$$\left\langle \begin{array}{l} p(\boldsymbol{\pi}, \mathbf{S} \mid \text{paths } \cdot, \mathbf{y}) \\ p(\text{paths } \cdot \mid \boldsymbol{\pi}, \mathbf{S}, \mathbf{y}) \end{array} \right\rangle$$