

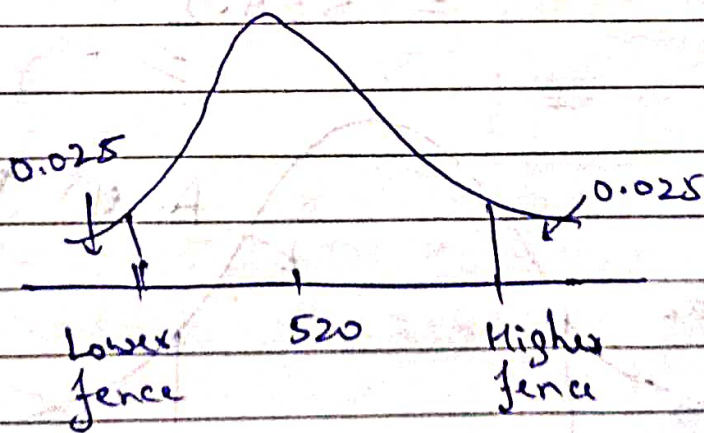
Q. In the Quant test of CAT exam, the population standard deviation is known to be 100. A sample of 25 test takers has a mean of 520. Construct a 95% CI about mean.

Sol $\sigma = 100$ $n = 25$ $\bar{x} = 520$

C.I. = 95%

$\alpha = 1 - 0.95$

~~$\alpha = 0.025$~~ $\alpha = 0.05$



Point Estimate \pm Margin of Error

$$\bar{x} \pm Z_{\alpha/2} \boxed{\frac{\sigma}{\sqrt{n}}} \Rightarrow \text{Standard Error}$$



z-score table
z-test

$$Z_{\alpha/2} = Z_{0.05/2} = Z_{0.025} = 1.96$$

$$\text{Lower fence} = \bar{x} - Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$= 520 - 1.96 \frac{100}{\sqrt{25}}$$

$$= 520 - 1.96 \times 20$$

$$= 480.8$$

$$\text{Higher fence} = \bar{x} + Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$= 520 + 1.96 \frac{100}{\sqrt{25}}$$

$$= 520 + 1.96 \times 20$$

$$= 559.2$$

