**EE2410 Data Structure Hw #1 (Chapter 1~2 of textbook)**

**due date 3/29/2024 23:59**

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**Note:** Use MS Word to **edit this file** by directly typing your student number and name in above blanks and your answer to each homework problem right in the **Sol:** blanks as shown below. Then save your file as **Hw1-SNo.pdf**, where SNo is your student number. Submit the **Hw1-SNo.pdf** file via eLearn. The grading will be based on the correctness of your answers to the problems, and the **format requirement**. Fail to comply with the aforementioned format (file name, header, problem, answer, problem, answer,…), will certainly degrade your score. If you have any questions, please feel free to ask. Submit your homework before the deadline (midnight of 3/29). Fail to comply (**late** homework) will have ZERO score. **Copy** homework will have SERIOUS consequences.

1. (10%) Determine the asymptotic complexity (()) by step table of the each of the following two program segments respectively:

Code (a):

1. for(i=1; i<=n; i++)
2. for(j=1; j<=i; j++)
3. for(k=1; k<=j; k++)
4. x++;

Code (b)

1. i=1;
2. while(i<=n)
3. {
4. x++;
5. i++;
6. }

**Sol:**

1. (10%) For the function Multiply() shown below,
2. Obtain the step count for the function using the step table method.
3. Repeat (a) but use () notation instead of exact step counts and frequency counts..

void Multiply(int \*\*a, int \*\*b, int \*\*c, int m, int n, int p)

{

for(int i=0;i<m;i++)

for(int j=0; j<p; j++)

{

c[i][j] = 0;

for(int k=0;k<n;k++)

c[i][j] += a[i][k] \* b[k][j];

}

}

**Sol:**

1. (10%) For each of the complexity expression below, determine its overall complexity. For example, given expression 2*n +* 3*n*, the overall complexity should be *O*(*n*), not *O*(*n*2), i.e., use the smallest possible class of functions.

(a) 2*n*2 *–* 3*n* = *O*(?)

(b) *n! +* 2*n* = *O*(?)

(c) 5*n*2 *+ n* log *n* = *O*(?)

(d) *n*1.001 *+ n* log *n* = *O*(?)

(e) 5*n*3 *–* 3*n*2log *n +* 2*n* = *O*(?)

**Sol:**

1. (10%) **(Recursion and Performance Analysis)** According to the below recursive method, answer the following questions.

int recurse(int n)

{

if (n <= 0)

return 1;

else

return 1 + recurse(n/2);

}

a) What does the method return for n=8?

b) How many times will your method be called recursively for n=256?

c) What is the algorithm complexity of the recursive method in big Oh notation?

d) What is the total variable space needed for the execution of the method for an input size of 256, if the integer size is 4 bytes?

**Sol:**

1. (10%) Given an algorithm that solves a problem in three phases. The first phase takes *O*(100*n*)to input the data of size *n*. The second phase takes *O*(*n* log *n*)to process the data. The third phase takes *O*(log *n*)to output the data.
2. What is the complexity of the algorithm?
3. If the data size is 10, which phase is most likely to take the longest time to execute?

**Sol:**

1. (10%)
2. Given a list of objects stored in a sorted array, describe an algorithm to search as efficiently as possible for an object based on a key. (Note that the key type matches the field type by which the array is sorted.) You may describe your algorithm in English, pseudocode, and/or C++ code, as long as your description is clear.
3. What will be the Big O running time of the algorithm you described in (a)? Why?
4. Given a list of objects stored in an unsorted array, describe an algorithm to search as efficiently as possible for an object based on a key. You may describe your algorithm in English, pseudocode, and/or C++ code, as long as your description is clear.
5. What will be the Big O running time of the algorithm you described in (c)? Why?

**Sol:**

1. (10%) A square band matrix An,a is an n x n matrix A in which all the nonzero terms lie in a band centered around the main diagonal. The band includes a-1 diagonals below and above the main diagonal as shown below.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| |  |  |  |  | | --- | --- | --- | --- | | 6  下方帶狀區域 | 7 | 8 | 0 | | 8 | 0 | 4 | 4 | | 9 | 3 | 2 | 9 | | 0 | 7 | 6 | 8 |   *A*4,3 | *a* 條對角線  上方帶狀區域   |  |  |  |  |  |  |  |  |  |  | | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | |  |  |  |  |  |  |  |  |  |  | |  |  |  |  |  |  |  | 0 | |  | |  |  |  |  |  |  |  |  | |  |  |  |  |  |  |  |  |  |  | | *n*列 |  |  |  |  |  |  |  |  |  | |  |  |  |  |  |  |  |  |  |  | |  |  |  |  |  |  |  |  |  |  | |  | 0 | |  |  |  |  |  |  |  | |  |  |  |  |  |  |  |  | |  |  |  |  |  |  |  |  |  |  |   *n* 行  *An*,*a*  主對角線 |

1. How many elements are there in the band of An,a?
2. What is the relationship between i and j for element Aij in the band of An,a?
3. Assume that the band of An,a is stored sequentially in an array b by diagonals starting with the lowermost diagonal. Thus A4,3 above would have the following representation:

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| b[0] | b[1] | b[2] | b[3] | b[4] | b[5] | b[6] | b[7] | b[8] | b[9] | b[10] | b[11] | b[12] | b[13] |
| 9 | 7 | 8 | 3 | 6 | 6 | 0 | 2 | 8 | 7 | 4 | 9 | 8 | 4 |
| A20 | A31 | A10 | A21 | A32 | A00 | A11 | A22 | A33 | A01 | A12 | A23 | A02 | A13 |

Obtain an addressing formula for the location of an element Aij in the lower band of An,a, e.g., LOC(A20) = 0, LOC(A31) = 1 in the example above.

**Sol:**

1. (10%) A generalized band matrix An,a,b is an n x n matrix A in which all the nonzero terms lie in a band made up of a-1 diagonals below the main diagonal, the main diagonal, and b-1 above the main diagonal as shown below.

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| *b*  *a* |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | 0 | |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
| *n*列 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  | 0 | |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

主對角線

*n* 行

*An*, *a*, *b*

1. How many elements are there in the band of An,a,b?
2. What is the relationship between i and j for element Aij in the band of An,a,b?
3. Obtain a sequential representation of the band of An,a,b in one-dimensional array c.

**Sol:**

1. (10%) String matching by KMP algorithm
2. Please describe the Knuth, Morris, and Pratt’s pattern matching algorithm.
3. Compute the failure function for the following string:

b a b c b c b a b c b a b c

1. Assume string s = “a pattern matching algorithm” with 28 characters, and p = “rithm” with 5 characters. Illustrate the matching process of the KMP algorithm graphically (as in the handout ppt file) and how many character comparisons are performed in the process?

**Sol:**

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| a |  | p | a | t | t | e | r | n |  | m | a | t | c | h | i | n | g |  | a | l | g | o | r | i | t | h | m |

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| r | i | t | h | m |

1. (10%) String matching by KMP algorithm
2. Please describe the Boyer-Moore Bad Character Heuristics pattern matching algorithm.
3. Compute the last occurrence function for the following string if the alphabet is  = {a, b, c, d}:

b a b c b c b a b c b a b c

1. Assume string s = “a pattern matching algorithm” with 28 characters, and p = “rithm” with 5 characters. Illustrate the matching process of BM algorithm graphically (as in the handout ppt file) and how many character comparisons are performed in the process?

**Sol:**

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| a |  | p | a | t | t | e | r | n |  | m | a | t | c | h | i | n | g |  | a | l | g | o | r | i | t | h | m |

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| r | i | t | h | m |