

# Project 2

## SF2568 Program construction in C++ for Scientific Computing

June 7, 2015

In this project you will implement a general class for matrices. The final aim is to provide all necessary functionality for computing elementary functions of matrices. You will learn details about the construction of classes in C++.

The exponential function has the series representation

$$e^x = \sum_{n=0}^{\infty} \frac{x^n}{n!}.$$

This series converges for all  $x \in \mathbb{R}$ . Therefore, an exponential for square matrices  $A \in \mathbb{R}^{m \times m}$  can be defined by

$$\exp(A) = \sum_{n=0}^{\infty} \frac{A^n}{n!}.$$

**Task 1** Implement the evaluation of the exponential for real numbers! The calling sequence should be

```
double myexp(double x, double tol = 1e-10);
```

The parameter `tol` indicates the required accuracy.

Validate your routine by checking it against the exponential function from the standard library!

**Task 2** Now we are interested in computing the matrix exponential. The idea consist of using the series for that. Therefore, you must construct a matrix class according to the following skeleton:

```

class Matrix {
public:
    Matrix(int m);
    Matrix(const& Matrix);
    Matrix& operator=(const Matrix&);
    Matrix& operator+=(const Matrix&);
    Matrix& operator*=(const Matrix&);
    double norm(const Matrix&);
    void printMatrix() const;
    void fillMatrix(...);
    ...
};

```

Add members as needed and convenient for the problem. For the implementation of the arrays you may use either C-style arrays or corresponding classes from the C++ standard library.

In order to check your computations, a C++ routine for computing the matrix exponential, `r8mat_expm1.cpp`, is provided. The latter implements Matlab's algorithm for `expm`. Show using a number of freely chosen matrices how accurate your matrix exponential is!

Note: The provided routines consist of two source files and two header files. The calling sequence is:

```
double* r8mat_expm1(int m, double a[])
```

Here, `m` is the dimension of the matrix and `a` denotes a C-style array where the matrix is stored in Fortran-style (column wise). The return result is a pointer to a C-style array holding the matrix exponential. Note: The header file `r8lib.h` assume that the namespace `std` has been opened. So do the following in your code:

```

using namespace std;
#include "r8lib.h"

```

Note: I recommend to have a look at the following paper: Cleve Moler, Charles Van Loan: *Nineteen dubious ways to compute the exponential of a matrix, twenty-five years later*. SIAM Review **45**(2003)1, 3–49

The programming exercises should be done individually, or in groups of two. Hand in a report containing:

- Comments and explanations that you think are necessary for understanding your program.
- Results as indicated in the tasks.
- Program listing.
- E-mail the source code to `hanke@nada.kth.se`.