

# Stack ADT using a model SEQ[G]

Class SEQ[G] is part of library **mathmodels**.

In OOSC2, the ADT specification of a stack is given as follows:

ADT specification of stacks	
<b>TYPES</b>	
• <i>STACK</i> [G]	
<b>FUNCTIONS</b>	
• <i>put</i> : <i>STACK</i> [G] $\times$ <i>G</i> $\rightarrow$ <i>STACK</i> [G]	
• <i>remove</i> : <i>STACK</i> [G] $\rightarrow$ <i>STACK</i> [G]	
• <i>item</i> : <i>STACK</i> [G] $\rightarrow$ <i>G</i>	
• <i>empty</i> : <i>STACK</i> [G] $\rightarrow$ <i>BOOLEAN</i>	
• <i>new</i> : <i>STACK</i> [G]	
<b>AXIOMS</b>	
For any <i>x</i> : <i>G</i> , <i>s</i> : <i>STACK</i> [G]	
A1 • <i>item</i> ( <i>put</i> ( <i>s</i> , <i>x</i> )) = <i>x</i>	
A2 • <i>remove</i> ( <i>put</i> ( <i>s</i> , <i>x</i> )) = <i>s</i>	
A3 • <i>empty</i> ( <i>new</i> )	
A4 • <b>not</b> <i>empty</i> ( <i>put</i> ( <i>s</i> , <i>x</i> ))	
<b>PRECONDITIONS</b>	
• <i>remove</i> ( <i>s</i> : <i>STACK</i> [G]) <b>require not empty</b> ( <i>s</i> )	
• <i>item</i> ( <i>s</i> : <i>STACK</i> [G]) <b>require not empty</b> ( <i>s</i> )	

We will use SEQ[G] as a mathematical model for an abstract stack class, allowing not only classical contracts but also complete contracts.

## Chart View of SEQ[G]

```
class
  SEQ [G -> attached ANY]

General
  cluster: mathmodels
  description:
    "(1) Model contracts for finite sequences for elements of type G.
    (2) Queries are side effect free and return sequences via
        deep_twin; thus inefficient (use only for contracts).
    (3) Commands change the current sequence.
    (4) A valid index is 1..count.
    (5) Array notation can be used, as well as iteration (across).
    (6) Empty sequences can be created, or creation can be from an array.
    (7) Sequences have a first item (the head), a tail and last item.
    (8) Infix notation for prepended_by(x:G):
        seq1 |< x
    (9) Infix notation for appended_by(x:G):
        seq1 |> x
    (10) For concatenation may use infix: seq1 |++| seq2
    (11) For queries, to assert that the state is not changed,
        the postcondition is
        Current ~ old Current.deep_twin"
  create: make_empty, make_from_array

Ancestors
  DEBUG_OUTPUT*
  ITERABLE* [G]

Queries
  appended alias "|->" (v: G): [like Current] attached SEQ [G]
  as_array: ARRAY [G]
  as_function: FUN [INTEGER_32, G]
  comprehension alias "|" (exp: PREDICATE [PAIR [INTEGER_32, G]]):
    [like Current] attached SEQ [G]
  concatenated alias "|++|" (other: [like Current] attached SEQ [G]):
    [like Current] attached SEQ [G]
    [like Current] attached SEQ [G]

  count alias "#": INTEGER_32
  debug_output: STRING_8
  first: G
  front: [like Current] attached SEQ [G]
  has (v: G): BOOLEAN
  hold_count (exp: PREDICATE [PAIR [INTEGER_32, G]]): INTEGER_32
  inserted (v: G; i: INTEGER_32): [like Current] attached SEQ [G]
  is_contiguous_subseq_of (other: [like Current] attached SEQ [G]): BOOLEAN
  is_empty: BOOLEAN
  is_equal (other: [like Current] attached SEQ [G]): BOOLEAN
  is_subsequence_of alias "|<:" (other: [like Current] attached SEQ [G]): BOOLEAN
  item alias "[]" (i: INTEGER_32): G
  last: G
  lower: INTEGER_32
  new_cursor: ITERATION_CURSOR [G]
  out: STRING_8
  overridden (v: G; i: INTEGER_32): [like Current] attached SEQ [G]
  prepended alias "|<-" (v: G): [like Current] attached SEQ [G]
  removed (i: INTEGER_32): [like Current] attached SEQ [G]
  reversed: [like Current] attached SEQ [G]
  slice (a_start, a_end, a_step: INTEGER_32): [like Current] attached SEQ [G]
  subsequenced (i, j: INTEGER_32): [like Current] attached SEQ [G]
  tail: [like Current] attached SEQ [G]
  twin2: [like Current] attached SEQ [G]
  upper: INTEGER_32
  valid_position (pos: INTEGER_32): BOOLEAN

Commands
  append (v: G)
  concatenate (other: [like Current] attached SEQ [G])
  insert (v: G; i: INTEGER_32)
  make_empty
```

```

make_from_array (a: ARRAY [G])
override (v: G; i: INTEGER_32)
prepend (v: G)
remove (i: INTEGER_32)
reverse
subsequence (i, j: INTEGER_32)

```

#### Constraints

```

value semantics
value semantics
value semantics
value semantics
properties:
  not is_empty implies
    Current ~ tail.prepended (first) and Current ~ front.appended (last)

```

## ADT-STACK

```

note
  description: "[
    Abstract Data Type for a Stack, with value semantics.
    Classic contracts vs. Complete contracts with a model.
  ]"
  author: "JSO"

deferred class
  ADT_STACK [G -> attached ANY]

inherit
  ANY
    undefine
      is_equal
    end

feature -- model
  model: SEQ [G]
    -- abstract mathematical description of stack
    -- abstraction function
  deferred
  end

feature -- queries
  count: INTEGER_32
    -- number of items in stack
  deferred
  ensure
    complete: Result = model.count
  end

  is_empty: BOOLEAN
    -- is the queue empty?
  deferred
  ensure
    complete: Result = model.is_empty
  end

  item: G
    -- Top element of stack ("peek")
  require
    not is_empty
  deferred
  ensure
    complete: Result ~ model.last
  end

```

```

is_equal (other: like Current): BOOLEAN
    -- Is `other' attached to an object considered
    -- equal to current object?
    deferred
    ensure then
        complete: model ~ other.model
    end

feature -- commands

    make_empty
        -- Initialization for `Current'.
        deferred
        ensure
            classic: is_empty
        end

    put (x: G)
        -- push 'x' on top of stack ("push")
        deferred
        ensure
            classic: count = old count + 1
            classic: item ~ x
            complete: model ~ ((old model) |-> x)
        end

    remove
        -- pop off top of stack ("pop")
        require
            not is_empty
        deferred
        ensure
            classic: count = old count - 1
            complete: (old model) ~ (model |-> (old item))
        end

feature -- axioms

    axiom (x: G)
        do
            Current.put (x)
            Current.remove
        ensure
            model ~ (old model)
        end

end -- class ADT_STACK

```

## MY\_STACK text

```
class
  MY_STACK [G -> attached ANY]

inherit
  ADT_STACK [G]

create
  make_empty

feature {ADT_STACK} -- Initialization

  imp: LINKED_LIST [G]
      -- implementation

  make_empty
      -- Initialization for `Current`.
      do
        create imp.make
        imp.compare_objects
      end

feature -- model

  model: SEQ [G]
      -- abstract mathematical description of stack
      -- abstraction function
      do
        create Result.make_empty
        across
          imp as cr
        loop
          Result.append (cr.item)
        end
      end

feature -- queries

  count: INTEGER_32
      -- number of items in stack
      do
        Result := imp.count
      end

  is_empty: BOOLEAN
      -- is the queue empty?
      do
        Result := imp.is_empty
      end

  item: G
      -- Top element of stack ("peek")
      do
        Result := imp.last
      end

  is_equal (other: like Current): BOOLEAN
      -- Is `other' attached to an object considered
      -- equal to current object?
      do
        Result := imp ~ other.imp
      end
```

```
feature -- command

  put (x: G)
    -- push 'x' on top of stack ("push")
    do
      imp.extend (x)
    end

  remove
    -- pop off top of stack ("pop")
    do
      imp.go_i_th (imp.count)
      imp.remove
    end

end -- class MY_STACK

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-- For more details: http://www.eiffel.com --
```