

Solutions and Screenshots

A1

1.1

A data frame is a labeled two-dimensional data structure containing columns that can be of different types.

	price (grands)	bedrooms	bathrooms	sqft_living	sqft_lot \
count	21613.000000	21613.000000	21613.000000	21613.000000	2.161300e+04
mean	540.088142	3.370842	2.114757	2079.899736	1.510697e+04
std	367.127196	0.930062	0.770163	918.440897	4.142051e+04
min	75.000000	0.000000	0.000000	290.000000	5.200000e+02
25%	321.950000	3.000000	1.750000	1427.000000	5.040000e+03
50%	450.000000	3.000000	2.250000	1910.000000	7.618000e+03
75%	645.000000	4.000000	2.500000	2550.000000	1.068800e+04
max	7700.000000	33.000000	8.000000	13540.000000	1.651359e+06
	floors	waterfront	view	condition	grade \
count	21613.000000	21613.000000	21613.000000	21613.000000	21613.000000
mean	1.494309	0.007542	0.234303	3.409430	7.656873
std	0.539989	0.086517	0.766318	0.650743	1.175459
min	1.000000	0.000000	0.000000	1.000000	1.000000
25%	1.000000	0.000000	0.000000	3.000000	7.000000
50%	1.500000	0.000000	0.000000	3.000000	7.000000
75%	2.000000	0.000000	0.000000	4.000000	8.000000
max	3.500000	1.000000	4.000000	5.000000	13.000000
	sqft_above	sqft_basement	age	renovated_age \	
count	21613.000000	21613.000000	21613.000000	21613.000000	
mean	1788.390691	291.509045	45.994864	2.380882	
std	828.090978	442.575043	29.373411	12.359528	
min	290.000000	0.000000	2.000000	0.000000	
25%	1190.000000	0.000000	20.000000	0.000000	
50%	1560.000000	0.000000	42.000000	0.000000	
75%	2210.000000	560.000000	66.000000	0.000000	
max	9410.000000	4820.000000	117.000000	114.000000	
	sqft_living15	sqft_lot15			
count	21613.000000	21613.000000			
mean	1986.552492	12768.455652			
std	685.391304	27304.179631			

1.2 In python file

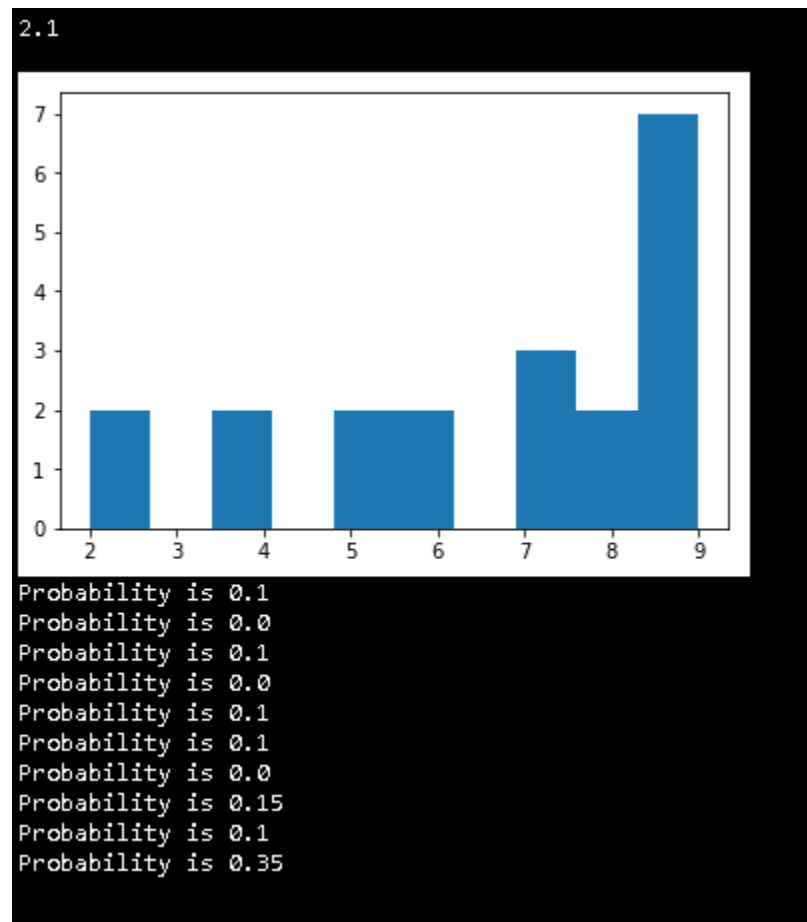
1.3 Best model obtained is with using learning rate 1.0. This wouldn't create a linear line as N dimensional is projected on to 2 d plane.

1.4 In Sol1 python file

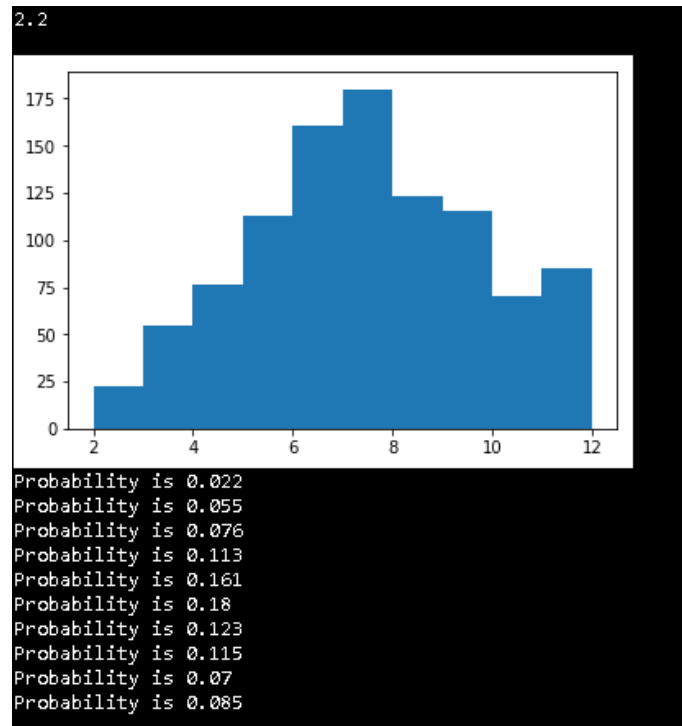
1.5 In sol1 python file

A2

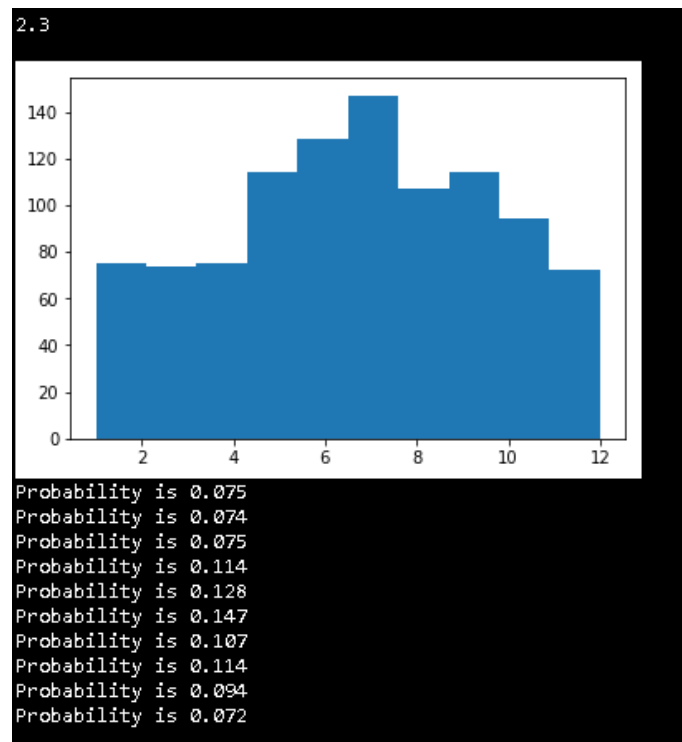
2.1



2.2



2.3



A3

Probability of sensor to be faulty $P(\text{faulty}) = 0.01$

Probability of sensor to be not faulty $P(\neg \text{faulty}) = 0.99$

Probability of getting a reading less than 1 when sensor is faulty $= P(<1 | \text{faulty}) = 1.0$

Probability of getting a reading less than 1 when sensor is not faulty $= P(<1 | \neg \text{faulty}) = .33$

$$P(\text{faulty} | <1) = \frac{P(<1 | \text{faulty}) * P(\text{faulty})}{P(<1 | \text{faulty}) * P(\text{faulty}) + P(<1 | \neg \text{faulty}) * P(\neg \text{faulty})}$$

$$\text{For 1}^{\text{st}} \text{ reading by the sensor} \quad = 1 * .01 / (1 * .01 + 1/3 * .99) = .029$$

$$\text{For 2}^{\text{nd}} \text{ consecutive reading by the sensor} \quad = 1 * .01 / (1 * .01 + 1/3 * 1/3 * .99) = .083$$

$$\text{Similarly, for 10}^{\text{th}} \text{ reading} \quad = 1 * .01 / (1 * .01 + 1/3^{10} * .99) = .998$$

$$\text{So, model will be} = 1 * .01 / (1 * .01 + 1/3^N * .99)$$

A4

The mean (μ_1) of the first class is 3 and second (μ_2) is 1. The Bell curve will intersect at 2. The standard deviation is 1. The Standard Score (z) is calculated by

$$z = (x - \mu_1) / \sigma$$

So, z will be -1. The probability of area under the curve onto the left is .1587. So, probability of remaining area is $1 - .1587 = 0.8413$. That is why the theoretical limit will be around 84%.

Another way to prove that is 68/95/99.7 rule. The first 68% area under the bell curve lies at the first standard deviation from the mean which is 0 and 2. Rest we must find the area between -1 to 0. As bell curves are symmetrical, remaining area will be half of 32% which is 16%. So, theoretical limit will be 68% + 16% = 84%

References

- [1] "Intro to Data Structures — pandas 0.20.3 documentation", Pandas.pydata.org, 2017. [Online]. Available: <https://pandas.pydata.org/pandas-docs/stable/dsintro.html>. [Accessed: 03- Oct- 2017].
- [2] "numpy.random.choice — NumPy v1.13 Manual", Docs.scipy.org, 2017. [Online]. Available: <https://docs.scipy.org/doc/numpy-1.13.0/reference/generated/numpy.random.choice.html>. [Accessed: 03- Oct- 2017].
- [3] F. Y-scaling?, "Fitting a Gaussian to a histogram with Matplotlib and Numpy - wrong Y-scaling?", Stackoverflow.com, 2017. [Online]. Available: <https://stackoverflow.com/questions/23447262/fitting-a-gaussian-to-a-histogram-with-matplotlib-and-numpy-wrong-y-scaling>. [Accessed: 03- Oct- 2017].
- [4] 2017. [Online]. Available: <http://www.stat.ufl.edu/~athienit/Tables/Ztable.pdf>. [Accessed: 03- Oct- 2017].