

Data Structures 2018

Exercise 5, solutions (Week 41)

- 1.-3. The example solution can be found in LinkedList.java file located in the exercise folder of the course home page.
4. a) 7, 1, 0, 3, 2, 5, 4, 6, 9, 8, 10
 b) 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10
 c) 0, 2, 4, 6, 5, 3, 1, 8, 10, 9, 7
5. Algoritmi 1.

Algorithm 1 Printing binary tree in postorder with the help of stack

PrintPostOrder(n)

 Create new stack S

$S.push(n)$

repeat

$n \leftarrow S.top()$

if $n.isInternal()$ **then**

$S.push(flagNode)$

$S.push(n.rightChild)$

$S.push(n.leftChild)$

else if $n.isFlagNode$ **then**

$S.pop()$

$n \leftarrow S.pop()$

 Print n

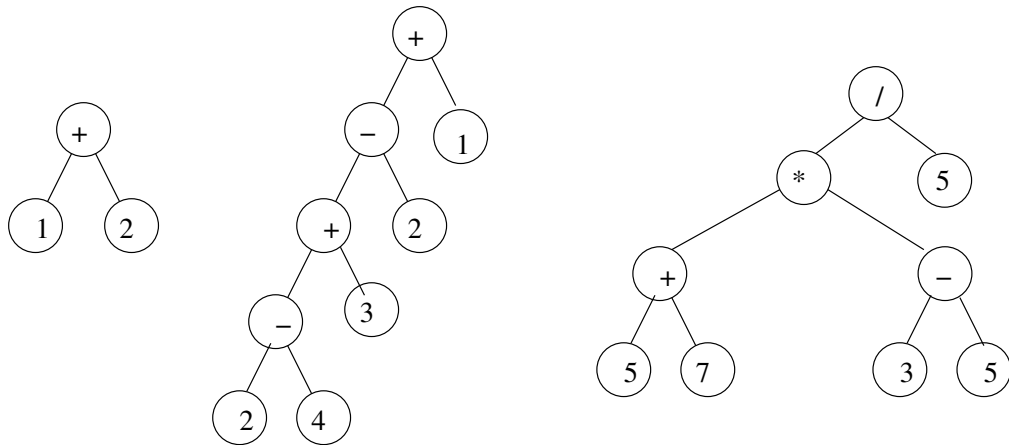
else

 Print n

$S.pop()$

end if

until S is empty



6.

7. (a) Algorithm 2

(b) Algorithm 3

(c) Algorithm 4

Algorithm 2 Computes the number of nodes (root node is given as a parameter).

CountNodes(N)

if $N.isLeaf()$ **then**

return 1

else

return 1 + CountNodes($N.leftChild$) + CountNodes($N.rightChild$)

end if

Algorithm 3 Counts the number of leaf nodes (the root node is given as a parameter).

CountLeaves(N)

if $N.isLeaf()$ **then**

return 1

else

return CountLeaves($N.leftChild$) + CountLeaves($N.rightChild$)

end if

Algorithm 4 Computes the height of a tree.

Height(N)

```
    if  $N.isLeaf()$  then
        return 0
    else
        return  $1 + \max\{\text{Height}(N.leftChild), \text{Height}(N.rightChild)\}$ 
    end if
```

8. Algorithm 5.

Algorithm 5 Calculates the number of nodes in the level k of a binary tree. r is the root node of the binary tree.

LevelNodes(k, r)

```
    if  $r = \text{NULL}$  then
        return 0
    else
        if  $k = 0$  then
            return 1
        else
            return LevelNodes( $k - 1, r.leftChild$ ) + LevelNodes( $k - 1, r.rightChild$ )
        end if
    end if
```
