606 Chapter 3 Lab

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```
load("more/bdims.RData")
mdims <- subset(bdims, sex == 1)
fdims <- subset(bdims, sex == 0)
head(bdims)
     bia.di bii.di bit.di che.de che.di elb.di wri.di kne.di ank.di sho.gi
##
## 1
       42.9
               26.0
                                      28.0
                                                     10.4
                                                                     14.1 106.2
                      31.5
                              17.7
                                              13.1
                                                             18.8
                                                                     15.1
## 2
       43.7
               28.5
                       33.5
                              16.9
                                      30.8
                                              14.0
                                                     11.8
                                                             20.6
                                                                           110.5
## 3
       40.1
               28.2
                      33.3
                              20.9
                                      31.7
                                              13.9
                                                     10.9
                                                             19.7
                                                                     14.1
                                                                           115.1
## 4
       44.3
               29.9
                       34.0
                              18.4
                                      28.2
                                              13.9
                                                     11.2
                                                             20.9
                                                                     15.0
                                                                           104.5
## 5
       42.5
               29.9
                      34.0
                              21.5
                                      29.4
                                              15.2
                                                             20.7
                                                                     14.9
                                                                           107.5
                                                     11.6
## 6
       43.3
               27.0
                      31.5
                              19.6
                                      31.3
                                              14.0
                                                     11.5
                                                             18.8
                                                                     13.9
                                                                           119.8
##
     che.gi wai.gi nav.gi hip.gi thi.gi bic.gi for.gi kne.gi cal.gi ank.gi
## 1
       89.5
               71.5
                                      51.5
                                              32.5
                                                     26.0
                                                             34.5
                                                                    36.5
                                                                            23.5
                      74.5
                              93.5
## 2
       97.0
               79.0
                       86.5
                              94.8
                                      51.5
                                              34.4
                                                     28.0
                                                             36.5
                                                                     37.5
                                                                            24.5
## 3
       97.5
               83.2
                      82.9
                              95.0
                                      57.3
                                              33.4
                                                     28.8
                                                             37.0
                                                                    37.3
                                                                            21.9
## 4
       97.0
               77.8
                       78.8
                              94.0
                                      53.0
                                              31.0
                                                     26.2
                                                             37.0
                                                                     34.8
                                                                            23.0
               80.0
                              98.5
## 5
       97.5
                      82.5
                                      55.4
                                              32.0
                                                     28.4
                                                             37.7
                                                                     38.6
                                                                            24.4
## 6
       99.9
               82.5
                       80.1
                              95.3
                                      57.5
                                              33.0
                                                     28.0
                                                             36.6
                                                                     36.1
                                                                            23.5
##
     wri.gi age wgt
                         hgt sex
       16.5
             21 65.6 174.0
## 1
                               1
## 2
       17.0
             23 71.8 175.3
                               1
## 3
       16.9
             28 80.7 193.5
                               1
## 4
       16.6
             23 72.6 186.5
                               1
              22 78.8 187.2
## 5
       18.0
                               1
## 6
       16.9
             21 74.8 181.5
```

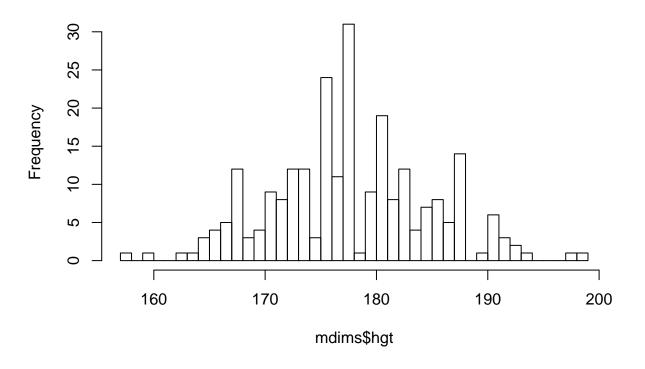
The normal distribution

1. Make a histogram of men's heights and a histogram of women's heights. How would you compare the various aspects of the two distributions?

Based on the histograms, most frequent height for men and women is around 178 and 158.

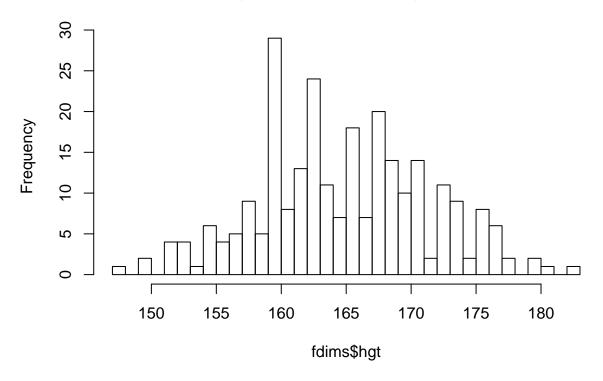
```
hist(mdims$hgt, breaks = 50, main = "Histogram of Men Heights in cm")
```

Histogram of Men Heights in cm



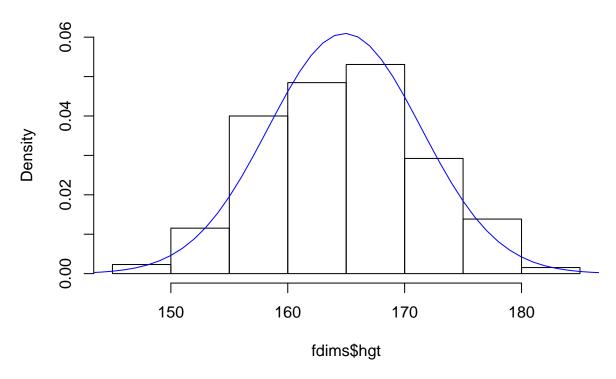
hist(fdims\$hgt, breaks = 50, main = "Histogram of Women Heights in cm")

Histogram of Women Heights in cm



```
fhgtmean <- mean(fdims$hgt)</pre>
fhgtsd <- sd(fdims$hgt)</pre>
fwgtmean <- mean(fdims$wgt)</pre>
fwgtsd <- sd(fdims$wgt)</pre>
fhgtmean
## [1] 164.8723
fhgtsd
## [1] 6.544602
fwgtmean
## [1] 60.60038
fwgtsd
## [1] 9.615699
hist(fdims$hgt, probability = TRUE, ylim = c(0, 0.06))
x <- 140:190
y <- dnorm(x = x, mean = fhgtmean, sd = fhgtsd)
lines(x = x, y = y, col = "blue")
```

Histogram of fdims\$hgt

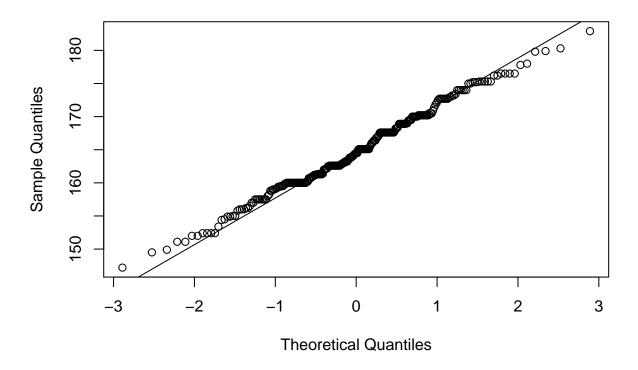


2. Based on the this plot, does it appear that the data follow a nearly normal distribution? Yes, based on the plot it appears to follow a normal distribution.

Evaluating the normal distribution

```
qqnorm(fdims$hgt)
qqline(fdims$hgt)
```

Normal Q-Q Plot

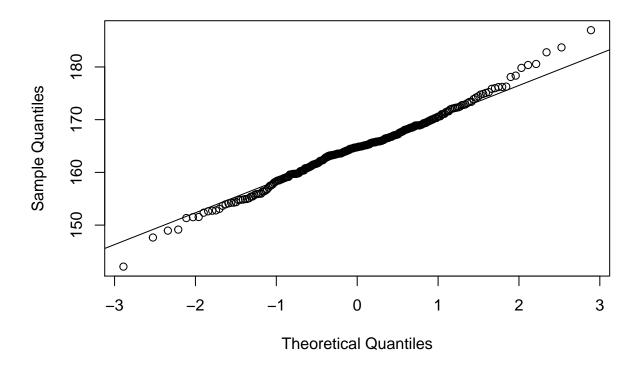


```
sim_norm <- rnorm(n = length(fdims$hgt), mean = fhgtmean, sd = fhgtsd)</pre>
```

3. Make a normal probability plot of sim_norm. Do all of the points fall on the line? How does this plot compare to the probability plot for the real data?

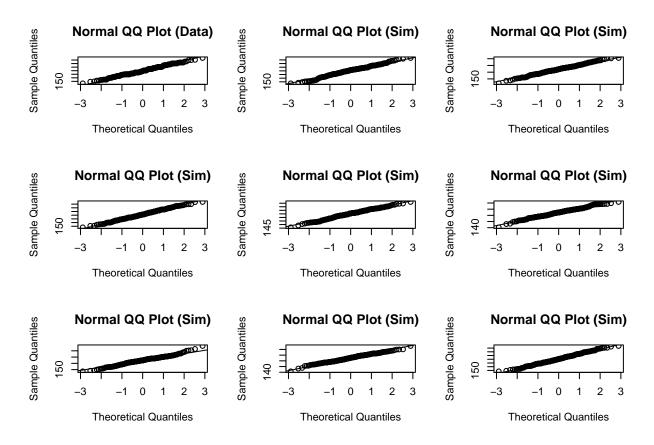
qqnorm(sim_norm)
qqline(sim_norm)

Normal Q-Q Plot



the simulated model is similar to the probability plot of the real data where most of the data is on the line except at the tails.

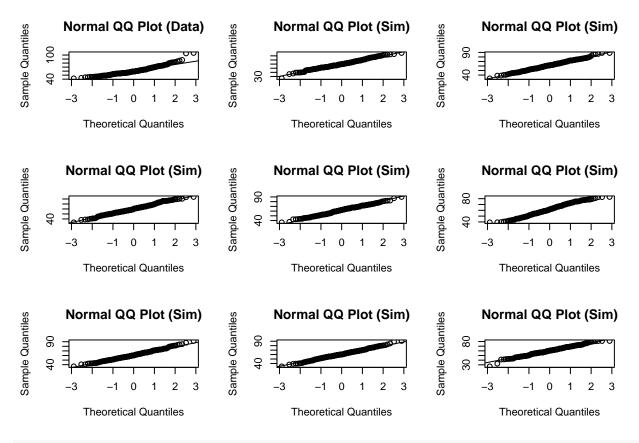
qqnormsim(fdims\$hgt)



4. Does the normal probability plot for fdims\$hgt look similar to the plots created for the simulated data? That is, do plots provide evidence that the female heights are nearly normal?

Yes, the normal probablity plot for female heights look similar the plots created for the simulated data. Its follows the line except for at the tails of the line.

F_Weight <- qqnormsim(fdims\$wgt)



F_Weight

\$mfrow ## [1] 3 3

5. Using the same technique, determine whether or not female weights appear to come from a normal distribution.

Female weight also appear to come from a normal distribution except at the tails but, the simulations do not have the outliers that are in the real data .

Normal probabilities

```
1 - pnorm(q = 182, mean = fhgtmean, sd = fhgtsd)
## [1] 0.004434387
sum(fdims$hgt > 182) / length(fdims$hgt)
```

[1] 0.003846154

6. Write out two probability questions that you would like to answer; one regarding female heights and one regarding female weights. Calculate the those probabilities using both the theoretical normal distribution as well as the empirical distribution (four probabilities in all). Which variable, height or weight, had a closer agreement between the two methods?

What is the probability that randomly chosen female is taller than (5'11) 180 cm?

```
1 - pnorm(q = 180, mean = fhgtmean, sd =fhgtsd)

## [1] 0.01040328

sum(fdims$hgt > 180) / length(fdims$hgt)

## [1] 0.007692308

What is the probablity that randomly chosen female is under 175 lbs?

pnorm(q = 79, mean = fwgtmean, sd =fwgtsd)

## [1] 0.9721578

sum(fdims$wgt < 79) / length(fdims$wgt)</pre>
```

[1] 0.9538462

Between the probability models, the weight had a closer agreement between the two methods. The theoretical normal distribution predicts that there are 97.2% chance that a random chosen female is under 175 lbs while the empirical distribution says that there are is a 95.4% chance.

On Your Own

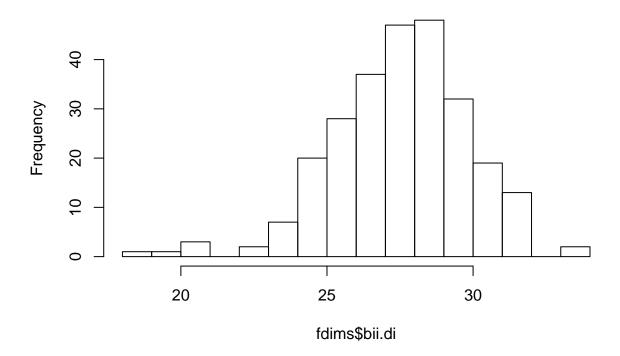
• Now let's consider some of the other variables in the body dimensions data set. Using the figures at the end of the exercises, match the histogram to its normal probability plot. All of the variables have been standardized (first subtract the mean, then divide by the standard deviation), so the units won't be of any help. If you are uncertain based on these figures, generate the plots in R to check.

```
fdims[1:20 ,]
```

```
##
       bia.di bii.di bit.di che.de che.di elb.di wri.di kne.di ank.di sho.gi
## 248
          37.6
                  25.0
                          31.3
                                  16.2
                                          24.9
                                                  11.2
                                                           9.2
                                                                  17.0
                                                                          12.3
                                                                                  95.0
##
   249
          36.7
                  26.4
                          31.0
                                  16.8
                                          24.5
                                                  12.1
                                                           9.9
                                                                  19.3
                                                                          12.8
                                                                                  99.5
   250
##
          34.8
                  25.9
                          30.2
                                  16.4
                                          24.2
                                                  11.3
                                                           8.9
                                                                  17.0
                                                                          12.2
                                                                                  88.0
  251
                  27.9
                                                  12.3
                                                                  18.6
                                                                          13.0
                                                                                  97.0
##
          36.6
                          31.8
                                  19.3
                                          24.9
                                                           9.5
##
   252
          35.5
                  28.2
                          31.0
                                  18.2
                                          26.2
                                                  11.5
                                                           9.1
                                                                  17.2
                                                                          12.4
                                                                                103.3
                                                                  17.2
##
  253
          37.0
                  28.0
                          32.0
                                  15.1
                                          25.7
                                                  12.5
                                                          10.0
                                                                          13.2
                                                                                  93.5
##
  254
          35.5
                  26.5
                          29.2
                                  15.4
                                          24.5
                                                  12.3
                                                           9.4
                                                                  17.2
                                                                          12.0
                                                                                  93.3
  255
                  30.2
          37.4
                          33.2
                                  18.8
                                          26.6
                                                  13.3
                                                          10.7
                                                                  19.8
                                                                          13.8
                                                                                  94.5
##
  256
          37.8
                  29.0
                          32.6
                                  18.6
                                          25.0
                                                  12.1
                                                           9.8
                                                                  17.8
                                                                          12.7
                                                                                  98.6
##
## 257
                  28.8
                          33.2
                                                  13.4
                                                                  20.9
          38.6
                                  19.7
                                          29.4
                                                          11.5
                                                                          13.2
                                                                                115.5
  258
          37.6
                  28.5
                          32.2
                                  15.5
                                          24.3
                                                  11.8
                                                           8.6
                                                                  17.1
                                                                          11.9
                                                                                  97.9
##
   259
          36.0
                  25.6
                          31.5
                                  15.4
                                          25.5
                                                  12.8
                                                           9.7
                                                                  17.6
                                                                          13.2
                                                                                  97.7
##
   260
          39.5
                  30.0
                          31.7
                                  17.3
                                          27.3
                                                  12.8
                                                           9.2
                                                                  18.1
                                                                          12.4
                                                                                100.5
##
  261
          34.0
                  25.0
                          27.0
                                  16.9
                                          22.6
                                                  10.6
                                                           8.3
                                                                  15.9
                                                                          11.6
                                                                                  88.7
## 262
          35.0
                  26.5
                          31.6
                                  18.3
                                          23.7
                                                  11.5
                                                           8.6
                                                                  16.8
                                                                          12.2
                                                                                  96.6
## 263
          35.6
                  25.8
                          32.0
                                  16.2
                                          25.7
                                                  11.5
                                                           9.0
                                                                  17.2
                                                                          11.8
                                                                                  92.0
## 264
          36.2
                  27.4
                          29.5
                                  14.6
                                          23.9
                                                  11.2
                                                           9.6
                                                                  16.7
                                                                          12.6
                                                                                  90.0
  265
##
          39.0
                  28.4
                          34.9
                                  19.6
                                          26.7
                                                  13.4
                                                          11.0
                                                                  18.9
                                                                          13.6
                                                                                104.0
  266
          32.6
                  25.6
                          30.0
                                  15.3
                                          22.6
                                                  10.3
                                                           8.1
                                                                  16.2
                                                                                 90.1
##
                                                                          11.6
##
   267
          37.6
                  30.0
                          33.9
                                  19.1
                                          28.8
                                                  13.4
                                                          10.5
                                                                  19.2
                                                                          13.2
                                                                                104.0
##
       che.gi wai.gi nav.gi hip.gi thi.gi bic.gi for.gi kne.gi cal.gi ank.gi
## 248
          83.0
                  66.5
                          79.0
                                  92.0
                                          53.5
                                                  24.3
                                                          20.5
                                                                  32.0
                                                                          32.2
                                                                                  21.0
## 249
          78.5
                  61.5
                          70.5
                                  90.5
                                          57.7
                                                  27.8
                                                          24.0
                                                                  38.5
                                                                          38.5
                                                                                  22.5
## 250
          75.0
                  61.2
                          66.5
                                  91.0
                                          53.0
                                                  24.0
                                                          22.0
                                                                  32.5
                                                                          32.5
                                                                                  19.0
                                                  28.0
## 251
          86.5
                  78.0
                          91.0
                                  99.5
                                          61.5
                                                          24.0
                                                                  35.2
                                                                          36.7
                                                                                  23.0
```

```
70.5
## 252
         91.0
                         80.5
                                91.5
                                        55.0
                                               26.9
                                                       22.7
                                                               33.0
                                                                      33.3
                                                                              19.9
## 253
                 66.5
                         78.5
                                94.0
                                               26.5
                                                       22.5
                                                               34.0
                                                                      35.0
                                                                              23.0
         79.5
                                        54.0
## 254
         77.0
                 58.0
                         64.0
                                85.5
                                        49.5
                                               24.1
                                                       22.0
                                                               32.5
                                                                      32.0
                                                                              19.0
## 255
                 74.5
         88.0
                         87.0
                               104.0
                                               29.2
                                                       26.2
                                                               38.5
                                                                      38.0
                                                                              22.0
                                        64.0
##
  256
         85.0
                 73.5
                         92.0
                               104.1
                                        65.3
                                               29.0
                                                       23.4
                                                               35.3
                                                                      37.4
                                                                              21.6
## 257
         98.8
                 90.5
                       103.5
                               108.1
                                               33.6
                                                       26.6
                                                               37.2
                                                                      35.8
                                                                              22.6
                                        61.1
## 258
         79.0
                 66.5
                         74.0
                                90.3
                                               24.8
                                                               32.2
                                                                      32.5
                                                                              19.9
                                        52.0
                                                       21.0
                         71.8
                                                                              20.5
## 259
         77.6
                 61.0
                                91.6
                                        53.0
                                               25.4
                                                       22.6
                                                               34.0
                                                                      34.5
## 260
         85.0
                 69.5
                         81.5
                                94.4
                                        55.8
                                               25.9
                                                       22.9
                                                               36.1
                                                                      35.3
                                                                              20.9
## 261
                                80.9
                                                       20.5
                                                                              17.9
         76.7
                 62.0
                         74.1
                                        48.8
                                               24.0
                                                               30.8
                                                                      30.4
## 262
         76.7
                 63.4
                         69.0
                                87.7
                                        54.0
                                               25.6
                                                       21.6
                                                               34.4
                                                                      32.8
                                                                              19.1
                                        54.5
## 263
         82.0
                 71.0
                         69.0
                                88.5
                                               26.0
                                                       21.8
                                                               33.5
                                                                      35.0
                                                                              21.0
## 264
         79.0
                 59.0
                        79.0
                                88.5
                                        51.2
                                               23.5
                                                       21.0
                                                               32.5
                                                                      29.6
                                                                              18.5
## 265
         89.5
                 74.0
                                        61.5
                                               31.0
                                                       26.5
                                                                      38.6
                                                                              23.8
                         92.0
                               101.0
                                                               38.6
## 266
         73.5
                 60.5
                         68.3
                                88.5
                                        54.0
                                               24.6
                                                       20.6
                                                               29.0
                                                                      33.0
                                                                              19.0
## 267
         90.0
                 75.0
                         80.5
                                99.0
                                        59.0
                                               28.7
                                                       24.9
                                                               37.0
                                                                      36.5
                                                                              20.6
##
       wri.gi age wgt
                           hgt sex
## 248
         13.5
                22 51.6 161.2
                                 0
         15.0
                20 59.0 167.5
## 249
                                 0
## 250
         14.0
                19 49.2 159.5
                                 0
## 251
         15.0
                25 63.0 157.0
                                 0
## 252
         14.5
                21 53.6 155.8
                                 0
## 253
         14.5
                23 59.0 170.0
                                 0
## 254
         13.9
                26 47.6 159.1
                                 0
         16.8 22 69.8 166.0
## 255
                                 0
## 256
         15.2
                28 66.8 176.2
                                 0
## 257
         16.3
                40 75.2 160.2
                                 0
## 258
         13.8
                32 55.2 172.5
                                 0
## 259
         15.3
                25 54.2 170.9
                                 0
                25 62.5 172.9
## 260
         14.4
                                 0
## 261
         13.2
                29 42.0 153.4
                                 0
## 262
         13.8
                22 50.0 160.0
                                 0
## 263
         14.0
                25 49.8 147.2
         14.5
                23 49.2 168.2
## 264
                                 0
## 265
         17.0
                37 73.2 175.0
                                 0
## 266
         13.2 19 47.8 157.0
                                 0
## 267
         15.9 23 68.8 167.6
hist(fdims$bii.di, breaks = 20)
```

Histogram of fdims\$bii.di



a. The histogram for female biiliac (pelvic) diameter (`bii.di`) belongs to normal probability plot letter ${\tt D}$.

b. The histogram for female elbow diameter (`elb.di`) belongs to normal probability plot letter C.

c. The histogram for general age (`age`) belongs to normal probability plot letter B.

d. The histogram for female chest depth (`che.de`) belongs to normal probability plot letter A.

• Note that normal probability plots C and D have a slight stepwise pattern. Why do you think this is the case?

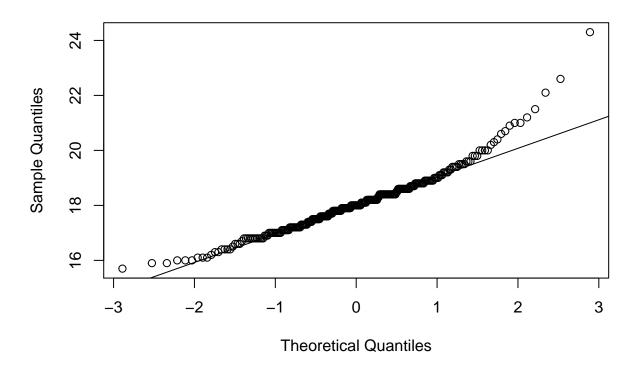
The are measurements of diameters of the pelvic and elbow, and there they're all around the same size.

• As you can see, normal probability plots can be used both to assess normality and visualize skewness. Make a normal probability plot for female knee diameter (kne.di). Based on this normal probability plot, is this variable left skewed, symmetric, or right skewed? Use a histogram to confirm your findings.

The normal probability plot for female knee diameter looks like it is skewed right.

```
qqnorm(fdims$kne.di)
qqline(fdims$kne.di)
```

Normal Q-Q Plot



```
range(fdims$kne.di)

## [1] 15.7 24.3

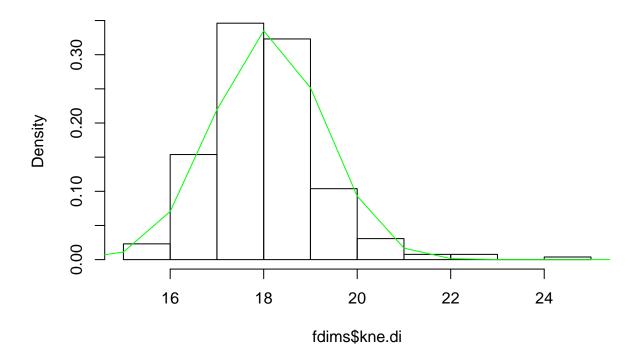
fknee.dimean <- mean(fdims$kne.di)

fknee.disd <-sd(fdims$kne.di)

hist(fdims$kne.di, probability = TRUE,)

x <- 1:100
y <- dnorm(x = x, mean = fknee.dimean, sd = fknee.disd)
lines(x = x, y = y, col = "green")</pre>
```

Histogram of fdims\$kne.di



Based on the historgram, it looks like the data is skewed right.