

$f(x) = \lambda \exp\{-\lambda x\}$ $I(x)$ ; $E(X) = \frac{1}{\lambda}$ ; $E(X^k) = \frac{k!}{\lambda^k}$ ; $K(X) = 6$ ;	<ul style="list-style-type: none"><li><math>X \sim Exp(\lambda) \Rightarrow Y = \lambda X \sim Exp(1)</math></li><li><math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim Exp(\lambda) \Rightarrow Y = \min\{X_1, \dots, X_n\} \sim Exp(n\lambda)</math></li><li><math>X_1, X_2</math> i.i.d. com <math>X_i \sim Exp(\lambda) \Rightarrow Y = X_1 - X_2 \sim La(0, \lambda)</math></li><li><math>X \sim Exp(\lambda) \Leftrightarrow X \sim Gama(1, \lambda)</math></li><li><math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim Exp(\lambda) \Rightarrow Y = \sum_{i=1}^n X_i \sim Gama(n, \lambda)</math></li></ul>
$F(x) = 1 - \exp\{-\lambda x\}$ $I(x)$ ; $x_p = \frac{-\ln(1-p)}{\lambda}$ ; $Var(X) = \frac{1}{\lambda^2}$ ;	
$Mo(X) = 0$ ; $M_X(t) = \frac{\lambda}{\lambda - t}, t < \lambda$ ; $A(X) = 2$ ; $Med(X) = \frac{\ln 2}{\lambda}$ ;	

<b>Weibull I</b> $[W_1(a, b), a > 0, b > 0]$	<b>Weibull II</b> $[W_2(\theta, \lambda), \theta > 0, \lambda > 0]$	<ul style="list-style-type: none"><li><math>X \sim Rayleigh(\beta) \Leftrightarrow X \sim W_1(1/2\beta^2, 2)</math></li><li><math>X \sim W_1(\lambda^{-1/\theta}, \theta) \Leftrightarrow X \sim W_2(\lambda, \theta)</math></li><li><math>X \sim W_1(\lambda, 1) \Leftrightarrow X \sim Exp(\lambda)</math></li><li><math>X \sim W_1(a, b)</math> e <math>Y = -\ln X \Rightarrow Y \sim Gumbel(b^{-1} \ln a, b^{-1})</math></li></ul>
$f(x) = abx^{b-1} \exp\{-ax^b\}$ $I(x)$ ; $Med(X) = (\frac{\ln 2}{a})^{1/b}$ ;	$f(x) = (\frac{\theta}{\lambda})(\frac{x}{\lambda})^{\theta-1} \exp\{-(\frac{x}{\lambda})^\theta\}$ $I(x)$ ;	
$Mo(X) = (\frac{b-1}{ab})^{1/b}$ ; $F(x) = 1 - \exp\{-ax^b\}$ $I(x)$ ;	$F(x) = 1 - \exp\{-(\frac{x}{\lambda})^\theta\}$ $I(x)$ ;	
$Var(X) = a^{\frac{2}{b}}[\Gamma(1 + \frac{2}{b}) - \Gamma^2(1 + \frac{1}{b})]$ ;	$E(X^k) = \lambda^k \Gamma(1 + \frac{k}{\theta})$ ;	
$x_p = [-\frac{\ln(1-p)}{a}]^{\frac{1}{b}}$ ; $E(X^k) = a^{\frac{-k}{b}} \Gamma(1 + \frac{k}{b})$ ;	$Var(X) = \lambda^2[\Gamma(1 + \frac{2}{\theta}) - \Gamma^2(1 + \frac{1}{\theta})]$ ;	

<b>Normal</b> $[N(\mu, \sigma^2), \mu \in \mathbb{R}, \sigma > 0]$	<ul style="list-style-type: none"><li><math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim N(0, 1) \Rightarrow Y = \sum_{i=1}^n X_i^2 \sim \chi_{(n)}^2</math></li><li><math>X \sim N(\mu, \sigma^2) \Rightarrow Y = (X - \mu)/\sigma \sim N(0, 1)</math></li><li><math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim N(\mu, \sigma^2) \Rightarrow Y = \sum_{i=1}^n a_i X_i \sim N(\mu \sum_{i=1}^n a_i, \sigma^2 \sum_{i=1}^n a_i^2)</math></li><li><math>X_1, X_2</math> i.i.d. com <math>X_i \sim N(0, 1) \Rightarrow Y = \frac{X_1}{X_2} \sim Ca(0, 1)</math></li></ul>
$f(x) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\{-\frac{(x-\mu)^2}{2\sigma^2}\}$ $I(x)$ ; $E[(X - E(X))^k] = \begin{cases} 0, & \text{se } k \text{ é ímpar} \\ \frac{\sigma^k k!}{2^{k/2} \Gamma(1 + \frac{k}{2})}, & \text{se } k \text{ é par} \end{cases}$	
$A(X) = K(X) = 0$ ; $M_X(t) = e^{\mu t + \sigma^2 \frac{t^2}{2}}$ ; $E(X) = Med(X) = Mo(X) = \mu$ ; $Var(X) = \sigma^2$ ;	

<b>Uniforme</b> $[U(a, b), -\infty < a < b < \infty]$	<ul style="list-style-type: none"><li><math>X \sim U(0, 1) \Rightarrow Y = 1 - X^{\frac{1}{n}} \sim Beta(1, n)</math></li><li><math>X \sim U(0, 1) \Rightarrow Y = X^2 \sim Beta(1/2, 1)</math></li><li><math>X \sim U(0, 1) \Rightarrow Y = -\frac{\ln X}{\lambda} \sim Exp(\lambda)</math></li><li><math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim U(0, 1) \Rightarrow Y = \min\{X_1, \dots, X_n\} \sim Beta(1, n)</math> e <math>Z = \max\{X_1, \dots, X_n\} \sim Beta(n, 1)</math></li><li><math>X \sim U(0, 1) \Rightarrow Y = tg[\pi(x - \frac{1}{2})] \sim Ca(0, 1)</math></li></ul>
$F(x) = \begin{cases} 0, & \text{se } x < a \\ \frac{x-a}{b-a}, & \text{se } a \leq x < b \\ 1, & \text{se } x \geq b \end{cases}$ $f(x) = \frac{1}{(b-a)} I(x)$ ; $E(X) = Med(X) = \frac{a+b}{2}$ ; $Var(X) = \frac{(b-a)^2}{12}$ ;	
$E(X^k) = \sum_{i=0}^k \frac{a^{k-i} b^i}{k+1}$ ; $E[(X - E(X))^k] = \begin{cases} 0, & \text{se } k \text{ é ímpar} \\ \frac{(b-a)^k}{2^k(k+1)}, & \text{se } k \text{ é par} \end{cases}$	
$M_X(t) = \frac{e^{tb} - e^{ta}}{t(b-a)}$ ; $A(X) = 0$ ; $K(X) = -\frac{6}{5}$ ;	

<b>Rayleigh</b> $[Rayleigh(\sigma), \sigma > 0]$	<ul style="list-style-type: none"><li><math>X \sim Rayleigh(1) \Leftrightarrow X \sim \chi_{(2)}^2</math></li><li><math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim Rayleigh(\sigma) \Rightarrow Y = \sum_{i=1}^n X_i^2 \sim Gama(n, 2\sigma^2)</math></li></ul>
$f(x) = \frac{x}{\sigma^2} \exp\{-\frac{x^2}{2\sigma^2}\}$ $I(x)$ ; $F(x) = 1 - \exp\{-\frac{x^2}{2\sigma^2}\}$ $I(x)$ ; $A(X) = \frac{(\pi-3)\sqrt{\frac{\pi}{2}}}{(2-\frac{\pi}{2})^{\frac{3}{2}}}$ ; $Var(X) = \frac{\sigma^2(4-\pi)}{2}$ ;	
$Med(X) = \sigma \sqrt{\ln 4}$ ; $E(X^k) = 2^{\frac{k}{2}} \sigma^k \Gamma(\frac{k}{2} + 1)$ ; $E(X) = \sigma \sqrt{\frac{\pi}{2}}$ ; $K(X) = \frac{8-3\pi^2}{(2-\frac{\pi}{2})^2} - 3$ ; $Mo(X) = \sigma$ ;	

<b>Pareto</b> $[Pareto(\alpha, \beta), \alpha > 0, \beta > 0]$	<ul style="list-style-type: none"><li><math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim Pareto(\alpha, \beta) \Rightarrow Y = \min\{X_1, \dots, X_n\} \sim Pareto(n\alpha, \beta)</math></li><li><math>X \sim Pareto(\alpha, \beta) \Rightarrow Y = \ln(\frac{X}{\beta}) \sim Exp(\alpha)</math></li></ul>
$f(x) = \frac{\alpha \beta^\alpha}{x^{\alpha+1}} I(x)$ ; $F(x) = 1 - (\frac{\beta}{x})^\alpha I(x)$ ; $E(X^k) = \frac{\alpha \beta^k}{\alpha - k}$ ; $Var(X) = \frac{\alpha \beta^2}{(\alpha - 2)(\alpha - 1)^2}$ ;	
$x_p = \frac{\beta}{\sqrt[p]{1-p}}$ ; $Med(X) = \beta \sqrt[p]{2}$ ; $A(X) = \frac{2(\alpha+1)}{\alpha-3} \sqrt{\frac{\alpha-2}{\alpha}}$ ; $K(X) = \frac{6(\alpha^3 + \alpha^2 - 6\alpha - 2)}{\alpha(\alpha-3)(\alpha-4)}$ ; $Mo(X) = \beta$ ;	

<b>Log – Normal</b> $[LN(\mu, \sigma), \mu \in \mathbb{R}, \sigma > 0]$	<ul style="list-style-type: none"><li><math>X \sim LN(\mu, \sigma) \Rightarrow Y = \ln X \sim N(\mu, \sigma^2)</math></li><li><math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim LN(\mu, \sigma) \Rightarrow Y = \prod_{i=1}^n X_i \sim LN(n\mu, \sqrt{n}\sigma)</math></li></ul>
$f(x) = \frac{1}{x\sqrt{2\pi\sigma^2}} \exp\{-\frac{(\ln x - \mu)^2}{2\sigma^2}\}$ $I(x)$ ; $E(X^k) = e^{k\mu + \frac{k^2\sigma^2}{2}}$ ; $Var(X) = e^{2\mu + \sigma^2}(e^{\sigma^2} - 1)$ ;	
$Med(X) = \mu$ ; $Mo(X) = e^{\mu - \sigma^2}$ ; $A(X) = (e^{\sigma^2} + 2)\sqrt{e^{\sigma^2} - 1}$ ; $K(X) = e^{4\sigma^2} + 2e^{3\sigma^2} + 3e^{2\sigma^2} - 6$ ;	

<b>Cauchy</b> $[Ca(a, b), a \in \mathbb{R}, b > 0]$	<ul style="list-style-type: none"><li><math>X \sim Ca(a, b) \Rightarrow Y = cX + d \sim Ca(ac + d, b c )</math></li><li><math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim Ca(a_i, b_i) \Rightarrow Y = \sum_{i=1}^n X_i \sim Ca(\sum_{i=1}^n a_i, \sum_{i=1}^n b_i)</math></li><li><math>X \sim Ca(0, 1) \Rightarrow Y = \frac{2X}{1-X^2} \sim Ca(0, 1)</math></li><li><math>X \sim Ca(0, b) \Rightarrow Y = 1/X \sim Ca(0, \frac{1}{b})</math></li></ul>
$f(x) = \frac{1}{\pi b [1 + (\frac{x-a}{b})^2]} I(x)$ ; $F(x) = \frac{1}{2} + tg^{-1}(\frac{x-a}{b})$ ;	
$Med(X) = a$ ; $C_X(t) = e^{iat - b t }$ ; $E(X^k) = indefinido$ ; $Mo(X) = a$ ;	

<b>Gama</b> $[Gama(\alpha, \beta), \alpha > 0, \beta > 0]$	<ul style="list-style-type: none"><li><math>X \sim Gama(\frac{n}{2}, \frac{1}{2}) \Leftrightarrow X \sim \chi_{(n)}^2</math></li><li><math>X \sim Maxwell(a) \Rightarrow Y = X^2 \sim Gama(\frac{3}{2}, \frac{1}{2a^2})</math></li><li><math>X_1, X_2</math> ind. com <math>X_1 \sim Gama(\alpha, \beta)</math> e <math>X_2 \sim Gama(\theta, \beta) \Rightarrow Y = \frac{X_1}{X_1 + X_2} \sim Beta(\alpha, \theta)</math></li></ul>
$f(x) = \frac{\beta^\alpha}{\Gamma(\alpha)} x^{\alpha-1} e^{-\beta x} I(x)$ ; $E(X^k) = \frac{\Gamma(\alpha+k)}{\Gamma(\alpha)\beta^k}$ ; $E(X) = \frac{\alpha}{\beta}$ ; $Var(X) = \frac{\alpha}{\beta^2}$ ;	
$A(X) = \frac{2}{\sqrt{\alpha}}$ ; $K(X) = \frac{6}{\alpha}$ ; $M_X(t) = (\frac{\beta}{\beta-t})^\alpha, t < \beta$ ; $Mo(X) = \frac{\alpha-1}{\beta}$ ;	

<b>Beta</b> $[Beta(a, b), a > 0, b > 0]$	<ul style="list-style-type: none"><li><math>X \sim Beta(a, b) \Rightarrow Y = 1 - X \sim B(b, a)</math></li><li><math>X \sim Beta(a, b) \Rightarrow Y = \frac{X}{1-X} \sim Beta\ Prime(a, b)</math></li><li><math>X \sim Beta(\frac{n}{2}, \frac{m}{2}) \Rightarrow Y = \frac{mX}{n(1-X)} \sim F(n, m)</math></li><li><math>X \sim Beta(a, 1) \Rightarrow Y = -\ln X \sim Exp(a)</math></li></ul>
$f(x) = \frac{1}{B(a, b)} x^{a-1} (1-x)^{b-1} I(x)$ ; $E(X^k) = \frac{\Gamma(a+b)\Gamma(a+k)}{\Gamma(a+b+k)\Gamma(a)}$ ; $Var(X) = \frac{ab}{(a+b)^2(a+b+1)}$ ;	
$E(X) = \frac{a}{a+b}$ ; $Mo(X) = \frac{a-1}{a+b+2}$ ; $A(X) = \frac{2(b-a)\sqrt{a+b+1}}{(a+b+2)\sqrt{ab}}$ ; $K(X) = \frac{3(a+b+1)[2(a+b)^2 + ab(a+b+6)]}{ab(a+b+2)(a+b+3)}$ ;	

<b>Qui – Quadrado</b> $[\chi_{(n)}^2, n > 0]$	<ul style="list-style-type: none"><li><math>X \sim \chi_{(2)}^2 \Leftrightarrow X \sim Exp(\frac{1}{2})</math></li><li><math>X_1 \sim \chi_{(n)}^2</math> e <math>X_2 \sim \chi_{(m)}^2 \Rightarrow Y = \frac{X_1/n}{X_2/m} \sim F(n, m)</math></li><li><math>X \sim \chi_{(n)}^2</math> e <math>c &gt; 0 \Rightarrow Y = \frac{X}{c} \sim Gama(\frac{n}{2}, \frac{c}{2})</math></li><li><math>X_1, \dots, X_n</math> ind. com <math>X_i \sim \chi_{(n_i)}^2 \Rightarrow Y = \sum_{i=1}^n X_i \sim \chi_{(\sum_{i=1}^n n_i)}^2</math></li></ul>
$f(x) = \frac{(\frac{1}{2})^{\frac{n}{2}}}{\Gamma(\frac{n}{2})} x^{\frac{n}{2}-1} e^{-\frac{x}{2}} I(x)$ ; $E(X^k) = 2^k \frac{\Gamma(k + \frac{n}{2})}{\Gamma(\frac{n}{2})}$ ; $E(X) = n$ ; $Var(X) = 2n$ ;	
$A(X) = \sqrt{\frac{8}{n}}$ ; $K(X) = \frac{12}{n}$ ; $M_X(t) = (1 - 2t)^{-\frac{n}{2}}$ ; $Mo(X) = n - 2, n > 2$ ;	

<b>t – Student</b> $[t(n), n > 0]$	<ul style="list-style-type: none"><li><math>X \sim t(1) \Leftrightarrow X \sim Ca(0, 1)</math></li><li><math>X_1 \sim N(0, 1)</math> e <math>X_2 \sim \chi_{(n)}^2</math>, ind. <math>\Rightarrow Y = \frac{X_1}{\sqrt{X_2/n}}</math></li><li><math>X \sim t(n) \Rightarrow Y = X^2 \sim F(1, n)</math></li></ul>
$f(x) = \frac{\Gamma(\frac{n+1}{2})}{\Gamma(\frac{n}{2})\sqrt{\pi n}} \left(1 + \frac{x^2}{n}\right)^{-\frac{(n+1)}{2}} I(x)$ ; $E(X^k) = \begin{cases} 0, & \text{se } k \text{ é ímpar} \\ \frac{\Gamma(\frac{k+1}{2})\Gamma(\frac{n-k}{2})n^{\frac{k}{2}}}{\sqrt{\pi}\Gamma(\frac{n}{2})}, & \text{se } k \text{ é par} \end{cases}$	
$Mo(X) = Med(X) = 0$ ; $Var(X) = \frac{6}{(n-2)}, n > 2$ ; $A(X) = 0, n > 3$ ; $K(X) = \frac{6}{n-4}, n > 4$ ;	

<b>F – Snedecor</b> $[F(n, m), n > 0, m > 0]$	<ul style="list-style-type: none"><li><math>X \sim F(n, m) \Rightarrow Y = \frac{n \frac{X}{m}}{1 + n \frac{X}{m}} \sim B(\frac{n}{2}, \frac{m}{2})</math></li><li><math>X \sim F(n, m) \Rightarrow Y = \lim_{m \rightarrow \infty} nX \sim \chi_{(n)}^2</math></li><li><math>X \sim F(n, m) \Rightarrow Y = X^{-1} \sim F(m, n)</math></li><li>e <math>x_p = \frac{1}{y_{1-p}}</math></li></ul>
$f(x) = \frac{n^{\frac{n}{2}} m^{\frac{m}{2}} x^{\frac{n}{2}-1}}{B(\frac{n}{2}, \frac{m}{2})(m+nx)^{\frac{n+m}{2}}} I(x)$ ; $E(X^k) = \frac{(\frac{m}{n})^k \Gamma(\frac{n}{2} + k) \Gamma(\frac{m-k}{2})}{\Gamma(\frac{n}{2}) \Gamma(\frac{m}{2})}$ ; $Var(X) = \frac{2m^2(n+m-2)}{n(m-2)^2(m-4)}, m > 4$ ;	
$Mo(X) = \frac{m(n-2)}{n(m+2)}$ ; $A(X) = \frac{(2n+m-2)\sqrt{8(m-4)}}{(m-6)\sqrt{n(n+m-2)}}$ , $m > 6$ ; $K(X) = \frac{12[(m-2)^2(m-4) + n(n+m-2)(5m-22)]}{n(m-6)(m-8)(n+m-2)}$ , $m > 8$ ;	

$f(x) = \frac{1}{2b}e^{-\frac{ x-a }{b}} \underset{(-\infty, \infty)}{I(x)} \quad ; \quad M_X(t) = \frac{e^{at}}{1-(bt)^2}, \quad  t  < \frac{1}{b}; \quad F(x) = \begin{cases} \frac{1}{2}e^{\frac{x-a}{b}}, & \text{se } x < a \\ 1 - \frac{1}{2}e^{-\frac{x-a}{b}}, & \text{se } x \geq a \end{cases}$	<ul style="list-style-type: none"><li>◦ <math>X \sim La(a, b) \Rightarrow Y = cX + d \sim La(ca + d, cb)</math></li><li>◦ <math>X \sim La(a, b) \Rightarrow Y =  X - a  \sim Exp(1/b)</math></li><li>◦ <math>X_1, X_2</math> i.i.d. com <math>X_i \sim La(a, b) \Rightarrow Y = \frac{ X_1 - a }{ X_2 - a } \sim F(2, 2)</math></li><li>◦ <math>X_1 X_2 \sim N(a, X_2)</math> com <math>X_2 \sim Rayleigh(b) \Rightarrow X_1 \sim La(0, 1)</math></li><li>◦ <math>X_1, X_2</math> i.i.d. com <math>X_i \sim U(0, 1) \Rightarrow Y = \ln(X_1/X_2) \sim La(0, 1)</math></li></ul>
$\mathbb{E}[(X - \mathbb{E}(X))^k] = \begin{cases} 0, & \text{se } k \text{ é ímpar} \\ k!b^k, & \text{se } k \text{ é par} \end{cases} \quad \mathbb{E}(X) = Med(X) = Mo(X) = a; \\ A(X) = 0; \quad K(X) = 1, 2; \quad Var(X) = \frac{(b\pi)^2}{3};$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Logística</b> [Logística(a, b), a ∈ ℝ, b > 0]	<ul style="list-style-type: none"><li>◦ <math>X \sim Logística(a, b) \Rightarrow Y = cX + d \sim Logística(ca + d, cb)</math></li><li>◦ <math>X \sim U(0, 1) \Rightarrow Y = a + b(\ln(X) - \ln(1 - X)) \sim Logística(a, b)</math></li><li>◦ <math>X \sim Exp(1) \Rightarrow Y = a - b \ln(\frac{e^{-X}}{1-e^{-X}}) \sim Logística(a, b)</math></li><li>◦ <math>X_1, X_2</math> i.i.d. com <math>X_i \sim Exp(1) \Rightarrow Y = a - b \ln(\frac{X_1}{X_2}) \sim Logística(a, b)</math></li></ul>
$f(x) = \frac{\exp\{-\frac{(x-a)/b}{(b-a)\exp\{-(x-a)/b\}}\}}{b(1+\exp\{-(x-a)/b\})^2} \underset{(-\infty, \infty)}{I(x)} \quad ; \quad F(X) = (1 + \exp\{-(x-a)/b\})^{-1};$ $\mathbb{E}(X) = Med(X) = Mo(X) = a; \quad M_X(t) = e^{at}B(1-bt, 1+bt);$ $A(X) = 0; \quad K(X) = 1, 2; \quad Var(X) = \frac{(b\pi)^2}{3};$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Triangular</b> [Tri(a, c, b), ∞ < a ≤ c ≤ b < ∞, a < b]	<ul style="list-style-type: none"><li>◦ <math>X_1, X_2</math> i.i.d. com <math>X_i \sim U(0, 1) \Rightarrow Y = \frac{X_1+X_2}{2} \sim Tri(0, \frac{1}{2}, 1)</math></li></ul>
$f(x) = \frac{2(x-a)}{(b-a)(c-a)} \underset{(a,c)}{I(x)} + \frac{2(b-x)}{(b-a)(b-c)} \underset{(c,b)}{I(x)} ; \mathbb{E}(X) = \frac{a+b+c}{3}; \quad Med(X) = \begin{cases} a + \frac{\sqrt{(b-a)(c-a)}}{\sqrt{2}}, & \text{se } c \geq \frac{a+b}{2} \\ b - \frac{\sqrt{(b-a)(b-c)}}{\sqrt{2}}, & \text{se } c \leq \frac{a+b}{2} \end{cases}$ $F(x) = \frac{(x-a)^2}{(b-a)(c-a)} \underset{(a,c)}{I(x)} + (1 - \frac{(b-x)^2}{(b-a)(b-c)}) \underset{(c,b)}{I(x)} + \underset{(b,\infty)}{I(x)} ; \quad Var(X) = \frac{a^2+b^2+c^2-ac-ab-bc}{18}; \quad Mo(X) = c;$ $M_X(t) = \frac{2(b-c)e^{at} - (b-a)e^{ct} + (c-a)e^{bt}}{t^2(b-a)(c-a)(b-c)};$ $A(X) = \frac{\sqrt{2}(a+b-2c)(2a-b-c)(a-2b+c)}{5(a^2+b^2+c^2-ab-ac-bc)^{3/2}};$ $K(X) = -\frac{3}{5};$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Kumaraswamy</b> [Kum(a, b), a > 0, b > 0]	<ul style="list-style-type: none"><li>◦ <math>X \sim U(0, 1) \Rightarrow Y = (1 - (1 - X)^{\frac{1}{b}})^{\frac{1}{a}} \sim Kum(a, b)</math></li><li>◦ <math>X \sim Kum(a, 1) \Rightarrow Y = (1 - X) \sim Kum(1, a)</math></li><li>◦ <math>X \sim Kum(1, 1) \Leftrightarrow X \sim U(0, 1)</math></li><li>◦ <math>X \sim Kum(a, 1) \Rightarrow Y = -\ln(X) \sim Exp(a)</math></li></ul>
$f(x) = abx^{a-1}(1-x^a)^{b-1} \underset{(0,1)}{I(x)} ; \quad F(x) = 1 - (1-x^a)^b \underset{(0,1)}{I(x)} + \underset{(1,\infty)}{I(x)} ; \quad \mathbb{E}(X^k) = bB(1+\frac{k}{a}, b);$ $Mo(X) = (\frac{a-1}{ab-1})^{1/a}; \quad Med(X) = (1 - 2^{-1/b})^{1/a}; \quad Var(X) = bB(1+\frac{2}{a}, b) - b^2B(1+\frac{1}{a}, b)^2;$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Beta Prime</b> [Beta Prime(a, b), a > 0, b > 0]	<ul style="list-style-type: none"><li>◦ <math>X \sim Beta\ Prime(a, b) \Rightarrow Y = \frac{1}{X} \sim B(b, a)</math></li><li>◦ <math>X \sim F(a, b) \Rightarrow Y = \frac{a}{b}X \sim Beta\ Prime(\frac{a}{2}, \frac{b}{2})</math></li><li>◦ <math>X_1, X_2</math> ind. com <math>X_i \sim G(a_i, 1) \Rightarrow Y = \frac{X_1}{X_2} \sim Beta\ Prime(a_1, a_2)</math></li></ul>
$f(x) = \frac{x^{a-1}}{B(a,b)(x+1)^{a+b}} \underset{(0,\infty)}{I(x)} ; \quad \mathbb{E}(X^k) = \frac{B(a+k,b-k)}{B(a,b)};$ $Mo(X) = \frac{a-1}{b+1}, \quad a \geq 1; \quad A(X) = \frac{2(2a+b-1)}{b-3} \sqrt{\frac{b-2}{a(a+b-1)}}, \quad b > 3;$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Binomial</b> [Bin(n, p), n ∈ ℕ, 0 ≤ p ≤ 1]	<ul style="list-style-type: none"><li>◦ <math>X \sim Bin(1, p) \Leftrightarrow X \sim Ber(p)</math></li><li>◦ <math>X_1, \dots, X_n</math> i.i.d com <math>X_i \sim Ber(p) \Rightarrow Y = \sum_{i=1}^n X_i \sim Bin(n, p)</math></li><li>◦ <math>X_1, \dots, X_n</math> ind com <math>X_i \sim Bin(n_i, p) \Rightarrow Y = \sum_{i=1}^n X_i \sim Bin(\sum_{i=1}^n n_i, p)</math></li></ul>
$\mathbb{P}(X = x) = \binom{n}{x}p^x(1-p)^{n-x} \underset{\{0,\dots,n\}}{I(x)} ; \quad \mathbb{E}(X) = np; \quad M_X(t) = (pe^t + 1 - p)^n; \quad \mathbb{E}[\frac{X!(n-k)!}{(X-k)!n!}] = p^k;$ $Med(X) = \lfloor \frac{np}{2} \rfloor \text{ ou } \lceil \frac{np}{2} \rceil; \quad Mo(X) = \lfloor (n+1)p \rfloor \text{ ou } \lceil (n+1)p \rceil; \quad Var(X) = np(1-p); \quad A(X) = \frac{1-2p}{\sqrt{np(1-p)}}; \quad K(X) = \frac{1-6p(1-p)}{np(1-p)^2};$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Geométrica I</b> [G0(p), 0 ≤ p ≤ 1]	<b>Geométrica II</b> [G1(p), 0 ≤ p ≤ 1]	<ul style="list-style-type: none"><li>◦ <math>X_1, \dots, X_n</math> ind. com <math>X_i \sim G_1(p_i) \Rightarrow Y = \min_{i=1,\dots,n} \{X_i\} \sim G_1(1 - \prod_{i=1}^n (1 - p_i))</math></li><li>◦ <math>X \sim Exp(\lambda) \Rightarrow Y = \lfloor X \rfloor \sim G_0(1 - e^{-\lambda})</math></li><li>◦ <math>X_1, \dots, X_r</math> i.i.d. com <math>X_i \sim G_0(p) \Rightarrow Y = \sum_{i=1}^r X_i \sim BN(r, p)</math></li></ul>
$\mathbb{P}(X = x) = p(1-p)^x \underset{\{0,1,\dots\}}{I(x)} ; \quad M_X(t) = \frac{p}{1-(1-p)e^t};$ $Mo(X) = 0; \quad F(x) = 1 - (1-p)^{x+1}; \quad \mathbb{E}(X) = \frac{1-p}{p};$ $A(X) = \frac{2-p}{\sqrt{1-p}}; \quad K(X) = 6 + \frac{p^2}{1-p}; \quad Var(X) = \frac{1-p}{p^2};$	$\mathbb{P}(X = x) = p(1-p)^{x-1} \underset{\{1,2,\dots\}}{I(x)} ; \quad M_X(t) = \frac{pe^t}{1-(1-p)e^t};$ $Mo(X) = 1; \quad F(x) = 1 - (1-p)^x; \quad \mathbb{E}(X) = \frac{1}{p};$ $A(X) = \frac{2-p}{\sqrt{1-p}}; \quad K(X) = \frac{6-6p+p^2}{(1-p)}; \quad Var(X) = \frac{1-p}{p^2};$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Binomial Negativa</b> [BN(r, p), r > 0, 0 ≤ p ≤ 1]	<b>Pascal</b> [Pa(r, p), r ∈ ℕ, 0 ≤ p ≤ 1]	<ul style="list-style-type: none"><li>◦ <math>X \sim Pa(1, p) \Leftrightarrow X \sim G_1(p)</math></li><li>◦ <math>X \sim BN(r, p)</math> e <math>\lambda = \frac{rp}{1-p} \Rightarrow X \sim Po(\lambda)</math>, quando <math>r \rightarrow \infty</math></li></ul>
$\mathbb{P}(X = x) = \frac{\Gamma(r+x)}{\Gamma(x+1)\Gamma(r)}p^r(1-p)^x \underset{\{0,1,\dots\}}{I(x)} ; \quad K(X) = \frac{p^2+6(1-p)}{r(1-p)};$ $\mathbb{E}(X) = \frac{r(1-p)}{p}; \quad Var(X) = \frac{r(1-p)}{p^2}; \quad \mathbb{E}[\frac{X!}{(X-k)!}] = \frac{(r+k-1)!(1-p)^k}{(r-1)!p^k};$ $A(X) = \frac{2-p}{\sqrt{r(1-p)}}; \quad M_X(t) = (\frac{p}{1-(1-p)e^t})^r; \quad Mo(X) = \lfloor \frac{(r-1)(1-p)}{p} \rfloor;$	$\mathbb{P}(X = x) = \binom{x-1}{r-1}p^r(1-p)^{x-r} \underset{\{r,r+1,\dots\}}{I(x)} ; \quad A(X) = \frac{2-p}{\sqrt{r(1-p)}};$ $\mathbb{E}[\frac{(X+k)!}{(X-1)!}] = \frac{(k+r)!}{(r-1)!p^{k+r}}; \quad K(X) = \frac{6-6p+p^2}{r(1-p)};$ $\mathbb{E}(X) = \frac{r}{p}; \quad M_X(t) = (\frac{pe^t}{1-(1-p)e^t})^r; \quad Var(X) = \frac{r(1-p)}{p^2};$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Uniforme Discreta</b> [UD(n), n ∈ ℕ]	<ul style="list-style-type: none"><li>◦ <math>X \sim Beta\ Binomial(n-1, 1, 1) \Leftrightarrow X \sim UD(n)</math></li></ul>
$\mathbb{P}(X = x) = \frac{1}{n} \underset{\{1,\dots,n\}}{I(x)} ; \quad \mathbb{E}(X) = \frac{n+1}{2}; \quad Var(X) = \frac{n^2-1}{12}; \quad M_X(t) = \frac{e^t(1-e^{nt})}{n(1-e^t)}; \quad A(X) = 0; \quad K(X) = -\frac{6(n^2+1)}{5(n^2-1)};$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Poisson</b> [Po(λ), λ > 0]	<ul style="list-style-type: none"><li>◦ <math>X_1, X_2, \dots</math> ind. com <math>X_i \sim Po(\frac{r^i}{i}) \Rightarrow Y = \sum_{i=1}^\infty iX_i \sim G_0(\frac{1-r}{r})</math></li><li>◦ <math>X_1, \dots, X_n</math> i.i.d. com <math>X_i \sim Po(\lambda) \Rightarrow Y = \sum_{i=1}^n X_i \sim Po(n\lambda)</math></li><li>◦ <math>X_1, \dots, X_n</math> ind. com <math>X_i \sim Po(\lambda_i) \Rightarrow Y = X_i   (\sum_{j=1}^n X_j = k) \sim Bin(k, \lambda_i / \sum_{j=1}^n \lambda_j)</math></li><li>◦ <math>X \sim Bin(n, p)</math> e <math>\lambda = np \Rightarrow X \xrightarrow{D} Po(\lambda)</math>, quando <math>n \rightarrow \infty</math></li></ul>
$\mathbb{P}(X = x) = \frac{\lambda^x e^{-\lambda}}{x!} \underset{\{0,1,\dots\}}{I(x)} ; \quad \mathbb{E}(X) = Var(X) = \lambda; \quad Mo(X) = \lfloor \lambda \rfloor \text{ ou } \lceil \lambda \rceil - 1; \quad A(X) = \lambda^{-1};$ $\mathbb{E}[(1-a)^X] = e^{-a\lambda}; \quad K(X) = \lambda^{-1/2}; \quad M_X(t) = e^{\lambda(e^t-1)}; \quad \mathbb{E}[\frac{X!}{(X-k)!}] = \lambda^k;$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Hipergeométrica</b> [Hipergeo(N, k, n), N ∈ ℕ, k ∈ {0, ⋯, N}, n ∈ {0, ⋯, N}]	<ul style="list-style-type: none"><li>◦ <math>X \sim Hipergeo(N, k, 1) \Leftrightarrow X \sim Bernoulli(\frac{k}{N})</math></li><li>◦ <math>X \sim Hipergeo(N, k, n)</math> e <math>p = \frac{k}{N} \Rightarrow X \xrightarrow{D} Bin(n, p)</math>, quando <math>n \rightarrow \infty</math></li></ul>
$\mathbb{P}(X = x) = \frac{\binom{k}{x}\binom{N-k}{n-x}}{\binom{N}{n}} \underset{\{\max\{0,n-(N-k)\}, \dots, \min\{k,n\}\}}{I(x)} ; \quad Var(X) = n\frac{k}{N}(1-\frac{k}{N})(\frac{N-n}{N-1});$ $\mathbb{E}(X) = n\frac{k}{N}; \quad Mo(X) = \lfloor \frac{(n+1)(k+1)}{N+2} \rfloor;$ $A(X) = \frac{(N-2k)(N-2n)\sqrt{N-1}}{(N-2)\sqrt{nk(N-k)(N-n)}};$	$\mathbb{E}(X) = Med(X) = Mo(X) = a;$

<b>Apêndice</b> <ul style="list-style-type: none"><li>◦ <math>Var(X) = \mathbb{E}[(X - \mathbb{E}(X))^2];</math></li><li>◦ <math>M_X(t) = \mathbb{E}(e^{tX}); \quad C_X(t) = \mathbb{E}(e^{itX})</math></li><li>◦ <math>x_p = F^{-1}(p) \Rightarrow Med(X) = x_{1/2};</math></li><li>◦ <math>A(X) = \frac{\mathbb{E}[(X - \mathbb{E}(X))^3]}{Var(X)^{3/2}};</math> <math>A(X) &lt; 0</math> (cauda pesada à esquerda); <math>A(X) &gt; 0</math> (cauda pesada à direita); <math>A(X) = 0</math> (distribuição simétrica);</li><li>◦ <math>K(X) = \frac{\mathbb{E}[(X - \mathbb{E}(X))^4]}{Var(X)^2} - 3;</math> <math>K(X) &lt; 0</math> (platicúrtica [achatada]); <math>K(X) &gt; 0</math> (leptocúrtica [afuniliada]); <math>K(X) = 0</math> (mesocúrtica);</li></ul>	<ul style="list-style-type: none"><li>◦ <math>e^x = \sum_{n=0}^\infty \frac{x^n}{n!};</math></li><li>◦ <math>\ln(x+1) = \sum_{n=0}^\infty \frac{(-1)^n x^{n+1}}{n+1}, \quad  x  &lt; 1;</math></li><li>◦ <math>sen\ x = \sum_{n=0}^\infty \frac{(-1)^n x^{2n+1}}{(2n+1)!};</math></li><li>◦ <math>cos\ x = \sum_{n=0}^\infty \frac{(-1)^n x^{2n}}{(2n)!};</math></li><li>◦ <math>\sum_{i=1}^n i = \frac{n(n+1)}{2};</math></li><li>◦ <math>\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6};</math></li><li>◦ <math>\sum_{i=1}^n i^3 = (\frac{n(n+1)}{2})^2;</math></li><li>◦ <math>\sum_{i=1}^n i^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30};</math></li><li>◦ <math>(\sum_{i=1}^m a_i)^n = \sum_{x_1+\dots+x_m=n} \frac{n!}{\prod_{j=1}^m x_j} \prod_{j=1}^m a_j^{x_j};</math></li></ul>	<ul style="list-style-type: none"><li>◦ <math>\binom{n}{x} = \frac{n!}{x!(n-x)!};</math></li><li>◦ <math>\binom{n}{x} + \binom{n}{x-1} = \binom{n+1}{x}, \quad n \in \mathbb{N} \text{ e } x \in \mathbb{Z};</math></li><li>◦ <math>\binom{-n}{x} = (-1)^x \binom{n+x-1}{x};</math></li><li>◦ <math>n! \sim (2\pi)^{1/2} e^{-n} n^{n+1/2};</math></li><li>◦ <math>(a+b)^n = \sum_{i=0}^n \binom{n}{i} a^i b^{n-i};</math></li><li>◦ <math>\binom{N_1+N_2}{x} = \sum_{i=0}^n \binom{N_1}{i} \binom{N_2}{n-i};</math></li><li>◦ <math>(1-x)^{-2} = \sum_{i=0}^\infty (i+1)x^i;</math></li><li>◦ <math>\max(a, b) = \frac{a+b+ a-b }{2};</math></li><li>◦ <math>\min(a, b) = \frac{a+b- a-b }{2};</math></li></ul>	<ul style="list-style-type: none"><li>◦ <math>\Gamma(a+1) = a\Gamma(a);</math></li><li>◦ <math>B(a, b) = \frac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)};</math></li><li>◦ <math>\Gamma(a)\Gamma(1-a) = \frac{\pi}{sen(\pi a)};</math></li><li>◦ <math>\Gamma(\frac{a}{2}) = \frac{\sqrt{\pi}(a-1)!}{2^{a-1}(\frac{a-1}{2})!};</math></li><li>◦ <math>a_1(x-b_1)^2 + a_2(x-b_2)^2 = (a_1+a_2)(x-c)^2 + \frac{a_1a_2}{a_1+a_2}(b_1-b_2)^2,</math> sendo <math>c = \frac{a_1b_1+a_2b_2}{a_1+a_2};</math></li><li>◦ <math>e^{ix} = cos\ x + i sen\ x;</math></li><li>◦ <math>e^a = \lim_{n \rightarrow \infty} \left(1 + \frac{a}{n}\right)^n;</math></li></ul>
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