# CSC 211: Computer Programming

(Recursive) Backtracking

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#### Administrative Announcements

- A03 due 03/28
- MC05 due 03/21
- Exam# 02 04/02

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#### **Recursion Reminder**

- Problem solving technique in which we solve a task by reducing it to smaller tasks (of the same kind)
  - √ then use same approach to solve the smaller tasks
- Technically, a recursive function is one that calls itself
- · General form:
  - ✓ base case
  - solution for a trivial case
  - it can be used to stop the recursion (prevents "stack overflow")
  - every recursive algorithm needs at least one base case
  - ✓ recursive call(s)
  - divide problem into **smaller instance(s)** of the **same structure**

#### **Recursion Reminder**

- Recursive Checklist:
  - Find what information we need to keep track of. What inputs/outputs are needed to solve the problem at each step?
  - Find our base case(s). What are the simplest (nonrecursive) instance(s) of this problem?
  - Find our recursive step. How can this problem be solved in terms of one or more simpler instances of the same problem that lead to a base case?
  - Figure every input is handled. Do we cover all possible cases? Do we need to handle errors?

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  - Find our recursive step. How can this problem be solved in terms of one or more simpler instances of the same problem that lead to a base case?
  - Ensure every input is handled. Do we cover all possible cases? Do we need to handle errors?

Backtracking

 Write a recursive function printAllBinary that accepts an integer number of digits and prints all binary numbers that have exactly that many digits, in ascending order, one per line

printAllBinary(2);	printAllBinary(3);			
00	000			
01	001			
10	010			
11	011			
	100			
	101			
	110			
	111			

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#### **Decision Trees**

#### printAllBinary(2);

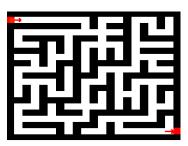
			digits	soFar			
			2	11 11			
			0				
	1	"0"		1	"1"		
	0	$\frown$	1		0	$\frown$	1
0	"00"	0	"01"	0	"10"	0	"11"

- · This kind of diagram is called a call tree or decision tree
- · Think of each call as a choice or decision made by the algorithm:
- Should I choose 0 as the next digit?
- Should I choose 1 as the next digit?
- The idea is to try every permutation. For every position, there are 2 options, either '0' or '1'. Backtracking
  can be used in this approach to try every possibility or permutation to generate the correct set of strings.

# Backtracking

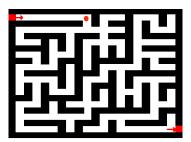
 Recursive Backtracking: using recursion to explore solutions to a problem and abandoning them if they are not suitable

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• Recursive Backtracking: using recursion to explore solutions to a problem and abandoning them if they are not suitable

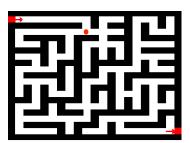
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## Backtracking

• Recursive Backtracking: using recursion to explore solutions to a problem and abandoning them if they are not suitable

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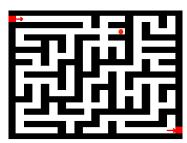


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# Backtracking

• Recursive Backtracking: using recursion to explore solutions to a problem and abandoning them if they are not suitable

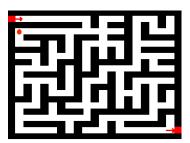
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# Backtracking

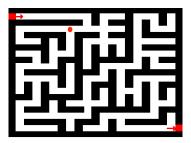
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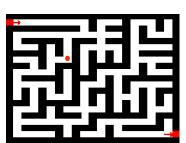
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#### Backtracking

 Recursive Backtracking: using recursion to explore solutions to a problem and abandoning them if they are not suitable

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# Backtracking

• Let's take a look at a problem similar to the binarySequence problem.

 Write a recursive function diceRoll that accepts an integer representing a number of 6-sided dice to roll, and output all possible permutations of values that could appear on the dice.

$\{1,1\}$	$\{3, 1\}$	$\{5, 1\}$
{1, 2}	{3, 2}	{5, 2}
$\{1, 3\}$	{3, 3}	{5, 3}
$\{1, 4\}$	{3, 4}	<i>{</i> 5 <i>,</i> 4 <i>}</i>
$\{1, 5\}$	{3, 5}	{5 <i>,</i> 5}
$\{1, 6\}$	{3, 6}	{5, 6}
$\{2, 1\}$	{4, 1}	{6, 1}
{2, 2}	{4, 2}	{6, 2}
$\{2, 3\}$	{4, 3}	{6, 3}
$\{2, 4\}$	$\{4, 4\}$	$\{6, 4\}$

 $\{4, 5\}$ 

 $\{4, 6\}$ 

 $\{6, 5\}$ 

 $\{6, 6\}$ 

 $\{2, 5\}$ 

 $\{2, 6\}$ 

diceRoll(2)

## Backtracking

- Backtracking Checklist:
  - Find what choice(s) we have at each step. What different options are there for the next step?

For each valid choice:

- **Make it and explore recursively.** Pass the information for a choice to the next recursive call(s).
- **Undo it after exploring.** Restore everything to the way it was before making this choice.
- **Find our base case(s).** What should we do when we are out of decisions?

- Backtracking Checklist:
  - Find what choice(s) we have at each step. What different options are there for the next step?

What die value should I choose next?

Undo it after exploring. Restore everything to the way i

#### Backtracking

- Backtracking Checklist:

#### For each valid choice:

- Make it and explore recursively. Pass the information for a choice to the next recursive call(s).

We need to communicate the dice chosen so far to the next recursive call

## **Backtracking**

Backtracking Checklist:

We need to be able to remove the die we added to our first roll so far

#### For each valid choice:

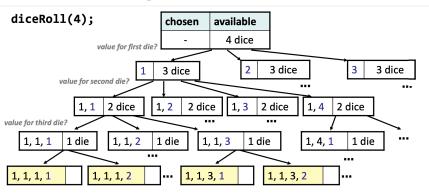
- **Undo it after exploring.** Restore everything to the way it was before making this choice.

# **Backtracking**

- Backtracking Checklist:

We have no dice left to choose, print them out

Find our base case(s). What should we do when we are out of decisions?



- · Observations?
- · This is a really big search space.
- Depending on approach, we can make wasteful decisions.
   Can we optimize it? Yes. Will we right now? No.

#### Backtracking

• Let's us write flexible code, allowing us to make a decision and "backtrack" if we need to

9	8	1	7 9 6	5		6	
9	8	1		5		6	
9	8		6			6	_
			6				
			, J				3
		8		3			1
			2				6
6					2	8	
		4	1	9			5 9
			8			7	9
	6	6	6	6 4 1	6 4 1 9	2 2 6 2 4 1 9	2 2 8 4 1 9

5	3	4	6	7	8	9	1	2
6	7	2	1	9	5	ര	4	8
1	9	8	3	4	2	5	6	7
8	5	9	7	6	1	4	2	3
4	2	6	8	5	3	7	9	1
7	1	3	9	2	4	8	5	6
9	6	1	5	3	7	2	8	4
2	8	7	4	1	9	6	3	5
3	4	5	2	8	6	1	7	9

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# Backtracking

- · Pseudocode
- function diceRolls(dice, chosenArr):
   if dice == 0:
   Print current roll.
- Write a recursive function diceRoll that accepts an integer representing a number of 6-sided dice to roll, and output all possible combinations of values that could appear on the dice.

else:

// handle all roll values for a single die; let recursion do the rest.

for each die value i in range [1..6]:

choose that the current die will have value i

// explore the remaining dice

diceRolls(dice-1, chosenArr)

un-choose (backtrack) the value I

\*\* Need to keep track of our choices somehow

Code Demo