MECE 4510: Evolutionary Computation and Design

Project - Phase A: Physics Simulator

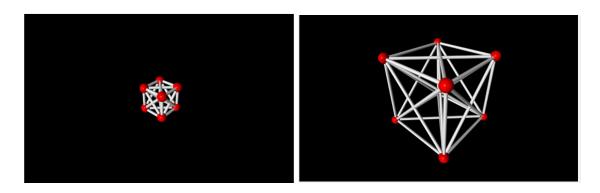
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> Instructor: Professor Hod Lipson Date Submitted: 11/01/2018

RESULTS SUMMARY

FULL VIDEO LINK: https://www.youtube.com/watch?v=nNQc2xbe9XU

Breathing Cube: https://www.youtube.com/watch?v=nNQc2xbe9XU



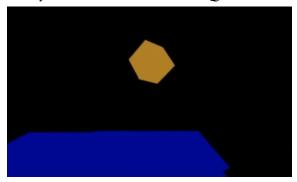
Bouncing Cube: https://www.youtube.com/watch?v=nNQc2xbe9XU#t=0m14s
Damped Bouncing Cube: https://www.youtube.com/watch?v=nNQc2xbe9XU#t=0m27s



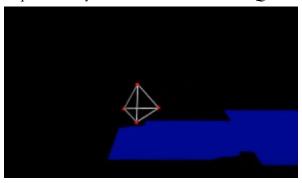
Complex Bouncing Cube: https://www.youtube.com/watch?v=nNQc2xbe9XU#t=0m42s
Damped Complex Bouncing Cube: https://www.youtube.com/watch?v=nNQc2xbe9XU#t=0m59s



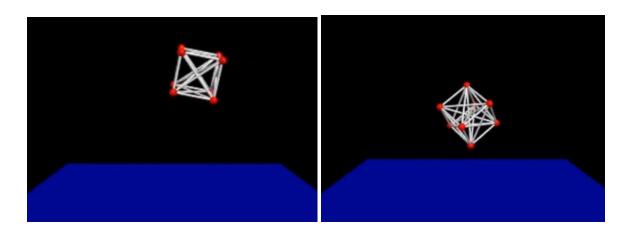
 $Triangles\ Shaded:\ https://www.youtube.com/watch?v=nNQc2xbe9XU\#t=1m17s$



Tetrahedron Debug Test: https://www.youtube.com/watch?v=nNQc2xbe9XU#t=1m36s



 $Grounded\ Node:\ https://www.youtube.com/watch?v=nNQc2xbe9XU\#t=1m54s$



METHODS

For phase A of this assignment, a cube was created in vpython with 8 balls (masses) and 28 springs to connect each individual mass. The cube is able to bounce once after dropping from any distance from the floor. Friction was added to the simulation and 8 cases have were simulated: the breathing cube, bouncing cube without a slight spin (damped + undamped), bouncing cube with a slight spin (damped + undamped), bouncing cube w/ triangles shaded, tetrahedron debugging test, and grounded node case. These cases could be evaluated both with damping and without dampening. The mass of each ball was 0.1 kg, or 0.8 kg for the entire cube. The gravity was specified to be 9.81 m/s^2, the spring constant for the springs in the cube was adjusted to 2000 N/m and the spring constant for the ground (rubber) was set to 10000 N/m. The dt set to 0.004 seconds to best fit the cube movement.

To simulate the various cases, force vectors that acted on all of the balls had to first be calculated. Each ball mass would experience eight forces from the other masses, (including itself, which was set 0) that came from the springs that it connected to. Subsequently, the force vectors were stored in an 8 x 8 matrix. Each time after the matrix updated, the force vectors in each column would be summed into one vector: the combined force vector that acting one each ball. Then once the force vectors were obtained, gravity was added into all force vectors. Using the force vectors, the acceleration vectors were calculated and updated into velocity vectors using kinematic equation vf = vi + a *t and then by using the new velocity vectors, the position of the balls were updated in relation with the forces. Once the ball positions were updated, the simulated spring positions updated with respect to the new position of the balls. If the ball position was below the floor position, a force vector from the floor $vector} (F = kc*delta(ball position - floor position)) would react on the ball force vectors to make the cube bounce back. Therefore, using a while loop allowed the process to keep updating for multiple bounces.$

For the breathing cube, the cube would just stay at its original place without adding neither gravity nor floor. The rest length L0 of the spring would be change in an order of a sine wave with respect to time. It was achieved by multiplying the rest length L0 by a breathing factor $1 + 0.5*\sin(5*t)$, where t =0.01 and it would be updated += 0.01 each time in the cycle of the while loop, producing the breathing effect.

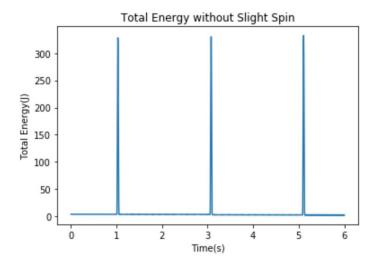
To add a damping effect to the cube, a dampening of 0.9 was multiplied by the velocity updates at the end of the loop and the damping would be updated each time so in the end the velocity would decay to zero.

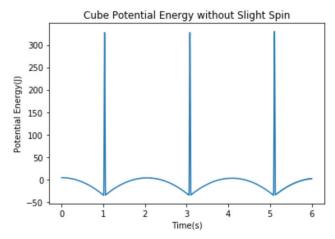
The energy calculations for the total energy (all of cube energy and ground energy), potential energy (gravity, spring, ground), kinetic energy (mass velocity) were obtained by using $K_g = m^*g^*h$, $K_k = \frac{1}{2}m^*v^2$ and $K_s = \frac{1}{2}k^*delta(L)^2$ and $K_g = \frac{1}{2}kc^*delta(y)^2$. After calculating the total energy (cube and ground), we can see in the plot below that the total cube energy stayed constant until it hit the ground and the energy transformation appeared in the plot which is a pulse that the ground energy added in. The potential energy and the kinetic energy plot were also reasonable that the changes of the energy were corresponding to the cube motion.

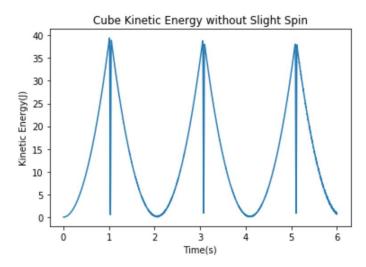
The triangle shading case was created by simulating triangles at every combination of 3 mass positions. The tetrahedron debugging test utilized 4 masses and 6 springs, which simplified the code, and proved uniformity. The grounded node case was created by only updating positions of 7 out of 8 masses and keeping one mass fixed.

PERFORMANCE PLOTS (ENERGY CURVES

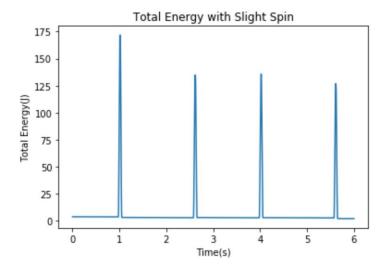
Bouncing Cube (no spin):

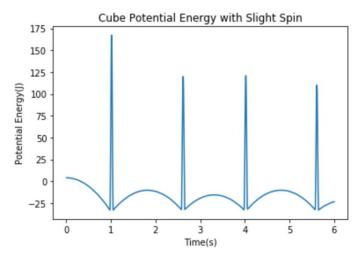


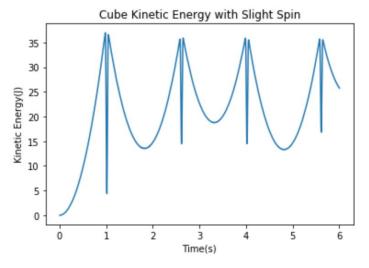




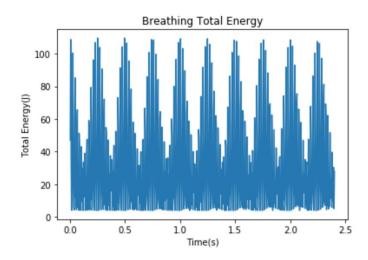
Complex Bounce:

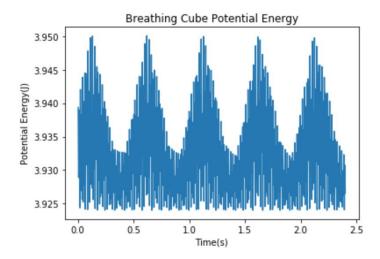


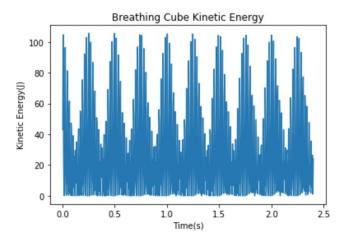




Breathing Cube:







BREATHING CUBE

```
import vpython as vp
import itertools
import numpy as np
from math import *
import matplotlib.pyplot as plt
scene = vp.canvas()
# vp.display(width=100, height=100)
# floor = vp.box(pos=vp.vector(0,-3,0), length=10, height=0.001, width=10, color=vp.color.blue)
ballname = ['b1', 'b2', 'b3', 'b4', 'b5', 'b6', 'b7', 'b8']
\texttt{ballvectors} = [\texttt{vp.vector}(0,\ 0,\ 0),\ \texttt{vp.vector}(0,\ 1,\ 0),\ \texttt{vp.vector}(0,\ 0,\ 1),\ \texttt{vp.vector}(1,\ 0,\ 0),
vp.vector(1, 1, 0),
              vp.vector(0, 1, 1),
              vp.vector(1, 0, 1), vp.vector(1, 1, 1)]
# for i in range(8):
   ballvectors[i] = ballvectors[i].rotate(angle=3.14/4, axis =vp.vector(1,1,1))
springvecs = []
for i in range(len(ballname)):
   ballname[i] = vp.sphere(pos=ballvectors[i], radius=0.1, color=vp.color.red,
velocity=vp.vector(0, 0, 0))
for z in itertools.combinations(ballvectors, 2):
   springvecs.append(z)
spring = ['s1', 's2', 's3', 's4', 's5', 's6', 's7', 's8', 's9', 's10', 's11', 's12', 's13',
's14', 's15', 's16', 's17',
         's18', 's19', 's20', 's21', 's22', 's23', 's24', 's25', 's26', 's27', 's28']
for i in range(28):
  position = springvecs[i][1] - springvecs[i][0]
   spring[i] = vp.cylinder(pos=springvecs[i][0], axis=position, length=vp.mag(position),
radius=.03,
                            color=vp.color.white)
\nabla = 0
dt = 0.003
mass = 0.1
q = 9.81
\# k sp = []
k1 = 2000
g vector = vp.vector(0, 9.81, 0)
for i in range(len(ballname)):
  ballname[i].velocity = vp.vector(0, 0, 0)
F c = vp.vector(0, 1000, 0)
L0 = np.zeros((8, 8))
```

```
for i in range(8):
   for j in range(8):
       if i == j:
           L0[j][i] = 0
           position = ballname[j].pos - ballname[i].pos
           L0[j][i] = vp.mag(position)
\# F = np.zeros((8,3))
t = 0.01
t1 = 0
Time = []
E H = []
ES = []
E K = []
while 1:
  vp.rate(100)
  k sp = 0.5 * sin(5 * t) + 1
   t += 0.01
   for i in range(8):
      ballvectors[i] = ballname[i].pos
   springvecs = []
   for z in itertools.combinations(ballvectors, 2):
       springvecs.append(z)
   for i in range(28):
       position = springvecs[i][1] - springvecs[i][0] # - L0[i]
       spring[i].pos = springvecs[i][0]
       spring[i].axis = position
       spring[i].length = vp.mag(position)
   dampening = 0.9
   F mat = np.zeros((8, 8))
   F \text{ vec} = []
  F v = []
   a = np.array(np.zeros((8, 8)))
   E s = []
   for i in range(8):
      for k in range(8):
           if k == i:
               L = 0
               F mat[i][k] = 0
               F_vec.append(vp.vector(0, 0, 0))
           else:
               L = vp.mag(ballname[k].pos - ballname[i].pos) - L0[k][i] * k sp
               E_s.append(1 / 2 * k_sp * L ** 2)
               F mat[i][k] = L * k1
               pf0 = ballname[k].pos - ballname[i].pos
               \# a[i,k] = vp.norm(pf0)*L*k sp
               F vec.append(vp.norm(pf0) * L * k1)
   E S.append(sum(E s) / 2)
   a = np.array(F vec).reshape(8, 8)
   F = a.sum(axis=0)
        for i in range(8):
            F[i] = F[i] + mass*g vector
             if ballname[i].pos.y < floor.pos.y:</pre>
```

```
F[i].y = F[i].y - dampening*((floor.pos.y-ballname[i].pos.y)**2)*10000
   E k = []
   E h = []
   for i in range(8):
      ballname[i].velocity -= F[i] / mass * dt
      E k.append(1 / 2 * mass * (vp.mag(ballname[i].velocity)) ** 2)
      ballname[i].pos += ballname[i].velocity * dt
      E h.append(mass * 9.81 * (ballname[i].pos.y))
   E K.append(sum(E k))
   E H.append(sum(E h))
   t1 += 0.004
   Time.append(t1)
   if t > 6:
      break
E total = []
E potential = []
for i in range(len(E H)):
   E total.append(E K[i] + E H[i] + E S[i])
for i in range(len(E_H)):
  E_potential.append(E_H[i] + E_S[i])
plt.plot(Time, E total)
plt.xlabel('Time(s)')
plt.ylabel('Total Energy(J)')
plt.title('Breathing Total Energy')
plt.show()
plt.plot(Time, E potential)
plt.xlabel('Time(s)')
plt.ylabel('Potential Energy(J)')
plt.title('Breathing Cube Potential Energy')
plt.show()
plt.plot(Time, E_K)
plt.xlabel('Time(s)')
plt.ylabel('Kinetic Energy(J)')
plt.title('Breathing Cube Kinetic Energy')
plt.show()
         if ballname[i].pos.y < floor.pos.y:</pre>
             ballname[i].velocity = dampening*-1*(ballname[i].velocity)+ F c*(floor.pos.y -
ballname[i].pos.y)*(floor.pos.y - ballname[i].pos.y)
```

BOUNCING CUBE WITHOUT A SLIGHT SPIN

```
import vpython as vp
import itertools
import numpy as np
from math import *
import matplotlib.pyplot as plt
scene = vp.canvas()
# vp.display(width=100, height=100)
floor = vp.box(pos=vp.vector(0, -5, 0), length=10, height=0.001, width=10, color=vp.color.blue)
ballname = ['b1', 'b2', 'b3', 'b4', 'b5', 'b6', 'b7', 'b8']
ballvectors = [vp.vector(0, 0, 0), vp.vector(0, 1, 0), vp.vector(0, 0, 1), vp.vector(1, 0, 0),
vp.vector(1, 1, 0),
             vp.vector(0, 1, 1),
              vp.vector(1, 0, 1), vp.vector(1, 1, 1)]
# for i in range(8):
     ballvectors[i] = ballvectors[i].rotate(angle=3.14/4, axis =vp.vector(1,1,1))
springvecs = []
for i in range(len(ballname)):
  ballname[i] = vp.sphere(pos=ballvectors[i], radius=0.1, color=vp.color.red,
velocity=vp.vector(0, 0, 0))
for z in itertools.combinations(ballvectors, 2):
   springvecs.append(z)
spring = ['s1', 's2', 's3', 's4', 's5', 's6', 's7', 's8', 's9', 's10', 's11', 's12', 's13',
's14', 's15', 's16', 's17',
         's18', 's19', 's20', 's21', 's22', 's23', 's24', 's25', 's26', 's27', 's28']
for i in range(28):
   position = springvecs[i][1] - springvecs[i][0]
   spring[i] = vp.cylinder(pos=springvecs[i][0], axis=position, length=vp.mag(position),
radius=.03,
                           color=vp.color.white)
\nabla = 0
dt = 0.004
mass = 0.1
g = 9.81
k \, sp = 2000
g \ vector = vp.vector(0, 9.81, 0)
for i in range(len(ballname)):
  ballname[i].velocity = vp.vector(0, 0, 0)
F c = vp.vector(0, 10000, 0)
L0 = np.zeros((8, 8))
for i in range(8):
   for j in range(8):
       if i == j:
          L0[j][i] = 0
           position = ballname[j].pos - ballname[i].pos
           L0[j][i] = vp.mag(position)
```

```
Time = []
t = 0
E_K = []
EG = []
E H = []
ES = []
while 1:
  vp.rate(100)
   for i in range(8):
      ballvectors[i] = ballname[i].pos
   springvecs = []
   for z in itertools.combinations(ballvectors, 2):
      springvecs.append(z)
   for i in range(28):
       position = springvecs[i][1] - springvecs[i][0] # - L0[i]
       spring[i].pos = springvecs[i][0]
       spring[i].axis = position
       spring[i].length = vp.mag(position)
   dampening = 1 # adjust damping here
   F mat = np.zeros((8, 8))
   F_{vec} = []
   F v = []
   a = np.array(np.zeros((8, 8)))
   E s = []
   for i in range(8):
      for k in range(8):
          if k == i:
               L = 0
               F mat[i][k] = 0
               F vec.append(vp.vector(0, 0, 0))
               L = vp.mag(ballname[k].pos - ballname[i].pos) - L0[k][i]
               E s.append(1 / 2 * k sp * L ** 2)
               pf0 = ballname[k].pos - ballname[i].pos
               # a[i,k] = vp.norm(pf0)*L*k sp
               F_vec.append(vp.norm(pf0) * L * k_sp)
   E_S.append(sum(E_s) / 2)
   a = np.array(F vec).reshape(8, 8)
   F = a.sum(axis=0)
   E_g = []
   for i in range(8):
       F[i] = F[i] + g_vector * mass
       if ballname[i].pos.y < floor.pos.y:</pre>
           F N = ((floor.pos.y - ballname[i].pos.y) ** 2) * 10000
           F[i].y = F[i].y - FN
           E g.append(1 / 2 * F N)
           mu = 1
           F st = mu * F N
           F \text{ horiz} = (F[i].x * 2 + F[i].z * 2) ** 0.5
           v xz = (ballname[i].velocity.x ** 2 + ballname[i].velocity.z ** 2) ** 0.5
           vx = ballname[i].velocity.x / v xz
           vz = ballname[i].velocity.z / v xz
```

```
if F_st < F_horiz:</pre>
              F[i].x += F_horiz * vx - F_N * vx
               F[i].z += F_horiz * vz - F_N * vz
               F[i].x = F horiz * vx
               F[i].z = F horiz * vz
              ballname[i].velocity.x = 0
               ballname[i].velocity.z = 0
   E G.append(sum(E g))
   E k = []
   E h = []
   for i in range(8):
      ballname[i].velocity -= (F[i] / mass * dt) * dampening
      E k.append(1 / 2 * mass * (vp.mag(ballname[i].velocity)) ** 2)
       ballname[i].pos += ballname[i].velocity * dt
       E_h.append(mass * 9.81 * (ballname[i].pos.y))
   E H.append(sum(E h))
   E K.append(sum(E k))
   t += 0.004
  Time.append(t)
   if t > 6:
      break
E_total = []
E potential = []
for i in range(len(E H)):
  E total.append(E K[i] + E H[i] + E S[i] + E G[i])
for i in range(len(E H)):
  E potential.append(E G[i] + E H[i] + E S[i])
plt.plot(Time, E total)
plt.xlabel('Time(s)')
plt.ylabel('Total Energy(J)')
plt.title('Total Energy without Slight Spin')
plt.show()
plt.plot(Time, E potential)
plt.xlabel('Time(s)')
plt.ylabel('Potential Energy(J)')
plt.title('Cube Potential Energy without Slight Spin')
plt.show()
plt.plot(Time, E_K)
plt.xlabel('Time(s)')
plt.ylabel('Kinetic Energy(J)')
plt.title('Cube Kinetic Energy without Slight Spin')
plt.show()
```

BOUNCING CUBE WITH A SLIGHT SPIN CODE:

```
import vpython as vp
import itertools
import numpy as np
from math import *
import matplotlib.pyplot as plt
scene = vp.canvas()
# vp.display(width=100, height=100)
floor = vp.box(pos=vp.vector(0, -5, 0), length=10, height=0.001, width=10, color=vp.color.blue)
ballname = ['b1', 'b2', 'b3', 'b4', 'b5', 'b6', 'b7', 'b8']
ballvectors = [vp.vector(0, 0, 0), vp.vector(0, 1, 0), vp.vector(0, 0, 1), vp.vector(1, 0, 0),
vp.vector(1, 1, 0),
             vp.vector(0, 1, 1),
              vp.vector(1, 0, 1), vp.vector(1, 1, 1)]
for i in range(8):
   ballvectors[i] = ballvectors[i].rotate(angle=3.14 / 4, axis=vp.vector(1, 1, 1))
springvecs = []
for i in range(len(ballname)):
  ballname[i] = vp.sphere(pos=ballvectors[i], radius=0.1, color=vp.color.red,
velocity=vp.vector(0, 0, 0))
for z in itertools.combinations(ballvectors, 2):
   springvecs.append(z)
spring = ['s1', 's2', 's3', 's4', 's5', 's6', 's7', 's8', 's9', 's10', 's11', 's12', 's13',
's14', 's15', 's16', 's17',
         's18', 's19', 's20', 's21', 's22', 's23', 's24', 's25', 's26', 's27', 's28']
for i in range(28):
  position = springvecs[i][1] - springvecs[i][0]
   spring[i] = vp.cylinder(pos=springvecs[i][0], axis=position, length=vp.mag(position),
radius=.03,
                           color=vp.color.white)
\nabla = 0
dt = 0.004
mass = 0.1
q = 9.81
k sp = 2000
g \ vector = vp.vector(0, 9.81, 0)
for i in range(len(ballname)):
  ballname[i].velocity = vp.vector(0, 0, 0)
F c = vp.vector(0, 10000, 0)
L0 = np.zeros((8, 8))
for i in range(8):
   for j in range(8):
       if i == j:
           L0[j][i] = 0
       else:
           position = ballname[j].pos - ballname[i].pos
           L0[j][i] = vp.mag(position)
Time = []
```

```
t = 0
E K = []
EG = []
E H = []
ES = []
while 1:
  vp.rate(100)
   for i in range(8):
      ballvectors[i] = ballname[i].pos
   springvecs = []
   for z in itertools.combinations(ballvectors, 2):
       springvecs.append(z)
   for i in range(28):
       position = springvecs[i][1] - springvecs[i][0] # - L0[i]
       spring[i].pos = springvecs[i][0]
       spring[i].axis = position
       spring[i].length = vp.mag(position)
   dampening = 1 # adjust damping here
   F mat = np.zeros((8, 8))
   F \text{ vec} = []
   F v = []
   a = np.array(np.zeros((8, 8)))
   E s = []
   for i in range(8):
      for k in range(8):
          if k == i:
               L = 0
               F mat[i][k] = 0
               F vec.append(vp.vector(0, 0, 0))
           else:
               L = vp.mag(ballname[k].pos - ballname[i].pos) - L0[k][i]
               E s.append(1 / 2 * k sp * L ** 2)
               pf0 = ballname[k].pos - ballname[i].pos
               \# a[i,k] = vp.norm(pf0)*L*k sp
               F vec.append(vp.norm(pf0) * L * k sp)
   E_S.append(sum(E_s) / 2)
   a = np.array(F vec).reshape(8, 8)
   F = a.sum(axis=0)
   Eg = []
   for i in range(8):
       F[i] = F[i] + g vector * mass
       if ballname[i].pos.y < floor.pos.y:</pre>
           F_N = ((floor.pos.y - ballname[i].pos.y) ** 2) * 10000
           F[i].y = F[i].y - FN
           E g.append(1 / 2 * F N)
           mu = 1
           F st = mu * F N
           F \text{ horiz} = (F[i].x * 2 + F[i].z * 2) ** 0.5
           v xz = (ballname[i].velocity.x ** 2 + ballname[i].velocity.z ** 2) ** 0.5
           vx = ballname[i].velocity.x / v xz
           vz = ballname[i].velocity.z / v xz
           if F st < F horiz:</pre>
```

```
F[i].x += F horiz * vx - F N * vx
               F[i].z \leftarrow F horiz * vz - F N * vz
           else:
               F[i].x = F horiz * vx
               F[i].z = F horiz * vz
               ballname[i].velocity.x = 0
               ballname[i].velocity.z = 0
   E G.append(sum(E g))
   E k = []
   E h = []
   for i in range(8):
       ballname[i].velocity -= (F[i] / mass * dt) * dampening
       E k.append(1 / 2 * mass * (vp.mag(ballname[i].velocity)) ** 2)
       ballname[i].pos += ballname[i].velocity * dt
       E h.append(mass * 9.81 * (ballname[i].pos.y))
   E H.append(sum(E h))
   E K.append(sum(E k))
   t += 0.004
   Time.append(t)
   if t > 6:
      break
      for i in range(8):
         F[i] = F[i] + mass*g_vector
          if ballname[i].pos.y < floor.pos.y:</pre>
              \texttt{F[i].y} = \texttt{dampening*}(\texttt{F[i].y} - ((\texttt{floor.pos.y-ballname[i].pos.y})**2)*10000)
              E g.append(1/2*10000*(floor.pos.y-ballname[i].pos.y)**2)
     E G.append(sum(E g))
     E k = []
     E h = []
     for i in range(8):
          ballname[i].velocity -= F[i]/mass*dt
          E k.append(1/2*mass*(vp.mag(ballname[i].velocity))**2)
          ballname[i].pos += ballname[i].velocity*dt
          E h.append(mass*9.81*(ballname[i].pos.y))
          if ballname[i].pos.y < floor.pos.y:</pre>
              ballname[i].velocity = dampening*((ballname[i].velocity)+ F c*(floor.pos.y -
ballname[i].pos.y)*(floor.pos.y - ballname[i].pos.y))
     E H.append(sum(E h))
     E K.append(sum(E k))
      t += 0.004
     Time.append(t)
     if t > 6:
         break
E total = []
E potential = []
for i in range(len(E H)):
   E total.append(E K[i] + E H[i] + E S[i] + E G[i])
for i in range(len(E H)):
   E potential.append(E G[i] + E H[i] + E S[i])
plt.plot(Time, E total)
plt.xlabel('Time(s)')
```

#

#

#

#

#

#

#

```
plt.ylabel('Total Energy(J)')
plt.title('Total Energy with Slight Spin')
plt.show()

plt.plot(Time, E_potential)
plt.xlabel('Time(s)')
plt.ylabel('Potential Energy(J)')
plt.title('Cube Potential Energy with Slight Spin')
plt.show()

plt.plot(Time, E_K)
plt.xlabel('Time(s)')
plt.ylabel('Kinetic Energy(J)')
plt.title('Cube Kinetic Energy with Slight Spin')
plt.show()
```

TRIANGLES SHADED CODE:

```
import vpython as vp
import itertools
import numpy as np
scene = vp.canvas(title = 'Box', width = 600, height = 400, center = vp.vector(0,0,0))
floor = vp.box(pos=vp.vector(0,-3,0), length=8, height=0.01, width=8, color=vp.color.blue)
ballname = ['b1', 'b2', 'b3', 'b4', 'b5', 'b6', 'b7', 'b8']
\texttt{ballvectors} = [\texttt{vp.vector}(0,\ 0,\ 0),\ \texttt{vp.vector}(0,\ 1,\ 0),\ \texttt{vp.vector}(0,\ 0,\ 1),\ \texttt{vp.vector}(1,\ 0,\ 0),
vp.vector(1, 1, 0), vp.vector(0, 1, 1),
              vp.vector(1, 0, 1), vp.vector(1, 1, 1)]
for i in range(8):
  ballvectors[i] = ballvectors[i].rotate(angle=3.14/4, axis =vp.vector(1,0,1))
triangles = []
for z in itertools.combinations(ballvectors, 3):
   triangles.append(z)
T = list(range(56))
for i in range(len(triangles)):
   T[i] = vp.triangle(v0 = vp.vertex(pos = triangles[i][0]), v1 = vp.vertex(pos = triangles[i][1]),
v2=vp.vertex(pos=triangles[i][2]), texture = "https://i.imgur.com/eQueRtf.jpg")
springvecs = []
for i in range(len(ballname)):
  ballname[i] = vp.sphere(pos=ballvectors[i], radius=0.001, color=vp.color.red, f k=
vp.vector(0,0,0))
for z in itertools.combinations(ballvectors, 2):
   springvecs.append(z)
spring = ['s1', 's2', 's3', 's4', 's5', 's6', 's7', 's8', 's9', 's10', 's11', 's12', 's13', 's14',
's15', 's16', 's17', 's18', 's19', 's20', 's21', 's22', 's23', 's24', 's25', 's26', 's27', 's28']
for i in range(28):
   position = springvecs[i][1] - springvecs[i][0]
   spring[i] = vp.cylinder(pos=springvecs[i][0], axis=position, length=vp.mag(position),
radius=.001, color=vp.color.white)
v = 0
dt = 0.003
mass = 0.1
a = 9.81
k sp = 1000
g \ vector = vp.vector(0, 9.81, 0)
for i in range(len(ballname)):
  ballname[i].velocity = vp.vector(0,0,0)
F c = vp.vector(0, 1000, 0)
L0= np.zeros((8,8))
for i in range(8):
   for j in range(8):
       if i == j:
           L0[j][i] = 0
       else:
           position = ballname[j].pos - ballname[i].pos
           L0[j][i] = vp.mag(position)
```

```
while 1:
  vp.rate(200)
   floor = vp.box(pos=vp.vector(ballvectors[1].x, -3, ballvectors[1].z), length=5, height=0.01,
width=5, color=vp.color.blue)
  scene.center.x = ballvectors[1].x
   scene.center.z = ballvectors[1].z
   for i in range(8):
      ballvectors[i] = ballname[i].pos
   springvecs = []
   for z in itertools.combinations(ballvectors, 2):
      springvecs.append(z)
   for i in range(28):
      position = springvecs[i][1] - springvecs[i][0] #- L0[i]
      spring[i].pos = springvecs[i][0]
       spring[i].axis = position
       spring[i].length = vp.mag(position)
   triangles = []
   for z in itertools.combinations(ballvectors, 3):
      triangles.append(z)
   for i in range(len(triangles)):
      T[i].v0.pos = triangles[i][0]
      T[i].v1.pos = triangles[i][1]
       T[i].v2.pos = triangles[i][2]
  dampening = 0.9
  F mat = np.zeros((8,8))
  F \text{ vec} = []
  F v = []
  a = np.array(np.zeros((8,8)))
   for i in range(8):
       for k in range(8):
           if k == i:
              L = 0
               F mat[i][k] = 0
               F vec.append(vp.vector(0, 0, 0))
           else:
               L = vp.mag(ballname[k].pos - ballname[i].pos) - L0[k][i]
               F mat[i][k] = L*k sp
               pf0 = ballname[k].pos - ballname[i].pos
               \#a[i,k] = vp.norm(pf0)*L*k_sp
               F_vec.append(vp.norm(pf0)*L*k_sp)
  a = np.array(F vec).reshape(8, 8)
   F = a.sum(axis=0)
   for i in range(8):
       F[i] = F[i] + g_vector*mass
       if ballname[i].pos.y < floor.pos.y:</pre>
           F N = ((floor.pos.y-ballname[i].pos.y)**2)*10000
          F[i].y = 0.99*(F[i].y - F N)
          mu = 1
           F st = mu*F N
           F \text{ horiz} = (F[i].x ** 2 + F[i].z ** 2) ** 0.5
           v xz = (ballname[i].velocity.x ** 2 + ballname[i].velocity.z ** 2) ** 0.5
           vx = ballname[i].velocity.x / v xz
```

TETRAHEDRON CODE:

```
import vpython as vp
import itertools
import numpy as np
scene = vp.canvas(title = 'Tetrahedron', width = 600, height = 400, center = vp.vector(0,0,0))
#vp.display(width=100, height=100)
floor = vp.box(pos=vp.vector(0,-7,0), length=10, height=0.01, width=10, color=vp.color.blue)
ballname = ['b1', 'b2', 'b3', 'b4'] #, 'b5', 'b6', 'b7', 'b8']
\texttt{ballvectors} = [\texttt{vp.vector}(-1, \ 0, \ -1/(2) **0.5), \ \texttt{vp.vector}(0, \ 1, \ 1/(2) **0.5), \ \texttt{vp.vector}(1, \ 0, \ 1/(2) **0.5)]
-1/(2)**0.5), vp.vector(0, -1, 1/(2)**0.5)] #, vp.vector(1, 1, 0), vp.vector(0, 1, 1),
             # vp.vector(1, 0, 1), vp.vector(1, 1 1)]
for i in range(4):
  ballvectors[i] = ballvectors[i].rotate(angle=3.14/4, axis =vp.vector(1,1,1))
springvecs = []
for i in range(4):
   ballname[i] = vp.sphere(pos=ballvectors[i], radius=0.1, color=vp.color.red, f k=
vp.vector(0,0,0))
for z in itertools.combinations(ballvectors, 2):
  springvecs.append(z)
spring = ['s1', 's2', 's3', 's4', 's5', 's6'] #, 's7', 's8', 's9', 's10', 's11', 's12', 's13',
's14', 's15', 's16', 's17', 's18', 's19', 's20', 's21', 's22', 's23', 's24', 's25', 's26', 's27',
's28'1
for i in range(6):
  position = springvecs[i][1] - springvecs[i][0]
   spring[i] = vp.cylinder(pos=springvecs[i][0], axis=position, length=vp.mag(position),
radius=.03, color=vp.color.white)
v = 0
dt = 0.003
mass = 0.1
q = 9.81
k sp = 1000
q \ vector = vp.vector(0, 9.81, 0)
for i in range(len(ballname)):
  ballname[i].velocity = vp.vector(0,0,0)
F c = vp.vector(0, 1000, 0)
L0= np.zeros((4, 4))
for i in range(4):
   for j in range(4):
      if i == j:
           position = ballname[j].pos - ballname[i].pos
           L0[j][i] = vp.mag(position)
\#F = np.zeros((8,3))
while 1:
   vp.rate(150)
   floor = vp.box(pos=vp.vector(ballvectors[1].x, -7, ballvectors[1].z), length=5, height=0.01,
width=5, color=vp.color.blue)
   scene.center.x = ballvectors[1].x
   scene.center.z = ballvectors[1].z
   for i in range(4):
```

```
ballvectors[i] = ballname[i].pos
   springvecs = []
   for z in itertools.combinations(ballvectors, 2):
       springvecs.append(z)
   for i in range(6):
      position = springvecs[i][1] - springvecs[i][0] #- L0[i]
       spring[i].pos = springvecs[i][0]
      spring[i].axis = position
      spring[i].length = vp.mag(position)
   dampening = 0.98
   F mat = np.zeros((4,4))
   F \text{ vec} = []
  F v = []
  a = np.array(np.zeros((4,4)))
  for i in range(4):
      for k in range(4):
           if k == i:
               L = 0
               F mat[i][k] = 0
               F vec.append(vp.vector(0, 0, 0))
           else:
               L = vp.mag(ballname[k].pos - ballname[i].pos) - L0[k][i]
               F mat[i][k] = L*k sp
               pf0 = ballname[k].pos - ballname[i].pos
               \#a[i,k] = vp.norm(pf0)*L*k_sp
               F_vec.append(vp.norm(pf0)*L*k_sp)
   a = np.array(F vec).reshape(4, 4)
   F = a.sum(axis=0)
   for i in range(4):
      F[i] = F[i] + g vector*mass
       if ballname[i].pos.y < floor.pos.y:</pre>
           F N = ((floor.pos.y-ballname[i].pos.y)**2)*10000
           F[i].y = 0.99*(F[i].y - F N)
           mu = 1
           F st = mu*F N
           F \text{ horiz} = (F[i].x ** 2 + F[i].z ** 2) ** 0.5
           v xz = (ballname[i].velocity.x ** 2 + ballname[i].velocity.z ** 2) ** 0.5
           vx = ballname[i].velocity.x / v xz
           vz = ballname[i].velocity.z / v xz
           if F st < F horiz:</pre>
               F[i].x += F horiz*vx - F N*vx
               F[i].z += F horiz*vz - F N*vz
           else:
               F[i].x = F horiz*vx
               F[i].z = F horiz*vz
               ballname[i].velocity.x = 0
               ballname[i].velocity.z = 0
           # print(F[i].x, F[i].z)
   for i in range(4):
       ballname[i].velocity -= F[i]/mass*dt
       ballname[i].pos += ballname[i].velocity*dt
       # if ballname[i].pos.y < floor.pos.y:</pre>
            ballname[i].velocity = dampening*-1*(ballname[i].velocity)+ F c*(floor.pos.y -
ballname[i].pos.y)*(floor.pos.y - ballname[i].pos.y)
```

GROUNDED NODE CODE:

```
import vpython as vp
import itertools
import numpy as np
scene = vp.canvas(width = 600, height = 400, center = vp.vector(0,0,0))
#vp.display(width=100, height=100)
floor = vp.box(pos=vp.vector(0,-5,0), length=8, height=0.01, width=8, color=vp.color.blue)
# -0.35 y for grounded node
ballname = ['b1', 'b2', 'b3', 'b4', 'b5', 'b6', 'b7', 'b8']
ballvectors = [vp.vector(0, 0, 0), vp.vector(0, 1, 0), vp.vector(0, 0, 1), vp.vector(1, 0, 0), vp.vector(1, 0, 0)]
vp.vector(1, 1, 0), vp.vector(0, 1, 1),
              vp.vector(1, 0, 1), vp.vector(1, 1, 1)]
for i in range(8):
   ballvectors[i] = ballvectors[i].rotate(angle=3.14/4, axis =vp.vector(1,0,1))
springvecs = []
for i in range(len(ballname)):
  ballname[i] = vp.sphere(pos=ballvectors[i], radius=0.1, color=vp.color.red, f k=
vp.vector(0,0,0))
for z in itertools.combinations(ballvectors, 2):
   springvecs.append(z)
spring = ['s1', 's2', 's3', 's4', 's5', 's6', 's7', 's8', 's9', 's10', 's11', 's12', 's13', 's14',
's15', 's16', 's17', 's18', 's19', 's20','s21', 's22', 's23', 's24', 's25', 's26', 's27', 's28']
for i in range (28):
  position = springvecs[i][1] - springvecs[i][0]
   spring[i] = vp.cylinder(pos=springvecs[i][0], axis=position, length=vp.mag(position),
radius=.03, color=vp.color.white)
\nabla = 0
dt = 0.003
mass = 0.1
q = 9.81
k sp = 1000
g vector = vp.vector(0, 9.81, 0)
for i in range(len(ballname)):
  ballname[i].velocity = vp.vector(0,0,0)
F c = vp.vector(0, 1000, 0)
L0= np.zeros((8,8))
dL = list(range(8))
for i in range(8):
   for j in range(8):
       if i == j:
           L0[j][i] = 0
       else:
           position = ballname[j].pos - ballname[i].pos
           L0[j][i] = vp.mag(position)
   dL[i] = (floor.pos.y - ballname[i].pos.y)
```

```
dt1 = dt
asdf = 100
\#F = np.zeros((8,3))
while 1:
   vp.rate(200)
   floor = vp.box(pos=vp.vector(ballvectors[1].x, -5, ballvectors[1].z), length=5, height=0.01,
width=5, color=vp.color.blue)
   #scene.center.x = ballvectors[1].x
   dL[i] += (floor.pos.y - ballname[i].pos.y)
   dt1 += .05
   for i in range(8):
      ballvectors[i] = ballname[i].pos
   springvecs = []
   for z in itertools.combinations(ballvectors, 2):
      springvecs.append(z)
   for i in range(28):
       position = springvecs[i][1] - springvecs[i][0] #- L0[i]
       spring[i].pos = springvecs[i][0]
       spring[i].axis = position
       spring[i].length = vp.mag(position)
   dampening = 0.9
   F mat = np.zeros((8,8))
   F \text{ vec} = []
   F v = []
   a = np.array(np.zeros((8,8)))
   for i in range(8):
      for k in range(8):
           if k == i:
               L = 0
               F mat[i][k] = 0
               F vec.append(vp.vector(0, 0, 0))
           else:
               L = vp.mag(ballname[k].pos - ballname[i].pos) - L0[k][i]
               F mat[i][k] = L*k sp
               pf0 = ballname[k].pos - ballname[i].pos
               \#a[i,k] = vp.norm(pf0)*L*k sp
               F vec.append(vp.norm(pf0)*L*k sp)
   a = np.array(F_vec).reshape(8, 8)
   F = a.sum(axis=0)
   #print(F)
   for i in range(1,8):
       F[i].y = F[i].y + g_vector.y*mass #- dampening*(dL[i])/dt1
       if ballname[i].pos.y < floor.pos.y:</pre>
           F N = ((floor.pos.y-ballname[i].pos.y)**2)*10000
           F[i].y = (F[i].y - F N) - dampening*(floor.pos.y-ballname[i].pos.y)
           mu = 1
           F st = mu*F N
           F \text{ horiz} = (F[i].x ** 2 + F[i].z ** 2) ** 0.5
           v xz = (ballname[i].velocity.x ** 2 + ballname[i].velocity.z ** 2) ** 0.5
           vx = ballname[i].velocity.x / v xz
           vz = ballname[i].velocity.z / v xz
           if F st < F horiz:</pre>
```

```
F[i].x += F_horiz*vx - F_N*vx
F[i].z += F_horiz*vz - F_N*vz
else:
    F[i].x = F_horiz*vx* dampening
    F[i].z = F_horiz*vz* dampening
    ballname[i].velocity.x = 0
    ballname[i].velocity.z = 0

print(F[i].x, F[i].z)
for i in range(1,8):
    ballname[i].velocity = ballname[i].velocity*0.999 - F[i]/mass*dt
    ballname[i].pos += ballname[i].velocity*dt
```