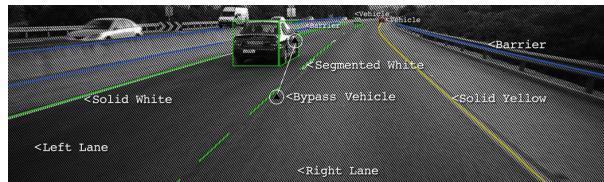




Tutorial 04 - Edge and Line Detection



- [Image source \(<https://towardsdatascience.com/tutorial-build-a-lane-detector-679fd8953132>\).](https://towardsdatascience.com/tutorial-build-a-lane-detector-679fd8953132)



Agenda

- [Why Do We Need Edge Detection?](#)
- [Edge Detection](#)
 - [Canny Edge Detection](#)
 - [Non-Maximum Suppression \(NMS\)](#)
- [Line Fitting](#)
 - [Hough Transform](#)
 - [RANSAC](#)
 - [SCNN](#)
- [Recommended Videos](#)
- [Credits](#)

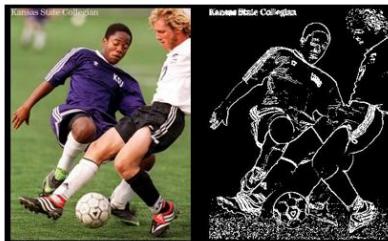
```
In [2]: # imports for the tutorial
import numpy as np
import matplotlib.pyplot as plt
from PIL import Image
import cv2
from scipy import signal
%matplotlib inline
```

```
In [3]: # plot images function
def plot_images(image_list, title_list, subplot_shape=(1,1), axis='off', fontsize=30, figsize=(4,4), cmap=['gray']):
    plt.figure(figsize=figsize)
    for ii, im in enumerate(image_list):
        c_title = title_list[ii]
        if len(cmap) > 1:
            c_cmap = cmap[ii]
        else:
            c_cmap = cmap[0]
        plt.subplot(subplot_shape[0], subplot_shape[1], ii+1)
        plt.imshow(im, cmap=c_cmap)
        plt.title(c_title, fontsize=fontsize)
        plt.axis(axis)
```



Corners For Features, Edges For What?

- We know edges are special
- Human visual system is based on edges
- Given an image that contains only edges we can identify objects without any additional information



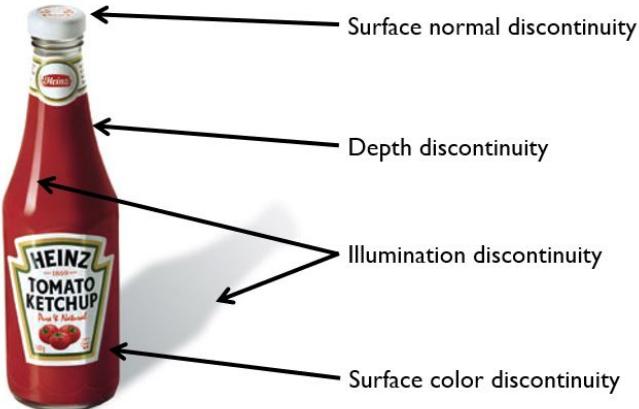
Edge Detection Goal

- **Goal:** Map image from 2d array of pixels to a set of curves, line segments, or contours.
 - Most semantic and shape information from the image can be encoded in the edges
 - A more compact representation than a complete image
- **Ideal:** Artist's Line drawing (but artists use prior knowledge)



What can cause an edge?





Derivatives and Edges

- An edge is a place of rapid change in the image intensity function.

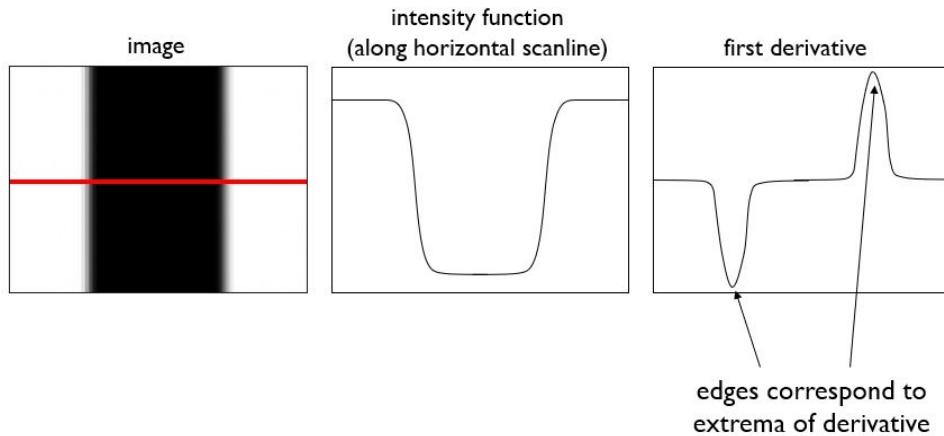


Image Gradient

- The gradient of an image: $\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$
- The gradient points in the direction of most rapid change in intensity

$$\nabla f = \left[\frac{\partial f}{\partial x}, 0 \right]$$

$$\nabla f = \left[0, \frac{\partial f}{\partial y} \right]$$

$$\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$$

- The gradient direction (orientation of edge normal) is given by: $\theta = \tan^{-1} \left(\frac{\frac{\partial f}{\partial y}}{\frac{\partial f}{\partial x}} \right)$
- The edge strength is given by the gradient magnitude $||\nabla f|| = \sqrt{\left(\frac{\partial f}{\partial y}\right)^2 + \left(\frac{\partial f}{\partial x}\right)^2}$



Differentiation and Convolution

- For 2D function, $f(x,y)$, the partial derivative is:

$$\frac{\partial f(x, y)}{\partial x} = \lim_{\epsilon \rightarrow 0} \frac{f(x + \epsilon, y) - f(x, y)}{\epsilon}$$

- For discrete data, we can approximate using finite differences:

$$\frac{\partial f(x, y)}{\partial x} = \frac{f(x + 1, y) - f(x, y)}{\Delta x}$$

- To implement above as convolution, what would be the associated filter?

-1	1
----	---



Assorted Finite Difference Filters

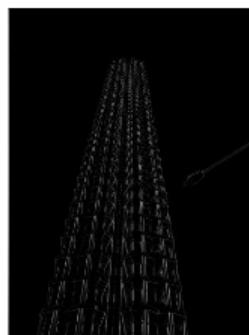
Prewitt: $M_x = \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix}$; $M_y = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix}$

Sobel: $M_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$; $M_y = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$

Roberts: $M_x = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$; $M_y = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$

```
In [4]: im = cv2.imread('assets/sobel_bulding.jpg')
im = cv2.cvtColor(im, cv2.COLOR_BGR2GRAY)
ksize = 3
im_x = np.abs(cv2.Sobel(im, cv2.CV_64F, 1, 0, ksize=ksize))
im_y = np.abs(cv2.Sobel(im, cv2.CV_64F, 0, 1, ksize=ksize))

plot_images([im, im_x, im_y], ['x', 'y', 'x+y'], subplot_shape=(1,3), figsize=(12,4))
```

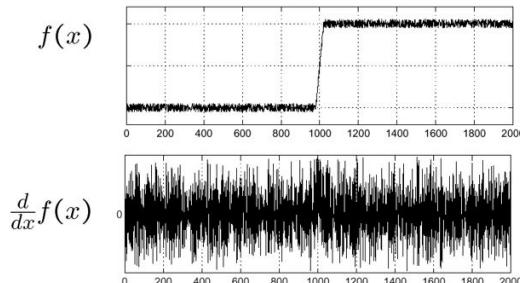


- Which show changes with respect to x ? y ?



Effects of Noise

- Consider a single row or column of the image
- Plotting intensity as a function of position gives a signal:



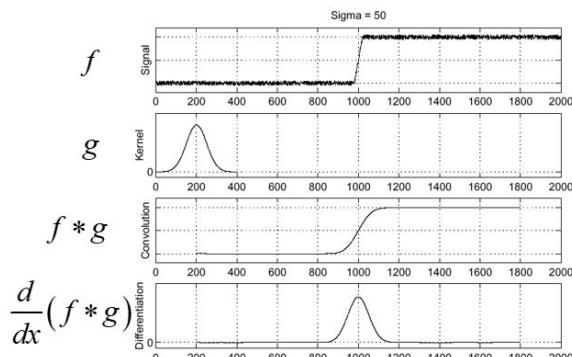
- Where is the edge?

- Finite difference filters respond strongly to noise
 - Image noise results in pixels that look very different from their neighbors
 - Generally, the larger the noise the stronger the response
- What can be done?

• Smoothing the image should help! – it forces pixels to look more like their neighbors



Solution: Smooth First

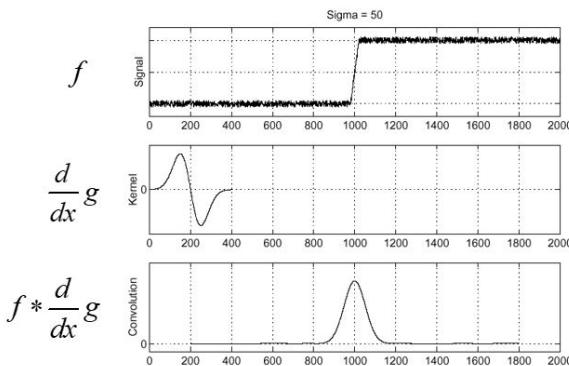


- Where is the edge?
 - Look for peaks in $\frac{d}{dx}(f * g)$



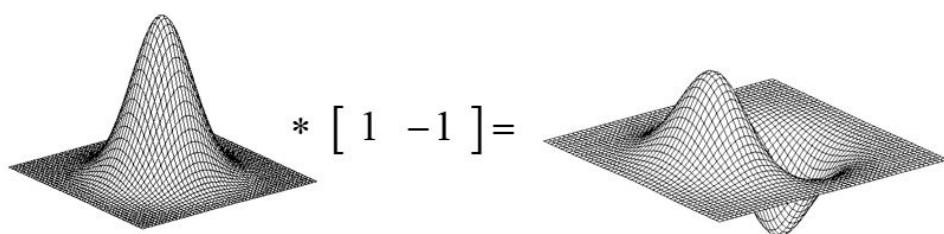
Derivative Theorem of Convolution

Differentiation property of convolution: $\frac{\partial}{\partial x}(f * g) = f * \frac{\partial}{\partial x}g$



Derivative of Gaussian Filter

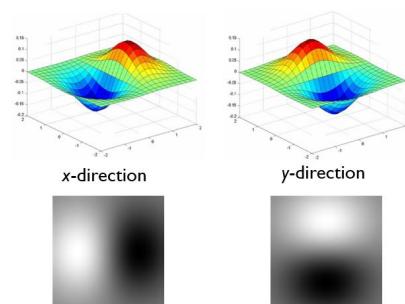
- Is this a separable filter?



- Yes, we can split it into two filters in which their order does not matter
- Median is a non-separable filter



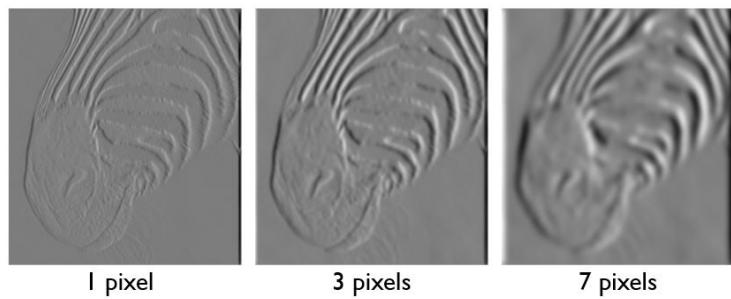
Derivative of Gaussian Filter



- Which one finds horizontal/vertical edges?



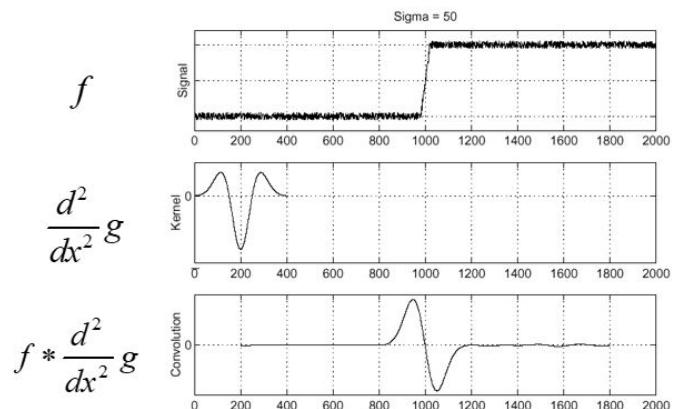
Smoothing Tradeoffs



- Smoothed derivative removes noise, but blurs edge.
 - Also finds edges at different “scales”.



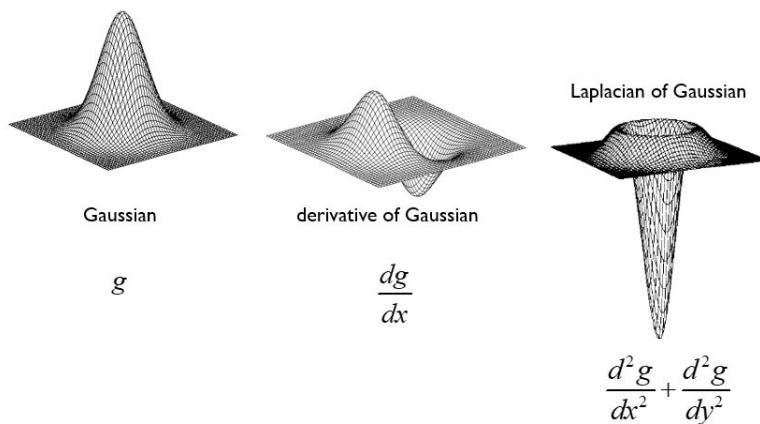
Laplacian of Gaussian (LoG)



- Where is the edge?
 - Zero-crossings of bottom graph



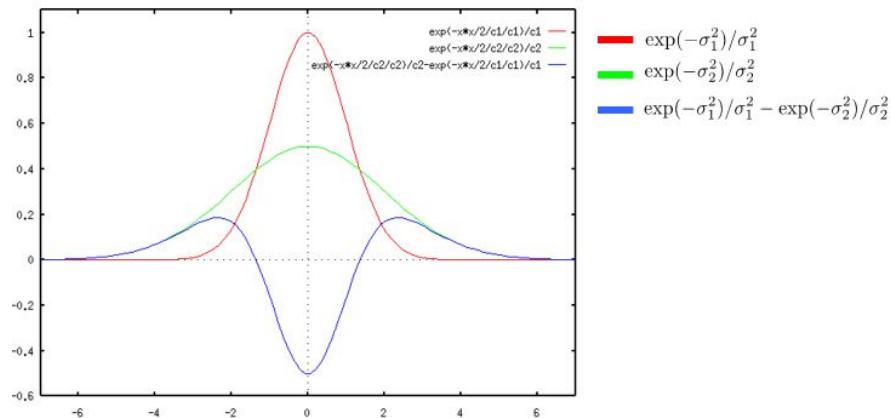
2D Edge Detection Filters





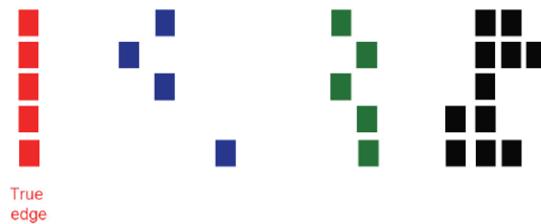
DoG: Difference of Gaussians

- Can approximate Laplacian filter



What is a Good Edge Detector?

- Good detection:
 - Minimize false positives (wrong detections)
 - Minimize false negatives (missing real edges)
 - Maximize true detections
- Good localization:
 - Detected edges should be as close as possible to the true edges
- Single response:
 - Return a single detection for each true edge point
- Connect detections to lines



- Which of these detections is the best?

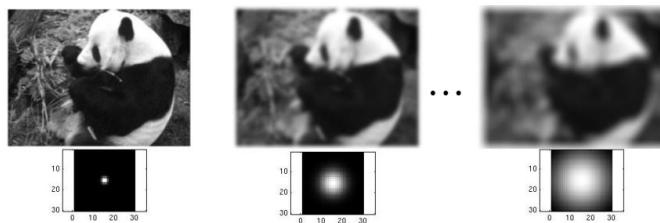


What Are the Parameters?

- Scale
- Threshold

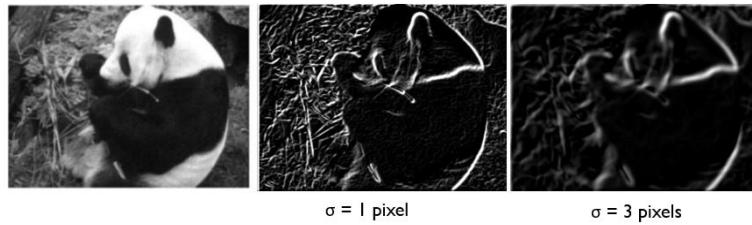
Scale Selection

- Recall: We first smooth the image with a Gaussian kernel to reduce noise.
- The scale of the Gaussian determines how much smoothing we apply



Effect of σ On Derivatives

- The apparent structures differ depending on Gaussian's scale parameter.
- Large scale: larger scale edges detected
- Small scale: finer features detected



How Do We Choose the Scale?

- It depends what we're looking for:



- Too fine of a scale...
 - Can't see the forest for the trees.
- Too coarse of a scale...
 - Can't tell the maple grain from the cherry.



What Are the Parameters?

- Scale
- Threshold

Thresholding

- Choose a threshold value
- Set any pixels less than thresh to zero (off)
- Set any pixels greater than or equal to thresh to one (on)

```
In [5]: im_o = cv2.imread('./assets/butterfly.png')
im = cv2.cvtColor(im_o, cv2.COLOR_BGR2GRAY)
ksize = 5

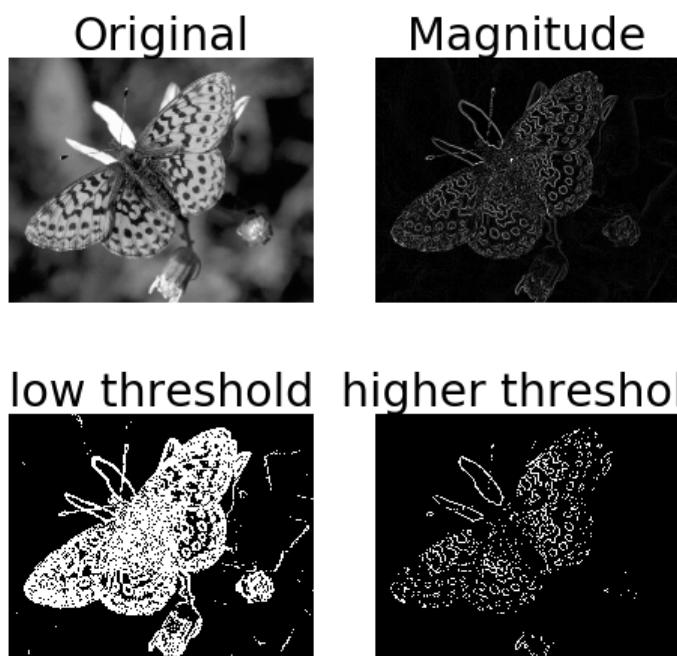
# blur image
im = cv2.GaussianBlur(im, (ksize, ksize), 0)

# edge extraction:
k_x = np.array([[0, 1, 0], [0, 0, 0], [0, -1, 0]])
k_y = np.array([[0, 0, 0], [-1, 0, 1], [0, 0, 0]])
im_x = cv2.filter2D(im, cv2.CV_64F, k_x)
im_y = cv2.filter2D(im, cv2.CV_64F, k_y)

# gradient magnitude:
im_grad_mag = np.sqrt(np.square(im_x) + np.square(im_y))

low_thresh = im_grad_mag > 7 # Low threshold
high_thresh = im_grad_mag > 30 # High threshold
```

```
In [6]: # figures:
plot_images([im, im_grad_mag, low_thresh, high_thresh], ['Original', 'Magnitude', 'low threshold', 'higher threshold'],
            subplot_shape=(2,2), figsize=(8,8))
```



The Canny Edge Detector

- Probably the most widely used edge detector in Computer Vision
- Key idea: Detect step-edges that are corrupted by additive Gaussian noise
- Theorem: Canny has shown that the first derivative of the Gaussian closely approximates the operator that optimizes the product of signal-to-noise ratio and localization
- [J. Canny, A Computational Approach To Edge Detection, IEEE Trans. Pattern Analysis and Machine Intelligence, 8:679--714, 1986. \(https://scholar.google.com/scholar?cluster=6445737130860653197&hl=en&as_sdt=0,5&sciodt=0,5\)](https://scholar.google.com/scholar?cluster=6445737130860653197&hl=en&as_sdt=0,5&sciodt=0,5)
 - 34189 citations until today!



The Canny Edge Detector - Building Blocks

- Filter image with derivative of Gaussian
- Find magnitude and orientation of gradient
- Non-maximum suppression: **(Localization)**
 - Thin multi-pixel wide “ridges” down to single pixel width
- Linking and thresholding (hysteresis): **(Linking)**
 - Define two thresholds: low and high
 - Use the high threshold to start edge curves and the low threshold to continue them
- In OpenCV: cv2.Canny()



Canny Example - Input

```
In [7]: # Load Image
img = cv2.imread('./assets/tut_panda.jpg')
img_rgb = cv2.cvtColor(img, cv2.COLOR_BGR2RGB)
gray = cv2.cvtColor(img, cv2.COLOR_BGR2GRAY)
in_x_min = 100
in_x_max = 400
in_y_min = 300
in_y_max = 700
gray_cut = gray[in_y_min:in_y_max, in_x_min:in_x_max]
```

```
In [8]: plot_images([img_rgb, gray, gray_cut], ['Original', 'Gray', 'Gray Cut'], cmap=[None, 'gray', 'gray'],
                 subplot_shape=(1, 3), figsize=(12, 4))
```

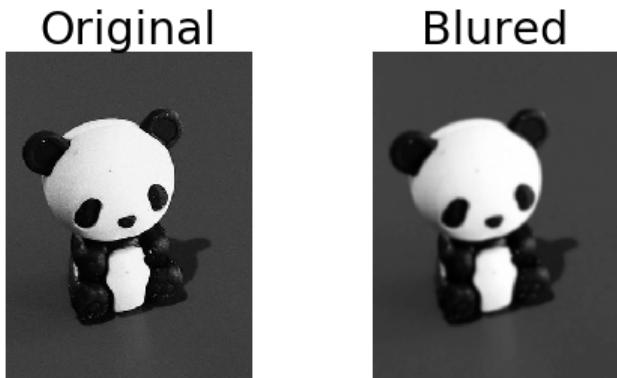


- Photo by [Pedro Gonzalez](https://unsplash.com/@pgonzalez_95?utm_medium=referral&utm_campaign=photographer-credit&utm_content=creditBadge) (https://unsplash.com/@pgonzalez_95?utm_medium=referral&utm_campaign=photographer-credit&utm_content=creditBadge), from [Unsplash](https://unsplash.com/) (<https://unsplash.com/>).



Canny Example - Step 1 - Blur

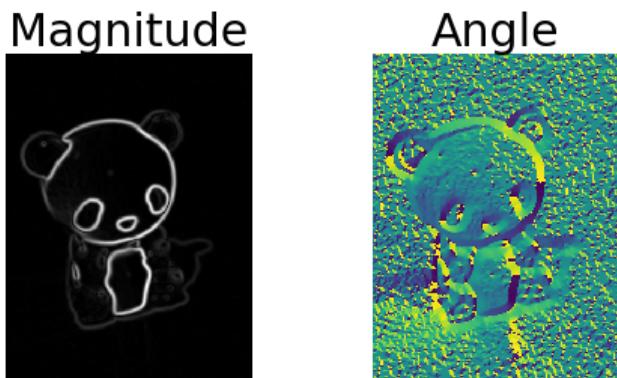
```
In [9]: # Gaussian Blurring  
blur = cv2.GaussianBlur(gray_cut, (9,9), 0)  
plot_images([gray_cut, blur], ['Original', 'Blurred'], cmap=['gray', 'gray'], subplot_shape=(1,2), figsize=(8,4))
```



Canny Example - Step 2 - Find Magnitude and Orientation of Gradient

```
In [10]: # Apply Sobel:  
sobelx_64 = cv2.Sobel(blur, cv2.CV_64F, 1, 0, ksize=3)  
sobely_64 = cv2.Sobel(blur, cv2.CV_64F, 0, 1, ksize=3)  
  
# From gradients calculate the magnitude and changing  
mag = np.hypot(sobelx_64, sobely_64)  
mag = mag / mag.max()  
  
# Find the direction and change it to degree  
theta = np.arctan2(sobely_64, sobelx_64)  
angle = np.rad2deg(theta)
```

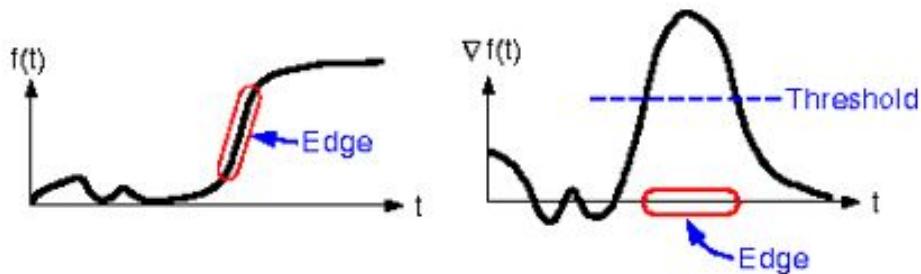
```
In [11]: plot_images([mag, angle], ['Magnitude', 'Angle'], subplot_shape=(1,2), figsize=(8,4), cmap=['gray', None])
```





Canny Example - Step 3 - Localization

- How to turn these thick regions of the gradient into curves?

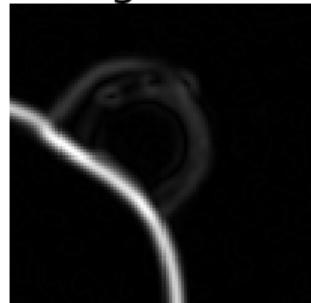


```
In [12]: in_x_min, in_x_max, in_y_min, in_y_max = (150, 250, 50, 150)
mag_cut = mag[in_y_min:in_y_max, in_x_min:in_x_max]
plot_images([mag, mag_cut], ['Magnitude', 'Magnitude'], subplot_shape=(1,2), figsize=(8,4))
```

Magnitude

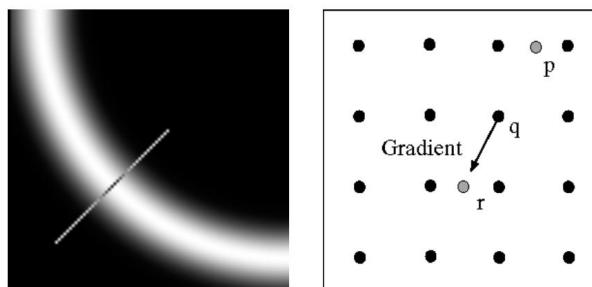


Magnitude



Non-Maximum Suppression (NMS)

- Check if pixel is local maximum along gradient direction, select single max across width of the edge
- Requires checking interpolated pixels p and r

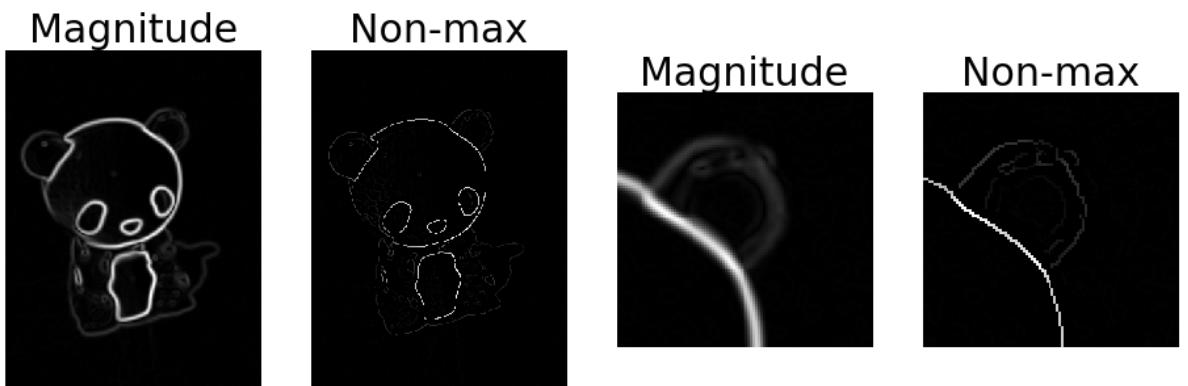


```
In [13]: # Find the neighbouring pixels (b,c) in the rounded gradient direction
# and then apply non-max suppression
M, N = mag.shape
Non_max = np.zeros((M,N), dtype= np.float64)

for i in range(1,M-1):
    for j in range(1,N-1):
        # Horizontal 0
        if (0 <= angle[i,j] < 22.5) or (157.5 <= angle[i,j] <= 180) or (-22.5 <= angle[i,j] < 0)\ 
        or (-180 <= angle[i,j] < -157.5):
            b = mag[i, j+1]
            c = mag[i, j-1]
        # Diagonal 45
        elif (22.5 <= angle[i,j] < 67.5) or (-157.5 <= angle[i,j] < -112.5):
            b = mag[i+1, j+1]
            c = mag[i-1, j-1]
        # Vertical 90
        elif (67.5 <= angle[i,j] < 112.5) or (-112.5 <= angle[i,j] < -67.5):
            b = mag[i+1, j]
            c = mag[i-1, j]
        # Diagonal 135
        elif (112.5 <= angle[i,j] < 157.5) or (-67.5 <= angle[i,j] < -22.5):
            b = mag[i+1, j-1]
            c = mag[i-1, j+1]

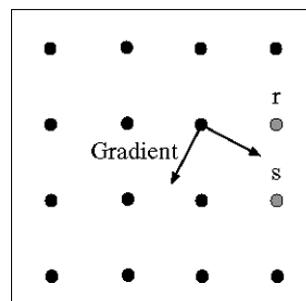
        # Non-max Suppression
        if (mag[i,j] >= b) and (mag[i,j] >= c):
            Non_max[i,j] = mag[i,j]
        else:
            Non_max[i,j] = 0
```

```
In [14]: mag_cut = mag[in_y_min:in_y_max, in_x_min:in_x_max]
Non_max_cut = Non_max[in_y_min:in_y_max, in_x_min:in_x_max]
plot_images([mag, Non_max, mag_cut, Non_max_cut], ['Magnitude', 'Non-max', 'Magnitude', 'Non-max'],
           subplot_shape=(1,4), figsize=(16,8))
```



Canny Example - Step 4 - Edge Linking

- Assume the marked point is an edge point.
- Then we construct the tangent to the edge curve (which is normal to the gradient at that point) and use this to predict the next points (here either r or s).





Hysteresis Thresholding

- Check that maximum value of gradient value is sufficiently large
 - Drop-outs? Use hysteresis
 - Use a high threshold to start edge curves and a low threshold to continue them.



```
In [15]: # Hysteresis - step 1 - two thresholds
# Set high and Low threshold
highThreshold = 40 / 255
lowThreshold = 10 / 255

M, N = Non_max.shape
out = np.zeros((M,N), dtype= np.float64)

# If edge intensity is greater than 'High' it is a sure-edge
# below 'Low' threshold, it is a sure non-edge
strong_i, strong_j = np.where(Non_max >= highThreshold)
zeros_i, zeros_j = np.where(Non_max < lowThreshold)

# weak edges
weak_i, weak_j = np.where((Non_max <= highThreshold) & (Non_max >= lowThreshold))

# Set same intensity value for all edge pixels
out[strong_i, strong_j] = 255
out=zeros_i, zeros_j ] = 0
out[weak_i, weak_j] = 75
```

```
In [16]: plot_images([out, out[in_y_min:in_y_max, in_x_min:in_x_max]], ['Two thresholds', ''],
                 subplot_shape=(1,2), figsize=(8,4))
```

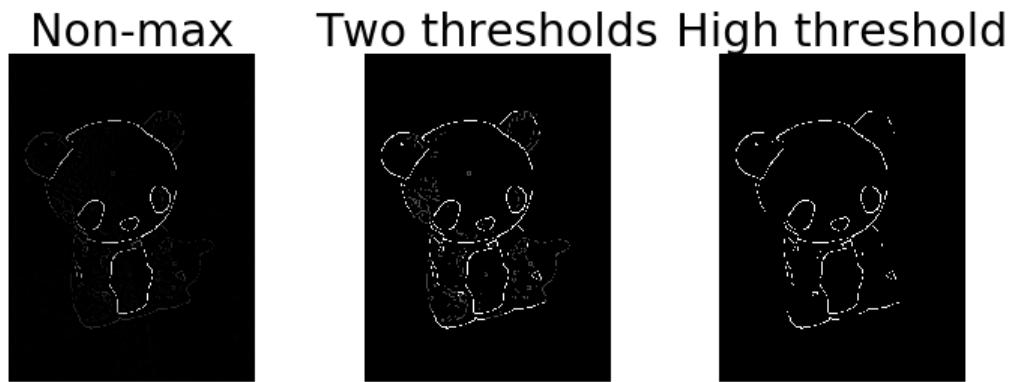
Two thresholds



Linking edges

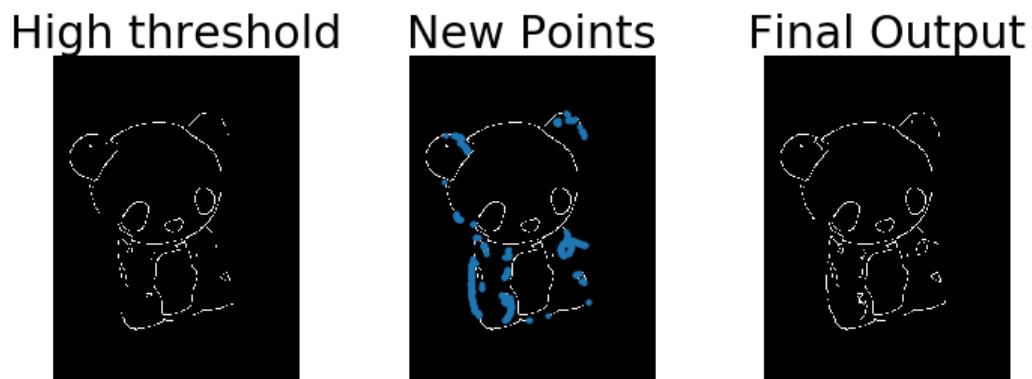
```
In [17]: # Hysteresis - step 2
out1 = np.copy(out)
new_points = []
M, N = out1.shape
for i in range(1, M-1):
    for j in range(1, N-1):
        if (out1[i,j] == 75):
            # 8 nieghbors search:
            if 255 in [out1[i+1, j-1], out1[i+1, j], out1[i+1, j+1], out1[i, j-1], out1[i, j+1],
                       out1[i-1, j-1], out1[i-1, j], out1[i-1, j+1]]:
                out1[i, j] = 255
                new_points.append(np.array([i,j]))
            else:
                out1[i, j] = 0
new_points = np.stack(new_points,-1)
```

```
In [29]: # Hysteresis output
plot_images([Non_max, out, out > 75], ['Non-max', 'Two thresholds', 'High threshold'], subplot_shape=(1,3), figsize=(12,4))
```



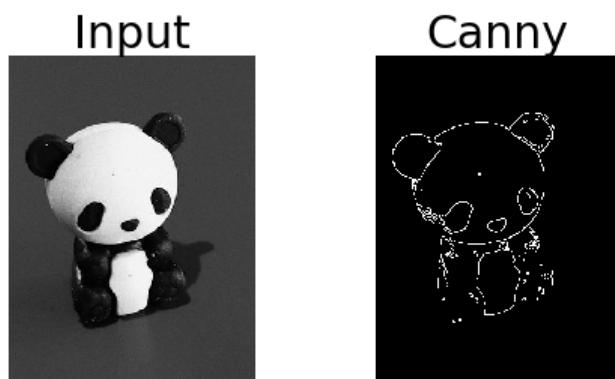
```
In [20]: plt.figure(figsize=(12,4))
plt.subplot(1,3,1)
plt.imshow(out > 75,cmap='gray')
plt.title('High threshold',fontsize=30)
plt.axis('off')
plt.subplot(1,3,2)
plt.imshow(out1,cmap='gray')
plt.title('New Points',fontsize=30)
plt.plot(new_points[1],new_points[0],'.')
plt.axis('off')
plt.subplot(1,3,3)
plt.imshow(out1,cmap='gray')
plt.title('Final Output',fontsize=30)
plt.axis('off')
```

Out[20]: (-0.5, 299.5, 399.5, -0.5)



Canny in one line (OpenCV)

```
In [27]: # Canny
im_canny = cv2.Canny(gray_cut, 50, 260)
plot_images([gray_cut, im_canny], ['Input', 'Canny'], subplot_shape=(1,2), figsize=(8,4))
```



Line Fitting

-
- Hough Transform
 - RANSAC
 - SCNN

Fitting a Parametric Model to Data

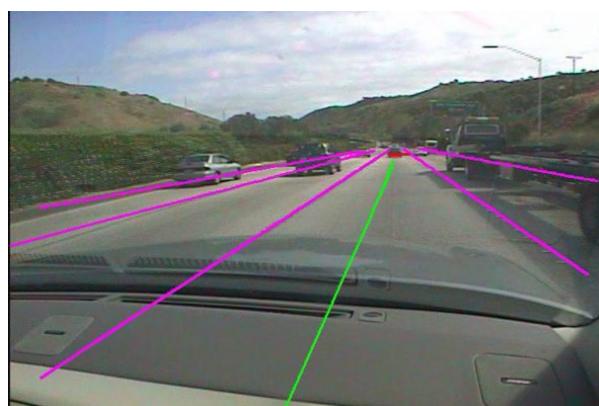
-
- Design questions:
 - What is a good model to represent our data?
 - Do we plan to fit multiple instances?
 - Challenges:
 - Which features belong to the model? To which instance?
 - How many instances are there?
 - Computational complexity (typically we cannot examine all possible models).

Line Fitting Applications

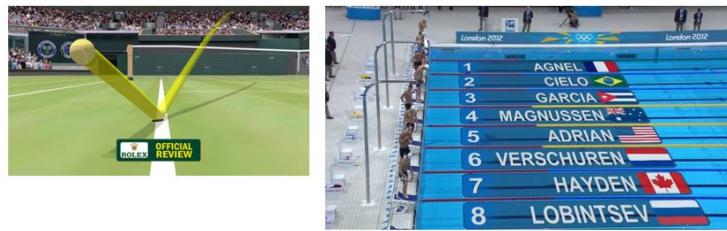
-
- Detection of power lines in helicopter navigation systems



- Image credit: Horev et al. SIAM'15
- Lane detection from car cameras in crash preventing systems



- Sports

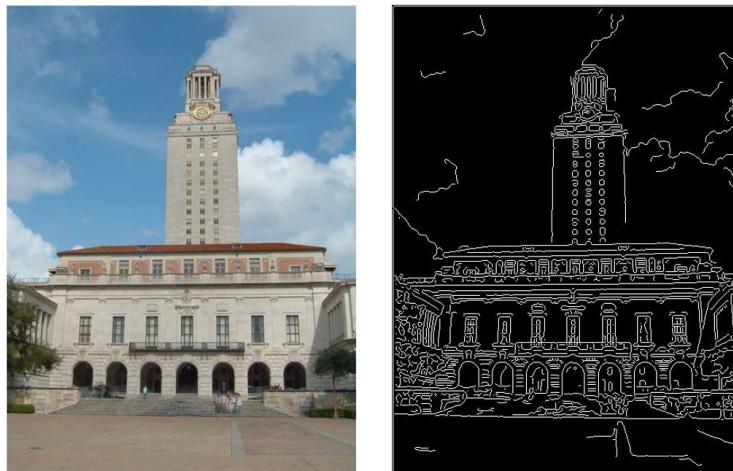


- “Interactive 3D Architectural Modeling from Unordered Photo Collections” Sinha et al. 2008*



Challenges of Line Fitting

- Not all the lines in the image are continuous

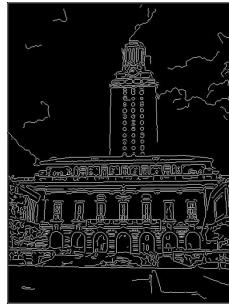


Challenges of Line Fitting

- Which points on which line?
- Noisy edge detection:
 - Clutter
 - Missed parts
 - Points are only approximately along the line

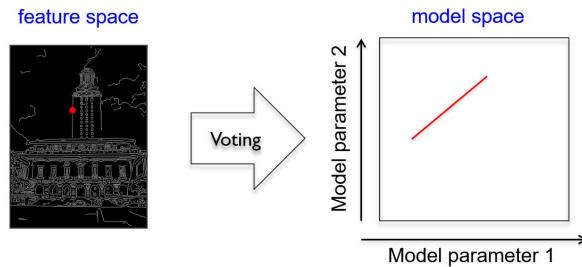


- Large search space
- How many lines are there?



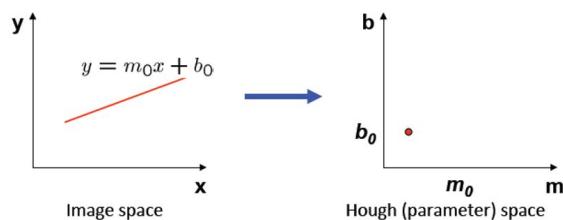
Voting

- Problem:
 - We cannot try all possible models
- Solution by voting:
 - Features (points) vote for models they are compatible with
 - Search for models with lots of votes

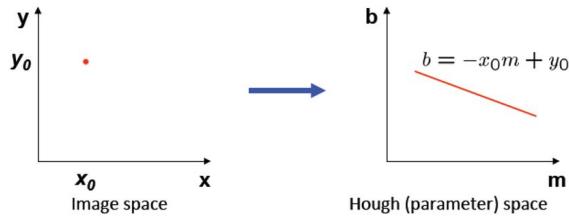


The Hough Transform

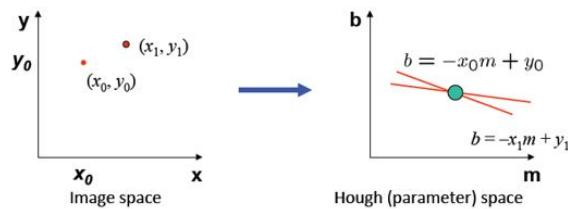
- Transformation from image space (x, y) to Hough space (m, b)
- A line in the image corresponds to a point in Hough space
 - Image \rightarrow Hough: Given a set of points (x, y) find all (m, b) such that $y = mx + b$



- Hough → Image: A point (x_0, y_0) in the image is the solution of $b = -x_0m + y_0$

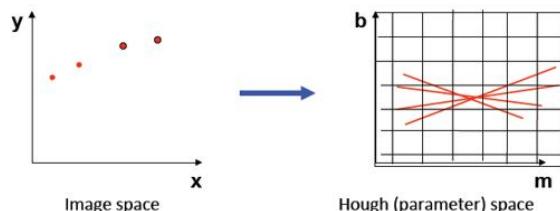


- The line that contains both points (x_0, y_0) and (x_1, y_1) is the intersection of the lines $b = -x_0m + y_0$ and $b = -x_1m + y_1$



Finding Lines with the Hough Transform

- Each edge point **votes** for a set of possible parameters in Hough space
- Count votes in a discrete set of bins
- Parameters with lots of votes indicate lines in image space



Polar Representation for Lines

- Problem: The familiar line equation $y = mx + b$ is problematic:
 - Can take infinite values (m, b)
 - Undefined for vertical lines
- Solution: Use polar representation

$$x \cos \theta + y \sin \theta = d$$

$$\theta \in [0, \pi), d \in \mathbb{R}$$



The Hough-Transform Algorithm

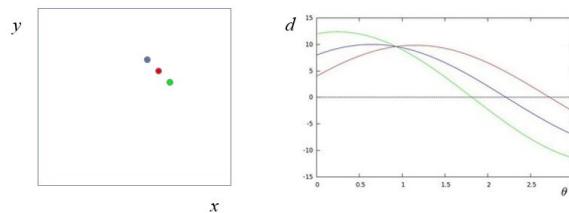
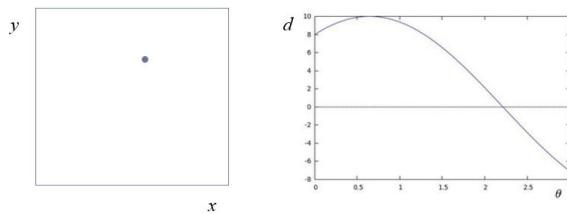
- Use polar representaton $x \cos \theta + y \cos \theta = d$, $\theta \in [0, \pi], d \in R$
- Quantize Hough space
- Loop:
 1. Initialize $H[d, \theta] = 0$
 2. For each edge point (x, y) in the image $H[d, \theta] += 1$
 3. Find bins $H[d, \theta] = 0$ with maximum value



Hough-Transform Example

- For a given point (x_0, y_0)

$$d(\theta) = x_0 \cos \theta + y_0 \sin \theta$$

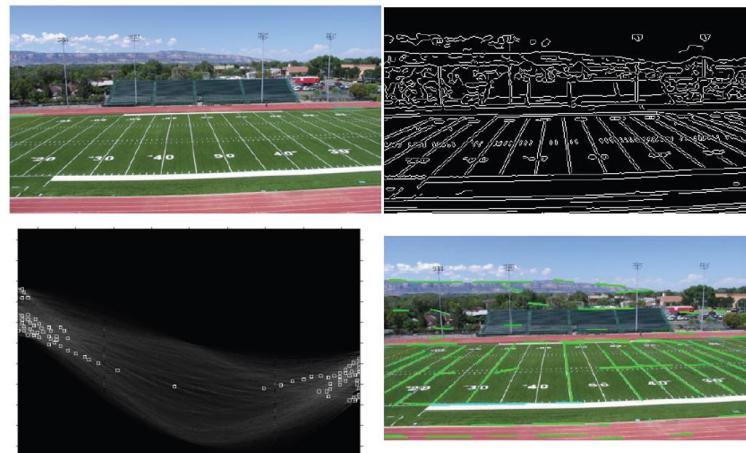


Hough-Transform Properties

- Noise and clutter votes are inconsistent, so will not accumulate.
- Can handle occlusions if not all points are present as long as model gets enough votes.
- Efficient.



Hough-Transform Example on Real Images

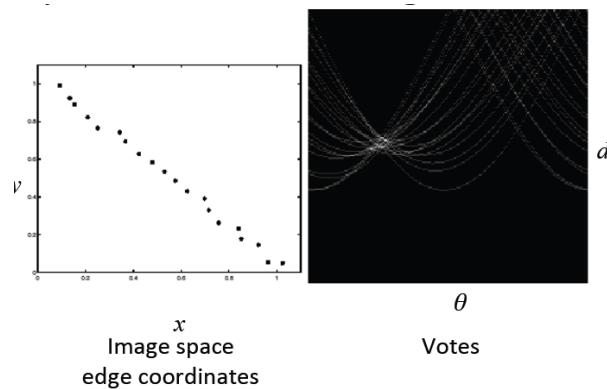


- Showing the longest segments found
- [Line detection video \(<https://youtu.be/u1pZE5VpDAQ>\)](https://youtu.be/u1pZE5VpDAQ)
 - [Video source \(<https://towardsdatascience.com/tutorial-build-a-lane-detector-679fd8953132>\)](https://towardsdatascience.com/tutorial-build-a-lane-detector-679fd8953132).

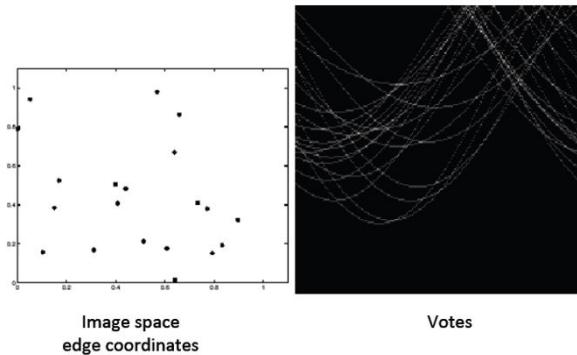


Impact of Noise on Hough Transform

- What difficulties does noise introduce?



- Here everything is “noise” but we still see peaks in the vote space



Voting: Practical Tips

- Use only trustworthy points
 - E.g., edges points with significant gradient magnitude (alternatively weight votes)
 - Szeliski suggests using edges instead of points
- Choose a good quantization grid
 - Not too coarse – too many lines fall in the same bucket
 - Not too fine – collinear points vote for different lines
- Smooth the voting (vote also for neighbors)
- Non-maxima suppression
- Refit line using accumulated votes
- Reduce number of parameters, if possible



Hough Transform Summary

- **Pros**
 - Can handle occlusions
 - Some robustness to noise
 - Can detect multiple lines in a single pass over the image
- **Cons**
 - Complexity increases exponentially with the number of parameters
 - Clutter can produce spurious peaks in parameter space
 - Hard to select the right quantization



Generalized Hough Transform

- Can be extended to other parametric models such as: **circles**, **ellipses**, **rectangles** etc.
- Complexity increases exponentially with the number of parameters.
- Can be used to detect complex non-parametric models as described in *Leibe et al. “Combined object categorization and segmentation with an implicit shape model”*.

RANSAC

RANdom SAmple Consensus [Fischler & Bolles 1981]

- Key ideas:
 - Look for “inliers” and use only them
 - If we fit a model to “outliers” we will not get a good fitting

RANSAC Algorithm

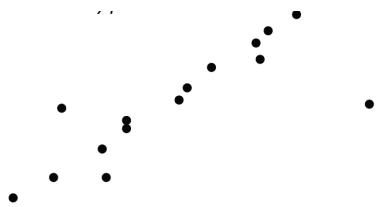
Loop:

1. Randomly select a group of points
2. Fit a model to the selected group
3. Find the inliers of the computed model
4. If number of inliers is large enough re-compute model using only inliers
5. Compute number of inliers of updated model

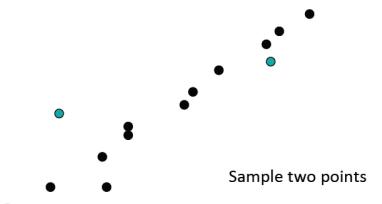
The winner: model with the largest number of inliers

Line Fitting with RANSAC

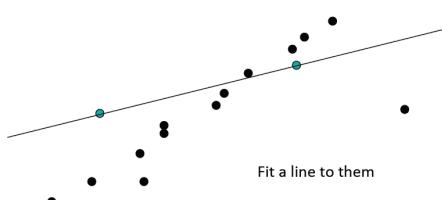
- Input: A set of edge points



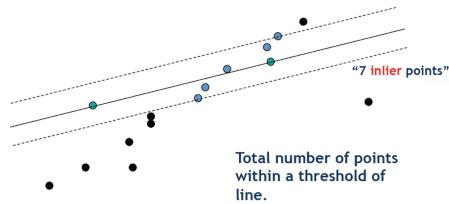
- **Step 1:** Select two points



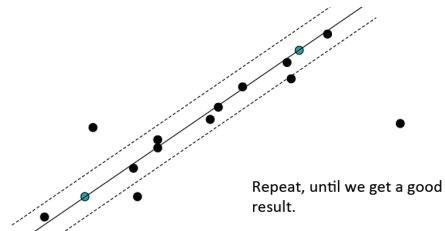
- **Step 2:** Fit a line to the selected points



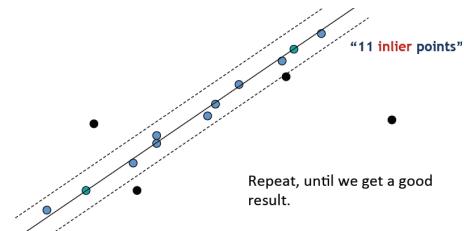
- Step 3: Identify inliers



- Step 4: Fit line to inliers



- Step 5: Count number of new inliers



RANSAC – Stopping Criteria

- Option 1: when the model is good enough:
 - By the number of inliers
 - By its fitting error
- Option 2: according to probability
 - Let K be the number of iterations
 - Let n be the number of points needed to compute the model
 - Let f be the fraction of inliers of a model
 - Then the probability that a single sample is correct: f^n
 - The probability that all K samples fail is $(1 - f^n)^K$
 - Choose K high enough to keep the failure rate low enough

RANSAC – For Multiple Models?

- How can we use RANSAC to compute multiple models?
 - Apply RANSAC multiple times, each time we remove the detected inliers.

RANSAC - Summary

- Pros
 - General method that works well for lots of model fitting problems
 - Easy to implement
- Cons
 - When the percentage of outliers is high too many iterations are needed and failure rate increases



CNNs for Line Detection



- [Image Source \(<https://towardsdatascience.com/tutorial-build-a-lane-detector-679fd8953132>\)](https://towardsdatascience.com/tutorial-build-a-lane-detector-679fd8953132)



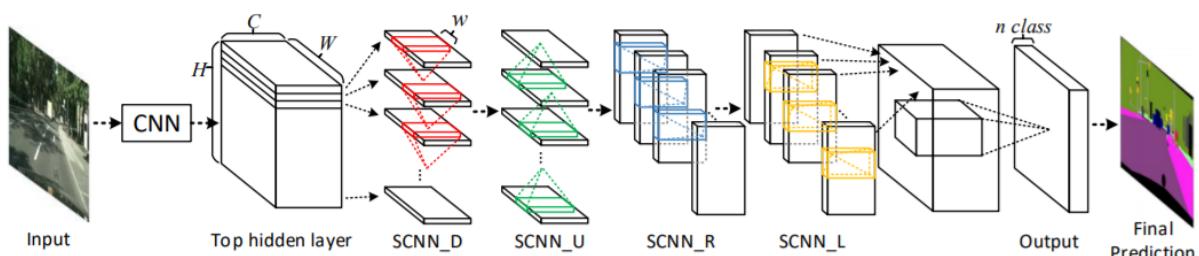
Spatial CNN (SCNN)

- Traditional CNN has no spatial awareness
 - Does not capture the spatial relationships (e.g. rotational and translational relationships)
- Spatial relationships are important
 - Traffic poles - usually exhibit similar spatial relationships such as to stand vertically and are placed alongside the left and right of roads
 - Lanes



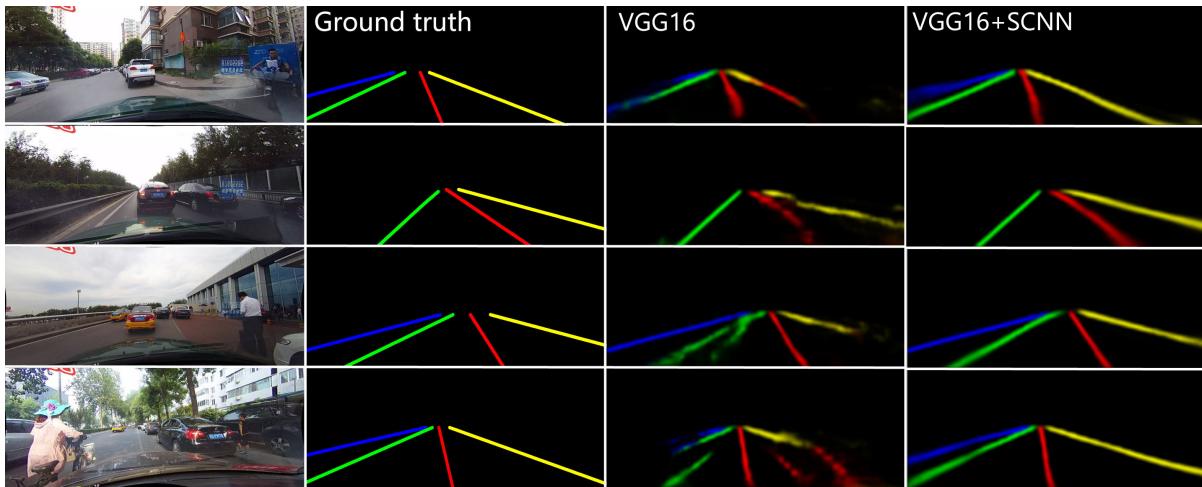
Spatial CNN - Architecture

- Based on layer-by-layer convolutions: each convolution layer receives input from its preceding layer, applies convolutions and nonlinear activation, and sends the output to the succeeding layer
- Refer to rows and columns as the “layers”





Spatial CNN - Results



- Line detection video - SCNN (<https://youtu.be/ey5XPs1012k?t=9>).
 - Video source (<https://github.com/XingangPan/SCNN>).



Recommended Videos



Warning!

- These videos do not replace the lectures and tutorials.
- Please use these to get a better understanding of the material, and not as an alternative to the written material.

Video By Subject

- Edge Detection (Sobel + Canny) - [CSCI 512 - Lecture 09-1 Edge Detection](https://www.youtube.com/watch?v=07qwMn2c5iY) (<https://www.youtube.com/watch?v=07qwMn2c5iY>) | [CSCI 512 - Lecture 09-2 Edge Detection](https://www.youtube.com/watch?v=PUCbhaGhgxE) (<https://www.youtube.com/watch?v=PUCbhaGhgxE>).
 - Edge Detection (Sobel) - [Finding the Edges \(Sobel Operator\)](https://www.youtube.com/watch?v=uihBwtPIBxM) - Computerphile (<https://www.youtube.com/watch?v=uihBwtPIBxM>).
 - Edge Detection (Canny) - [Canny Edge Detector](https://www.youtube.com/watch?v=sRFM5IEqR2w) - Computerphile (<https://www.youtube.com/watch?v=sRFM5IEqR2w>).
- Hough Transform - [Computer Vision Basics: Hough Transform](https://www.youtube.com/watch?v=6yVMpaloxIU) | By Dr. Ry @Stemplicity (<https://www.youtube.com/watch?v=6yVMpaloxIU>).
 - Circle Hough Transform - [How Circle Hough Transform works](https://www.youtube.com/watch?v=Ltqt24SQQoI) (<https://www.youtube.com/watch?v=Ltqt24SQQoI>).
- RANSAC - [Robotics - 4.3.3 - RANSAC - Random Sample Consensus](https://www.youtube.com/watch?v=BpOKB3OzQBQ) (<https://www.youtube.com/watch?v=BpOKB3OzQBQ>).
 - RANSAC - [RANSAC - Random Sample Consensus \(Cyrill Stachniss, 2020\)](https://www.youtube.com/watch?v=Cu1f6vpEilg) (<https://www.youtube.com/watch?v=Cu1f6vpEilg>).



Credits

- Slides - Lih Zelnik-Manor
- Computer Vision: Algorithms and Applications - Richard Szeliski - Sections 4.2 and 4.3.
- Canny Edge Detector - Code - [theailearner](https://theailearner.com/2019/05/22/canny-edge-detector) (<https://theailearner.com/2019/05/22/canny-edge-detector>)
- Tutorial: Build a lane detector - [Chuan-en Lin](https://towardsdatascience.com/tutorial-build-a-lane-detector-679fd8953132) (<https://towardsdatascience.com/tutorial-build-a-lane-detector-679fd8953132>).
- SCNN - [Pan et al.](https://arxiv.org/pdf/1712.06080.pdf) (<https://arxiv.org/pdf/1712.06080.pdf>) - [code](https://github.com/XingangPan/SCNN) (<https://github.com/XingangPan/SCNN>).
- Photo by [Pedro Gonzalez](https://unsplash.com/@pgonzalez_95?utm_medium=referral&utm_campaign=photographer-credit&utm_content=creditBadge/) (https://unsplash.com/@pgonzalez_95?utm_medium=referral&utm_campaign=photographer-credit&utm_content=creditBadge/) from [Unsplash](https://unsplash.com/) (<https://unsplash.com/>).
- Icons from [Icon8.com](https://icons8.com/) (<https://icons8.com/>) - <https://icons8.com> (<https://icons8.com>).