Memory allocations test

April 11, 2023

1 Memory allocations test

1.1 Loading packages and functions

```
[1]: using LinearAlgebra
using OrdinaryDiffEq
using Plots
```

```
PATH_SRC="../../src_simd/"
include(string(PATH_SRC,"IRKGL_SIMD.jl"))
using .IRKGL_SIMD

PATH_SRC="../../src_seq/"
include(string(PATH_SRC,"IRKGL_SEQ.jl"))
using .IRKGL_SEQ
```

1.2 Definition of the N-body problem

In Nbody.jl below, the following functions are defined: NbodyEnergy(u,Gm), Nbody-ODE!(du,u,Gm,t), and NbodyODE1!(du,u,Gm,t), where

$$u = \begin{pmatrix} q_1 & v_1 \\ \vdots & \vdots \\ q_N & v_N \end{pmatrix} \in \mathbb{R}^{2\times 3\times N}, \quad Gm = (G\,m_1, \dots, G\,m_N) \in \mathbb{R}^N.$$

The energy, as a function of the positions $q_1,\dots,q_N\in\mathbb{R}^3$ and the velocities $v_1,\dots,v_N\in\mathbb{R}^3$ of the N bodies is:

$$\mathrm{Energy}(q_1, \dots, q_N, v_1, \dots, v_N) = \frac{1}{2} \sum_{i=1}^N m_i \, \|v_i\|^2 - G \sum_{1 < i < j < N} \frac{m_i m_j}{\|q_i - q_j\|}.$$

The ODE system of the N-body problem, as a function of the positions $q_1, \dots, q_N \in \mathbb{R}^3$ and the velocities $v_1, \dots, v_N \in \mathbb{R}^3$ of the N bodies is:

$$\begin{split} \frac{d}{dt}q_i &= v_i, \\ \frac{d}{dt}v_i &= G\sum_{j\neq i}\frac{m_j}{\|q_j - q_i\|^3}\,(q_j - q_i). \end{split}$$

This system of ODEs can be writen in compact form as

$$\frac{du}{dt} = f(t, u, Gm)$$

```
[3]: PATH_ODES="../../ODEProblems/"

include(string(PATH_ODES, "Initial5Body.jl"))
include(string(PATH_ODES, "Nbody.jl"))
```

[3]: NbodyODE! (generic function with 2 methods)

Back to the top

1.3 Initial value problem: 5-body problem (outer solar system)

We consider N=5 bodies of the outer solar system: the Sun, Jupiter, Saturn, Uranus, and Neptune. The initial values u_{00} are taken from DE430, Julian day (TDB) 2440400.5 (June 28, 1969).

```
[4]: u0, Gm, bodylist = Initial5Body(Float64)
    u0_B, Gm_B, bodylist = Initial5Body(BigFloat)
    q0=u0[:,:,1]
    v0=u0[:,:,2]
    dim=length(size(u0))

N = length(Gm)

show(bodylist)
E0=NbodyEnergy(u0,Gm)
```

["Sun" "Jupiter" "Saturn" "Uranus" "Neptune"]

[4]: -9.522696242724855e-12

Back to the top

1.4 Memory allocations

```
[5]: t0 = 0.
    dt = 500. # 500.

tF = 100*dt
    tF2 = 2*tF
    tF4 = 4*tF

prob = ODEProblem(NbodyODE!, u0, (t0,tF), Gm)
    prob2 = ODEProblem(NbodyODE!, u0, (t0,tF2), Gm)
```

```
prob4 = ODEProblem(NbodyODE!, u0, (t0,tF4), Gm);
```

1.4.1 Sequential version

```
[6]: alg_seq=IRKGL_Seq(s=8)
     solx=solve(prob,alg_seq,dt=dt, save_everystep=false);
     solx2=solve(prob2,alg_seq,dt=dt, save_everystep=false)
     solx4=solve(prob4,alg seq,dt=dt, save everystep=false);
[7]: println(solx.retcode,",tspan=",prob.tspan,",steps=",prob.tspan[2]/

¬dt,",length(solx.t)=",length(solx.t))
     @time solve(prob,alg seq,dt=dt, save everystep=false);
    Success, tspan=(0.0, 50000.0), steps=100.0, length(solx.t)=2
      0.004448 seconds (855 allocations: 57.227 KiB)
[8]: println(solx2.retcode,",tspan=",prob2.tspan,",steps=",prob2.tspan[2]/

dt,",length(solx2.t)=",length(solx2.t))

     @time solve(prob2,alg_seq,dt=dt, save_everystep=false);
    Success, tspan=(0.0, 100000.0), steps=200.0, length(solx2.t)=2
      0.008994 seconds (1.16 k allocations: 69.727 KiB)
[9]: println(solx4.retcode,",tspan=",prob4.tspan,",steps=",prob4.tspan[2]/

dt,",length(solx4.t)=",length(solx4.t))
     @time solve(prob4,alg_seq,dt=dt, save_everystep=false);
```

Success,tspan=(0.0, 200000.0),steps=400.0,length(solx4.t)=2 0.017920 seconds (1.75 k allocations: 94.727 KiB)

1.4.2 Simd version

Success,tspan=(0.0, 50000.0),steps=100.0,length(solx.t)=2 0.001002 seconds (827 allocations: 55.117 KiB)

```
[12]: println(solx2.retcode,",tspan=",prob2.tspan,",steps=",prob2.tspan[2]/

dt,",length(solx2.t)=",length(solx2.t))
      @time solve(prob2,alg_simd,dt=dt, save_everystep=false);
     Success, tspan=(0.0, 100000.0), steps=200.0, length(solx2.t)=2
       0.001967 seconds (1.13 k allocations: 67.617 KiB)
[13]: println(solx4.retcode,",tspan=",prob4.tspan,",steps=",prob4.tspan[2]/

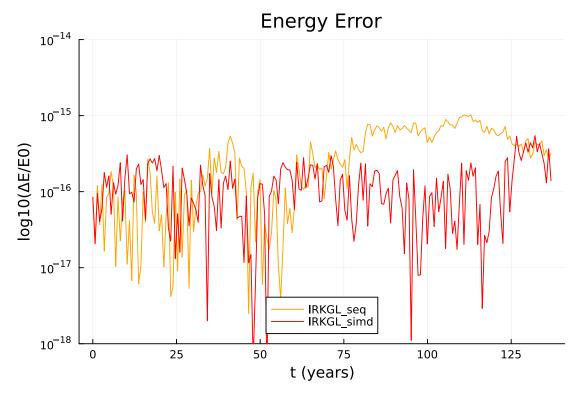
dt,",length(solx4.t)=",length(solx4.t))
      @time solve(prob4,alg_simd,dt=dt, save_everystep=false);
     Success,tspan=(0.0, 200000.0),steps=400.0,length(solx4.t)=2
       0.003403 seconds (1.73 k allocations: 92.617 KiB)
     1.4.3 Vern9
[14]: sol_Vern =solve(prob, Vern9(), dt=dt, save_everystep=false)
      sol_Vern2 =solve(prob2, Vern9(), dt=dt, save_everystep=false)
      sol_Vern4 =solve(prob4, Vern9(), dt=dt, save_everystep=false);
[15]: println(sol_Vern.retcode,",tspan=",prob.tspan,",steps=",prob.tspan[2]/

dt,",length(sol_Vern.t)=",length(sol_Vern.t))
      @time solve(prob, Vern9(), dt=dt, save_everystep=false);
     Success, tspan=(0.0, 50000.0), steps=100.0, length(sol Vern.t)=2
       0.000129 seconds (52 allocations: 8.781 KiB)
[16]: println(sol_Vern2.retcode,",tspan=",prob2.tspan,",steps=",prob2.tspan[2]/
       dt,",length(sol_Vern2.t)=",length(sol_Vern2.t))
      @time solve(prob2, Vern9(), dt=dt, save everystep=false);
     Success, tspan=(0.0, 100000.0), steps=200.0, length(sol_Vern2.t)=2
       0.000229 seconds (52 allocations: 8.781 KiB)
[17]: println(sol_Vern4.retcode,",tspan=",prob4.tspan,",steps=",prob4.tspan[2]/

dt,",length(sol_Vern4.t)=",length(sol_Vern4.t))
      @time solve(prob4, Vern9(), dt=dt, save_everystep=false);
     Success, tspan=(0.0, 200000.0), steps=400.0, length(sol_Vern4.t)=2
       0.000440 seconds (52 allocations: 8.781 KiB)
     1.4.4 Errors in Energy
[18]: sol1=solve(prob,alg_seq,dt=dt/2, adaptive=false)
      println(sol1.retcode,",length(sol1.t)=",length(sol1.t))
      sol2=solve(prob,alg_simd,dt=dt/2, adaptive=false)
      println(sol2.retcode,",length(sol2.t)=",length(sol2.t))
```

```
Success,length(sol1.t)=201
Success,length(sol2.t)=201
```

[19]:



[]: