

## CS 344 Problem Set 1: Asymptotics

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1. If  $f(n) = o(g(n))$  and  $g(n) = o(h(n))$ , we need to show that there exist the cost.  $C$  and  $n_0$  such that

$$a) f(n) + g(n) \leq c * g(n) \quad \forall n \geq n_0$$

$$b) f(n) + g(n) \leq c * h(n) \quad \forall n \geq n_0$$

Since  $f(n) = O(\log n)$  there exist the cost  $c_1$  and  $n_1$  such that

$$f(n) \leq c_1 * \log n$$

Similarly  $g(n) = O(h(n))$  there exist the cost  $c_2$  and  $n_2$  such that

$$g(n) \leq c_2 * h(n)$$

Now, let's choose  $n_0 \geq \max(n_1, n_2)$  and  $C = C_1 + C_2$

$$f(n) + g(n) \leq C_1 * g(n) + C_2 * g(n)$$

$$f(n) = O(g(n))$$

$$\text{and } g(n) = O(h(n))$$

$$= (C_1 + C_2) * g(n)$$

$$= C * g(n)$$

Therefore, we show that

$$f(n) + g(n) = O(g(n))$$

$$\text{Similarly } f(n) + g(n) = O(h(n))$$