

	DList	Array	BST
data member in a node	_prev, _next, _data	_data	_left, _right, _data
operator++	Access by _next $O(1)$	Acquired by pointer arithmetic $O(1)$	1.Find the right child. If it exists, return right child. 2.一路往左上走，直到 parent 有 right child 為止 About $O(\log(n))$ if balanced
operator--	Access by _prev $O(1)$	Acquired by pointer arithmetic $O(1)$	1.Find the left child. If it exists, return left child. 2.一路往右上走，直到 parent 有 left child 為止 About $O(\log(n))$ if balanced
begin()	An iterator maintained in the class. $O(1)$	An iterator maintained in the class $O(1)$	An iterator maintained in the class $O(1)$
end()	An iterator maintained in the class. $O(1)$	Acquired by pointer arithmetic $O(1)$	An iterator maintained in the class $O(1)$
sort()	Insertion sort, $O(n^2)$	STL sort, $O(n\log(n))$	N/A
size()	Count the path from _head through _next to _head $O(n)$	A data member kept in the class $O(1)$	A data member kept in the class. $O(1)$
push_front()	Modify the first and the second to let them point to the new element $O(1)$	1.Move all the element backward to space out the memory for new element 2.Assign the element to the first position $O(n)$	1.Set _head->_leftChild to the newly added element. 2.Update _head by _head-- About $O(\log(n))$ if balanced
push_back()	Modify the last and the second last element to let them point the new element $O(1)$	1.Check whether capacity is enough, if not, declare a new memory. 2.Directly assign the element to the last. $O(1)$	1.Set _tail->rightChild to the newly added element 2.Update _tail by _tail++ About $O(\log(n))$ if balanced

insert(T&)	N/A	N/A	<p>1.Check whether the newly added element would change the head and the tail, if so, call push_front() and push_back() to handle it.</p> <p>2.Using binary search to find the appropriate position to insert.</p> <p>About <math>O(\log(n))</math> if balanced</p>
pop_front()	<p>Connect the second and the last element</p> <p><math>O(1)</math></p>	<p>1.Delete the first element.</p> <p>2.Move all the element forward.</p> <p><math>O(n)</math></p>	<p>1.Delete _head</p> <p>2.Assign the new head to _head</p> <p><math>O(1)</math></p>
pop_back()	<p>Connect the second last element and the first one.</p> <p><math>O(1)</math></p>	<p>Directly delete the last element.</p> <p><math>O(n)</math></p>	<p>1.Delete _tail</p> <p>2.Assign the new tail to _tail</p> <p><math>O(1)</math></p>
erase(T&)	<p>1.Find the required element from begin()</p> <p>2.Call the function below</p> <p><math>O(n)</math> to find</p>	<p>1.Find the required element from begin()</p> <p>2.Call the function below</p> <p><math>O(n)</math> to find</p>	<p>1.Find the required element from begin()</p> <p>2.Call the function below</p> <p><math>O(n)</math> to find</p>

erase(iterator)	Connect the neighbor nodes of the node to be deleted $O(1)$	1.Delete the element 2.Move the elements behind forward. $O(n)$	1.Check whether <code>_head</code> or <code>_tail</code> , if so, call <code>pop_back()</code> and <code>push_back()</code> to handle it, which can also maintain <code>_head</code> and <code>_tail</code> 2.For degree-0 node, delete it directly. 3.For degree-1 node, assign its child to its parent. 4.For degree-2 node, replace its value with its successor, then delete its successor. About $O(\log(n))$ if balanced
adta -r 200000	Prediction: Fast	Prediction: Fast	Prediction: Medium slow
	0.02sec	0.04sec	0.13sec
adtd -f 200000	Prediction: Fast	Prediction: Slow $O(n)$	Prediction: Medium slow
	0.01sec	239.4sec	0.05sec
adtd -b 200000	Prediction: Fast	Prediction: Slow $O(n)$	Prediction: Medium slow
	0.02sec	~0	0.06sec
adts	Prediction: very slow $O(n^2)$	Prediction: slow $O(n\log(n))$	N/A
	486.7sec	0.06sec	
adtd -r 20000	Prediction: Slow	Prediction: Fast $O(1)$	Prediction: Medium slow $O(\log(n))$
	1.17sec	3.57sec	260.1sec
memory use	10.24MB	12.1MB	10.98MB

p.s. the “`_tail`” in bst here I means the last element, not the dummy point.

“adtd -r 20000” is most beyond prediction. Maybe the most time consuming for bst is “getPos”, from `_head` to traverse to the given position. BST needs much more time than dlist to access the next node.(Maybe there’s better solution for it)

And the time needed for random delete for array is also non-intuitive. I guess most time is consumed on moving the elements.

Conclusion: dlist and array are easy and intuitive, but both has drawbacks, which is extremely slow and can be fatal disadvantage. Though BST is harder to visualize, but its  $\log(n)$  performance is obviously better than  $O(n)$ .