

# ML\_HW1\_mj2776

Mike Jaron

2/2/2017

Q1

a)

$$p(x_1 \dots x_n | \pi_i) = \prod_{i=1}^n \left[ \binom{x_i + r - 1}{x_i} \pi^{x_i} (1 - \pi)^r \right]$$

b)

$$\sum_{i=1}^n \nabla_{\pi} \ln \left[ \binom{x_i + r - 1}{x_i} \pi^{x_i} (1 - \pi)^r \right] = 0$$

$$\sum_{i=1}^n \nabla_{\pi} \ln \left[ \binom{x_i + r - 1}{x_i} + x_i * \ln(\pi) + r * \ln(1 - \pi) \right] = 0$$

$$\sum_{i=1}^n \left( \frac{x_i}{\pi} - \frac{r}{1 - \pi} \right) = 0$$

$$\nabla_{\pi} L = \frac{x}{r} + 1 + \frac{a - 1}{\pi} - \frac{b - 1}{1 - \pi} = 0$$

$$\hat{\pi}_{ML} = \frac{x}{r} + 1$$

c)

$$Prior = p(\pi) = \frac{\Gamma(a + b)}{\Gamma(a)\Gamma(b)} \pi^{a-1} (1 - \pi)^{b-1}$$

$$\hat{\pi}_{MAP} = \arg \max_{\pi} \ln p(\pi | y, X) = \arg \max_{\pi} \ln \left( \frac{p(y | \pi, X) p(\pi)}{p(y | X)} \right)$$

$$\hat{\pi}_{MAP} = \arg \max_{\pi} \ln(p(y | \pi, X)) + \ln(p(\pi))$$

$$\frac{b - 1}{1 - \pi} = \frac{r(a - 1) + \pi x + \pi r}{\pi r}$$

$$r(1 - a) = \pi(x - \pi x - rb - ra + 3r - \pi r)$$

$$\hat{\pi}_{MAP} = \frac{a - 1}{a + b - 2}$$

d)

$$\prod_{i=1}^n \left[ \binom{x_i + r - 1}{x_i} \pi^{x_i} (1 - \pi)^r \right] * p(\pi)$$

It is now the beta posterior distribution

e)

\$\$

\$\$

Q2

a)

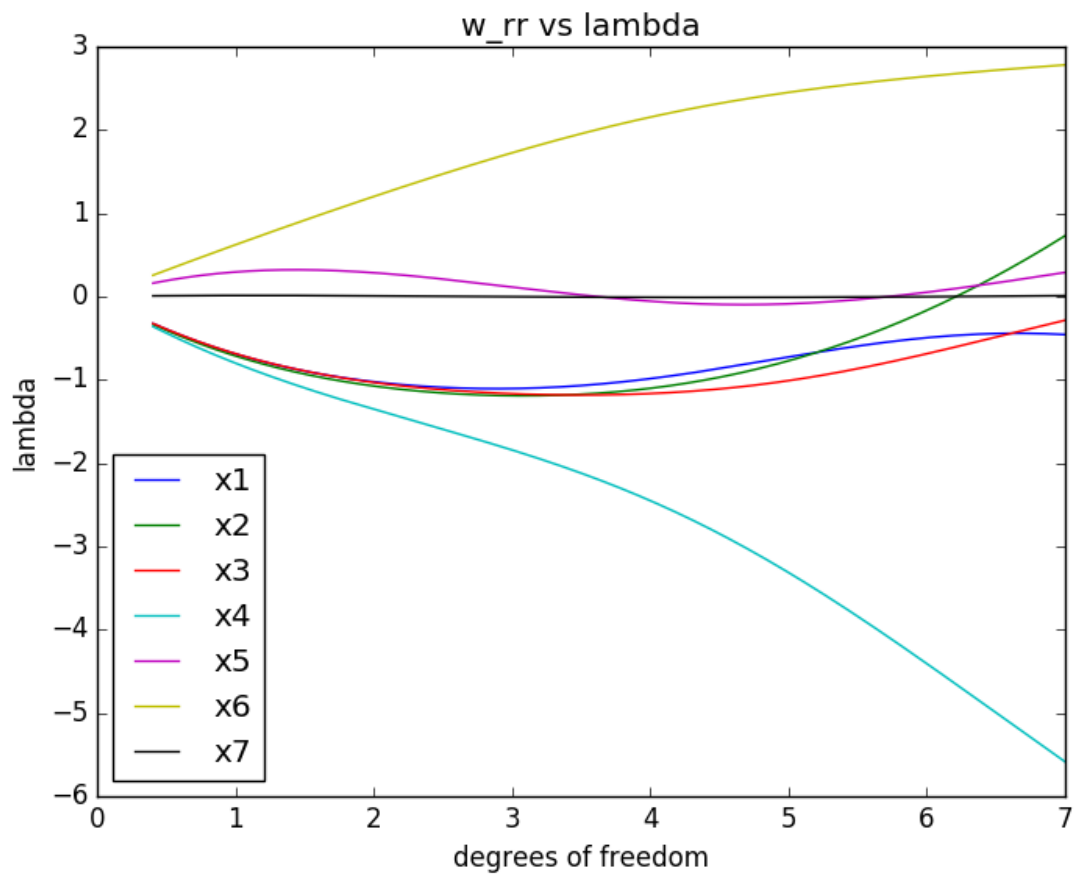


Figure 1:

b)

That the 4th and 6th dimensions are the most important factors in predicting  $y$ .

c)

Well you want to minimize RMSE, and according to my graph that happens as  $\lambda$  decreases to 0, so Ridge Regression is no better (same accuracy) than Least Squares for this.

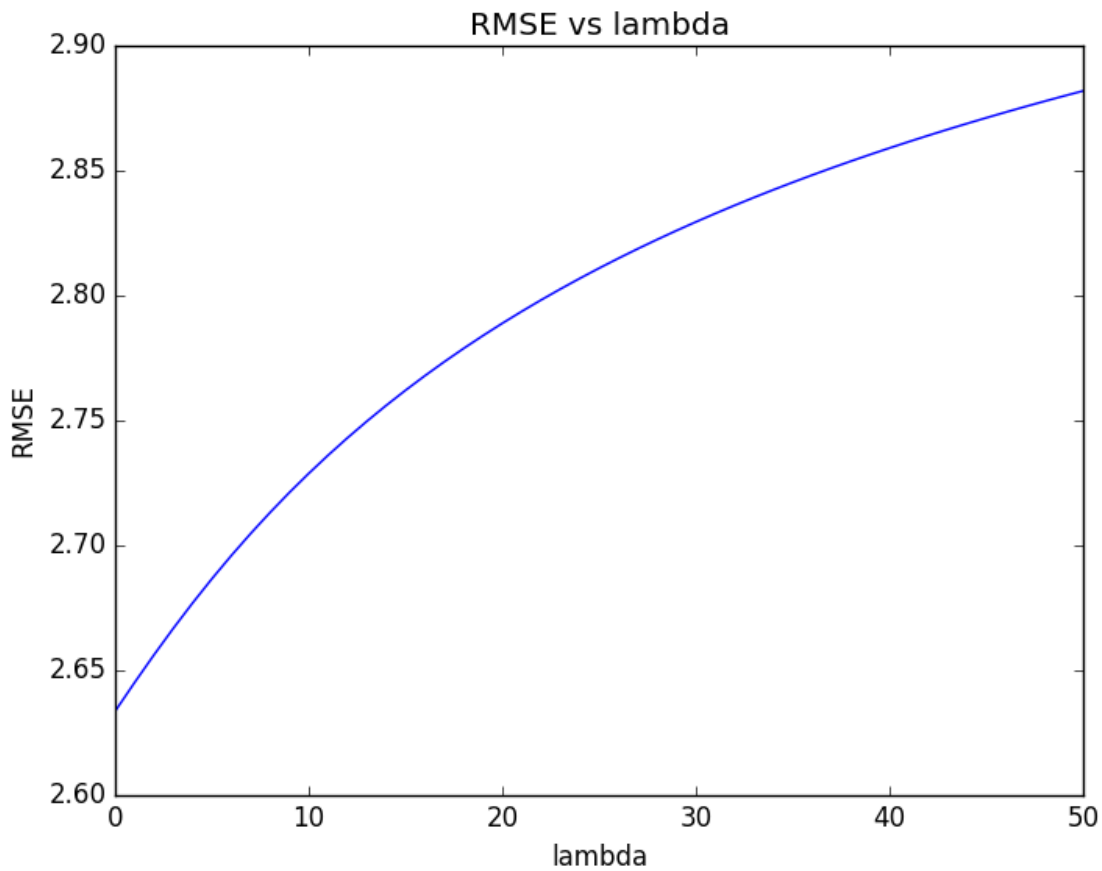


Figure 2:

d)

Again I would want to minimize the RMSE, and the graph shows me that the 2nd and 3rd order have about the same RMSE at their lowest points. The ideal  $\lambda$  changes for this as it is greater than 0 (roughly  $\sim 30$ ), so Ridge Regression is more accurate in this case.

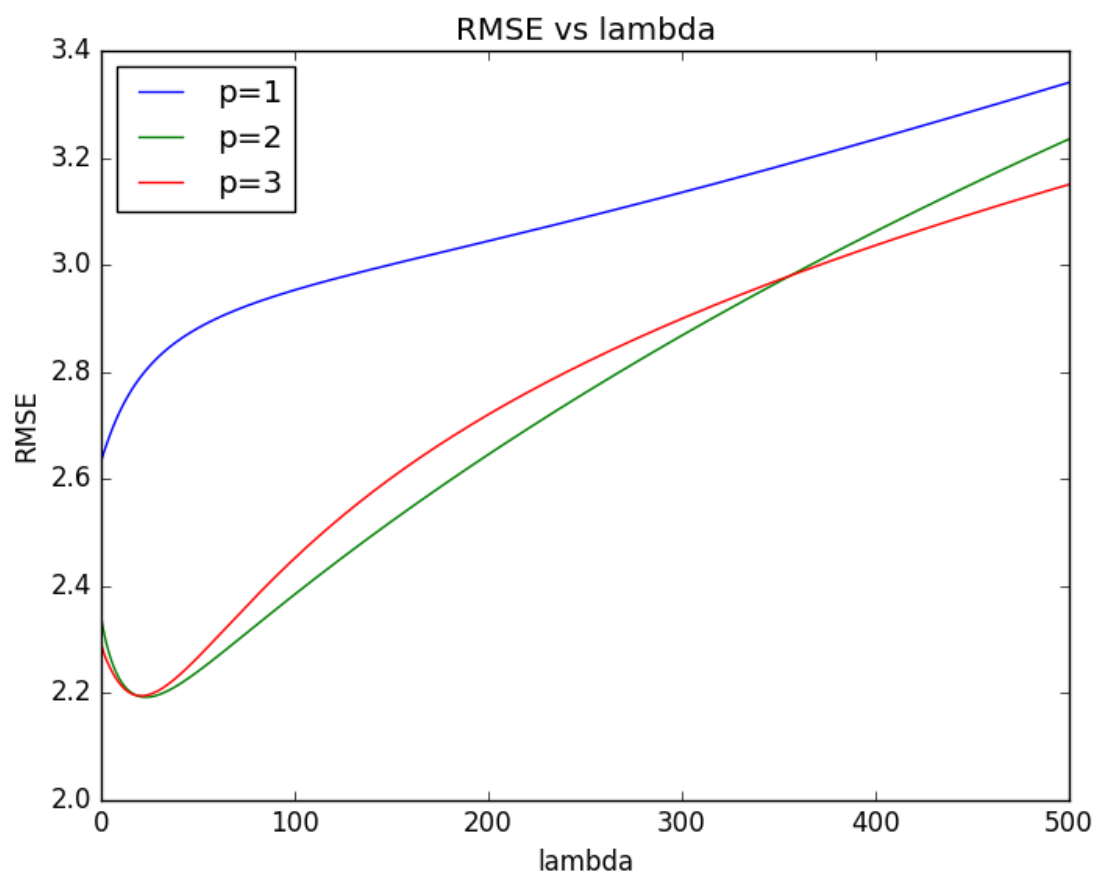


Figure 3: