

2. Unlike Expectimax, Minimax 'can take a risk' and end up in a state with a higher utility as opponents are random. [1 point]

False, based on the nature of expectimax and minimax search algorithms.

3. The importance of an accurate evaluation function increases by increasing the depth. [1 point]

False, because we have more uncertainty further up in the tree; therefore, it is more important to have an accurate evaluation function higher up in the tree.

4. Identify the appropriate type of search for the problems listed below: [3 points]

CPU job scheduling -> goal itself is important

Graph coloring problem -> goal itself is important

Finding the shortest route from city A to city B -> path to goal itself is important

Chess game -> path to goal itself is important (This will be graded manually as the autograder response is incorrect.)

5. Specify two problems with the Hill-climbing algorithm and explain two different methods (one for each problem) that alleviate these problems.

[6 points - 3 points for two problems and 3 points for two reasonable solutions]

1. Problem 1

- a. We get stuck in a local optimum and not the global optimum.
- b. Solution: We can implement hill-climbing with random restarts, pick the best solution, or use the simulated annealing approach.

2. Problem 2

- a. Plateau points, a flat portion of the state-space landscape hill-climbing tries to find uphill parts, and if there are none, we are stuck.
- b. Solution: Implement a limited number of side-way movements in an attempt to leave the plateau.

6. How is local beam search equivalent to AND different from multiple parallel runs of hill-climbing algorithms? Explain these shared and dissimilar characteristics.

[4 points - 2 points for shared characteristics, 2 points for dissimilarities]

Similarities: If $k=1$, then the beam search is just a single thread of climbing a hill without keeping track of other good choices. They both consider k nodes at any given time.

Dissimilarities: Local beam search is not equivalent to parallel runs of several hill-climbing because, in the parallel runs, there is no sense of memory of the best states. Local beam

search is like k parallel runs, but the information is shared, and successors are chosen by considering all neighbors.

7. Simulated annealing is more likely to accept a bad move late in the search than earlier. [1 point]

False, based on the definition of the temperature schedule in the simulated annealing algorithm.

8. Consider the general less-than chain CSP below. Each of the N variables X_i has the domain $\{1, 2, \dots, M\}$. The constraints between adjacent variables X_i and X_{i+1} require that $X_i < X_{i+1}$. [10 points]



For now, assume $N = M$.

a. How many solutions does the CSP have? [2 points]

One solution: $1 < 2 < 3 < \dots < N$

b. What will be the domain of X_1 after enforcing the consistency of only arc $X_1 \rightarrow X_2$? [3 points]

X_1 domain = $\{1, 2, 3, \dots, N-1\}$

c. What will be the domain of X_1 after enforcing the consistency of only arc $X_2 \rightarrow X_3$ and then $X_1 \rightarrow X_2$? [3 points]

X_1 domain = $\{1, 2, 3, \dots, N-2\}$

d. What will be the domain of X_1 after fully enforcing arc consistency in the entire problem? [2 points]

X_1 domain = $\{1\}$

9. a. Why do we prefer to change nearly tree-structured CSPs to tree-structured CSPs? How would this conversion happen? [3 points]

We prefer tree-structured CSPs because this reduces the time complexity since the arc-consistency algorithm will not backtrack and consistency of arcs will be maintained as variables are assigned. $O(nd^2)$ vs. $O(d^n)$.

We can do this conversion by:

Identify the minimum number of nodes, that if removed, we are left with a tree (cut-set). Then we do cut-set conditioning (pick one of those nodes call it C and assign a value to them (conditioning), then remove conflicting values from the domain of the neighbors), and run the tree-structured algorithm on each instantiated problem.

b. Describe the algorithm for solving a tree-structured CSP and discuss its runtime.

[3 points]

Given a tree-structured CSP, we apply topological ordering (ordering nodes, from 1 to n, so that all parents come before their children in the sequence). Then:

i) Do a backward pass, from node n-1 down to 1, enforce arc consistency between the parent of node and the node itself ($\text{Parent}(X_i) \rightarrow X_i$ arc consistency)

ii) Do a forward pass selecting a value from the domain of each variable that is not conflicting with the values assigned previously.

Solving a tree-structured CSP gives us a quadratic runtime versus an exponential run time because now we have to check each node in the tree and at each node ($O(n)$), we perform arc consistency in $O(d^2)$.

Runtime: $O(nd^2)$

10. If A and B are two events such that $P(A) = 0.2$, $P(B) = 0.6$ and $P(A|B) = 0.2$ then what is the value of $P(\sim A | \sim B)$? Show your work.

[3 points]

$P(A|B) = 0.2$ and $P(B) = 0.6$ so $P(A, B) = 0.12$ and therefore:

$P(A, \sim B) = P(A) - P(A, B) = 0.2 - 0.12 = 0.08$

$P(\sim A | \sim B) = 1 - P(A | \sim B)$

$P(A | \sim B) = P(A, \sim B) / P(\sim B) = 0.08 / 0.4 = 0.2 \rightarrow P(\sim A | \sim B) = 1 - 0.2 = 0.8$