

Task Management System

Imagine you're developing a task management system for a company that prioritizes tasks based on urgency. A **task** is defined by a pair (**task_id**, **urgency**). Your goal is to efficiently manage these tasks using a heap structure H so that the task with **lower urgency is handled first**. Each task has a unique **task_id** and urgency, ensuring no two tasks have the same urgency level. You are assigned to perform the following:

Tasks:

- (a) **AddTask(H , task)**: Insert the given task with unique **task_id** and unique **urgency** (both positive integers $\in [1, 10^6]$) into the Heap H . After insertion, perform the necessary operations to maintain the heap property.
- (b) **UpdateUrgency(H , task_id, newValue)**: Update the urgency of the given task with **task_id** to the **newValue**. Perform the necessary operations to maintain the heap property.
- (c) **DeleteUrgency(H)**: Delete the task with the lowest urgency from H and print the corresponding **task_id**. After deletion, perform the necessary operations to maintain the heap property.
- (d) **Display(H)**: Display the current state of H as a space-separated list of **task_ids** in level-order traversal.
- (e) **PrintKthLevelMin(H , level)**: Print the **task_id** with the lowest urgency at the k -th level of H . If the k -th level does not exist, print -1 .

Assume that all task_ids and urgencies are unique at all times.

Input Format:

Each line contains a character from {'i', 'u', 'd', 'e', 'p', 'q'} followed by zero or more positive integers.

- Character 'i' is followed by two positive integers: **task_id** and **urgency**. Perform the **AddTask(H , task)** operation.
- Character 'u' is followed by two positive integers **task_id** and **newValue**. Perform the **UpdateUrgency(H , task_id, newValue)** operation.
- Character 'd' performs the **Display(H)** operation.
- Character 'e' performs the **DeleteUrgency(H)** operation.
- Character 'p' is followed by a positive integer **level**. Perform the **PrintKthLevelMin(H , level)** operation.
- Character 'q' is to terminate the sequence of operations.

Output Format:

The output (if any) of each command should be printed on a separate line. However, no output is printed for 'i' and 'q'.

- For Option 'u': Print -1 if the node is not found else print `task_id`.
- For Option 'e': Print -1 if the heap is empty else print `task_id`.
- For Option 'd': Print H as a space-separated list of `task_ids` in level-order traversal. If H is empty, print -1.
- For Option 'p': Print the `task_id`.

Sample Test Cases

Input 1:

```
i 5 60
i 6 25
d
e
i 7 85
p 1
i 8 125
i 9 10
u 8 5
d
q
```

Output 1:

```
6 5
6
7
8
8 5 9 7
```

Input 2:

```
i 31 70
i 32 85
i 33 50
d
u 31 45
i 34 95
i 35 30
```

p 2
u 35 110
d
e
q

Output 2:

33 32 31
31
32
35
31 32 33 34 35
31