Reality

Difficult shapes
Difficult stress fields
Non linear materials
Tangential forces from friction
Impossible to solve

Simplifying Assumptions: Shapes simplified by taylor

series expansion (Both shapes represented by parabolas)
Surfaces are treated as half spaces There is no friciton
Materials are purely elastic

The problem Hertz solved:

What normal pressure distribution can be applied to two half spaces so the total deflection in the normal direction is equal to the interferance between two parabolas:

Parabola for first surface u(x,y): total deflection Parabola for second surface P(x,y): load E_1 , V_1 E_2 , V_2