

Homework 4

Free fall is a special case of motion with constant acceleration. In most real cases, the acceleration is not constant because the objects do not move through a vacuum.

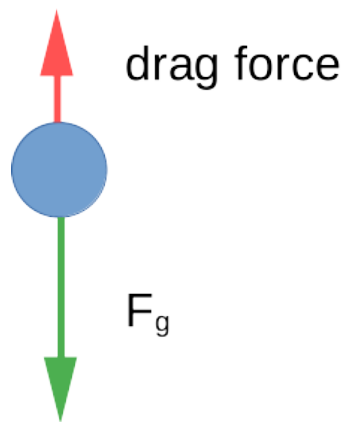
When an object moves through a fluid, it experiences a force that counteracts its motion and tends to slow it down. The fluid can be a gas (air), a liquid (water) or a solid.

Linear drag force can be written as $F_{drag} = -kv$. Two forces act on a free-falling object. Thus we write:

$$F_g + F_{drag} = ma$$

$$F_g - kv = ma = m \frac{dv}{dt}$$

See lecture notes for velocity, acceleration, and displacement in the case of a linear resisting force.



Task 1

Find the velocity, acceleration and displacement function of an object moving through a fluid and experiencing a *quadratic drag force*.

$$F_{drag} = -kv^2$$

Draw a graph of (use Matlab):

- velocity vs time
- acceleration vs time
- displacement vs time

for four different masses ($m=1, 2, 5, 10$).

Task 2

Find at what time falling object reaches 50% of its terminal velocity.

Find the solution for four different masses ($m=1, 2, 5, 10$).

Hint-Matlab code:

```
f=@(x) x.^2-10==4;  
solve(f, x)
```

```
f=@(x) x.^2-10-4==0;  
solve(f, x)
```

```
f=@(x) x.^2-16==0;  
solve(f, x)
```