominika Mihálová

**Študijný program:** aplikovaná informatika (Jednoodborové štúdium,

magisterský II. st., denná forma)

Študijný odbor:informatikaTyp záverečnej práce:diplomováJazyk záverečnej práce:anglickýSekundárny jazyk:slovenský

**Názov:** Software for isometric gene tree reconciliation

Softvér pre izometrickú rekonciliáciu génových stromov

Anotácia: Izometrická rekonciliácia génových stromov je výpočtový problém, v ktorom

je cieľom identifikovať zodpovedajúce si vrcholy v dvoch stromoch, z ktorých jeden reprezentuje evolučnú históriu skupiny organizmov a druhý reprezentuje evolučnú históriu jedného génu v rámci týchto organizmov. Cieľom práce je implementovať praktický softvér na rekonciliáciu génových stromov a experimentálne otestovať jeho presnosť na simulovaných aj reálnych

biologických dátach.

Vedúci:doc. Mgr. Bronislava Brejová, PhD.Katedra:FMFI.KI - Katedra informatikyVedúci katedry:prof. RNDr. Martin Škoviera, PhD.

**Dátum zadania:** 14.10.2019

**Dátum schválenia:** 29.11.2019 prof. RNDr. Roman Ďurikovič, PhD.

garant študijného programu

študent	vedúci práce

## Abstrakt

Evolučná história môže byť zobrazená fylogenetickými stromami. Používame dva typy fylogenetických stromov: strom druhov a génový strom. Strom druhov predstavuje vývoj druhu a genový strom predstavuje vývoj jedného génu. Izometrická rekonciliácia génových stromov je problém mapovania génového stromu na strom druhov so zachovaním dĺžok hrán. V tejto práci sa zameriavame na riešenie problému izometrickej rekonciliácie génových stromov s nepresnými dĺžkami hrán. Nadviazali sme na predchádzajúci výskum a predstavujeme dva algoritmy, ktoré sú implementované v softvéri v kombinácii s algoritmami z predchádzajúceho výskumu. Implementovaný softvér je experimentálne testovaný na simulovaných a reálnych biologických dátach a porovnávaný s inými softvérmi.

**Kľúčové slová:** izometrická rekonciliácia génových stromov, nepresné dĺžky hrán, fylogenetický strom

## Abstract

Evolutionary history can be presented by phylogenetic trees. We use two types of phylogenetic trees: species tree and gene tree. A species tree represents the evolution of a species and a gene tree represents the evolution of one gene. Isometric gene tree reconciliation is a problem of mapping the gene tree to species tree with preserving the edge lengths. In this work, we focus on solving the problem of isometric gene tree reconciliation with inexact branch lengths. We built on the previous research and present two algorithms that are implemented in software in combination with algorithms from previous research. The implemented software is experimentally tested on simulated and real biological data and compared with other software.

**Keywords:** isometric gene tree reconciliation, inexact branch lengths, phylogenetic tree

## List of Figures

1.1	Unrooted tree and its rooted version	Ę
1.2	Reconciliation and evolutionary history	7
1.3	Isometric reconciliation	13
1.4	Isometric reconciliation with inexact branch lengths	14
2.1	Rooting the gene tree	21
3.1	Entity-relationship diagram with differences	30
4.1	Duplication consistency score	51

## Contents

In	$\mathbf{trod}_{1}$	$\operatorname{uction}$	2
1	Ove	erview	3
	1.1	Background	3
	1.2	Different approaches to gene tree reconciliation	5
		1.2.1 Scoring gene tree reconciliation	7
		1.2.2 Probabilistic gene tree reconciliation	10
		1.2.3 Isometric gene tree reconciliation	12
		1.2.3.1 Exact branch length	12
		1.2.3.2 Inexact branch lengths	13
2	$\mathbf{Alg}$	${f orithms}$	18
	2.1	Rooting the gene tree	18
	2.2	Counting algorithm	20
		2.2.1 Preprocessing	23
		2.2.2 Main algorithm	26
3	Imp	olementation	28
	3.1	Classes and variables	28
	3.2	Differences from the original source code	29
4	Exp	periments and results	35
	4.1	Simulated dataset	35
		4.1.1 Without rerooting the gene tree	35
		4.1.2 With rerooting the gene tree	38
	4.2	Real dataset	50
$\mathbf{C}'$	melu	ısion	52

CONTENTS	viii
List of Appendices	57

## Introduction

In bioinformatics, the evolutionary relationships between entities are expressed with a phylogenetic tree depicted by a tree from a graph theory. We are working with two types of phylogenetic trees in this thesis: species tree and gene tree. Species tree describes the evolutionary events for a set of species and gene tree represent evolutionary events of a gene. We consider that only evolutionary event as speciation, duplication and gene loss can happen in the history. The mapping of the gene tree to species tree is called the reconciliation, which allows better detection of evolutionary events. Over the years, a lot of reconciliation approaches have been developed. In 2008, an isometric reconciliation was introduced, where branch lengths of both phylogenetic trees are known and considered in mapping phylogenetic trees. We divide the isometric reconciliation into two subsections: with exact branch length and with inexact branch lengths. We discuss the basic terminology and different approaches to solving the problem of reconciliation with concrete solutions to this problem in the form of software in the first chapter.

In this thesis, we aim at studying the problem of isometric reconciliation with inexact branch lengths since the exact branch lengths are estimated, thus not exactly known. This field was studied before [5] with a proposed algorithm to compute a reconciliation with minimizing the duplication and gene loss evolutionary events. The running time of their algorithm is  $O(N^4 log N)$ . We build on their algorithm and introduce two new algorithms described in more details in Chapter 2.

The proposed algorithms are then implemented into the source code from [5]. In Chapter 3, we describe the properties of the implemented software with highlighted changes from the previous source code. We define the needed input for our software with an optional setting for the user and subsequent output.

In the last chapter, we experimentally test the implemented software on the simu-

CONTENTS 2

lated and real biological data. We run the software for different settings, evaluate it and compare it with other reconciliation software. We interpret and discuss the results of testing the implemented software.

## 1 Overview

In this chapter, we introduce basic information and define essential terminology from the field of bioinformatics. We describe different ways for solving the problem of gene tree reconciliation with examples of existing software in more details.

### 1.1 Background

Every organism has its complete set of genetic information encoded in a genome. A genome consists of several DNA (deoxyribonucleic acid) molecules and contains all the information, which are required for the organism to function.

DNA is a long molecule composed of two complementary strands. Each strand is made up of four chemical bases: adenine, guanine, cytosine and thymine, and connected to its complementary strand by pairing rules, where adenine is paired up with thymine and cytosine is paired up with guanine. The sequence of these bases encodes the genetic information important for building and maintaining an organism. Specific parts of DNA are called genes.

A gene is a subsequence of a DNA strand that contains information for the synthesis of a specific molecule, usually a protein. It is a basic unit of heredity.

The DNA sequence of a gene can be altered by mutation. It is a process that allows small changes in the DNA of organisms that refers to differences between individuals within a population. We will be working with two types of mutations: duplication and gene loss.

Duplication is a type of mutation where one or more genes are copied and inserted to some other position in the same genome. A duplicated gene sometimes develops a new function [9].

The opposite of duplication is gene loss (deletion). It is a type of mutation in which

some part of a DNA sequence containing a gene is left out from the genome during DNA replication or it loses its function.

Speciation is an evolutionary process of in which a single population evolves populations into two distinct species. It can happen for various reasons, for example, when a group separates from other members of its species to a different geographical area. Members of a new group develop their own unique characteristics due to the demands of another environment and this process will differentiate the new species.

Duplications and speciations result in the formation of groups of similar genes, called gene families, from a single gene. A gene family consists of evolutionarily related genes from one or multiple species, which are structurally and usually functionally similar.

Evolutionary relationships formed by evolutionary events are represented in a form of graph called a phylogenetic tree, which is a branching diagram that shows evolutionary relationships between organisms. A phylogenetic tree is a tree T with nodes V(T), edges E(T) and leaves L(T). It is called weighted when branch length w(u, v) is defined for each edge (u, v).

Phylogenetic trees can be either rooted or unrooted (Fig. 1.1). A rooted tree is a phylogenetic tree T where for  $(u,v) \in E(T)$ : node u is the parent of node v, node v is the children of node u, root(T) does not have parent and leaves L(T) do not have children. An ancestor of node v is any node of tree T on the path from node v to root(T). Every ancestor have at least one descendant. An descendant of node v is any node of tree T of which v is an ancestor [12]. We will denote for  $u, v \in V(T)$  that  $v <_T u$  if v is an ancestor of v and v is descendant of v.

Every rooted tree has a height, which symbolizes the longest path. It is the number of nodes between the root(T) and one of the leaves.

Nodes in rooted trees have levels. The level of node l(u) is the number of ancestors on the path from the node u to the root(T). The root of a tree root(T) has level 0, since it has no parents.

If a rooted tree is weighted, nodes in the tree have depths. The depth of node u, D(u), is the sum of the lengths of all edges between node u and the root(T) of a rooted tree.

For a group of nodes in a rooted tree, their lowest common ancestor (LCA) is

the farthest node from the root that has all nodes in the group as descendants.

An unrooted tree is a phylogenetic tree without root. Unrooted tree can be rooted by placing a root r on some edge (u, v). The original edge (u, v) is subdivided into two edges (u, r) and (r, v). If edge (u, v) is weighted, then w(u, r) + w(r, v) = w(u, v).

A special type of an unrooted tree is a semi-rooted tree, where we presume the new root of an unrooted gene tree G is positioned on edge  $(u, v) \in E(G)$  and subtrees are rooted at nodes u and v.

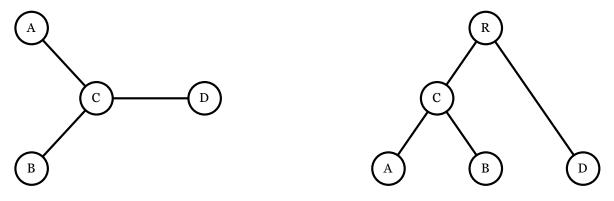


Figure 1.1: Unrooted tree(left) and its rooted version (right) tree. We placed the root R on the edge (C, D) replacing it with two new edges (C, R) and (R, D).

We will be using two types of phylogenetic trees for showing evolutionary relationships: species trees (to describe the evolution of a set of species) and gene trees (to describe the evolution of a particular gene).

A species tree is a phylogenetic tree S where L(S) represent present-day species and internal nodes from V(S) represent speciation events in the history.

A gene tree is a phylogenetic tree G where L(G) represent present-day copies of the gene and internal nodes from V(S) represent duplication and gene loss events in the history.

Phylogenetic trees are reconstructed from a multiple alignments of the DNA sequences of present-day species by various methods [10] to find the most likely phylogenetic tree to given DNA sequences.

### 1.2 Different approaches to gene tree reconciliation

Evolutionary history is a possible sequence of evolutionary events that lead to observed members of a gene family in present-day species (Fig. 1.2). It illustrates how

many duplications and gene losses happened during the evolution of one or more genes inside the evolution of a group of species.

The problem of gene tree and species tree reconciliation was introduced in 1979 by Goodman et al. [11] as a method to infer the evolutionary history of duplications and gene losses in a gene family to decode evolutionary relationships between copies of a gene. The goal of reconciliation consists in mapping nodes of a gene tree into a species tree and thus inducing the evolution of a gene family in terms of speciations, duplications and gene losses. An important prerequisite for reconciliation is to have a gene tree without errors as misplaced leaves can lead to a different history of the gene family.

**Definition 1** A reconciliation between gene tree G and species tree S is mapping  $\phi$ :  $V(G) \rightarrow V(S)$  such that:

- 1.  $\forall u \in L(G) : \phi(u) = \mu(u)$
- 2.  $\forall u, v \in V(G)$  such that  $v <_G u$ :  $\phi(v) <_S \phi(u)$

An example of gene tree reconciliation is shown in Figure 1.2. We are given the gene tree G, the species tree S and a leaf mapping  $\mu: L(G) \to L(S)$  that maps each leaf from G to leaf of its species in S. We will map internal nodes according to the second condition in Definition 1. The node d is mapped to node Y, because it has  $\phi(d)$  and  $\phi(c)$  as descendants. It cannot be mapped to node X since node X does not have  $\phi(c)$  as descendant thus  $\phi(c) <_S \phi(d)$  would not hold. Then node e is mapped above node Y to have  $\phi(a)$  and  $\phi(d)$  as descendants.

The LCA-mapping  $\sigma: V(G) \to V(S)$  maps each node  $u \in V(G)$  as low as possible to the unique node  $\sigma(u) = LCA(\mu(v)|\forall v \in L(G), v <_G u)$  in S. It satisfy both conditions in Definition 1 and minimize the number of duplications and gene losses. This reconciliation can be found in linear time [12].

In this work, we divide approaches to reconciliation into three types: scoring, probabilistic and isometric. Every one of these approaches has its way to compute the gene tree reconciliation. They will be described with presented examples of software that have implemented gene tree reconciliation.

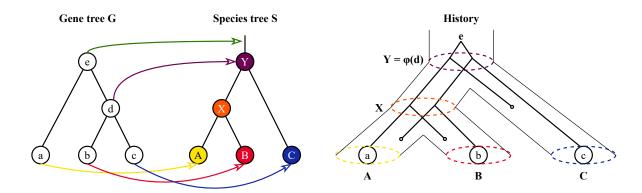


Figure 1.2: Reconciliation and evolutionary history. On the left, the gene tree G is mapped to the species tree S. On the right, we can see the evolutionary history implied by this reconciliation. This history contains one duplication e, two speciations Y and X and three gene losses (empty circles).

#### 1.2.1 Scoring gene tree reconciliation

One of the known approaches to find the best reconciliation is to minimize the duplication-loss score, which signifies the sum of duplications and gene losses during the reconciliation. Various software for scoring gene tree reconciliation are known such as TreeBeST, TreeFix, Treerecs or Notung.

#### TreeBeST

Software TreeBeST [13] takes a rooted species tree and multiple sequence alignment of gene trees for the gene family as input. It uses a method to merge various input gene trees into one gene tree with a model to penalize duplications and gene losses relative to a known species tree. The method first resolves the topology of a gene tree with five methods: neighbour-joining synonymous distance, non-synonymous distance, p-distance and max-likelihood under the WAG and the HKY model. Then the topology is bootstrapped 100 times. The output of the software is one rooted tree.

The TreeBeST reconciliation method was then compared with PhyML+RAP method, where multiple sequence alignment of gene trees are reconciled to one gene tree without the presence of species tree [19]. To evaluate these two methods, authors developed a duplication consistency score represented by intersection of species between left and right branches. Low duplication consistency score means poor topology of the resultant gene tree. PhyML+RAP approach leads to more duplication nodes that TreeBeST and the supplementary duplication nodes made by PhyML+RAP had a low

duplication consistency score. Authors found this result unexpected as TreeBeST uses the species tree and tends to produce duplication when the gene tree has extensive extant members on each side of the duplication.

#### TreeFix

TreeFix [1] takes a rooted species tree, a maximum likelihood gene tree and a multiple sequence alignment of gene trees for the gene family as input. It infers duplications and gene losses using maximum parsimony reconciliation with a duplication-loss cost function, which looks for the reconciliation with the minimum total number of duplications and gene losses. Duplication (D) and gene loss (L) have their costs  $(c_D)$  and  $(c_L)$  that are set to one by default and can be changed by the user. The duplication-loss cost for one reconciliation can be written as:  $(c_D) \cdot (c_L) \cdot (c_L) \cdot (c_L) \cdot (c_L)$ 

The main method [20] uses a hill-climbing search strategy to find an optimal rooted gene tree with the statistically equivalent likelihood to the given maximum likelihood gene tree and with minimum duplication-loss cost as output. Basics of the method are to compute duplication-loss cost and perform neighbour interchange and subtree prune and regraft on the current optimal gene tree. After finding proposals, it chooses the proposal with the lowest duplication-loss cost and with the statistically equivalent likelihood to the given maximum likelihood gene tree. This process is repeated for a given number of iterations.

Authors compared TreeFix with RAxML, SPIMAP, TreeBeST, Notung and tt using simulated and real datasets of two types of species: 12 Drosophila and 16 fungi [21]. The software was judged from the point of view of phylogenetic accuracy in 5 categories (topology, branch, orthologs, duplications, losses) and runtime. TreeFix and SPIMAP show the best accuracy in all 5 categories, Notung has slightly worse accuracy in reconstructing the topology of fungi and precision of inferring duplication and gene losses. tt has problems in the same categories as Notung. The worst accuracy demonstrate RAxML and TreeBeST. While TreeFix and SPIMAP have great phylogenetic accuracy their average running time is longer than others. The best runtime has Notung followed by tt and RAxML.

#### Treerecs

Software Treerecs [14] takes a rooted species tree, one or more rooted or unrooted gene trees and a mapping of gene tree leaves to species tree leaves. It provides recon-

ciling gene tree within the associated species tree minimizing the duplication and gene loss score and rooting the gene tree along the way if needed. The output is, depending on the input, one or more rooted gene trees.

The main aim of the authors was to create a more efficient software. They compared Treerecs with EcceTERA, Notung and Ranger-DTL in 3 categories: root (find the root that minimizes duplication-loss score), correction and root+correction (do both previous categories at the same time). In the first category, Treerecs is better than Ranger-DTL and Notung, which shows a large increase in execution time as the number of leaves increases. Treerecs show the best performance in the correction of trees followed by Notung, while Ranger-DTL has big execution time even with a small increase of leaves. The last category is only supported by Treerecs and EcceTERA, where Treerecs has also better performance.

#### Notung

Notung [8] takes a rooted species tree, a rooted or unrooted gene tree and the leaf mapping as input. If the gene tree is not rooted, it can be rooted by Notung rooting mode that gives each edge a root score (weighted sum of duplications and gene losses). Apart from a reconciliation of binary trees, Notung can reconcile binary gene trees with non-binary species trees and non-binary gene trees with the binary species tree. The non-binary tree is a tree with at least one polytomy (a node with more than two children). Reconciliation of binary gene trees to non-binary species trees results into binary gene tree.

They use an algorithm, that can distinguish between duplication and deep coalescence (divergence, when the time of separation of two lineages precede the time of speciation) and leads to the smaller total number of duplications and losses than duplication-loss cost function used in reconciliation of two binary trees [18]. The duplication-loss cost function is the same as in TreeFix. Reconciliation of non-binary gene tree to binary species tree results into non-binary gene tree. The general approach is to convert the non-binary gene tree to binary gene tree that has minimal duplication-loss score when reconciled with the binary species tree. The resolution is then rearranged back to non-binary gene tree, where all nodes and edges not present in the original gene tree are removed and their assigned duplications and gene losses are reassigned to their polytomy.

#### 1.2.2 Probabilistic gene tree reconciliation

Probabilistic methods have been designed to increase the accuracy of reconciled trees. We introduce two software tools that use probabilistic methods to reconcile gene trees: SPIMAP and Phyldog.

#### **SPIMAP**

SPIMAP software [16] takes a rooted species tree and multiple gene sequences of species from the species tree. Normally, the gene sequences are compared and clustered according to their similarity, which results in a set of homologous gene families. Each gene family has its multiple sequence alignment that is reconstructed into gene trees and they are reconciled with the known species tree. Into this classic pipeline, SPIMAP inserts a parameter estimation model using Bayesian approach creating a new phylogenomic pipeline. It learns duplication, gene loss rates during clustering and gene, species substitution rates during the process of alignment. These parameters are then used while building and reconciling the gene tree with the known species tree. The output is a special reconciliation file format that contains gene node ID, species node ID and evolutionary event that occurred on a given node.

The parameter estimation model [17] infers duplication and gene loss rate using the birth-death process. The birth-death process is a continuous-time process that generates a gene tree according to the constant birth rate (representing duplication) and death rate (representing gene loss). After running it for a time that represents branch length, all branches that exist at the time are "surviving" and others are "extinct". If a node has no surviving descendants, it is called "doomed". Every branch has its length, which can be written as  $\frac{substitutions}{site}$  or a product of a duration of time and a substitution rate. The substitution rates signify the number of substitutions per site per unit of time. The model computes gene-specific rate (measures all rate in a tree) for every gene family and species-specific (specifies rate to given branch in the gene tree) rate for every branch.

To determine if the new phylogenomic pipeline improved accuracy, authors compare SPIMAP with PrIME-GSR, SPIDIR, MrBayes, PHYML, BIONJ, RAxML and SYNERGY. They used the same data as TreeFix: 12 Drosophila and 16 fungi. Firstly, they measured the average runtime. The best runtime, under 1 minute, have RAxML, MrBayes, PhyML and BionJ, which was the fastest method. With the same amount

of iterations, SPIMAP was quicker than SPIDIR or PrIME-GSR, which was the slowest method. Next, they decided to apply the duplication consistency score (used in TreeBeST) to determine method with better accuracy. The smallest number of duplication with low duplication consistency score have SPIMAP and SYNERGY. The moderate performance shows PrIME-GSR and SPIDIR. Remaining four methods have a similar number of duplication with low duplication consistency score. Lastly, they evaluate phylogenetic accuracy depending on 5 categories (used in TreeFix) for 6 abovementioned methods (except RAxML and SYNERGY). SPIMAP has higher accuracy in every category. In the category of inferring the topology, PrIME-GSR has slightly worse accuracy while SPIDIR, MrBayes, PHYML, BIONJ shows bad accuracy in the topology of fungi dataset. The accuracy of reconstructed branches is better than the topology in every method, SPIMAP and PrIME-GSR are first two. SPIDIR, MrBayes, PHYML, BIONJ are a little worse at the sensitivity of detection orthologs in fungi dataset. They have the biggest problem with the precision of inferring the duplications in fungi dataset and losses in both datasets. The same problem has also PrIME-GSR, but only in precision of inferring losses.

#### PhylDog

Another software is PhylDog [2] takes multiple gene alignments, a mapping between gene names and species names, and a list of species names as input. The method infers species tree, gene trees, duplication and gene loss rates by maximizing the probability of alignments overall gene families composed from the likelihood of a phylogeny given an alignment and the likelihood of the reconciliation of a gene tree with a species tree according to duplication and gene loss rates. This method uses the birth-death process and is similar to SPIMAP, but they differ in two aspects. First, while SPIMAP assumes duplication and gene loss rates to be constant for all branches in the species tree, PhylDog chooses to use a particular pair of duplication and gene loss rates to each branch of the species tree. Second, SPIMAP requires time-anchored species tree (branch length shows the amount of time between two nodes) to compute the likelihood of a gene family. Alternately, PhylDog calculates likelihood from the expected numbers of duplications and gene losses. The output is reconciled gene trees.

PhylDog was compared with TreeBeST and PhyML [3] in terms of the number

of duplications and the reconstructed ancestral genome size. PhyML has the biggest number of predicted duplication events, TreeBeST reconciled trees with a much smaller number, but still much higher than PhylDog. The same order of software was also in the number of reconstructed ancestral genome size, where both PhyML and TreeBeST have bigger ancestral genomes that lead to deeper nodes in the species tree.

#### 1.2.3 Isometric gene tree reconciliation

Another variant of reconciliation is isometric gene tree reconciliation, where both species tree S and gene tree G has known branch lengths. These branch lengths are taken into account while mapping a gene tree G to a species tree S. The output of isometric reconciliation is reconciled gene tree with preserved evolutionary distances. The branch lengths of phylogenetic tree express estimated time between evolutionary events. The time can signify the actual geological time, amount of evolutionary changes that happened on the edge or expected number of substitution per site between two nodes.

#### 1.2.3.1 Exact branch length

This problem was introduced and named by Ma et al. [15] in 2008 for the first time. They defined isometric reconciliation of rooted species tree and unrooted gene trees, where all input trees have exact branch lengths. The algorithm executes all input gene trees one by one. First of all, it maps all leaves from the gene tree to leaves in the species tree. Then it takes an unmapped node, which has to be connected with at least 2 already mapped nodes, and call function, that map the unmapped node into the species tree and root the gene tree. The presented algorithm had  $O(N^2)$  running time, where N stands for the total number of nodes in the gene tree and the species tree. However, their definition of isometric reconciliation has some flaws since it does not preserve all evolutionary distances between nodes as it allows them to develop a reconciliation that does not satisfy any history of evolution.

As a result, Brejová et al. [4] later corrected and modified algorithm by Ma et al. to a more efficient algorithm with  $O(N \log N)$  running time. Their modify algorithm firstly maps every leaf from gene tree to the species tree. Next, it maps all unmapped nodes to the species tree. After all nodes are correctly mapped, the algorithm roots

the gene tree and maps the found root to the species tree. Eventually, it verifies if the reconciled tree is correct due to the definition of isometric reconciliation. They also proposed two extensions of the problem. In the first extension, they considered both input trees (gene tree and species tree) to be unrooted and designed an algorithm with  $O(N^5 \log N)$  running time. The second extension presents an algorithm, where both input trees are rooted, but gene tree branch lengths are assumed to be scaled by an unknown scaling factor.

**Definition 2** An isometric reconciliation between gene tree G and species tree S with exact branch lengths w, which are strictly positive, is mapping  $\phi: V(G) \to V(S) \times R$  such that:

- 1.  $\forall u \in L(G) : \phi(u) = [\mu(u), 0]$
- 2.  $\forall u, v \in V(G)$  such that  $v <_G u$ :  $\phi(v) <_S \phi(u)$  and  $w(u, v) = d(\phi(u), \phi(v))$ , where d is the length of path between u and v in reconciled gene tree.

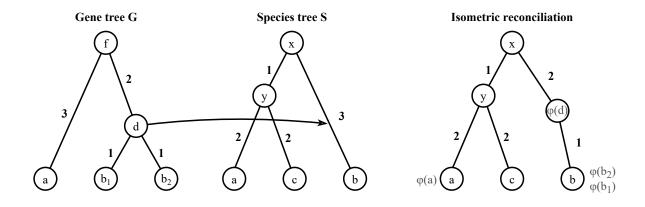


Figure 1.3: Isometric reconciliation. On the left is mapping of the node d of the gene tree G to the edge (x, b) of the species tree S. The result of the isometric reconciliation with mapped node d is on the right.

#### 1.2.3.2 Inexact branch lengths

Input to the above-mentioned algorithms, gene trees and species trees with their branch lengths, are practically estimated from DNA sequences, which were gathered from present-day species [10]. The branch lengths are computed from observed mutations in collected DNA sequences. However, mutations happen randomly in the evolution and DNA sequences are also random samples from studied present-day species. It

means that inferred gene trees and species trees with their branch lengths are estimated with an error.

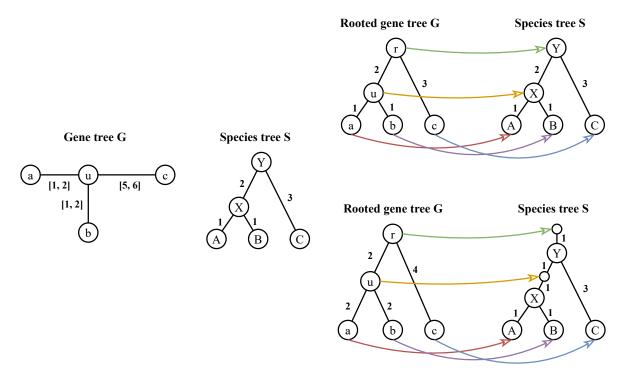


Figure 1.4: Isometric reconciliation with inexact branch lengths. On the left, we can see an unrooted gene tree G with inexact branch lengths and a rooted species tree S. On the right are two possible solutions with rooting the gene tree on the edge (u, c): the first reconciliation is without duplications and gene losses while the second solution maps gene tree to species tree with two duplications (u and r) and four gene losses.

To avoid defectiveness and make isometric reconciliation more precise, the isometric reconciliation with inexact branch lengths was introduced by Chládek in [6] and [5]. They define inexact branch length as an interval, where for every weighted edge stands:  $w(u, v) = \langle w(u, v)_{min}, w(u, v)_{max} \rangle$ . They present three types of algorithm.

#### Linear programming algorithm

The algorithm is based on linear programming and takes a rooted species tree and a rooted gene tree with inexact branch lengths as an input. They introduce a term of mapping depth, which represents a depth of mapped node  $u \in V(G)$  in species tree:  $D(\phi(u))$ . The solution of isometric reconciliation is to find mapping depths to all nodes from gene tree to species tree. They suggest a set of 5 inequalities that can be solved by a linear program.

The first two inequalities assume that the difference of mapping depths of two nodes, where the one is a parent and the other is his child, has to be between the maximal and minimal length of the edge. The second two inequalities are similar and say that the distance between depths of two neighbouring nodes in species tree must be within the maximal and minimal length of the edge. Last inequality restricts mapping depth of node from gene tree to be same smaller than the depth of its LCA-mapping node in the species tree. The algorithm also defines that leaves from gene tree map to leaves from species tree and the root of the species tree is in depth 0, so every node, which maps above the root has negative depths.

For N nodes, the algorithm can get to the result in polynomial time. It also works if the gene tree and species tree are non-binary trees. With a few changes in inequalities, the linear program can find reconciliation to semi-rooted and unrooted species and gene trees.

#### Two-pass algorithm

The two-pass algorithm is faster than the linear programming algorithm. The input for the algorithm is a rooted species tree with exact branch lengths and a rooted gene tree with inexact branch lengths. It consists of two parts: upward and downward sweep.

The upward sweep goes from the leaves of the gene tree to the root and it computes preliminary interval  $\langle x[u]_{min}, x[u]_{max} \rangle$  for each node u. The interval is a set of all potential mapping depths values of node u over all reconciliations of a subtree of the gene tree rooted at node u to the species tree. It does not take into account the rest of the gene tree, only the descendants of node u. The highest mapping point of node u,  $x[u]_{min}$ , is computed by taking the maximum value of both children highest mapping points subtracted by the longest branch length values. Similarly is calculated the lowest mapping point  $x[u]_{max}$ , where both children lowest mapping points are subtracted by the shortest branch length values and the minimum of these values is taken. If  $x[u]_{min} > x[u]_{max}$ , the interval is empty thus for the input is no reconciliation.

To get the final interval  $\langle X[u]_{min}, X[u]_{max} \rangle$  for each node u, the downward sweep goes from the root of the gene tree to its leaves. For all nodes in gene tree (except root), the final interval is computed from their parent final interval, where the minimal mapping depth  $X[u]_{min}$  is the maximum value of the highest mapping point of node u and minimal mapping depth of parent added by the shortest branch length value. The maximum mapping depth  $X[u]_{max}$  is computed as the minimum value of the lowest

mapping point of node u and maximal mapping depth of parent added by the longest branch length value.

Running time of this algorithm is O(N). The same running time is for semi-rooted gene tree. In this situation, it needs to be used linear programming to obtain final intervals of the possible root and its children. The algorithm can be as well applied to an unrooted gene tree, where the running time is  $O(N^2)$ , because it needs to run on every edge as we do not know on which edge the root is located. This algorithm will be used in further work.

#### Parsimonious algorithm

The parsimonious algorithm looks for the most parsimonious solution over all isometric reconciliations by counting the number of duplications and gene losses. The aim is to find the smallest number of duplications and gene losses. In the thesis, [5] are considered 3 different types of parsimonious algorithms for 3 types of gene tree: rooted with exact branch lengths, rooted with inexact branch lengths and semi-rooted or unrooted.

The algorithm designed for reconciliation of a rooted gene tree and species tree with exact branch lengths count duplication and gene losses on subtrees. It has the best running time of  $O(N \log N)$ . If node u from gene tree is not mapped to its LCA-mapping in the species tree, the mapping of node u to the species tree is considered as duplication. The number of gene losses is computed from a path in species tree between mappings of node u and node v, where u is the parent of v. Each node from the species tree, that occurs on this path, is considered as speciation. It creates a copy of gene represented by the edge (u, v) from gene tree, but the gene continuous to only one child, so there is a loss on the other lineage.

Improved algorithm for a rooted gene tree with inexact branch lengths and a rooted species tree with exact branch lengths counts duplication and gene losses on subintervals. It splits the mapping depth interval into non-overlapping subintervals. The goal is to compute the number of duplication and gene losses for all possible subintervals, which is done by counting function from the previous algorithm. The time complexity of the algorithm is  $O(N^3 \log N)$ .

The most parsimonious algorithm assumes semi-rooted or unrooted gene tree with inexact branch lengths and a rooted species tree with exact branch lengths. In both cases of the gene tree, the exact location of the root is unknown. The algorithm firstly runs the previous algorithm on nodes of edge, where the possible root can be located. Then, it uses linear programming to find the location of the root based on computed numbers of duplications and gene losses in subintervals of the possible edge nodes. The running time of this algorithm is  $O(N^4 \log N)$ .

## 2 Algorithms

In this chapter, we will show two new algorithms which combined with the two-pass algorithm described in Chapter 1.2.3.2 [5] can be used to obtain the most parsimonious isometric gene tree reconciliation. This approach is then implemented in our software.

The required input for our overall approach is a rooted species tree with exact branch lengths and an unrooted gene tree with inexact branch lengths. The input is processed by the following algorithms. Using our first algorithm, we select a set of possible roots of the gene tree and root the gene tree, which results in multiple rooted gene trees. Afterwards, for each rooted gene tree, we perform the two-pass algorithm to find a reconciliation (Chapter 1.2.3.2) and use our second algorithm to count the number of duplications and gene losses in the found reconciliation. Finally, we select the most parsimonious reconciliation among those considered. Although the reconciliation may not be optimal, as we do not try all possible roots and our selected set of considered roots may not contain the optimal one. We allow only evolutionary events as duplication, gene loss and speciation can happen in evolutionary history.

## 2.1 Rooting the gene tree

An unrooted gene tree has an infinite number of possible root locations. We present an algorithm to select a finite set of possible roots that are spaced by a given step on every edge e of an unrooted gene tree G. However, our set of possible roots may not always contain the optimal solution.

For each edge  $e \in E(G)$ , we transform the unrooted gene tree into a semi-rooted gene tree by rooting the subtrees at vertices  $u \in V(G)$  and  $v \in V(G)$  of the edge e = (u, v). The edge is subsequently used as the parameter for the Algorithm 1 to select a set of roots on edge e, each root given by a pair of intervals. Let r be the root

of a semi-rooted gene tree G then the first interval of the pair represents the length of edge (u, r) and the second interval represents the length of edge (r, v).

#### **Algorithm 1** Possible intervals to subdivide given edge e

```
1: function GETINTERVALS(e \in E(G), step \in R)
        intervals.add([\epsilon, \epsilon], [w(e)_{min} - \epsilon, w(e)_{max} - \epsilon])
 2:
 3:
        intervals.add([w(e)_{min} - \epsilon, w(e)_{max} - \epsilon], [\epsilon, \epsilon])
         difference = w(e)_{min} - w(e)_{max}
 4:
         if step > difference / 2 then
 5:
             intervalSize = difference / 2
 6:
         else
 7:
 8:
             intervalSize = step
 9:
         w(u,r)_{min} = w(e)_{min}
         w(u,r)_{max} = w(e)_{max} - intervalSize
10:
         w(r,v)_{min} = \epsilon
11:
         w(r, v)_{max} = intervalSize
12:
        if step > 0 then
13:
             while w(r, v)_{max} < w(e)_{max} and w(u, r)_{max} > 0 do
14:
                 intervals.add([w(u,r)_{min},w(u,r)_{max}],[w(r,v)_{min},w(r,v)_{max}])
15:
16:
                 w(u,r)_{min} -= step
                 if w(u,r)_{min} \leq 0 then
17:
                     w(u,r)_{min} = \epsilon
18:
                 w(u,r)_{max} -=step
19:
20:
                 w(r,v)_{min} += step
21:
                 w(r,v)_{max} += step
         return intervals
```

At the beginning of Algorithm 1, we define essential variables. The set of possible pairs of intervals for subdividing the edge e are stored at the variable *intervals* that is also the return value of the function.

To cover most of the possibilities, we allow rooting the gene tree right above the vertices u and v of the edge e with  $\epsilon$  distance from the vertices. The  $\epsilon$  is by default set to  $1 \times 10^{-6}$  and signifies the edge length close to the 0. We do not allow 0 edge length or interval starting with 0 as  $[0, \epsilon]$  to avoid mapping the root into vertex u or v.

We get two possible roots after subdividing the edge e right above the vertices u and v. The first possible root subdivides edge e into two edges with interval lengths  $w(u,r) = [\epsilon, \epsilon]$  on the left from the root and  $w(r,v) = [w(e)_{min} - \epsilon, w(e)_{max} - \epsilon]$  on the right from the root, where  $w(e)_{min}$  is original minimal length of the edge e and  $w(e)_{max}$  is original maximal length of the edge e. The second option of the root subdivide the edge e with intervals of the same length, that are flipped, so the original interval  $w(u,r) = [w(e)_{min} - \epsilon, w(e)_{max} - \epsilon]$  is on the left from the root and  $w(r,v) = [\epsilon, \epsilon]$  in

on the right from the root.

After creating the first two options for the possible root, we prepare variables for the while loop. We added condition for special cases, where the difference between the maximal and minimal original length of edge e divided by 2 is less than the size of the step. With the special case condition, we can infer intervals with a better range or intervals that would be normally skipped (Fig. 2.1). We run a while loop to get possible roots inside the edge e. In each iteration, we subtract the step from the minimal and maximal length of the left interval of the subdivided edge e and add the step to the minimal and maximal length of the right interval of the subdivided edge e. The size of the step is set to 0.01 by default. The while loop goes until the maximal length of the right interval is the same or bigger as the original maximal length of the edge e or the maximal length of the left interval reaches 0 or less.

Rooting the gene tree goes over all edges (u, v) in the unrooted gene tree G. Firstly, we semi-root the gene tree at vertices u and v. Rooting each subtree takes O(MlogM) time, where M is the number of gene nodes in a subtree. When we semi-root on an edge from a leaf, the number of nodes in subtrees are 1 and N, where N is the number of nodes in the gene tree subtracted by 1, thus the number of edges in the unrooted tree G. Then, we run the function getIntervals in Algorithm 1. It has a running time O(p), where p stands for number of iterations in while loop, which can be expressed as  $p = \lceil w(e)_{max}/step \rceil - 1$ . The result of function getIntervals is a set of p+2 pairs of intervals for subdividing the edge e. Subsequently, the intervals are used in a loop to root the semi-rooted gene tree G resulting in a set of rooted gene trees with inexact branch lengths. Rooting the semi-rooted gene tree takes O(1) time. The running time of rooting one edge of an unrooted gene tree G is O(NlogN + p) = O(h). Therefore, the total running time of rooting the unrooted gene tree G is O(Nh).

## 2.2 Counting algorithm

A similar counting algorithm was proposed by Chládek [5]. In the algorithm, they introduce a bearing node for each node of the gene tree. A bearing node is a node from a species tree that is the closest descendant of mapping of a node from a gene tree. Each bearing node has a height, which is a number of species nodes on the longest

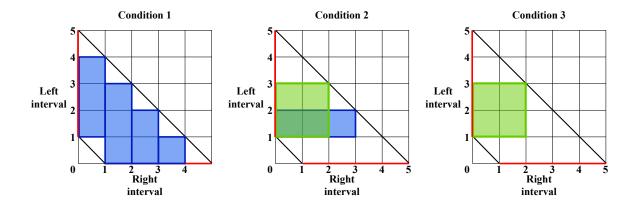


Figure 2.1: The X-axis on the graph stands for the possible length of interval on the right from the root and the y-axis signify the possible length of interval on the left from the root. Space between black lines represents all possible intervals after subdividing the edge e with the root. Red lines are for the root right above the vertices u and v, where one interval takes the original size and the second interval is  $[\epsilon, \epsilon]$ . Blue rectangles means intervals for the root inside the edge e without the special case condition. Green squares are inferred intervals for the root with special case condition.

Condition 1: step < difference/2 (the left figure)

Parameters: w(e) = [1, 5] and step = 1.

As the size of the step is less than the difference between the original minimal and maximal length divided by 2, we do not use the special case condition and create only red lines and blue rectangles intervals. We get a set of 6 pairs of intervals, where two pairs are for the root above the vertices u and v and the remaining four pairs are for the root inside the edge, such as: w(u,r) = [1,4] and w(r,v) = [0,1], w(u,r) = [0,3] and w(r,v) = [1,2], w(u,r) = [0,2] and w(r,v) = [2,3], w(u,r) = [0,1] and w(r,v) = [3,4], where w(u,r) is on the left from the root and w(r,v) is on the right from the root.

Condition 2: step > difference/2 (the middle figure)

Parameters: w(e) = [1, 5] and step = 3.

In this case, the size of the step is bigger than the difference between the original minimal and maximal length divided by 2. Without the special case condition, we would only get the blue rectangle intervals w(u,r) = [1,2] on the left from the root and  $w(r,v) = [\epsilon,3]$  on the right from the root. The special case condition changes the blue rectangle into the green square which gives us intervals w(u,r) = [1,3] on the left from the root and  $w(r,v) = [\epsilon,2]$  on the right from the root with better coverage of the space.

Condition 3: step > difference (the right figure)

Parameters: w(e) = [1, 5] and step = 5.

The size of the step is bigger than the difference between the original minimal and maximal length. Without the special case condition, we would not get any possible intervals for subdividing the edge e. However, the special case condition infer green intervals w(u,r) = [1,3] on the left from the root and  $w(r,v) = [\epsilon,2]$  on the right from the root.

path between the bearing node and a leaf of the species tree. They count duplications and gene losses in subtrees, where duplication of node u is when its mapping depth is smaller than the depth of  $\sigma(u)$  and gene loss is the difference between bearing nodes heights of node u and its children.

We present an algorithm for counting the number of duplications and gene losses in a rooted gene tree G with inexact branch lengths depending on a rooted species tree S with exact branch lengths. In comparison with the previous similar algorithm, we introduce new variables for nodes in species tree and gene tree. Each species node  $a \in V(S)$  has its level l(a) signifying the number of species nodes on the path from a to the root(S). For each node  $u \in V(G)$ , we denote its reconciliation mapping to the species tree as  $\phi(u)$ . Each gene node  $u \in V(G)$  has its speciesNodeBelow(u), l(u), level Distance From Parent(u) and mapped ToLca(u). The species Node Below(u)(denoted as the bearing node by Chládek [5]) is defined as the closest species node below  $\phi(u)$ . The level l(u) is defined as the level of closest species node below  $\phi(u)$  such as l(speciesNodeBelow(u)). The levelDistanceFromParent(u) signifies the difference between levels of node l(u) and its parent. The mappedToLca(u) is a boolean variable representing if the node u is mapped to its  $\sigma(u)$ . It is true when  $D(\phi(u)) - D(\sigma(u)) < \epsilon$ , where  $\epsilon$  is the rounding error. We count the duplications from leaves to the root of the gene tree. The duplication occur when mappedToLca(u) is false. The gene losses are calculated for each edge (u, v) as difference between levels of node u and v stored in levelDistanceFromParent(u).

The counting algorithm consists of two parts: preprocessing and the main algorithm. In the preprocessing, we compute essential variables for the gene tree G that are subsequently used in the main algorithm.

The prerequisites for the counting algorithm are calculated depth D(a) and level l(a) for each  $a \in V(S)$ . For the gene tree G, we assume an interval of possible mapping depths  $X[u] = [X[u]_{min}, X[u]_{max}]$  for each  $u \in V(G)$  that can be computed with the two-pass algorithm (Chapter 1.2.3.2) and LCA-mapping  $\sigma(u)$  for each  $u \in V(G)$ . In our algorithm, we use only the  $X[u]_{max}$  as the  $D(\phi(u))$  since we want to mapped each node of the gene tree as lowest as possible to minimize the number of duplications and gene losses.

#### 2.2.1 Preprocessing

In the preprocessing, we calculate necessary variables for nodes in the gene tree G that are used in the main algorithm. For each  $u \in V(G)$ , we compute l(u), speciesNodeBelow(u), levelDistanceFromParent(u) and mappedToLca(u). The level l(u) variable of gene node u signifies the number of species nodes on the path from the mapping of node  $\phi(u)$  to the root of the species tree S. It is calculated from the speciesNodeBelow(u) variable that represents node  $s \in V(S)$ , which is right below the mapping of gene node  $\phi(u)$ , so the mapping of gene node  $\phi(u)$  lies on the edge from node s to parent(s). The levelDistanceFromParent(u) means the number of species nodes between the mapping of gene node  $\phi(u)$  and the mapping of its parent  $\phi(parent(u))$ . It is not calculated for the root of the gene tree G as it has no parent. The variable mappedToLca(u) represents the truth value of the statement:  $X[u]_{max} - D(\sigma(u)) < \epsilon$ , that is, whether the node u is mapped to  $\sigma(u)$  or not.

We use three algorithms for calculating the variables: Algorithm 2 for calculating the speciesNodeBelow(u), Algorithm 3 that sets level distance from parent  $u \in V(G)$  to its children and Algorithm 4, which uses both previous algorithms and computes the level of gene node l(u) and mappedToLca(u).

```
Algorithm 2 Computes species node below given gene node u
1: function COMPUTESPECIESNODEBELOW(u \in V(G), s \in V(S))
 2:
       speciesNodeBelow = s
 3:
       while D(s) > X[u]_{max} do
          speciesNodeBelow = s
 4:
          if parent(s) = null then
 5:
             break
 6:
          else
 7:
             s = parent(s)
 8:
       return speciesNodéBelow
```

The computeSpeciesNodeBelow function in Algorithm 2 takes gene node u and species node s as argument. For the species node s holds that  $D(s) < D(\phi(u))$  and  $\phi(u)$  is on the path between s and the root of the species tree s. The function saves the given species node s to the variable speciesNodeBelow. The variable always remembers the last species node below the given gene node s and serves as a return value. The while loop iterates over species nodes on the path from given species node s towards the root of the species tree. If s is true, it means the species node s is

below the gene node u. Every iteration, we save the species node to the return value speciesNodeBelow and move on the path closer to the root by assigning parent(s) to the s variable. If the species node s does not have a parent, the gene node s is above the root of the species tree. The while loop ends when the while condition does not hold, so the new species node s is above gene node s or if the gene node s is above the root.

#### **Algorithm 3** Sets level distance from parent to children of node u

- 1: function LEVELDISTANCEFROMCHILDREN $(u \in V(G))$
- 2: **for**  $v \in children(u)$  **do**
- 3: levelDistanceFromParent(v) = l(v) l(u) mappedToLca(u)

In the levelDistanceFromChildren function shown in Algorithm 3, we compute the levelDistanceFromParent(v) for each child v of the given node u. The level distance is calculated as the difference between the level of child v and the level of its parent, node u. The distance is decreased by 1 if the node u is mapped to the same depth as its  $\sigma(u)$ .

The computeLevel function in Algorithm 4 goes over all nodes in gene tree G in the direction from the leaves to the root. The leaves of gene tree  $t \in L(G)$  are always mapped to its  $\sigma(t)$  and their variables are set according to it. For each inner node  $u \in V(G) \setminus L(G)$ , we recognize whether the node u has the same maximal mapping depth  $X[u]_{max}$  as  $\sigma(u)$  or the difference between  $X[u]_{max}$  and  $\sigma(u)$  is smaller than  $\epsilon$ , which allows us to determine if the node u is mapped to its  $\sigma(u)$  even when the depths are not same because of the rounding error. By default, the  $\epsilon$  is set to  $1 \times 10^{-6}$ .

In case that node u has not the same depth as  $\sigma(u)$  and also their depthDifference is bigger than  $\epsilon$ , we set mappedToLca(u) to false. From the children of node u, we save the closest species node to the gene node u into variable node and run function computeSpeciesNodeBelow in Algorithm 2 to get speciesNodeBelow(u).

Otherwise, when the node u has the same depth as  $\sigma(u)$  or the depthDifference is smaller or equal to the  $\epsilon$ , we consider three cases can happen, where the first two cases check if both or at least one child is already mapped to  $\sigma(u)$ , because exactly one node from the gene tree can be mapped to exactly one node from species tree to be considerate as speciation. In the first case, we consider that both  $v \in children(u)$  have the same speciesNodeBelow(v) as  $\sigma(u)$ . It means that both children of node u

#### **Algorithm 4** Compute levels for nodes from gene tree G

```
1: function COMPUTELEVEL(u \in V(G))
 2:
       if u \in L(G) then
           mappedToLca(u) = true
 3:
           speciesNodeBelow(u) = \sigma(u)
 4:
           l(\mathbf{u}) = l(\sigma(u))
 5:
        else
 6:
           for v \in children(u) do
 7:
               computeLevel(v)
 8:
           \operatorname{depthDifference} = D(\sigma(u)) - X[u]_{max}
 9:
           if depthDifference > \epsilon then
10:
               mappedToLca(u) = false
11:
12:
               node = arg \min_{v \in children(u)} (D(speciesNodeBelow(v)))
               speciesNodeBelow(u) = computeSpeciesNodeBelow(u, node))
13:
           else
14:
               if \forall v \in children(u) : speciesNodeBelow(v) = \sigma(u) then
15:
                   if \forall v \in children(u) : mappedToLca(v) \land v \notin L(G) then
16:
17:
                       v = \arg\min_{v \in children(u)} (X[v]_{max})
                       levelDistanceFromChildren(v)
18:
                   mappedToLca(u) = false
19:
               else if \exists v \in children(u) : speciesNodeBelow(v) = \sigma(u) then
20:
                   mappedToLca(u) = false
21:
22:
               else
                   mappedToLca(u) = true
23:
               speciesNodeBelow(u) = \sigma(u)
24:
           l(u) = l(speciesNodeBelow(u))
25:
           levelDistanceFromChildren(u)
26:
```

can be mapped to the same species node, so we check if their mappedToLca(v) is set to true. We skip the case, where children(u) are leaves as they are allowed to map to the same species node. If the condition holds such that children(u) are mapped to the same species node and they are not leaves, we take the child v that is closer to the node u and set its mappedToLca(v) to false that also affects the distance from children(v), thus we call the levelDistanceFromChildren(v) to reset the distance. As the other child is already mapped to the species node, we set mappedToLca(u) to false.

The second case checks if at least one  $v \in children(u)$  is mapped to  $\sigma(u)$ . If the condition holds, we can not map another gene node to the species node, so we set mappedToLca(u) to false.

In the third case, any  $v \in children(u)$  has the same speciesNodeBelow(v) as the  $\sigma(u)$ , thus we set the mappedToLca to true.

Lastly, we set the speciesNodeBelow(u) to the  $\sigma(u)$  and level of node u to the level of computed speciesNodeBelow(u). Then, we run function levelDistanceFromChildre in Algorithm 3.

The computeLevel function goes over all nodes in the rooted gene tree G. If the gene tree G is balanced, the function computeSpeciesNodeBelow has running time O(logN), where N is number of nodes in gene tree G. The levelDistanceFromChildren function is computed in constant time. So the total preprocessing running time is O(NlogN) for balanced gene tree G. However, if the gene tree G is not balanced, the preprocessing running time is  $O(N^2)$ .

### 2.2.2 Main algorithm

The prerequisites for the countDL function shown in Algorithm 5 are computed in preprocessing. Besides, we need to have set the countLossesAboveRoot variable. If it is true, we count losses above root that occurred as a result of the gene tree G not containing genes of all species from the species tree S.

We count the evolutionary events in the direction from leaves to the root of gene tree G. For each node  $u \in V(G)$  and its parent  $v \in V(G)$ , we consider evolutionary events that occur in the node u and on the edge (u, v). We do not compute evolutionary event in the parent, they are determined directly in the parent. In the root, we only calculate the evolutionary events that happened in the node as the root has no parent

**Algorithm 5** Counts duplications and gene losses in gene tree G

```
1: function COUNTDL(u \in V(G))
     if u \neq L(G) then
2:
         v, w = children(u)
3:
         DL_u = DL_v + DL_w
4:
     loss = levelDistanceFromParent(u)
5:
6:
     if parent(u) = null and parent(\sigma(u)) \neq null and countLossesAboveRoot
  then
         loss += l(u);
7:
     if not mappedToLca(u) then
8:
         duplication = 1
9:
       return DL_u +(duplication, loss)
```

thus no edge to consider.

The number of duplications and gene losses are depicted as pair DL = (duplication, loss) introduced by Chládek [5]. The sum of the pairs  $DL_1$  and  $DL_2$  is computed as  $DL_1 + DL_2 = (duplication_1 + duplication_2, loss_1 + loss_2)$ . For each node  $u \in V(G)$ , we calculate the  $DL_u$ , which corresponds to the number of duplications and gene losses inferred in the subtree of node u. Thereafter, we infer the duplication and gene losses in the node u and on the edge above the node u.

The number of gene losses on the edge (u, v) is calculated as the number of species nodes on the path from node u to node v, which is precomputed in variable levelDistanceFromParent(u). If  $\sigma(root(G)) \neq root(S)$ , thus the  $\sigma(root(G))$  is below root(S) means that some species do not have their gene in the gene tree. Therefore, the gene loss occurred before the root(G), which resolves in extra gene loss that can be added if the variable countLossesAboveRoot is true. The truth value of countLossesAboveRoot is set by the user.

Duplication and speciation are easy to determine since it depends on whether the node u is mapped to  $\sigma(u)$  or above, which we already precomputed in mappedToLca(u).

The function return pair DL corresponds to the number of duplication and gene losses in the subtree of node u, in the node u and on the edge above node u.

Gene losses and duplications are computed in constant time for one gene node. The countDL function goes over all nodes in gene tree G thus the running time is O(N), where N is the number of all nodes in the gene tree G.

## 3 Implementation

The implementation of our software is built on Chládek's source code from his diploma thesis [5]. We apply his implementation of basic classes for defining the phylogenetic tree, parsing an unrooted gene tree and a rooted species tree from a file with several changes. We also use his implementation of the two-pass algorithm, which we mentioned before in Chapter 1.2.3.2, to compute the gene tree possible mapping depths.

On this basis, we implement our algorithms described in Chapter 2 to find the most parsimonious reconciliation.

Our software is implemented in the programming language Java and has a command-line interface.

### 3.1 Classes and variables

The implemented software consists of 15 classes that we briefly introduce:

- Class Node represents a node in a phylogenetic tree
- Class Edge represents an edge in a phylogenetic tree
- Class Interval represents a length of edge as interval
- Class DL represents a score of reconciliation
- Class UnrootedNode represents a node in an unrooted gene tree
- Class UnrootedTree represents an unrooted gene tree
- Class RootedExactNode represents a node in a rooted species tree with exact branch lengths

- Class RootedExactTree represents a rooted species tree with exact branch lengths
- Class RootedIntervalNode represents a node in a rooted gene tree with inexact branch lengths
- Class RootedIntervalTree represents a rooted gene tree with inexact branch lengths
- Class Parser parses phylogenetic trees and their leaf-mapping from files
- Class Loader load arguments from a command line and calls Parser on files with stored phylogenetic trees
- Class Printer prints reconciliation solutions into files
- Class Reconciliator computes reconciliation with its score
- Class Main the main class of the software that calls other classes to load files, compute and print reconciliation

# 3.2 Differences from the original source code

As our source code is built on Chládek's source code, we show the differences in relations and entities between source codes in Fig. 3.2. The differences, new variables and classes are described below by classes in more details.

#### Class Interval

We change the name of parameters to minLength and maxLength and delete the unnecessary variable OriginalMappingDepth as we use the Interval to store the minimal and maximal length of new possible edges that can be created after subdividing the original root edge in function getIntervals (Algorithm 1) in Reconciliator class. The parameters are numbers of type double.

## Class RootedExactNode

In the *RootedExactNode* class, we define a new *level* variable. It is a number of type integer. The variable is set while parsing the species tree in the *Parser* class and used

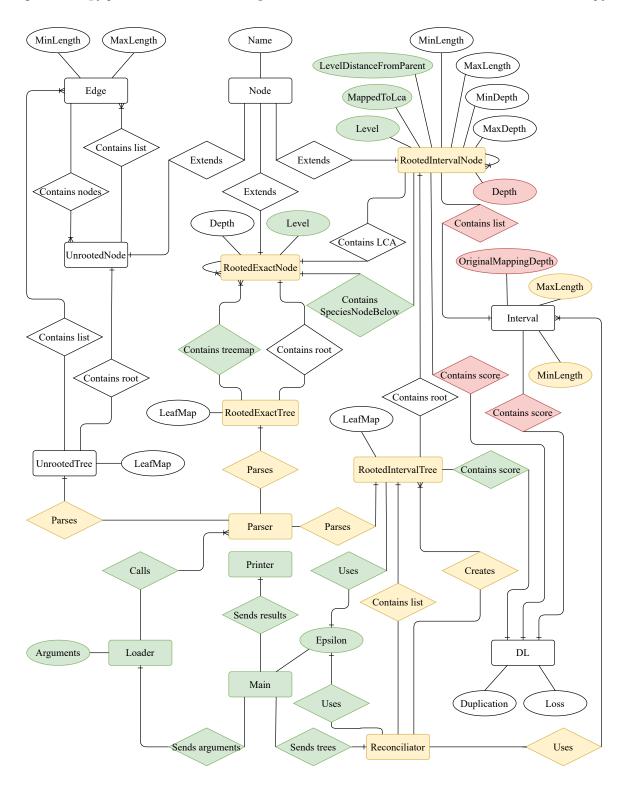


Figure 3.1: Red entities and relations represent deleted variables or functions. Yellow entities and relations show changes to the original source code. Green entities and relations depict added classes, variables or functions.

for computing the level of gene nodes as shown in function *computeLevel* (Algorithm 4) in *Reconciliator* class.

#### Class RootedExactTree

We add structure *TreeMap* containing leaves, where the key is the name of the leaf and the value is an object representation of that leaf as *RootedExactNode*. It is used to set the LCA-mapping variable of leaves in a gene tree according to the leaf-mapping.

#### Class RootedIntervalNode

The unnecessary depth variable was deleted as we store the mapping depth of a RootedIntervalNode in variables minDepth and maxDepth. We also delete the DL, because we do not store the reconciliation score in nodes and the list of Interval since we have the mapping depth interval and the interval of the edge above stored in separated variables. Besides, we add new variables: level, mappedToLca, levelDistanceFromParent and speciesNodeBelow that are computed and used in algorithms in Chapter 2.2. The level and levelDistanceFromParent are numbers of type integer. The mappedToLca is data type boolean speciesNodeBelow is object of type RootedExactNode.

## Class RootedIntervalTree

In the RootedIntervalTree, we implement our algorithms from Chapter 2.2 and their are called from the Reconciliator class. We add the variable of type DL to store the number of duplication and gene losses inferred in the gene tree.

## Class Parser

We change the parsing method for a species tree and an unrooted gene tree. In the species tree parsing method, we infer level in species tree nodes. In the unrooted gene tree parsing method, we resolve inexact branch lengths if the given gene tree has inexact branches or we transform exact branch lengths to inexact branch lengths if the given gene tree has exact branch lengths. To modify the exact branch lengths into inexact branch lengths, the user needs to set the tolerance value that has to be from interval [0,1]. The interval of the edge e is compute as:  $w(e) = [length - (tolerance \cdot length), length + (tolerance \cdot length)]$ . However, if the  $w(e)_{min} < 2*\epsilon$  or  $w(e)_{max} < 2*\epsilon$ , we set them to  $2*\epsilon$  to avoid problems with zero or negative length branches in Algorithm 1.

Furthermore, we add a parsing method for a rooted gene tree that can either resolve inexact branch lengths or transform exact branch lengths to inexact branch lengths. We included a method to parse mapping of gene leaves to species leaves from a file and a method for transforming a rooted gene tree to an unrooted gene tree. This allows us to forget the original root of a gene tree and find a new one with function getIntervals (Algorithm 1). All methods in the class are called from the Loader class.

## Class Loader

The *Loader* class is initialized with arguments from the command line. It loads the arguments and calls functions from *Parser* according to the requirements specified in the arguments. We recognize 11 arguments that are listed in Table 3.1.

Table 3.1: Input arguments

Argument	Description				
-help	shows help information with all possible input argumen				
-S <species tree=""></species>	path to the rooted species tree file in Newick tree format				
-5 <species tree=""></species>	(mandatory input)				
C < cono troo	path to the rooted or unrooted gene tree in Newick tree				
-G <gene tree=""></gene>	format (mandatory input)				
-M <species map=""> mapping of genes to species</species>					
-t <tolerance></tolerance>	required tolerance from interval [0,1] (By default, it is				
-t <tolerance></tolerance>	set to 0.5)				
-s <step></step>	required step from $[0, \infty]$ (By default, it is set to 0.01)				
r.	signifies that the given gene tree is rooted (By default,				
-r	the given gene tree is considered to be unrooted)				
roroot	signifies that the given rooted gene tree is wished to be				
-reroot	rerooted				
-1	signifies counting the gene losses above the root of given				
<b>-</b> 1	gene tree				
-p <pri>type&gt;</pri>	required print type from two options "sol" and "rel" (By				
	default, the print type is set to be "sol"				
angilan <angilan></angilan>	required epsilon as number of type double (By default,				
-epsilon <epsilon></epsilon>	it is set to $1 \times 10^{-6}$				

The main method is loadArgs which is called from the Main class and returns an array of Object: a rooted species tree, a rooted gene tree or an unrooted gene tree, step and countLossesAboveRoot needed for algorithms from Chapter 2.2 implemented in Reconciliator class along with dirPathGene and printType required in Printer class functions.

#### Class Reconciliator

The algorithms from Chapter 2 and the two-pass algorithm by Chládek from Chapter 1.2.3.2 are called in the *Reconciliator* class. These are the main methods to obtain the most parsimonious reconciliation.

The *Reconciliator* class is initialized with a rooted species tree, a rooted gene tree or an unrooted gene tree, *step* and *countLossesAboveRoot* that are inferred in *Loader* 

class. It uses Interval to store the minimal and maximal length of new edges in function getIntervals (Algorithm 1), which are used for subdividing the root edge and creating the RootedIntervalTree. The class returns a list of RootedIntervalTree with most parsimonious reconciliation that has its reconciliation score store in DL.

#### Class Printer

The class is initialized with list of RootedIntervalTree, dirPathGene and printType. We recognise two types of printing the results of the reconciliation into the file: "rel" and "sol".

With the "rel" type, the function prints relations between genes in the gene tree for each inferred RootedIntervalTree. If solutions contain more trees with the same topology and reconciliation score, it prints the number of the same tree after each gene relation printout. For each  $u \in L(G)$ , it prints "gene" and name of the node u. For each  $v \in V(G) \setminus L(G)$ , it allows evolutionary events as speciation, duplication and gene loss depending on what occurred in the node v or on the branch from the node v to its parent parent(v). The speciation and duplication are inferred in the node v. They print as "spec" for speciation and "dup" for duplication with names of children(v) separated by a tab. The gene loss happens on the branches. It prints as "loss" with the name of node v. The name of each node consists of genes found in the subtree of that node separated by commas.

The "sol" type prints gene trees in Newick format. For each edge (u, v), we compute branch length as difference between  $D(\phi(u))$  and  $D(\phi(v))$ . All computed solutions are printed into one .tree file, where solutions are separated with an empty line.

The file with results is saved in the same directory as the given gene tree.

## Class Main

The Main class receives arguments given by user and send it to the Loader class for processing. Sequentially, sends a rooted species tree, a rooted gene tree or an unrooted gene tree, step and countLossesAboveRoot to the Reconciliator class to infer the most parsimonious reconciliation, which returns list of RootedIntervalTree. Eventually, it sends the list of RootedIntervalTree, printType and dirPathGene to the Printer to print the results. Also, it stores the value of  $\epsilon$  that are required in functions getIntervals (Algorithm 1) in Reconciliator class and computeLevel (Algorithm 4) in RootedIntervalTree class.

# 4 Experiments and results

We evaluate our software for isometric reconciliation on a simulated and real dataset that were used to evaluate SPIMAP [17] and TreeFix [20] in previous studies. The simulated dataset consists of 1000 simulated gene families of two clades of species: 12 Drosophila genomes and 16 fungal genomes, generated with the SPIMAP model. The real dataset includes 5351 real gene families from 16 fungal genomes.

To compare the results, we run other software for computing the gene tree reconciliation: Notung [8], TreeFix [20] and Treerecs [7], on the same dataset.

# 4.1 Simulated dataset

In the simulated dataset, we know the correct gene tree with its evolutionary events, which allows us to test several aspects. We evaluate our software for isometric reconciliation for two cases: without rerooting the gene tree and with rerooting the gene tree. In the experiments, we measure the precision of inferred duplications and gene losses, the average runtime for computing the results for each gene tree and the number of gene trees without solution, as our isometric reconciliation software takes branch lengths into account and occasionally the gene tree can not fit the species tree correctly, because some small errors in branch lengths. In the second case with rerooting the gene tree, we also measure the precision of the correctly inferred root.

# 4.1.1 Without rerooting the gene tree

We take the rooted gene tree as it is from the dataset and run a reconciliation with countDL function (Algorithm 5 in Chapter 2.2.2). We evaluate it several times with different tolerance setting to scale up the edges. The tolerance setting are  $0.0, 1 \times 10^{-6}, 1 \times 10^{-5}, 1 \times 10^{-3}, 0.1, 0.3, 0.5, 1.0$  and the  $\epsilon = 1 \times 10^{-6}$ . We compare our

results with only Notung and Treerecs, as the TreeFix software automatically reroot the given gene tree.

#### Flies dataset

On the flies dataset (Tab. 4.1), our software has a problem to infer reconciliation for all gene trees with tolerance set to 0.0, thus 3.97% of the gene trees are without reconciliation. Still, the reconciled trees have perfect precision and sensitivity of inferred duplication and gene losses. With the tolerance set to  $1 \times 10^{-6}$ , we computed isometric reconciliation for all gene trees, but some nodes are incorrectly detected as duplications or gene losses, so the inferred duplications have precision 99.93\% with the sensitivity of 100% and gene losses has precision 99.76% with the sensitivity of 99.98%. It is caused by a rounding error on the last decimal place since the edge length of the gene trees in the dataset has 6 decimal places. Higher tolerance settings show the same results, where our isometric reconciliation software infer reconciliation for all gene trees from the dataset with 100% precision and sensitivity of duplication and gene losses. The Noting and Treerecs computed reconciliation for all gene trees with perfect precision and sensitivity of inferred duplication and gene losses. However, the average running time for each gene tree is best in our reconciliation software, which is about 0.003617 for each tree in each tolerance setting. In comparison, the Treerecs average time is bigger by 90.23% from our average running time. The Notung has the longest average time, which is bigger by 94.49% from the Treerecs average running time and by 99.46% from our average running time.

## Fungi dataset

The results for the fungi dataset (Tab. 4.2) are similar to the results for the flies dataset. Our isometric reconciliation software has also a problem inferring reconciliation for all gene trees with a tolerance setting of 0.0, ergo the 9.03% of gene trees has no reconciliation solution. For the remaining 90.97% of gene trees, our software finds the correct reconciliation with 100% precision and sensitivity of inferred duplications and gene losses. Our software recognizes isometric reconciliation for all gene trees from the dataset with tolerance set to  $1 \times 10^{-6}$ , but the precision of duplications and gene losses decrease to 99.99% and 99.98%, respectively, because of the rounding error on the last decimal place since the edge lengths of gene trees from the fungi dataset has also 6 decimal places. However, the sensitivity of inferred duplications and gene losses stays

Duplication Gene loss  $W/o sol^b$ Software<sup>a</sup> Runtimeg  $\overline{\mathrm{Prec^c}}$  $Sens^d$  $\overline{\mathrm{Prec^e}}$  $\overline{\mathrm{Sens}^{\mathrm{f}}}$ Our (t - 0.0)3.97 100 100 100 100 0.007415Our (t -  $1 \times 10^{-6}$ ) 0 99.93 100 99.76 99.98 0.008160Our (t -  $1 \times 10^{-5}$ ) 0 100 100 100 100 0.003050Our (t -  $1 \times 10^{-3}$ ) 0 100 100 100 100 0.003026Our (t - 0.1)0 100 100 100 100 0.001785Our (t - 0.3) 0 100 100 100 100 0.001771Our (t - 0.5)0 100 100 100 100 0.0019190 Our (t - 1.0) 100 100 100 100 0.001810Notung 0 100 100 100 100 0.6715990 100 100 0.037014Treerecs 100 100

Table 4.1: Flies: results of phylogenetic software on simulated dataset without rerooting the gene tree

- <sup>a</sup> Phylogenetic software with "t" as tolerance setting.
- <sup>b</sup> Percentage of gene trees without a solution.
- <sup>c</sup> Precision of inferred duplications.
- <sup>d</sup> Sensitivity of inferred duplications.
- <sup>e</sup> Precision of inferred gene losses.
- f Sensitivity of inferred gene losses.
- <sup>g</sup> Average runtime of computing the reconciliation for each gene tree in seconds.

100%. With the remaining tolerance setting, we infer reconciliation for all gene trees from the dataset with perfect precision and sensitivity of duplications and gene losses. The other software, Notung and Treerecs, compute reconciliation for all gene trees with 100% precision and sensitivity of inferred duplications and gene losses. To compare the average running time for each gene tree, our software has the best average running time about 0.004006 for each tolerance setting. The Treerecs has the second-best average running time bigger by 93.11% from our average running time. The longest average running time has Notung, which is bigger by 91.8% from the Treerecs average running time and by 99.43% from our average running time.

# Conclusion

To sum up, our software runs the best with tolerance  $1 \times 10^{-5}$ , which is by one decimal place shorter than the edge length of gene trees from both datasets. Thus, if the tolerance has less than or an equal number of decimal places, our software may not find reconciliation for all rooted gene trees or may find a reconciliation with wrongly detected duplications and gene losses, which decreases the precision and sensitivity of inferred duplications and gene losses. In terms of time, our software infers the reconciliation for each gene tree the fastest compared to the Notung and Treerecs.

**Duplication** Gene loss  $W/o sol^b$ Software<sup>a</sup> Runtimeg  $\overline{\mathrm{Prec^c}}$ Sens<sup>d</sup>  $\overline{\mathrm{Prec^e}}$  $\overline{\mathrm{Sens}^{\mathrm{f}}}$ Our (t - 0.0)9.03 0.007225100 100 100 100 Our (t -  $1 \times 10^{-6}$ ) 0 99.99 100 99.98 100 0.005962Our (t -  $1 \times 10^{-5}$ ) 0 100 100 100 100 0.003898Our (t -  $1 \times 10^{-3}$ ) 0 100 100 100 0.004728100 Our (t - 0.1)0 100 100 100 100 0.0031580 Our (t - 0.3) 100 100 100 100 0.0022310 Our (t - 0.5)100 100 100 0.002366100 Our (t - 1.0) 0 100 100 100 100 0.002481Notung 0 100 100 100 100 0.7086650 Treerecs 100 100 100 100 0.058145

Table 4.2: Fungi: results of phylogenetic software on simulated dataset without rerooting the gene tree

# 4.1.2 With rerooting the gene tree

The software for isometric reconciliation takes the rooted gene tree as input with an argument to reroot the given gene tree. We forget the root of the rooted gene tree and transform it into the unrooted gene tree. On the obtained unrooted gene tree, we run the getIntervals function (Algorithm 1 in Chapter 2.1) to get a set of roots given by a pair of intervals for subdividing each edge of the unrooted gene tree, where the first interval from the pair signifies the edge length on the left from the new root and the second interval from the pair signifies the edge length on the right from the new root. Then we run a reconciliation with countDL function (Algorithm 5 in Chapter 2.2.2). We want to find a new root minimizing the number of inferred duplications and gene losses in reconciliation. The process is executed several times with different tolerance and step settings. The tolerance and  $\epsilon$  setting are the same as in the first case without rerooting the gene tree (Chapter 4.1.1). The step settings are 0.0, 0.1, 0.3, 0.5, 1.0, 2.0 since the edge lengths of species trees and gene trees from the dataset are in a range from about 1 to 78 expressed in million years.

# Flies dataset

At first, we run our software with all tolerance settings and step set to 0.0, as we can

<sup>&</sup>lt;sup>a</sup> Phylogenetic software with "t" as tolerance setting.

<sup>&</sup>lt;sup>b</sup> Percentage of gene trees without a solution.

<sup>&</sup>lt;sup>c</sup> Precision of inferred duplications.

<sup>&</sup>lt;sup>d</sup> Sensitivity of inferred duplications.

<sup>&</sup>lt;sup>e</sup> Precision of inferred gene losses.

f Sensitivity of inferred gene losses.

<sup>&</sup>lt;sup>g</sup> Average runtime of computing the reconciliation for each gene tree in seconds.

see in Table 4.3, where for each edge  $(u,v) \in E(G)$ , the getIntervals function returns a set of roots subdividing the edge right above the vertices u and v. Because of that, our software is not able to infer reconciliation for all gene trees at all tolerance settings. It not finds any reconciliation with tolerance set to  $0.0, 1 \times 10^{-6}, 1 \times 10^{-5}, 1 \times 10^{-3}$ . With the tolerance of 0.1, it recognizes the first isometric reconciliations for 82.37% of gene trees from the dataset. The percentage of gene trees without computed reconciliation decreases with the increasing tolerance. With the tolerance of 1.0, only 0.48% of gene trees does not have inferred reconciliation. As our software does not find solutions for the reconciliation with the first 4 tolerance settings, we can not calculate and compare the precision of inferred root and precision and sensitivity of inferred duplications or gene losses. For the remaining tolerance settings, the precision of correctly inferred root is highest with tolerance set to 1.0. It rises with increasing tolerance. A slight decrease is between tolerances 0.3 and 0.5 caused by newly inferred reconciliations for gene trees that have no solution with tolerance 0.3 but find a solution with tolerance 0.5. The precision of inferred duplications has a growing tendency for all remaining tolerance settings. The sensitivity of inferred duplications is sensitive to the rooting of a gene tree on a different edge than the original edge, so when the precision of correctly inferred root drops between tolerances 0.3 and 0.5, the sensitivity drops by 0.09\% too. Finding the root on different edge induces duplications and gene losses on different nodes. Apart from that, it has an increasing tendency. The precision of inferred gene losses is increasing for the remaining tolerance settings with a slight drop of 0.01% between tolerances 0.3 and 0.5 also caused by the wrongly inferred roots. The sensitivity of inferred gene losses is highest with the tolerance of 0.1 and then it drops by 18.56%. It is induced by a decrease in the percentage of gene trees without solutions, where we infer reconciliation for more gene trees with tolerance 0.3 than with the tolerance 0.1, but some of them has wrongly inferred gene losses, where the gene loss is not supposed to be. Besides this drop, it has a growing tendency from tolerance 0.3 to tolerance 1.0.

With step set to 0.1, we find reconciliation solutions already at tolerance set to 0.0 for 1.65% gene trees from the dataset. The percentage of gene trees without solution decreases as the tolerance increase and it is 0% from tolerance 0.1 and more. The precision of correctly inferred root is 100% for tolerance settings from 0.0 till 0.1 include.

It does not even drop with the big increase of inferred reconciliations between tolerances  $1 \times 10^{-5}$  and  $1 \times 10^{-3}$  for gene trees that have not solution at tolerance  $1 \times 10^{-5}$ , but the solution exists at tolerance  $1 \times 10^{-3}$ . It starts decreasing with tolerance 0.3 and bigger induced by increasing tolerance, allowing finding a solution on another edge than the original edge with a better reconciliation score. The precision of inferred duplications has similar development as the precision of correctly inferred root with one exception at the tolerance set to  $1 \times 10^{-3}$ . The high increase of gene trees with solution caused a big drop, where a lot of these solution contains wrongly inferred duplications which correct the increase in tolerance to 0.1. The decrease from tolerance set to 0.3 and more is caused by a change in finding a different root, which induces duplications on different nodes. The sensitivity of inferred duplications is perfect for tolerances from 0.0 to 0.1 include. It starts decreasing between tolerances 0.1 and 0.3 induced for the same reason as the decrease in precision of inferred duplications. The precision of inferred gene losses is perfect except tolerance set to  $1 \times 10^{-3}$ , where the cause of the drop is the same as for the precision of inferred duplications. The sensitivity of inferred gene losses is perfect until it starts decreasing between tolerances 0.1 and 0.3 caused by finding a reconciliation solution with different root and fewer gene losses, where the inferred gene losses are correct, as shown by the precision of inferred gene losses, but we do not find all expected gene losses.

The next tested step setting is 0.3, where the results are almost the same as the result with the step setting 0.1 with the exception for tolerances set to  $1 \times 10^{-3}$  and 0.1. At the tolerance  $1 \times 10^{-3}$ , we are not able to infer solutions for as many gene trees as with step set to 0.1. Still, the 4.27% increase in inferred reconciliation solutions for gene trees between tolerances  $1 \times 10^{-5}$  and  $1 \times 10^{-3}$  induces a decrease in precision of inferred duplications and gene losses. The second exception is at the tolerance 0.1, where the precision of inferred duplications and gene losses are 99.89% and 99.72%, respectively, again caused by a big increase of inferred solutions for gene trees with no solution at tolerance  $1 \times 10^{-3}$  and a found solution at tolerance 0.1, where some of these solutions have incorrectly detected duplications and gene losses.

The step set to 0.5 is big enough that our software is not capable to find a solution for gene trees with tolerance from 0.0 till  $1 \times 10^{-5}$  include. It finds solutions for 81.97% of the gene trees from the dataset at tolerance  $1 \times 10^{-3}$ . For the tolerance

Table 4.3: Flies: results of phylogenetic software on simulated dataset with rerooting the gene tree

the gene tree	337 / 1b	D40	Duplication <sup>d</sup>		Gene loss <sup>e</sup>		D 4' f
Software <sup>a</sup>	$\mathbf{W}/\mathbf{o} \ \mathbf{sol^b}$	$\mathbf{Root^c}$	Prec	Sens	Prec	Sens	$\mathbf{Runtime^f}$
Our (t - 0.0; s - 0.0)	100	-	-	-	-	-	0.004377
Our $(t - 1 \times 10^{-6}; s - 0.0)$	100	-	-	-	<u>-</u>	-	0.002373
Our (t - $1 \times 10^{-5}$ ; s - 0.0)	100	-	-	-	-	-	0.002402
Our (t - $1 \times 10^{-3}$ ; s - 0.0)	100	-	-	-	-	_	0.002352
Our $(t - 0.1; s - 0.0)$	17.63	98.64	25.42	98.58	8.99	99.42	0.004743
Our (t - 0.3; s - 0.0)	2.47	99.47	45.56	99.44	17.61	80.86	0.005165
Our (t - 0.5; s - 0.0)	2.32	99.39	45.63	99.35	17.60	80.99	0.005745
Our (t - 1.0; s - 0.0)	0.48	99.98	46.37	99.98	23.23	91.98	0.005148
Our (t - 0.0; s - 0.1)	98.35	100	100	100	100	100	0.213234
Our (t - $1 \times 10^{-6}$ ; s - 0.1)	98.3	100	100	100	100	100	0.315081
Our (t - $1 \times 10^{-5}$ ; s - 0.1)	98.3	100	100	100	100	100	0.237645
Our (t - $1 \times 10^{-3}$ ; s - 0.1)	0.28	100	34.6	100	17.03	100	0.460089
Our (t - 0.1; s - 0.1)	0	100	100	100	100	100	0.500895
Our (t - 0.3; s - 0.1)	0	99.93	99.95	99.95	100	99.94	0.622866
Our (t - 0.5; s - 0.1)	0	99.81	99.86	99.86	100	99.83	0.777619
Our (t - 1.0; s - 0.1)	0	99.65	99.76	99.76	100	99.70	0.914920
Our (t - 0.0; s - 0.3)	98.35	100	100	100	100	100	0.042934
Our (t - $1 \times 10^{-6}$ ; s - 0.3)	98.3	100	100	100	100	100	0.046455
Our (t - $1 \times 10^{-5}$ ; s - 0.3)	98.3	100	100	100	100	100	0.047223
Our (t - $1 \times 10^{-3}$ ; s - 0.3)	94.03	100	25.77	100	17.15	100	0.047767
Our (t - 0.1; s - 0.3)	0	100	99.91	100	99.76	100	0.100275
Our (t - 0.3; s - 0.3)	0	99.96	99.96	99.96	100	99.95	0.121550
Our (t - 0.5; s - 0.3)	0	99.89	99.91	99.91	100	99.88	0.144801
Our (t - 1.0; s - 0.3)	0	99.77	99.82	99.82	100	99.77	0.172164
Our (t - 0.0; s - 0.5)	100	-	-	- 55.02	-		0.027602
Our $(t - 0.0, s - 0.5)$ Our $(t - 1 \times 10^{-6}; s - 0.5)$	100	_	_	_	_	_	0.027832
Our $(t - 1 \times 10^{-5}; s - 0.5)$	100	_	_	_	_	_	0.027652 $0.028455$
Our $(t - 1 \times 10^{-3}; s - 0.5)$	18.03	100	31.96	100	12.33	100	0.023499 $0.052290$
Our (t - 0.1; s - 0.5)	0	100	100	100	100	100	0.052290 $0.059033$
Our (t - 0.3; s - 0.5)	0	99.96	99.96	99.96	100	99.95	0.039033 $0.072567$
Our (t - 0.5; s - 0.5)	0	99.90 $99.92$	99.90	99.90	100	99.93	0.072307 $0.088120$
Our (t - 1.0; s - 0.5)	0	99.83	99.86	99.86	100	99.81	0.003120 $0.109294$
Our (t - 0.0; s - 0.0)	100	99.00	99.00	99.00	100	99.01	0.109294
Our $(t - 0.0, s - 1.0)$ Our $(t - 1 \times 10^{-6}; s - 1.0)$	100	-	-	_	_	_	0.014086 $0.017554$
Our $(t - 1 \times 10^{-3}; s - 1.0)$ Our $(t - 1 \times 10^{-5}; s - 1.0)$	100	-	_	_	_	-	0.017534 $0.015989$
Our $(t - 1 \times 10^{-3}; s - 1.0)$	l .	100	- 21 O1	100	19.96	100	
	18.32	100	31.91	100	12.26	100	0.028652
Our (t - 0.1; s - 1.0)		100	99.77	100	99.42	100	0.031903
Our (t - 0.3; s - 1.0)	0	99.97	99.95	99.97	99.96	99.96	0.038490
Our (t - 0.5; s - 1.0)	0	99.94	99.94	99.94	100	99.92	0.045830
Our (t - 1.0; s - 1.0)	0	99.89	99.90	99.90	100	99.87	0.053317
Our (t - 0.0; s - 2.0)	100	-	-	_	-	-	0.008342
Our $(t - 1 \times 10^{-6}; s - 2.0)$	100	-	-	_	-	-	0.009238
Our $(t - 1 \times 10^{-5}; s - 2.0)$	100	-	-	-	-	-	0.009383
Our $(t - 1 \times 10^{-3}; s - 2.0)$	99.97	100	50	100	60	100	0.009198
Our (t - 0.1; s - 2.0)	0	99.29	94.95	99.26	87.47	100	0.018753
Our (t - 0.3; s - 2.0)	0	99.87	99.17	99.87	98.02	99.96	0.022397
Our (t - 0.5; s - 2.0)	0	99.95	99.95	99.95	100	99.94	0.025403
Our (t - 1.0; s - 2.0)	0	99.93	99.93	99.93	100	99.91	0.028850
Notung	0	92.63	99.98	99.98	93.32	93.3	1.689122
Treerecs	0	81.07	99.09	99.09	96.12	95.14	0.081646
TreeFix	0	99.98	98.98	98.94	100	98.68	4.065790

<sup>&</sup>lt;sup>a</sup> Phylogenetic software with "t" as tolerance setting and "s" as step setting.

b Percentage of gene trees without a solution.
c Precision of correctly inferred root.
d Precision ("Prec") and sensitivity ("Sens") of inferred duplications.
e Precision ("Prec") and sensitivity ("Sens") of inferred gene losses.

f Average runtime of computing the reconciliation for each gene tree in seconds.

0.1 and more, the percentage of gene trees without a solution is 0%. The precision of correctly inferred root is best at tolerances set to  $1 \times 10^{-3}$  and 0.1 as in the step setting before. It begins decreasing with tolerance 0.3 and more, where it finds solutions with better reconciliation score while rooting the gene trees at other edges. The precision of inferred duplications is low at tolerance  $1 \times 10^{-3}$ , where the gene trees are not able to fit right into the species tree and create more duplications and gene losses than are correct. The precision of inferred duplications decreases with increasing tolerance as the software finds different root and also different duplications on different nodes. The sensitivity of inferred duplications is perfect until tolerance set to 0.3 and more, where our software finds a root on a different edge than expected causing us not to find all correct duplications. The precision of inferred gene losses is low at tolerance  $1 \times 10^{-3}$ induces by the same cause as with the precision of inferred duplications. Besides, it is perfect for the rest of the tolerance settings. The sensitivity of inferred gene losses has the same development as the sensitivity of inferred duplications. At the tolerance 0.1, we see the same scenario as with the step set to 0.1 with the same tolerance, where our software infers reconciliation with correct root and perfect precision and sensitivity of duplications and gene losses.

The results with the step set to 1.0 have the same development in all categories as the results for the step setting 0.5 with exceptions for the precision of inferred duplications and gene losses at tolerance setting 0.1 and 0.3. With the tolerance of 0.1, the precision of duplications and gene losses is 99.77% and 99.42%, respectively, not 100% like with the step 0.5. This is caused by a big step, where we skip the perfect root which induces duplications and gene losses at wrong nodes. The precision of duplications and gene losses rises a little bit with tolerance 0.3 because the duplications and gene losses can find the right nodes, but it also decreases the precision of correctly inferred root as the higher tolerance allows to find rooting at other edges with better reconciliation score. From the tolerance set to 0.5, the precision of inferred gene losses is again 100%.

With the last step setting 2.0, our software finds reconciliation only for 0.03% of gene trees from the dataset. For tolerance 0.1 and more, we infer reconciliation for all gene trees. The precision of correctly inferred root is best with the tolerance  $1 \times 10^{-3}$  caused by a small amount of found reconciliation solutions. It decreases to 99.29

with finding the solution for all gene trees and slowly rises till tolerance 1.0, where it decreases because it finds a better rooting with a smaller reconciliation score. With smaller step settings, the decrease caused by better rooting starts with a tolerance of 0.3. The late decrease in precision of correctly inferred root is induced by a big step 2.0 because of which we skip a lot of possible roots. The similar progress is with the precision of inferred duplications, where it rises from tolerance  $1 \times 10^{-3}$  to 0.5 include and decreases with tolerance 1.0 by the same cause as the precision of correctly inferred root. The sensitivity of inferred duplications has the same progress as the precision of correctly inferred root as it is sensitive to the change in the rooting of the gene tree. The precision of inferred gene losses rises until it obtains 100% at tolerance 0.5. The sensitivity of inferred gene losses has the same development as in the previous step settings.

The common development of average running time of computing the reconciliation for each gene tree is the same for all steps and tolerances. It always increases with the increasing value of the tolerance and decreases with the increasing value of the step except for the running times of steps 0.0 and 0.1 as the average running times of step 0.0 are lower than the average running times of step 0.1.

To compare with other software, Notung, Treerecs and TreeFix are able to find a solution for all gene trees. We calculated our average values in all examined categories, where the percentage of gene trees without a solution is 0%. The average precision of correctly inferred root is 99.88%. The average precision and sensitivity of inferred duplications are 99.62% and 99.89%, respectively. The average precision and sensitivity of inferred gene losses are 99.23% and 99.92%, respectively. The average runtime of computing the reconciliation for each gene tree is 0.197452 seconds. Our average precision of correctly inferred root is better than Notung by 7.25% and Treerecs by 18.81%. The best results in the precision of correctly inferred root have TreeFix with 99.98%, which is better by 0.1% from our average. In the precision of inferred duplications, our average has better results than Treerecs by 0.53% and TreeFix by 0.64%. Our average is worse by 0.36% from Notung that has the best precision of inferred duplications. In the case of sensitivity of inferred duplications, our average is better than Treerecs by 0.8% and TreeFix by 0.95%. Our average is worse by 0.09% from Notung, which has the best sensitivity of inferred duplications. The precision of inferred gene losses

is worse in Treerecs by 3.11% and in Notung by 5.91% from our average. The best is TreeFix with perfect precision better by 0.77% from our average precision of inferred gene losses. Our average sensitivity of inferred gene losses is the best compare to the other software. It is worse in TreeFix by 1.24%, in Treerecs by 4.78% and in Notung by 6.62%. Our average runtime of computing the reconciliation for each gene tree is better by 88.31% from Notung and by 95.14% from TreeFix. The fastest runtime has Treerecs, better by 58.65% from our average.

With the average values, our software is the best only in the category of sensitivity of inferred gene losses. However, we computed reconciliation for all gene trees from the dataset with the precision of correctly inferred root and precision and sensitivity of inferred duplications and gene losses to be 100% two times with tolerance set to 0.1 and step set to 0.1 and 0.5. This makes our software best in the precision of correctly inferred root, precision and sensitivity of inferred duplications and sensitivity of inferred gene losses. For the precision of correctly inferred gene losses, we split the first place with TreeFix.

# Fungi dataset

The first step setting is 0.0, where we consider subdividing each edge  $(u,v) \in$ E(G) right above the vertices u and v, so the size of the set of possible roots for each edge is 2. Our software is not able to find reconciliation with tolerance set to  $0.0, 1 \times 10^{-6}, 1 \times 10^{-5}$  (Tab. 4.4). It finds solutions to the reconciliation for 0.02%of the gene trees at tolerance set to  $1 \times 10^{-3}$ . The percentage of gene trees without inferred reconciliation decreases with increasing tolerance. The precision of correctly inferred root is 100% with tolerance  $1 \times 10^{-3}$ , thus the percentage of gene trees without reconciliation solution is big. It drops with finding the reconciliation solution for more gene trees at tolerance 0.1, where most of the gene trees find root at the different edge. It increases with increasing tolerance. The precision of inferred duplications and gene losses has the same development. They are also perfect with tolerance  $1 \times 10^{-3}$  as the precision of correctly inferred root, because of the big percentage of gene trees without a solution. They drop with tolerance 0.1 as 3.33% of gene trees find a reconciliation solution and almost half of all solution do not find the correct rooting. The precision of duplications and gene losses is sensitive to the change in the percentage of gene trees without solution, caused by inferring reconciliation solutions for gene trees with no solution before. The gene trees, that have no solution before, do not fit correctly to the species tree inducing duplications and gene losses on wrong nodes. So when the percentage of gene trees without solution significantly drops between tolerance settings 0.1, 0.3 and 0.5, 1.0, the precision of inferred duplications and gene losses also drops. They increase between tolerances 0.3 and 0.5, where the decrease in the percentage of gene trees without a solution is not so big, only 7.18%. The sensitivity of inferred duplications has the same progress as the precision of correctly inferred root as it depends on changes in rooting of the gene trees. The sensitivity of inferred gene losses is perfect for tolerances  $1 \times 10^{-3}$  and 0.1, where the percentage of gene trees with a solution is small. It starts decreasing with tolerance set to 0.3 as the percentage of gene trees without solutions considerably decreases, where gene losses are inferred incorrectly due to incorrectly inferred duplications.

With the step set to 0.1, we do not find reconciliation solutions merely with a tolerance setting of 0.0. The percentage of gene trees without solutions considerably drops with tolerance  $1 \times 10^{-3}$  and is 0% from tolerance 0.1 and more. The precision of correctly inferred root is 100% for tolerances  $1 \times 10^{-6}$ ,  $1 \times 10^{-5}$  and  $1 \times 10^{-3}$  and slowly decreases from tolerance 0.1 and more caused by increasing tolerance, where our software finds solutions to the reconciliation with a smaller number of duplications and gene losses on other edges than on the original edge. We could already observe this development of precision of correctly inferred root with the simulated flies dataset (Tab. 4.3). The precision of inferred duplications increases with increasing tolerance from  $1 \times 10^{-6}$  till 0.1 include causing more accurate mapping of duplications to the correct nodes. It decreases from 0.1 to 1.0 include induced by rooting at different edges, where the software finds reconciliation with a better score, but the duplications are on wrong nodes. The sensitivity of inferred duplications is perfect until tolerance 0.1, where it starts decreasing caused by the decrease in precision of correctly inferred root. The precision of inferred gene losses has similar progress as the precision of inferred duplications. It increases between tolerance settings  $1 \times 10^{-6}$  and 0.1. Unlike the precision of inferred duplications, it starts decreasing with tolerance between 0.5 and 1.0. The sensitivity of inferred gene losses is perfect for almost all tolerance settings. It only decreases with tolerance set to 1.0 caused by a quite big percentage of gene trees, that are rooted at a different edge than the original edge inducing different gene losses.

The results for step setting 0.3 has comparable development as results with step set to 0.1. The percentage of gene trees without a solution at tolerance 0.0 is also 100% as with the step 0.1 and in addition, our software does not find any solutions at tolerance  $1 \times 10^{-6}$  either. We find solutions at tolerance  $1 \times 10^{-5}$  and from tolerance 0.1 and more is the percentage of gene trees without solution 0%. The precision of correctly inferred root and precision and sensitivity of inferred duplications and gene losses has the same progress as with step 0.1. Only one exception rises, when the sensitivity of inferred gene losses slightly decrease by 0.01 for tolerance setting  $1 \times 10^{-3}$  induced by a bigger step, where we skip a solution containing correct gene loss.

For the step setting 0.5, our software is not able to find a solution for all gene trees with tolerance set to 0.0 and  $1 \times 10^{-6}$  like with the step 0.3. It finds a lot less solutions with tolerances  $1 \times 10^{-5}$  and  $1 \times 10^{-3}$  than with the previous step. The precision of correctly inferred root has the same development as with the step 0.3. To compare, we have higher precision of correctly inferred root as in the step 0.3 with the identical tolerance settings. The precision of inferred duplications with tolerance set to  $1 \times 10^{-5}$ is smaller than with the step before as the step is bigger and we skip solutions with correct duplications nodes. However, at tolerance  $1 \times 10^{-3}$ , it is bigger compare to step 0.3 because of the low percentage of gene trees with reconciliation solution. The sensitivity of inferred duplication is equal to the results from the previous step. The precision of inferred gene losses for tolerance  $1 \times 10^{-5}$  and  $1 \times 10^{-3}$  is bigger than with the step 0.3 because the percentage of gene trees without solutions is bigger, but it is smaller by 0.02 with tolerance 0.1 as the step is bigger and our software misses solutions with accurate gene losses locations. From tolerance 0.3 and more, the precisions of inferred gene losses values are alike with the step 0.3. The sensitivity of inferred gene losses is perfect for tolerance settings from  $1 \times 10^{-5}$  to 0.5 include. It decreases between tolerances 0.5 and 1.0 as with the step 0.3.

The percentage of gene trees without solution with step setting 1.0 and tolerance settings  $1 \times 10^{-5}$  and  $1 \times 10^{-3}$  is again bigger than with the previous step setting caused by an increased step. The values at other tolerances are not changed from step 0.5. The precision of correctly inferred root is generally higher compare to the step before caused by the increase of the step. The precision of inferred duplications is

Table 4.4: Fungi: results of phylogenetic software on simulated dataset with rerooting the gene tree

337 / 1b	D 46	c Duplication <sup>d</sup>		Gene loss <sup>e</sup>		D '' f
, , , , , , , , , , , , , , , , , , ,	Root	Prec	Sens	Prec	Sens	${f Runtime^f}$
	-	-	-	-	-	0.006002
	-	-	-	-	-	0.004688
	-	-	-	-		0.004670
						0.004678
						0.005205
					1	0.006203
					1	0.006832
	98.05	35.38	98.07	11.78	90.97	0.009312
	-	-	-	-	-	1.001114
						1.031367
						1.057450
					1	2.106134
						2.385887
						2.947574
						3.354926
0	94.97	98.18	98.18	99.99	99.61	4.346881
100	-	-	-	-	-	0.217207
100	-	-	-	-	-	0.223558
99.92	100	55.36	100	16.67	100	0.222740
16.05	100	31.89	100	16.05	99.99	0.427555
0	99.97	99.99	99.99	100	100	0.491044
0	99.56	99.82	99.82	100	100	0.590541
0	98.98	99.58	99.58	100	100	0.688235
0	95.07	98.18	98.18	99.99	99.61	0.848628
100	-	_	-	_	-	0.125547
100	-	-	-	-	_	0.134174
99.95	100	51.35	100	23.4	100	0.131749
90.27	100	64.06	100	42.17	100	0.153825
0	99.97	99.98	99.99	99.98	100	0.291047
0	99.58	99.82	99.82	100	100	0.355765
0	99.01	99.58	99.58	100	100	0.409451
0	95.17	98.18	98.18	99.99	99.61	0.535211
100	-	-	-	-	-	0.079327
100	-	_	-	_	_	0.110613
99.97	100	45.83	100	21.21	100	0.111556
						0.095454
0	99.96	99.98	99.98	99.99	100	0.257746
0			99.82		1	0.316109
0			99.58		1	0.219381
0					99.61	0.329572
100	-	_	-	_	_	0.064227
100	-	-	-	-	_	0.052543
99.97	100	45.83	100	21.21	100	0.047304
				42.06	1	0.051702
0	99.98	99.95	99.98	99.82	100	0.112863
0	99.66		99.82	99.77	100	0.128979
0	99.17			100	100	0.139579
0						0.168751
0						1.887500
					1	0.099334
o 0					1	10.510925
	100 100 99.92 16.05 0 0 0 0 100 100 99.95 90.27 0 0 0 0 100 100 99.97 92.95 0 0 0 0 0 0 0 0 0 0	100       -         100       -         99.98       100         96.65       56.94         78.68       62.06         71.50       88.68         0.52       98.05         100       -         99.95       100         99.95       100         0       99.97         0       99.53         0       98.95         0       94.97         100       -         100       -         99.92       100         16.05       100         0       99.97         0       99.95         0       99.96         0       99.97         0       99.95         0       99.97         0       99.97         0       99.97         0       99.97         0       99.97         0       99.98         0       99.97         0       99.98         0       99.97         0       99.98         0       99.96         0       99.96         0 <td>W/6 sol         Root         Prec           100         -         -           100         -         -           100         -         -           99.98         100         100           96.65         56.94         42.27           78.68         62.06         40.91           71.50         88.68         48.59           0.52         98.05         35.38           100         -         -           99.95         100         56.67           99.65         100         61.14           0.02         100         86.57           0         99.97         99.99           0         99.53         99.81           0         98.95         99.58           0         94.97         98.18           100         -         -           100         -         -           100         -         -           100         -         -           100         -         -           100         -         -           100         -         -           100         -         -</td> <td>  Note</td> <td>  Note</td> <td>  Note</td>	W/6 sol         Root         Prec           100         -         -           100         -         -           100         -         -           99.98         100         100           96.65         56.94         42.27           78.68         62.06         40.91           71.50         88.68         48.59           0.52         98.05         35.38           100         -         -           99.95         100         56.67           99.65         100         61.14           0.02         100         86.57           0         99.97         99.99           0         99.53         99.81           0         98.95         99.58           0         94.97         98.18           100         -         -           100         -         -           100         -         -           100         -         -           100         -         -           100         -         -           100         -         -           100         -         -	Note	Note	Note

<sup>&</sup>lt;sup>a</sup> Phylogenetic software with "t" as tolerance setting and "s" as step setting.

b Percentage of gene trees without a solution.
c Precision of correctly inferred root.
d Precision ("Prec") and sensitivity ("Sens") of inferred duplications.
e Precision ("Prec") and sensitivity ("Sens") of inferred gene losses.

f Average runtime of computing the reconciliation for each gene tree in seconds.

lower from the previous step with tolerance settings  $1 \times 10^{-5}$  and  $1 \times 10^{-3}$  and stays the same from 0.1 and more. The lower values are induced by a bigger percentage of gene trees without solutions, where we find solutions with more duplications on incorrect nodes. The sensitivity is almost the same with the step 0.5 except small decrease by 0.01 at a tolerance of 0.1. The precision of inferred gene losses compare to the step 0.5 is also lower with tolerance  $1 \times 10^{-5}$ , but higher at tolerance  $1 \times 10^{-3}$  and 0.1. This irregularity is caused by the bigger step, when we infer fewer solutions per gene tree, thus we skip some wrongly inferred gene losses. The results for tolerances 0.3 and more are the same as the previous step. The sensitivity of inferred gene losses remains the same as with step 0.5.

With the last step setting 2.0, the development of all categories is the same as with the previous step, but the values are slightly different due to the higher step, where we skip a lot of possible solutions. Our software has the same results for the percentage of gene trees without solution as with the step before with one exception at tolerance  $1 \times 10^{-3}$ , where we find a solution for only 2.95% of all gene trees. The precision of correctly inferred root remains 100% for tolerances  $1 \times 10^{-5}$  and  $1 \times 10^{-3}$ and increases for the tolerances 0.1 and more. The precision and sensitivity of inferred duplications and gene losses stay the same for tolerance  $1 \times 10^{-5}$ , as the percentage of gene trees without solutions does not change either. The precision of inferred duplications increases with the tolerance increase till tolerance 0.1 and then decreases caused by rooting the gene trees at a different edge with a better reconciliation score. The decrease from tolerance 0.1 and more is also in the sensitivity of inferred duplications that is perfect for tolerances  $1 \times 10^{-5}$  and  $1 \times 10^{-3}$ . The precision of inferred gene losses is smaller from the previous step but has an increasing tendency from tolerance  $1 \times 10^{-5}$  to 0.5, where it is 100%. It decreases from the tolerance 0.5 and more. The sensitivity of inferred gene losses does not change compared to step 1.0.

The average running time of computing the reconciliation for each gene tree at all steps and tolerances is generally increasing with the increasing tolerance and decreases with increasing step except the average running times in steps 0.0 and 0.1, same as with the flies dataset.

As in the flies dataset, we calculated our average values for all categories, where the percentage of gene trees without a solution is 0% as Notung, Treerecs and TreeFix find

solutions for all gene trees in the dataset. The average precision of correctly inferred root is 99.46%. The average precision and sensitivity of inferred duplications are 99.39% for both. The average precision and sensitivity of inferred gene losses are 99.99% and 99.9%, respectively. The average running time of computing the reconciliation for each gene tree is 0.945909 seconds. Our average precision of correctly inferred root is the best among the tested software. It is better by 0.24% from TreeFix, by 2.54% from Notung and by 38.71% from Treerecs. In terms of precision of inferred duplications, our average has better results than TreeFix by 3.56% and Treerecs by 6.62%. The best precision of inferred duplications has Notung with 99.76%, which is better than our average by 0.37%. In the sensitivity of inferred duplications, our average is again better from Treefix by 3.7% and from Treerecs by 6.64%, while Notung has the best sensitivity of inferred duplications, where our average is worse by 0.35%. Our average is also best in the precision of inferred gene losses, where the TreeFix is worse by 0.22%, Treerecs is worse by 1.19% and Notung is worse by 2.88%. In the case of the sensitivity of inferred gene losses, our average is best too. It is better by 3.15% from Notung, by 5.04% from Treerecs and by 5.48% from TreeFix. Our average running time of computing the solution for each gene tree is better by 49.89% from Notung and by 99.05% from TreeFix. The fastest running time has Treerecs with 0.099334, which is better than our average by 89.5%.

Our average values are the best in the precision of correctly inferred root and the precision and sensitivity of inferred gene losses. However, our best result is with tolerance set to 0.1 and step settings 0.1 and 0.3, where the precision and sensitivity of inferred duplications is 99.99% for both, which is better than the results of Notung and makes our software the best in all categories.

## Conclusion

In conclusion, for both datasets, the best tolerance setting to infer isometric reconciliation for all gene trees is between  $1 \times 10^{-3}$  and 0.1 as the percentage of gene trees without solutions is never 0% at tolerance  $1 \times 10^{-3}$  and is always 0% at tolerance 0.1. With the lower setting of tolerance, we do not find solutions for all gene trees and contrarily, with the higher setting of tolerance, we find solutions at a different edge than the original edge, but with a better reconciliation score. The best tolerance for inferring the gene trees with the correct root is also somewhere between tolerances  $1 \times 10^{-3}$  and

0.1. The precision of correctly inferred root is always 100% until tolerance  $1 \times 10^{-3}$  (or with flies in some cases until tolerance 0.1), where the percentage of gene trees with a solution is not 0% and it decreases with the increasing tolerance. The precision and sensitivity of inferred duplications depend mostly on the precision of correctly inferred root means that when the precision of correctly inferred root decreases, the precision and sensitivity of inferred duplications decrease with it. The precision and sensitivity of gene losses show a higher number of 100% values, but as they depend on the correctly inferred duplications, they also depend on the precision of correctly inferred root. The average running time for computing the reconciliation for each gene tree in both datasets increases as the step decreases and decreases as the tolerance increases. This rule does not apply to step 0.0 as for each edge, the set of possible roots is of size 2, thus the running time is quite fast.

The best settings to infer the correct reconciliation on these datasets is tolerance set between  $1 \times 10^{-3}$  and 0.1 as we explained and step 0.1 as our software finds the best solutions for tolerance 0.1 and steps 0.1 and 0.5 on the flies dataset and for the same tolerance and steps 0.1 and 0.3 on the fungi dataset. These best solutions are also best in comparison with the other software: Notung, Treerecs and Treefix.

# 4.2 Real dataset

The correct gene tree is unknown in the real dataset, thus we use different metrics as with the simulated dataset except for the average running time of computing the reconciliation for each gene tree. We measure the number of inferred duplications and gene losses and the average consistency score of duplications for each gene tree overall gene trees in the dataset.

The duplication consistency score (Figure 4.2), dcs, was previously used in [19] and [17] to compare the plausibility of inferred duplications in different software. For a duplication node u with children v and w, the duplication consistency score is computed as the number of common species in both children nodes v and w divided by a number of all species present in the descendants of node u such as  $dcs(u) = (L \cup R) \mid (L \cap R)$ , where L is the set of species represented in left child v and R is the set of species represented in right child w. It is sensitive to recognizing the duplications that are

wrongly inferred due to error in reconciliation. The higher the duplication consistency score, the more credible the duplication.

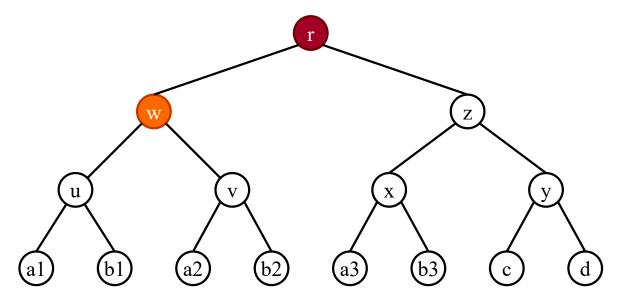


Figure 4.1: Duplication consistency score for node w

The set of species of left child u is  $L = \{A, B\}$  and the set of species of right child v is  $R = \{A, B\}$ . The duplication consistency score is computed as:  $dcs(w) = (L \cup R) \mid (L \cap R) = 2/2 = 1$ .

# Duplication consistency score for node r

The set of species of left child w is  $L = \{A, B\}$  and the set of species of right child z is  $R = \{A, B, C, D\}$ . The duplication consistency score is computed as:  $dcs(r) = (L \cup R) \mid (L \cap R) = 2/4 = 0.5$ .

The real fungi dataset consists of multiple sequence alignment for each gene family of the presented 5351 gene families. To obtain unrooted gene trees from the alignments, we run a RAxML program on each alignment with GTRGAMMA model. We run our software on the acquired unrooted gene trees with tolerance set to 1.0 and step set to 0.01 to infer the smallest possible number of duplications and gene losses. To compare, Notung and Treerecs on the acquired gene trees as well (Tab. 4.5). We do not run TreeFix on the real dataset as TreeFix takes only rooted gene trees.

All compared software infer the same number of duplications. The least number of founded gene losses has Treerecs. Our software and Notung infer the same number of gene losses which is higher by 9525 gene losses from the Treerecs. The duplication consistency score is also highest with Treerecs, which is understandable since it has the smallest number of gene losses. Notung has the duplication consistency score worse by 0.000012 from the Treerecs. Even though we have the same number of duplications

and gene losses with Notung, our duplication consistency score is smaller by 0.000014 from Notung caused by multiple reconciliation solution, where some of them have duplications with worse duplication consistency score than Notung. The best average running time of computing the reconciliation for each gene tree has Treerecs. Our average running time is worse by 75.22% from Treerecs and better by 20.51% from Notung.

Table 4.5: Results of phylogenetic software on real dataset

Softwarea	$\mathrm{Dup^b}$	$Loss^{c}$	$\mathrm{DCS^d}$	${f Runtime^e}$
Our	20534	67521	0.106953	0.679773
Notung	20534	67521	0.106967	0.855182
Treerecs	20534	57996	0.106979	0.168448

<sup>&</sup>lt;sup>a</sup> Phylogenetic software with "t" as tolerance setting.

<sup>&</sup>lt;sup>b</sup> Number of inferred duplications.

<sup>&</sup>lt;sup>c</sup> Number of inferred gene losses.

<sup>&</sup>lt;sup>d</sup> Average duplication consistency score for each gene tree.

<sup>&</sup>lt;sup>e</sup> Average runtime of computing the reconciliation for each gene tree in seconds.

# Conclusion

In this thesis, we presented two new algorithms that we implemented in an isometric reconciliation software which takes a rooted species tree with exact branch lengths and a rooted or unrooted gene tree with inexact branch lengths as an input. The output of our software is one or more reconciled gene trees with minimizing the number of duplications and gene losses.

We firstly analyse the current approach of solving the problem of reconciliation in general. We divided it into three main approaches: scoring, probabilistic and isometric gene tree reconciliation. We made an overview of existing software for the scoring and probabilistic reconciliation. We further focused on the isometric reconciliation which we subdivide into two sections. The first section is dealing with the isometric reconciliation with exact branch lengths introduced by Ma et al. [15] in 2008 and later corrected by Brejová et al. [4], who suggested extension for reconciliation of unrooted gene tree and species tree in running time  $O(N^5logN)$ . The second section is isometric reconciliation with inexact branch lengths introduced by Chládek [5] suggesting algorithms to infer the most parsimonious reconciliation for a rooted species tree and a semi-rooted or unrooted gene tree with the running time  $O(N^4logN)$ .

We built on the algorithms from [5] and created a new algorithm for rooting an unrooted gene tree. For each edge in the unrooted gene tree, it semi-roots the gene tree and subdivides the root edge by given step. The running time of the rooting algorithm is O(Nh). The second algorithm is for counting the evolutionary events in the gene tree and requires precomputed variables by the two-pass algorithm by [5]. For each node in the gene tree, we count the duplications in the gene node and gene losses on the edge from the gene node to its parent. We split the algorithm into preprocessing and the main algorithm. The running time of preprocessing is  $O(N^2)$  and of the main algorithm is O(N). Therefore, the total running time of isometric reconciliation with

our two algorithms and the two-pass algorithm [?] is  $O(N^2)$  for a rooted gene tree and  $O(N^3h)$  for an unrooted gene tree.

Created algorithms were implemented into a source code by Chládek [5] which resulted in an isometric reconciliation software with a command-line interface. We made several changes in the original source code and additions that we highlighted and described.

Eventually, we tested the implemented software on the simulated and real dataset and compared it to other software. The simulated dataset consisted of two clades with 1000 simulated gene families, where the gene trees are rooted. We run the software without and with rerooting the gene trees. Without rerooting the gene trees, we were testing the impact of different tolerance settings on the reconciliation. We found that the best tolerance needs to be by one decimal place shorter than the number of decimal places in the edge length in a rooted gene tree. Our software was the fastest in inferring the isometric reconciliation. With rerooting the gene tree, we were testing the impact of the tolerance and step settings on the reconciliation. We found the optimal tolerance and step settings for the simulated dataset. In both clades, our software infers the best solution compared to the other software two times. The real dataset consisted of 5351 alignments that we transform into unrooted trees. Our software had comparable good results with other software.

# Bibliography

- [1] Mukul Bansal. Tutorial: Treefix and treefix-dtl. Available from: http://compbio.mit.edu/treefix/tutorial.html, 2014. [Accessed 12 Jan 2021].
- [2] Bastien Boussau. Phyldog: joint reconstruction of species and gene phylogenies. Available from: https://pbil.univ-lyon1.fr/software/phyldog/, 2012. [Accessed 12 Jan 2021].
- [3] Bastien Boussau et al. Genome-scale coestimation of species and gene trees. Genome Research, 23(2):323–330, Feb. 2013.
- [4] Broňa Brejová et al. Isometric gene tree reconciliation revisited. Algorithms for Molecular Biology, 12(1):17, Jun. 2017.
- [5] Radoslav Chládek. Algorithms for isometric gene tree reconciliation. Master's thesis, Comenius University in Bratislava, 2019.
- [6] Radoslav Chládek et al. Isometric gene tree reconciliation with software.interval software.edge lengths.
- [7] Nicolas Comte et al. Treerecs: an integrated phylogenetic tool, from sequences to reconciliations. bioRxiv, Oct. 2019.
- [8] Dave Danicic et al. *Notung 2.8: A Manual*. Notung Development Team, Mar. 2015.
- [9] Jean-Philippe Doyon, Cedric Chauve, and Sylvie Hamel. Algorithms for exploring the space of gene tree/species tree reconciliations. In Nelson C.E., Vialette S. (eds) Comparative Genomics. RECOMB-CG 2008. Lecture Notes in Computer Science, volume 5267, pages 1–13. Springer-Verlag, Berlin, Heidelberg, Oct. 2008.

BIBLIOGRAPHY 56

- [10] Joseph Felsenstein. Inferring Phylogenies. Sinauer, Sunderland, 2003.
- [11] Morris Goodman et al. Fitting the gene lineage into its species lineage, a parsimony strategy illustrated by cladograms constructed from globin sequences. Systematic Zoology, 28(2):132–163, Jun. 1979.
- [12] Damir Hasić and Eric Tannier. Gene tree species tree reconciliation with gene conversion. *Journal of Mathematical Biology*, 78(6):1981–2014, May 2019.
- [13] Li Heng. Treesoft: Treebest. [online]. Available from: http://treesoft.sourceforge.net/treebest.shtml. [Accessed 12 Jan 2021].
- [14] INRIA. Tutorial treerecs. Available from: https://project.inria.fr/treerecs/tutorial/, 2011. [Accessed 12 Jan 2021].
- [15] Jian Ma et al. The infinite sites model of genome evolution. *Proceedings of the National Academy of Science*, 105(38):14254–14261, Sep. 2008.
- [16] Matthew D. Rasmussen. Spimap documentation. Available from: http://compbio.mit.edu/spimap/pub/spimap/doc/spimap-manual.html, 2011. [Accessed 12 Jan 2021].
- [17] Matthew D. Rasmussen and Manolis Kellis. A bayesian approach for fast and accurate gene tree reconstruction. *Molecular Biology and Evolution*, 28(1):273– 290, Jan. 2011.
- [18] Benjamin Vernot et al. Reconciliation with non-binary species trees. *Journal of Computational Biology*, 15(8):981–1006, Oct. 2008.
- [19] Albert J. Vilella et al. Ensembloompara genetrees: Complete, duplication-aware phylogenetic trees in vertebrates. *Genome Research*, 19(2):327–335, Feb. 2009.
- [20] Wu Yi-Chieh et al. Treefix: Statistically informed gene tree error correction using species trees. Systematic Biology, 62(1):110–120, Jan. 2013.
- [21] Wu Yi-Chieh et al. Treefix. Available from: https://www.cs.hmc.edu/~yjw/software/treefix/, 2014. [Accessed 12 Jan 2021].

# List of appendices

 $\begin{array}{c} {\rm Appendix} \ {\rm A} \mbox{ - Source code} \\ {\rm Appendix} \ {\rm B} \mbox{ - User manual} \end{array}$ 

# Appendix B - User manual

Our isometric reconciliation software has a command line interface.

# Input

The needed input for our software is a rooted species tree with exact branch lengths in Newick format and a rooted or unrooted gene tree with exact or inexact branch lengths in Newick format with mapping of gene tree leaves to the species tree leaves.

Inexact branch lengths are required in format, where minimal branch length and maximal branch length are separated with a dash "-" such as "geneName:minimalLength-maximalLength" shown in an example "cat:1.3785-2.3375".

We recognise two types of leaves mapping. The first type of leaves mapping is directly in the gene tree file, where each gene leaf name consists of the name of the gene and the name of the species to which it is mapping separated with underscore "\_" such as "geneName\_speciesName" shown in an example "cat12\_cat". The second type of leaves mapping is stored in an ".smap" file, where each gene name has assigned a species. It is a pattern-matching mapping and we consider only matching at prefix. For example, if the gene name starts always with "CAT", the mapping is "CAT\* cat", where the "\*" is optional postfix after the matching pattern and the gene leaf in a gene tree is "CAT12:0.8324".

# Output

The output of our software is a relations file or reconciled gene trees in Newick format.

The relations file recognise 4 types of relations for each node in gene tree:

BIBLIOGRAPHY 59

- "gene" for a gene node in a leaf,
- "spec" if the evolutionary event occurred on the gene node is speciation,
- "dup" if the evolutionary event occurred on the gene node is duplication,
- "loss" if the evolutionary event occurred on the gene node is gene loss.

Each relation type is written in a new line with information about the node separated with spaces, such as:

- "gene geneName", where geneName is for the name of the gene
- "spec leftChild rightChild", where leftChild is the name of a left child of the speciation node and rightChild is the name of a right child of the speciation node,
- "dup leftChild rightChild", where leftChild is the name of a left child of the duplication node and rightChild is the name of a right child of the duplication node,
- "loss node", where node is the name of a node above which the loss occurred.

Each name of an internal node of a gene tree consists of genes presented in a subtree of that node separated by commas ", ". If the the found solutions have the same relations, we print only the first and the number of reconciled trees with the same relations.

# Settings

# Running the reconciliation