

3. electron density is $\rho_e = N_e/a^3 = 112 / (0.543 \text{ nm})^3 \approx 700 \text{ nm}^{-3}$

a) $\rho_e \cdot 1000 \text{ nm}^3 \approx 7 \cdot 10^5 \text{ electrons}$

b) $1 \mu\text{m}^3 = (10^3 \text{ nm})^3 = 10^9 \text{ nm}^3$

$\rho_e \cdot 10^9 \text{ nm}^3 = 7 \cdot 10^{11} \text{ electrons}$

c) $1 \text{ nm}^3 = (10^{-9} \text{ m})^3 = 10^{-27} \text{ m}^3$

$1 \text{ nm}^3 = (10^6 \text{ nm})^3 = 10^{18} \text{ nm}^3$

$\rho_e \cdot 10^{18} \text{ nm}^3 \approx 7 \cdot 10^{20} \text{ electrons}$

4. 100 petaFLOPS (10^{17} FLOPS)

a) A person weighing 100 kg, with approximately the same density as water will have a volume of approximately:
 $V = 100 \text{ dm}^3 = 100 (10^8 \text{ nm})^3 = 10^{26} \text{ nm}^3$

the number of electrons is then:

$\rho_e \cdot V \approx 7 \cdot 10^{28} \text{ electrons}$

To calculate all electrons would take
 $7 \cdot 10^{28} / 10^{17} = 7 \cdot 10^{11} \text{ seconds}$

That is $7 \cdot 10^{11} / (3600 \cdot 24 \cdot 365) \approx 22197 \text{ years}$

In a lifetime of 80 years it would be able to calculate:

$100 \cdot \frac{80}{22197} \approx 0.36\% \text{ of the person}$

b) The total number of terms is the product of terms in the first sum and the number in the second.

$\sum_{i=1}^{N_e} i$ has N_e terms while $\sum_{j=1}^{N_e} j$ has N_e terms

The number of terms is $\sum_{i=1}^{N_e} \sum_{j=1}^{N_e} 1 = 1 + 2 + 3 + \dots + (N_e - 2) + (N_e - 1) + N_e$

N_e terms

(Assuming i starting at 1) reordering the terms: $\sum_{i=1}^{N_e} \sum_{j=1}^{N_e} 1 = 1 + (N_e - 1) + 2(N_e - 2) + \dots + \frac{N_e}{2} + (N_e - \frac{N_e}{2})$

$= \sum_{i=1}^{N_e} N_e = \frac{N_e}{2} \cdot N_e = N_e^2 / 2 = (7 \cdot 10^{20})^2 / 2 = 2.45 \cdot 10^{41}$